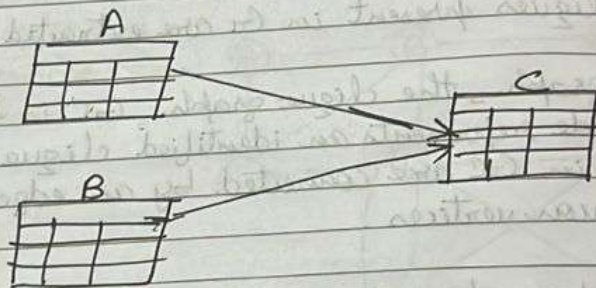


Page Rank -

- The term page ranking can be defined as a classical method used to arrange web pages acc. to its Obj. & usage of terms involved in it on the world wide web by using any link data etc.
- We have 3 pages A, B, C in a given domain of websites.



- No. of back links that exist b/w 2 pages can be categorized as:

i) Back links:

- Wrt. to fig. A & B are back links for web page 'C'.
- Back link indicates given web page is referred by how many no. of other web pages.

ii) Forward links:

- Represents the fact that, how many web pages will be referred by given web pages.
- Back links are very imp. from Ranking of docs. perspective.
- A web page that contains no. of backlinks is said to

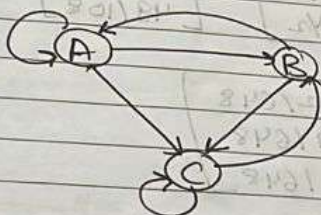


be imp. webpage will get upper pos in ranking

Example:- Algo:

1. Consider a website with n diff. web pages.
2. Set vector r_0 as $1/n$ for each web page.
3. Compute transiti matrix M .
4. For calc. next vector r_1 : $r_1 = M * (r_0)$
5. " " $r_2 = M * (r_1)$
6. Hence, in general next vector can be calc. as:
 $r_{i+1} = M * (r_i)$
7. Distribute vector r is PageRank of each webpage.

Example:



$$r_0 = \begin{bmatrix} 1/3 \\ 1/3 \\ 1/3 \end{bmatrix}$$

Compute PageRank of each page in foll. graph after 3 iters \rightarrow

$$\text{Transiti mat. } (M) = \begin{matrix} & \begin{matrix} A & B & C \end{matrix} \\ \begin{matrix} A \\ B \\ C \end{matrix} & \begin{bmatrix} 1/3 & 1/2 & 0 \\ 1/3 & 0 & 1/2 \\ 1/3 & 1/2 & 1/2 \end{bmatrix} \end{matrix}$$

$$r_{i+1} = M * r_i$$

• Iter 1:

$$\begin{matrix} & \begin{matrix} A & B & C \end{matrix} \\ \begin{matrix} A \\ B \\ C \end{matrix} & \begin{bmatrix} 1/3 & 1/2 & 0 \\ 1/3 & 0 & 1/2 \\ 1/3 & 1/2 & 1/2 \end{bmatrix} \end{matrix} \times \begin{matrix} r_0 \\ r_1 \end{matrix} = \begin{matrix} r_1 \end{matrix}$$

$$\begin{bmatrix} 1/3 & 1/2 & 0 \\ 1/3 & 0 & 1/2 \\ 1/3 & 1/2 & 1/2 \end{bmatrix} \times \begin{bmatrix} 1/3 \\ 1/3 \\ 1/3 \end{bmatrix} = \begin{bmatrix} 5/18 \\ 5/18 \\ 8/18 \end{bmatrix}$$

Iter 2:

$$\begin{array}{c}
 \begin{array}{ccc}
 & \text{H} & \\
 \begin{array}{c} \text{A} \\ \text{B} \\ \text{C} \end{array} & \begin{array}{c} \text{A} \quad \text{B} \quad \text{C} \\ \frac{1}{3} \quad \frac{1}{2} \quad 0 \\ \frac{1}{3} \quad 0 \quad \frac{1}{2} \\ \frac{1}{3} \quad \frac{1}{2} \quad \frac{1}{2} \end{array} & \times \begin{array}{c} r_1 \\ \begin{bmatrix} 5/18 \\ 5/18 \\ 8/18 \end{bmatrix} \end{array} = \begin{array}{c} r_2 \\ \begin{bmatrix} 25/108 \\ 34/108 \\ 49/108 \end{bmatrix} \end{array}
 \end{array}$$

Iter 3:

$$\begin{array}{c}
 \begin{array}{ccc}
 & \text{H} & \\
 \begin{array}{c} \text{A} \\ \text{B} \\ \text{C} \end{array} & \begin{array}{c} \text{A} \quad \text{B} \quad \text{C} \\ \frac{1}{3} \quad \frac{1}{2} \quad 0 \\ \frac{1}{3} \quad 0 \quad \frac{1}{2} \\ \frac{1}{3} \quad \frac{1}{2} \quad \frac{1}{2} \end{array} & \times \begin{array}{c} r_2 \\ \begin{bmatrix} 25/108 \\ 34/108 \\ 49/108 \end{bmatrix} \end{array} = \begin{array}{c} r_3 \\ \begin{bmatrix} 152/648 \\ 197/648 \\ 299/648 \end{bmatrix} \end{array}
 \end{array}$$

$$r_3 = \begin{bmatrix} 152/648 \\ 197/648 \\ 299/648 \end{bmatrix}$$

∴ Node C (Page C) has highest PageRank value

$$\begin{array}{c}
 \begin{array}{ccc}
 & \text{B} & \text{A} \\
 \begin{array}{c} \text{A} \\ \text{B} \\ \text{C} \end{array} & \begin{array}{c} \text{A} \quad \text{B} \quad \text{A} \\ 0 \quad \frac{1}{2} \quad \frac{1}{2} \\ \frac{1}{2} \quad 0 \quad \frac{1}{2} \\ \frac{1}{2} \quad \frac{1}{2} \quad \frac{1}{2} \end{array} & \begin{array}{c} \text{A} \\ \text{B} \\ \text{C} \end{array}
 \end{array}$$

$$\begin{array}{c}
 \begin{array}{ccc}
 & \text{B} & \text{A} \\
 \begin{array}{c} \text{A} \\ \text{B} \\ \text{C} \end{array} & \begin{array}{c} \text{A} \quad \text{B} \quad \text{A} \\ 0 \quad \frac{1}{2} \quad \frac{1}{2} \\ \frac{1}{2} \quad 0 \quad \frac{1}{2} \\ \frac{1}{2} \quad \frac{1}{2} \quad \frac{1}{2} \end{array} & \begin{array}{c} \text{A} \\ \text{B} \\ \text{C} \end{array}
 \end{array}$$