24 YR 9 PATH MATHS: LESSON OUTLINE: INDICES A-C (MATHSPACE – M.S)

Instructions: Every lesson: Remember to work off "Lesson Instructions" you glued in the front of your book (also on GC).

- 1. Mathspace: Complete "Check-in" date check-in's table on Lesson Outline.
- 2. Copy ALL the "Theory Notes" supplied by Teacher in class.
- 3. Mathspace Lesson Activity: Read through the "Lesson" Add any additional notes to your "Theory Notes" from the class.

4. Practical Exercises:

- Write Heading for Exercise with date.
- Complete set work showing ALL working out in your Exercise Book.
- Any work not completed in class AUTOMATICALLY becomes homework.
- When finished, entering answers into M.S and marking your answers in your exercise book.

- Upload working out on G.C. This is considered part of homework. MATHSPACE/PRACTICAL EXERCISE: MATHSPACE (M.S) ACTIVITY: Set by teacher: Custom Task (C.T), Adaptive Task (A.T), Worksheet (W.S) ALL FROM YEAR 9 2024 TEXTBOOK

First lesson: Draw up a table with a small column called Word and larger column called Definition: This is your Definition Table (D.T). You are to add the definitions of words from LESSONS throughout the topic.

Subtopics	DATE	LESSON	MATHSPACE/PRACTICAL EX: (M.S) ACTIVITY: Set by teacher	M.S C.T/WS		
INDICES A						
Multiplication		• Complete "Check-in" (record date on table	❖ Complete M.S: "Activity: 1.01C			
law		below)	Multiplication law". Remember			
		• Read "Lesson 1.01C Multiplication law "	follow instructions above for "4.			
		& complete the practice questions.	Practical Exercise".			
		• ADD: Definitions to D.T	A -			
Division Law		• Complete "Check-in"	❖Complete M.S : "Activity: 1.02C			
		Read "Lesson 1.02C Division Law "	Division Law".			
Power of a		• Complete "Check-in"	❖ Complete M.S : "Activity: 1.03C			
power law		• Read "Lesson 1.03C Power of a power law	Power of a power law".			
Zero and		• Complete "Check-in"	❖ Complete M.S: "Activity: 1.04C			
negative indices		 Read "Lesson 1.04C Zero and negative 	Zero and negative indices with			
with numeric		indices with numeric bases "	numeric bases".			
bases		• Read "Lesson (YR 10) 2.05 Negative	❖ Complete M.S : "Activity: (YR 10)			
		indices "	2.05 Negative indices".			
	ı	INDICES B		T		
Index laws with		 Read "Lesson 1.05C/P Index laws with 	❖ Complete M.S : "Activity: 1.05C/P			
algebraic bases		algebraic bases "	Index laws with algebraic bases".			
Irrational		 Read "Lesson 2.01P Simplifying surds" 	❖ Complete M.S: "Activity: 2.01P			
numbers/			Simplifying surds".			
simplifying						
surds						
Add & subtract		• Read "Lesson 2.02P Add & subtract surds	❖ Complete M.S: "Activity: 2.02P			
surds			Add & subtract surds".			
Multiply &		 Read "Lesson 2.03P Multiply & divide 	❖ Complete M.S: "Activity: 2.03P			
divide surds		surds "	Multiply & divide surds".			
Binomial		• Read "Lesson 2.04P Binomial expansions	❖ Complete M.S: "Activity: 2.04P			
expansions		with surds "	Binomial expansions with surds".			
with surds						
Rationalise the		• Read "Lesson 2.05P Rationalise the	❖ Complete M.S: "Activity: 2.05P			
denominator		denominator	Rationalise the denominator".			

REMEMBER:

- Pre-set Mathspace is to be continually completed throughout the topic.
- Work not completed in class **automatically** becomes homework.
- Challenge yourself by completing other topic tasks from Mathspace when finished set work.
- Always date your work in your Exercise Book with ALL working out & your Lesson Outline.

YR 9 STAGE 5 SKILLS COMPLETE "CHECK-IN" (10 Q's per check-in).

- 1					
	TOPIC	First Topic	SUB-TOPICS	Additional	Understanding

	Check – ins		 E- excellent G- Good S- Satisfactory X – need extra help
Algebra	Check: Date:	Patterns & Algebra	
2 Check - ins	Check: Date:	Indices	
		Algebraic Techniques	

TOPIC: INDICES A

Outcomes: A student:

- develops understanding and fluency in mathematics through exploring and connecting mathematical concepts, choosing and applying mathematical techniques to solve problems, and communicating their thinking and reasoning coherently and clearly MAO-WM-01
- simplifies algebraic expressions involving positive-integer and zero indices, and establishes the meaning of negative indices for numerical bases MA5-IND-C-01

Content: Extend and apply the index laws to variables, using positive-integer indices and the zero index

Apply the index laws for numerical bases with positive-integer indices to develop the index laws in algebraic form

Example(s):

Generalising numerical expressions, such as $2^2 \times 2^3 = 2^{2+3} = 2^5$ to $a^m \times a^n = a^{m+n}$

Generalising numerical expressions, such as $2^5 \div 2^3 = 2^{5-3} = 2^2$ to $a^m \div a^n = a^{m-n}$.

- Generalising numerical expressions, such as $(2^2)^3 = 2^{2 \times 3} = 2^6$ to $(a^m)^n = a^{mn}$.
- Establish that $x^0 = 1$ algebraically using index laws

By considering $\frac{x^4}{x^4} = x^{4-4} = x^0$ and $\frac{x^4}{x^4} = \frac{x \times x \times x \times x}{x \times x \times x \times x} = 1$, establish that $x^0 = 1$.

Simplify algebraic expressions that involve the zero index

Example(s):

Recognising and explaining that $7m^0 = 7 \times 1 = 7$ and $(3x)^0 + 5 = 6$.

Content: Simplify algebraic products and quotients using index laws

Simplify algebraic expressions that involve powers, products and quotients of simple algebraic terms containing positive-integer indices

Example(s): Simplifying $(3x^2)^3 = 27x^6$ and $15a^6 \div 3a^2 = 5a^4$.

Content: Apply index laws to numerical expressions with negative-integer indices

Apply index notation, patterns and index laws to establish the meaning of negative indices for numerical bases

Example(s):

Using numerical patterns:

3 ³	3 ²	3 ¹	3°	3 ⁻¹	3-2
27	9	3	1	1/3	$\frac{1}{3^2} = \frac{1}{9}$

Image long description: 6 columns in a table showing descending powers with a base of 3 on the top row and their calculations on the bottom row. On the top row, 3 cubed, 3 squared, 3 to the power of 1, 3 to the power of 0, 3 to the power of minus 1 and 3 to the power of minus 2. The bottom row is 27, 9, 3, 1, one-third, and 1 over 3 squared equals 1 over 9.

Applying index laws: $4^3 \div 4^5 = 4^{-2}$ and $\frac{4^3}{4^5} = \frac{1}{4^2}$ to establish that $4^{-2} = \frac{1}{4^2}$.

• Evaluate numerical expressions involving a negative index by first representing them with a

positive index

Example(s): Evaluating $3^{-4} = \frac{1}{3^4} = \frac{1}{81}$.

Represent given numbers in index form (integer indices and bases only) and vice versa

Example(s): Representing $\frac{1}{125}$ as $\frac{1}{53}$ and 5^{-3} .

TOPIC: INDICES B

Outcomes: A student:

- develops understanding and fluency in mathematics through exploring and connecting mathematical concepts, choosing and applying mathematical techniques to solve problems, and communicating their thinking and reasoning coherently and clearly MAO-WM-01
- applies the index laws to operate with algebraic expressions involving negative-integer indices (Path: Adv) MA5-IND-P-01

Content: Apply index laws to algebraic expressions involving negative-integer indices

Apply index notation, patterns and index laws to establish $a^{-1} = \frac{1}{a}$, $a^{-2} = \frac{1}{a^2}$, $a^{-3} = \frac{1}{a^3}$ and $a^{-n} = \frac{1}{a^n}$

Example(s): Explaining the difference between x^{-2} , $-x^2$ and -2x by first examining the differences numerically using a calculator.

 Represent expressions involving negative-integer indices as expressions involving positive-integer indices and vice versa

Example(s): Examining expressions such as $x^{-3} = \frac{1}{x^3}$, $2x^{-1} = \frac{2}{x^1} = \frac{2}{x}$, $\frac{4}{x} = \frac{4}{x^1} = 4x^{-1}$ and $\frac{1}{x^2} = x^{-2}$.

 Apply the index laws to simplify algebraic products and quotients involving negativeinteger indices

Example(s): Justifying why the following statements of equality are true or false:

$$\frac{9x^5}{3x^{-5}} = 3x^{10}$$

$$9x^{-7} \div 3x^5 = 3x^2$$

$$a^{-5} \times a^3 = a^8$$

 $a^5 \times a^{-7} = a^{-2}$.

- Describe and use x^{-1} as the reciprocal of x and generalise this relationship to expressions of the form $\left(\frac{a}{b}\right)^{-1}$
- Use knowledge of the reciprocal to simplify expressions of the form $\left(\frac{a}{b}\right)^{-n}$

Example(s): Simplifying $\left(\frac{2x^2}{3}\right)^{-2}$ and expressing without a negative index.

TOPIC: INDICES C

Outcomes: A student:

- develops understanding and fluency in mathematics through exploring and connecting
 mathematical concepts, choosing and applying mathematical techniques to solve problems,
 and communicating their thinking and reasoning coherently and clearly MAO-WM-01
- describes and performs operations with surds and fractional indices (Path: Adv) MA5-IND-P-02

Content: Describe surds

- Describe a real number as a number that can be represented by a point on the number line
- ☐ Examine the differences between rational and irrational numbers and recognise that all rational and irrational numbers are real

Convert between recurring decimals and their fractional form using digital tools
 Describe the term *surd* as referring to irrational expressions of the form ⁿ√x where x is a rational number and n is an integer such that n ≥ 2, and x > 0 when n is even
 Recognise that a surd is an exact value that can be approximated by a rounded decimal
 Demonstrate that √x is undefined for x < 0 and that √x = 0 when x = 0 using digital tools
 Example: Explaining why an error occurs when attempting to find a value of √-4 as opposed to √4.
 Describe √x as the positive square root of x for x > 0 and √0 = 0
 Example: Reasoning why the negative solution of the relevant quadratic equation is not feasible when solving problems involving Pythagoras' theorem.

Content: Apply knowledge of surds to solve problems

* Establish and apply the following results for x > 0 and y > 0:

$$(\sqrt{x})^2 = x = \sqrt{x^2}, \sqrt{xy} = \sqrt{x} \times \sqrt{y} \text{ and } \sqrt{\frac{x}{y}} = \frac{\sqrt{x}}{\sqrt{y}}$$

Apply the 4 operations to simplify expressions involving surds

Example(s): Demonstrating why $\sqrt{6} + \sqrt{8}$ and $\sqrt{14}$ are different.

Expand and simplify expressions involving surdsExample(s):

Expanding and simplifying: $(\sqrt{15} + 2\sqrt{3})(5\sqrt{8} - \sqrt{10})$

$$= 5\sqrt{120} - \sqrt{150} + 10\sqrt{24} - 2\sqrt{30}$$

$$= 5\sqrt{4 \times 30} - \sqrt{25 \times 6} + 10\sqrt{4 \times 6} - 2\sqrt{30}$$

$$= 10\sqrt{30} - 5\sqrt{6} + 20\sqrt{6} - 2\sqrt{30}$$

$$= 8\sqrt{30} + 15\sqrt{6}.$$

■ Rationalise the denominators of surds of the form $\frac{a\sqrt{b}}{c\sqrt{d}}$

Example: Rationalising the denominator of $\frac{2\sqrt{3}}{3\sqrt{5}}$ by multiplying the numerator and denominator by $\sqrt{5}$.

Content: Describe and use fractional indices

• Apply index laws to describe fractional indices as: $a^{\frac{1}{n}} = \sqrt[n]{a}$ and $a^{\frac{m}{n}} = \sqrt[n]{a^m} = \left(\sqrt[n]{a}\right)^m$

Example(s): Explaining why finding the square root of an expression is the same as raising the expression to the power of a half by considering that if $(\sqrt{9})^2 = 9$ and $(9^{\frac{1}{2}})^2 = 9$, then $\sqrt{9} = 9^{\frac{1}{2}}$.

Translate expressions in surd form to expressions in index form and vice versa
 Evaluate numerical expressions involving fractional indices including using digital tools