

COMP 3710 - 3 Applied Artificial Intelligence (3,1,0) Fall 2017

Seminar/Lab 5.

Propositional logic, and genetic algorithm for TSP

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1. (2 marks) Which of the followings are correct? You need to prove or disprove using truth tables.

a.
$$(A \land B) \rightarrow C \equiv (A \rightarrow C) \lor (B \rightarrow C)$$

b.
$$(C \lor (\sim A \land \sim B)) \equiv ((A \to C) \land (B \to C))$$

a.

$$(A \land B) \rightarrow C \equiv (A \rightarrow C) \lor (B \rightarrow C)$$
 (Correct)

A	В	С	$A \wedge B$	$(A \wedge B) \to C$
Т	T	T	Т	Т
Т	T	F	Т	F
Т	F	T	F	T
Т	F	F	F	T
F	T	T	F	Т
F	T	F	F	T
F	F	T	F	Т
F	F	F	F	Т

A	В	С	$(A \to C)$	$(B \to C)$	$(A \to C) \lor (B \to C)$
Т	Т	T	T	T	T
Т	Т	F	F	F	F
Т	F	T	T	T	T
Т	F	F	F	Т	T
F	Т	T	Т	Т	T
F	Т	F	T	F	T
F	F	T	T	T	T
F	F	F	Т	Т	T

$$(C \lor (\sim A \land \sim B)) \equiv ((A \to C) \land (B \to C))$$
 (Correct)

A	В	С	~A	~B	~A ∧ ~B	$(C \vee (\sim A \wedge \sim B))$
T	Т	T	F	F	F	Т
T	Т	F	F	F	F	F
T	F	T	F	T	F	Т
T	F	F	F	T	F	F
F	Т	T	T	F	F	Т
F	Т	F	T	F	F	F
F	F	T	T	T	Т	Т
F	F	F	T	T	T	Т

A	В	С	$A \to C$	$B \to C$	$((A \to C) \land (B \to C))$
T	T	T	T	T	T
Т	T	F	F	F	F
T	F	T	Т	Т	T
T	F	F	F	F	F
F	Т	T	Т	Т	T
F	Т	F	Т	F	F
F	F	T	Т	Т	T
F	F	F	T	T	T

2. (2 marks) Simplify the followings as much as possible.

c.
$$\sim (\sim A \wedge B) \wedge (A \vee B)$$

d.
$$\sim ((\sim A \wedge B) \vee (\sim A \wedge \sim B))$$

t: tautology c:contradiction

c.

$$\mathord{\sim}(\mathord{\sim} A \wedge B) \wedge (A \vee B) = (\ A \vee \mathord{\sim} B\) \wedge (A \vee B\) = A \vee (\ \mathord{\sim} B \wedge B) = A \vee c = A$$

d.

$$\sim ((\sim A \land B) \lor (\sim A \land \sim B)) = \sim (\sim A \land (B \lor \sim B)) = \sim (\sim A \land t) = A \lor c = A$$