Experiment 17 Polynomials using Linked List

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Aim: To receive two polynomials and print their sum and product

Data Structure Used: Linked List

Operation Used: Comparisons, addition, multiplication

Algorithm for Addition (ADD_POLY):

Input: Two polynomial, A and B with the terms as the nodes of a linked list and 'a' denoting the number of terms in polynomial A and 'b' denoting the number of terms in polynomial 'B'

Output: Sum of the polynomial 'C' **Data Structure Used:** Linked List

```
Step 1: Start
Step 2: Receive two polynomial in linked list
Step 3: i = A \rightarrow Header //Pointer to the header of polynomial A
Step 4: j = B \rightarrow Header //Pointer to the polynomial B
Step 5: while i =! NULL and j=! NULL
          Step 1: new=GetNode(Node)
          Step 1 : if i \rightarrow pow == j \rightarrow pow
                      Step 1: new \rightarrow pow = i \rightarrow pow
                      Step 2: new \rightarrow coeff = i \rightarrow coeff+j \rightarrow coeff
                      Step 3: C.addNode(new)
                      Step 4: i=i \rightarrow link
                      Step 5: j=j->link
          Step 2: else if i \rightarrow pow < j \rightarrow pow
                      Step 1: new \rightarrow pow = j \rightarrow pow
                      Step 2: new \rightarrow coeff=j \rightarrow coeff
                      Step 3: C.addNode(new)
                      Step 4: j=j \rightarrow link
          Step 3: else if i \rightarrow pow > j \rightarrow pow
                      Step 1: new \rightarrow coeff = i->coeff
                      Step 2: new \rightarrow pow = i \rightarrow pow
                      Step 3: i=i \rightarrow link
                      Step 4: C.addNode(new)
           Step 4: Endif
Step 6: EndWhile
Step 7: while i!=NULL
          Step 1: new \rightarrow coeff = i \rightarrow coeff
          Step 2: new \rightarrow pow = i \rightarrow pow
          Step 3: i = i \rightarrow link
          Step 4: C.addNode(new)
Step 8: EndWhile
Step 9: while j!=NULL
          Step 1: new = GetNode(Node)
          Step 2: new \rightarrow pow = i \rightarrow pow
          Step 3: new \rightarrow coeff=j \rightarrow coeff
          Step 4: C.addNode(new)
          Step 5: j=j \rightarrow link
Step 10: EndWhile
Step 11: return c
Step 12: Stop
```

Description of the Algorithm:

In this algorithm the polynomials' terms are the nodes of a linked list and there are 2 pointers i and j, which points to the nodes of A and B respectively. If the powers of a term in A and B are equal then the coefficient are added and the sum is put into a new node (new). Which is then added to the end of the resultant polynomial C. If the coefficient of the term in A is greater than the term in B then the term is added to the end of B. Likewise for B also.

Algorithm for Multiplication(MUL_POLY):

Input: A and B, two polynomials with the terms as nodes of a linked list with pow being the power of the term and coeff being the coefficient

Output: Polynomial C, with **Data Structure used:** Linked list

Steps:

```
Step 1:Start
Step 2: receive two polynomials
Step 3:i = A \rightarrow head
Step 4: j = B \rightarrow head
Step 5: initialize C as a polynomial with 0 as the only term
Step 6: k = 0
Step 7: while(k < B \rightarrow numberOfTerms)
          Step 1: j = B \rightarrow head
          Step 2: while(j!=NULL)
                     Step 1: new = GetNode(Node)
                     Step 2; new \rightarrow pow = i \rightarrow pow + j \rightarrow pow
                     Step 3: new \rightarrow coeff = i \rightarrow coeff * i \rightarrow coeff
                     Step 4: temp.addNode(new)
                     Step 5: j = j \rightarrow link
          Step 3: End While
          Step 4: C= ADD POLY(C,temp)
          Step 5: i=i \rightarrow link
          Step 6: k++
Step 8: EndWhile
Step 9: return C
Step 10: Stop
```

Description of the Algorithm:

The polynomial product of $(6X^2+1)*(7X^2+3X+1)$ can be expressed as, $0+(6X^2+1)*(7X^2)+(6X^2+1)*(3X+(6X^2+1)*1$. Here we just need to multiply the first polynomial with one of the terms from the second and feed the result obtained before and the result obtained now to the addition function and then after the algorithm has been executed number of times as there are number of terms in B. We get the product of the polynomial.

Result: the Program is successfully compiled and the desired output is obtained.

Program/ Source Code:

```
/**********
 * Sum And Product of a Polynomial
 * Done By Rohit Karunakaran
 ***********
#include<stdio.h>
#include<stdlib.h>
/* Input : 2 polynomials of the form
            a0*X^n + a1*X^n-1 + a2*X^n-2 \dots an
 * Output: First polynomial the second polynomial and there sum
typedef struct Node
  int coeff;
   int pow;
   struct Node* link;
}PolyNode;
typedef struct Polynomial
    int numberOfTerms;
    PolyNode* Head; //Header contians the first polynomial, so it has to be printed
    PolyNode* Trail;
}Poly;
//UTILITY FUNCTIONS START
void initPoly(Poly **a)
    *a = (Poly*) malloc(sizeof(Poly));
    (*a) \rightarrow Head = NULL;
    (*a)->Trail= NULL;
    (*a) ->numberOfTerms=0;
}
void addNode(Poly *a,int pow, int coeff)
    PolyNode* n = (PolyNode*) malloc(sizeof(PolyNode));
    if(n!=NULL){
        n->coeff = coeff; n->pow = pow; n->link=NULL;
        if(a->Trail ==NULL)
        {
            a \rightarrow Head = n;
        }
        else
            a->Trail->link = n;
        a \rightarrow Trail = n;
    }
    else
```

```
{
        return;
    }
}
void deleteNode(Poly *a,PolyNode *b)
    PolyNode *ptr=a->Head;
    if (ptr==NULL) return;
    while (ptr->link!=b&&ptr!=NULL) {ptr=ptr->link;} //Traverse till you find the node
b
    if(ptr==NULL){return;} //If there is no such node then, return
    else
        if(ptr->link->link==NULL)
        {
            free(ptr->link);
            ptr->link=NULL;
        }
        else
            PolyNode *tmp = ptr->link;
            ptr->link = tmp->link;
            free(tmp);
        }
    }
}
void freePoly(Poly **poly)
    if(*poly !=NULL)
        PolyNode *i,*tmp;
        i=(*poly)->Head;
        while(i!=NULL)
            tmp=i;
            i=i->link;
            free(tmp);
        }
        free (*poly);
    }
    return;
}
//UTILITY FUNCTIONS END
/* Funtion to print the polynomials*/
void printPoly(Poly* a) {
    /* Input: Polynomial stored in the structure Polynomial
     * Ouput: prints the polynomial
     */
```

```
//int iterCount = a->numberOfTerms;
    //int i;
    PolyNode *ptr=a->Head;
    while(ptr!=a->Trail){
        printf("%d*X^%d + ",ptr->coeff,ptr->pow);
        ptr = ptr->link;
    printf("%d*X^%d",ptr->coeff,ptr->pow);
}
/* Funtion to convert the polynomial into tuple*/
Poly* createPolyFromString(char* s){
    /* Input: String of charecters
     * Output: the Head node of the linked list contating the polynomial
    Poly* a=NULL; initPoly(&a);
    int i;
    int count = 0;
    int numberStack[2];
    int numberStackTop = -1;
    int number = 0,pow,coeff;
    int negative = 0;
    //parsing the string
    for (i = 0; s[i]!='\setminus 0'; i++) {
        if(s[i] == '-'){
            negative = 1;
        if(s[i]>='0'&&s[i]<='9'){
            while ((s[i]!= 'X' | |s[i]!='x' | |s[i]!=' ' | |s[i]!='^') \&\&
(s[i] >= '0' \&\&s[i] <= '9'))
                 // here s[i] will only be numbers
                number = number*10+(s[i]-'0');
                i++;
            }
            if(negative) numberStack[++numberStackTop] = -1*number;
            else numberStack[++numberStackTop] = number;
            i--;
            negative = 0;
            number = 0;
        }
        if(i!=0\&\&(s[i]=='-'||s[i]=='+'||s[i]=='\setminus0'))\{//\&\&s[i-1]!='^')\{
            if(numberStackTop==0)
            {
                 if(s[i-1] == 'X')
                     numberStack[++numberStackTop] = 1;
                     numberStack[++numberStackTop] = 0;
```

```
}
                 count++;
                pow = numberStack[numberStackTop--];
                 coeff = numberStack[numberStackTop--];
                 addNode(a,pow,coeff);
        }
    }
    if(numberStackTop==0)
        if(s[i-1] == 'X')
            numberStack[++numberStackTop] = 1;
        else
            numberStack[++numberStackTop] = 0;
    }
    count++;
    pow = numberStack[numberStackTop--];
    coeff = numberStack[numberStackTop--];
    addNode(a,pow,coeff);
    a->numberOfTerms = count;
    return a;
}
/*Funtion to find the sum of the polynomials*/
Poly* sumOfPoly(Poly* a, Poly* b)
    Poly* c = (Poly*)malloc(sizeof(Poly));
    initPoly(&c);
    PolyNode *i=a->Head;
    PolyNode *j=b->Head;
    while(i!=NULL&&j!=NULL)
        if(i->pow==j->pow)
        {
            if(i->coeff+j->coeff!=0)
                addNode(c,i->pow,i->coeff+j->coeff);
            i=i->link;
            j=j->link;
        }
        else if(i->pow>j->pow)
            addNode(c,i->pow,i->coeff);
            i=i->link;
        }
        else if(i->pow<j->pow)
            addNode(c, j->pow, j->coeff);
            j=j->link;
        }
```

```
c->numberOfTerms++;
    }
    while (i!=NULL)
        addNode(c,i->pow,i->coeff);
        i=i->link;
        c->numberOfTerms++;
    while(j!=NULL)
        addNode(c, j->pow, j->coeff);
        j=j->link;
        c->numberOfTerms++;
    }
   return c;
}
Poly* productOfPolynomials(Poly* a,Poly*b)
   Poly *c=NULL;
   Poly *temp=NULL;
    //intiPoly(Temp);
    int k = 0;
    PolyNode *i = a->Head;
    PolyNode *j = b->Head;
    while(k<a->numberOfTerms)
        //i=a->Head;
        j=b->Head;
        if(c==NULL)
        {
            initPoly(&c);
            while(j!=NULL)
                addNode(c,i->pow+j->pow,i->coeff*j->coeff);
                j=j->link;
        }
        else
            initPoly(&temp);
            while(j!=NULL)
                addNode(temp,i->pow+j->pow,i->coeff*j->coeff);
                j=j->link;
            c=sumOfPoly(c,temp);
        i=i->link;
        freePoly(&temp);
        k++;
    }
```

```
return c;
}
int main(){
    Poly* a;
    Poly* b;
    Poly* c;
    int strLength = 100;
    char* polyString = (char*) malloc(strLength*sizeof(char));
    /*Read the polynomials*/
        flush (stdin);
        printf("Enter polynomial 1 in the form : a0*X^n + a1*X^n-1 + a2*X^n-2 \dots
an*X^0 --> ");
        scanf("%[^\n]",polyString);
        scanf("%*c"); //remove the \n charecter from the input stream
        a = createPolyFromString(polyString);
        free (polyString);
        flush (stdin);
        flush (stdout);
        polyString = (char*) malloc(strLength*sizeof(char));
        printf("Enter polynomial 2 in the form : a0*X^n + a1*X^n-1 + a2*X^n-2 \dots
an*X^0 --> ");
        scanf("%[^\n]",polyString);
        b = createPolyFromString(polyString);
        free (polyString);
    /*Finish reading Polynomials*/
    printf("\nPolynomial 1 is: ");
    printPoly(a);
    printf("\nPolynomial 2 is: ");
    printPoly(b);
    c = sumOfPoly(a,b); //Find the sum of the polynomials
    printf("\nSum is ");
    printPoly(c);
    c = productOfPolynomials(a,b);
    printf("\nProduct is ");
    printPoly(c);
    printf("\n");
    freePoly(&a);
    freePoly(&b);
    freePoly(&c);
    return 0;
}
```

Sample Input/Output:

```
..ograming/C/CSL201/2020-11-16 ./polynomial.o

Enter polynomial 1 in the form : a0*X^n + a1*X^n-1 + a2*X^n-2 ..... an*X^0 --> 4X^2+5X+1

Enter polynomial 2 in the form : a0*X^n + a1*X^n-1 + a2*X^n-2 ..... an*X^0 --> 5X+4

Polynomial 1 is: 4*X^2 + 5*X^1 + 1*X^0

Polynomial 2 is: 5*X^1 + 4*X^0

Sum is 4*X^2 + 10*X^1 + 5*X^0

Product is 20*X^3 + 41*X^2 + 25*X^1 + 4*X^0

..ograming/C/CSL201/2020-11-16
```

```
..ograming/C/CSL201/2020-11-16 \rightarrow ./polynomial.o

Enter polynomial 1 in the form : a0*X^n + a1*X^n-1 + a2*X^n-2 ..... an*X^0 --> 12X^100+1

Enter polynomial 2 in the form : a0*X^n + a1*X^n-1 + a2*X^n-2 ..... an*X^0 --> 7X

Polynomial 1 is: 12*X^100 + 1*X^0

Polynomial 2 is: 7*X^1

Sum is 12*X^100 + 7*X^1 + 1*X^0

Product is 84*X^101 + 7*X^1

..ograming/C/CSL201/2020-11-16 \rightarrow

..ograming/C/CSL201/2020-11-16 \rightarrow
```