

---

# FIRST PRINCIPLES STUDIES OF $7 \times 7$ GRAPHENE SUPERLATTICES WITH TOPOLOGICAL DEFECTS AND TRANSITION METAL ADATOMS

---

**Sánchez Rolando**

School of Physical Sciences and Nanotechnology  
Yachay Tech University  
Urcuquí - Ecuador.  
rolando.sanchez@yachaytech.edu.ec

May 7, 2025

## ABSTRACT

Graphene's unique properties have made it a promising material for many emerging areas. However, the absence of a bandgap and magnetic attributes restricts its potential for application in nanoelectronics and spintronics. These properties can be significantly altered by topological defects, such as Flower-Like Defects (FLD), which can also offer insights into their efficient applicability in those fields. Previous studies show that FLD in  $5 \times 5$  and  $6 \times 6$  supercells remove the characteristic Dirac cone, while in  $7 \times 7$  supercells, the Dirac cone is recovered. Consequently, these findings prompt inquiries regarding the significance of defect size and symmetry in the electronic structure of graphene. This study examines the impact of FLD in  $7 \times 7$  supercells on the electronic properties of graphene and the additional modification of these properties by transition metal adatoms. Using density functional theory (DFT), we analyze changes in band structure, density of states, and magnetic properties.

**Keywords** Graphene · Flower-Like Defects · Density Functional Theory · Electronic Properties

## 1 Introduction

Graphene is one of the most fascinating materials known today. Its exceptional mechanical strength, thermal conductivity, and electron mobility make it a prime candidate for next-generation technologies. However, its lack of a bandgap and non-magnetic character significantly limit its application in areas like nanoelectronics and spintronics.

Previous studies carried out by our group investigated the effects of FLDs embedded in periodic graphene supercells. In these studies, it was observed that:

- In  $5 \times 5$  and  $6 \times 6$  supercells, FLDs disrupted the Dirac cone.
- But in  $7 \times 7$  supercells, the Dirac cone re-emerged.

Now, graphene's lack of a bandgap and magnetism limits its applications in several fields, including electronics and spintronics. Topological defects, such as flower-like defects (FLDs) observed via scanning tunneling microscopy (STM) [1], can modify these properties. One-dimensional extended defects also exhibit unique behaviors like one-dimensional conductivity [2]. A systematic study of graphene's structural, mechanical, electronic, and magnetic properties is crucial to overcoming these limitations. In this study, we investigate a hexagonal array of FLDs forming a  $7 \times 7$  superlattice to understand their influence on graphene's electronic properties.

## 2 Methodology

The calculations were performed using the Vienna Ab-initio Simulation Package (VASP) [3], employing the *R2SCAN+rvv10* functional [4]. Visualizations were generated using VESTA [5] as shown in Figure 1. We used a  $900\text{ eV}$  plane-wave cutoff and a k-point mesh spacing of  $0.022\text{ \AA}^{-1}$  for both pristine graphene and the  $7 \times 7$  FLD superlattice.

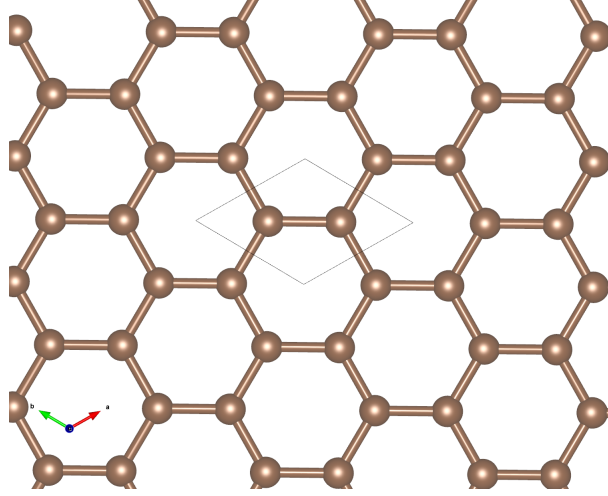


Figure 1: Graphical representation of pristine lattice.

### 2.1 Convergence Criteria

To ensure the accuracy of our calculations, we established convergence criteria of less than  $1\text{ meV}$  for the total energy per atom. This criterion was applied to the k-point mesh and the energy cutoff (ENCUT) as shown in Figure 2.

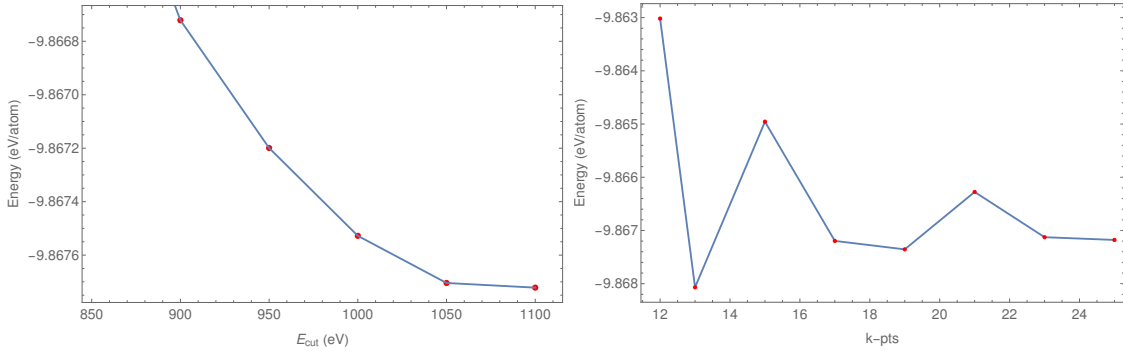


Figure 2: Convergence window of the total energy per atom with respect to the energy cutoff and number of k-points.

## 3 Results

### 3.1 Pristine Graphene

We began our analysis by examining pristine graphene, which serves as a reference for our study. The energy equation of state (EOS) for pristine graphene was obtained from Andrew, et al. [6], then our calculated data was fitted to it as shown in Figure 3. From here, we inferred mechanical properties such as the layer modulus, the force per unit length derivative, and the second derivative of the layer modulus as shown in Table 1.

Table 1: Mechanical properties of pristine graphene.

System	$a_{opt}$	$N_{atom}$	$\gamma$ (eV/Å <sup>2</sup> )	$\gamma'$	$\gamma''$ (Å <sup>2</sup> /eV)	$E_{gap}$
Pristine	2.454	2	13.51	4.47	-0.34	0

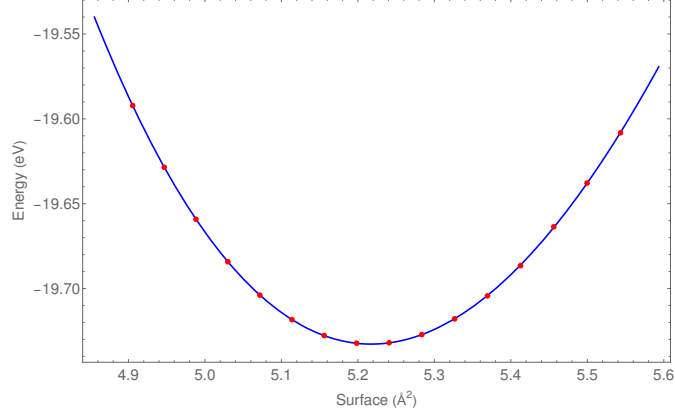


Figure 3: Fitted energy EOS for pristine graphene.

Then, we ran calculations on the band structure, density of states for pristine graphene, and create STM simulated images, as presented in Figure 4. We can observe the characteristic Dirac cone at the Fermi level and, in the partial density of states (PDOS) shown in Figure 5, the  $p_z$  being the only orbital contributing to near the Fermi level. These results are consistent with previous knowledge of pristine's electronic properties.

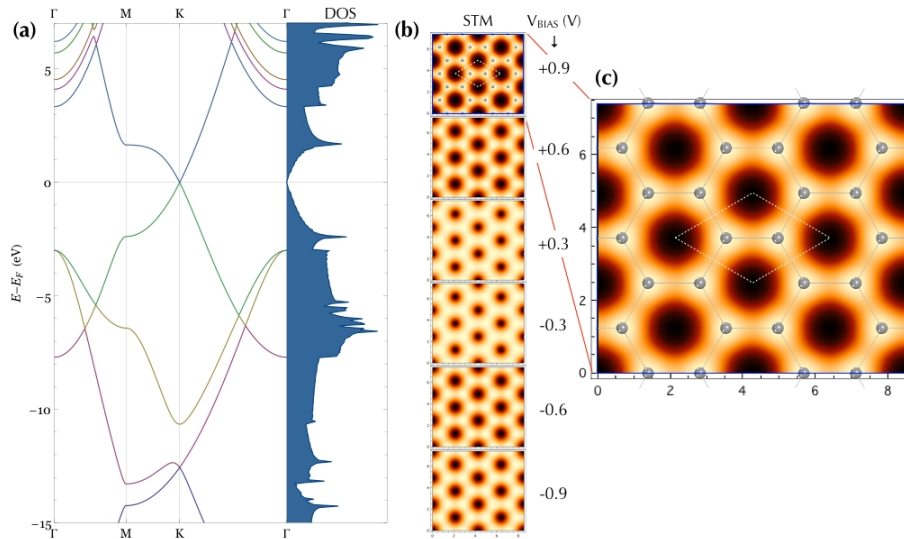


Figure 4: (a) Band Structure and Density of States (DOS) for pristine. (b, c) Simulated STM images for each corresponding VBIAS.

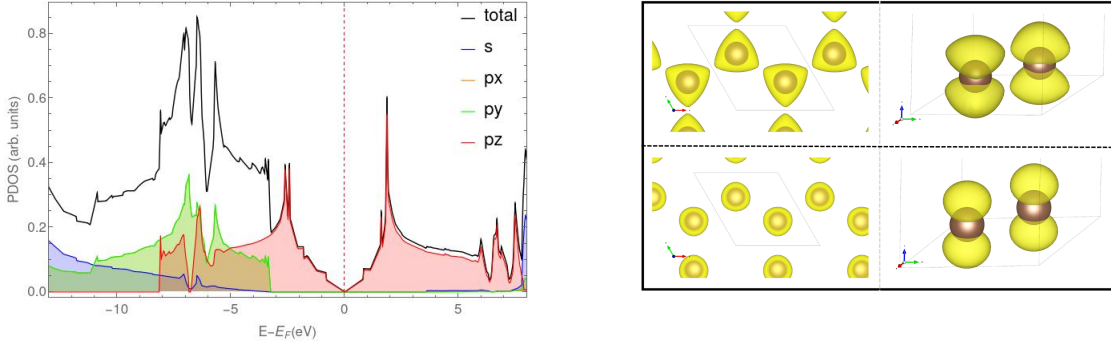


Figure 5: Left: PDOS for pristine graphene. Right: (Top) Isosurface images of partial charge density of last occupied band. (Bottom) Isosurface images of partial charge density of first unoccupied band.

### 3.2 $7 \times 7$ FLD Superlattice

Figure 6 presents the  $7 \times 7$  FLD superlattice structure. The corresponding energy–volume equation of state (EOS) fit is shown in Figure 7, and the derived mechanical properties are summarized in Table 2. The electronic band structure and partial density of states (PDOS) are depicted in Figure 8, while simulated scanning tunneling microscopy (STM) images under various bias voltages are presented in Figure 10.

From the calculated band structure and PDOS, the characteristic Dirac cone is clearly preserved, indicating that the semimetallic nature of graphene is maintained in the  $7 \times 7$  FLD superlattice. The PDOS further demonstrates that the states near the Fermi level are primarily derived from the  $p_z$  orbitals of the carbon atoms within the FLD regions, highlighting their dominant role in shaping the low-energy electronic structure.

To further investigate the spatial distribution of these electronic states, we computed the isosurface images of the partial charge density associated with the valence band maximum (VBM) and conduction band minimum (CBM), shown in Figure 9. The isosurface corresponding to the VBM reveals a noticeable localization of electronic density around the outer regions of the FLD, suggesting that the defect geometry modulates the spatial character of the occupied states. Finally, Figure 10 presents the computed STM image for the  $7 \times 7$  defect array under a bias voltage of  $V_{\text{bias}} = -0.3$  eV, offering a simulated topographic contrast consistent with the presence and periodicity of the FLD structures.

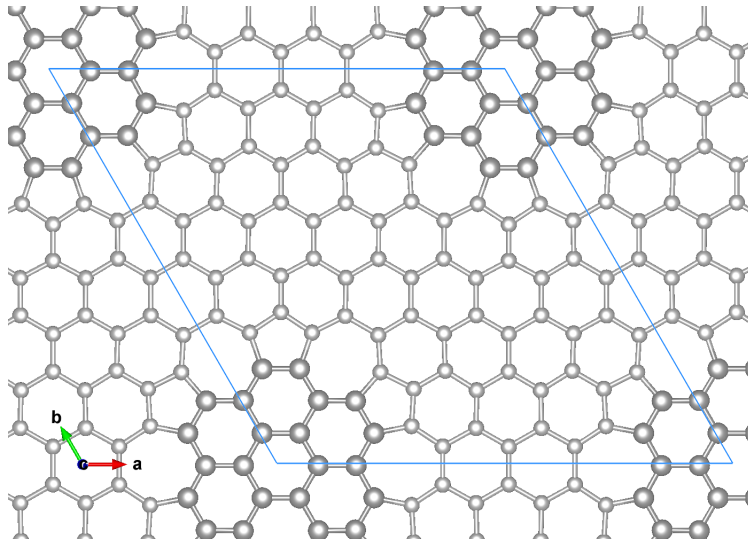


Figure 6: Graphical representation of the  $7 \times 7$  superlattice with FLDs. The highlighted spheres represent the FLD's carbon atoms.

Table 2: Mechanical properties of  $7 \times 7$  FLD superlattice.

System	$a_{opt}$	$N_{atom}$	$\gamma$ (eV/Å <sup>2</sup> )	$\gamma'$	$\gamma''$ (Å <sup>2</sup> /eV)	$E_{gap}$
$7 \times 7$	17.262	98	13.24	4.436	-0.35	0

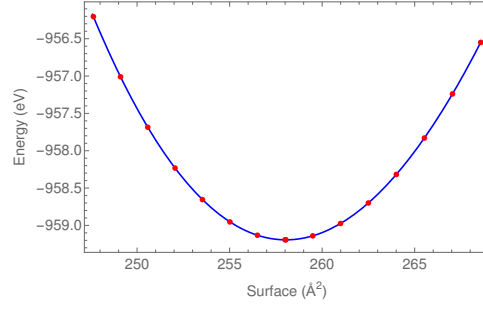
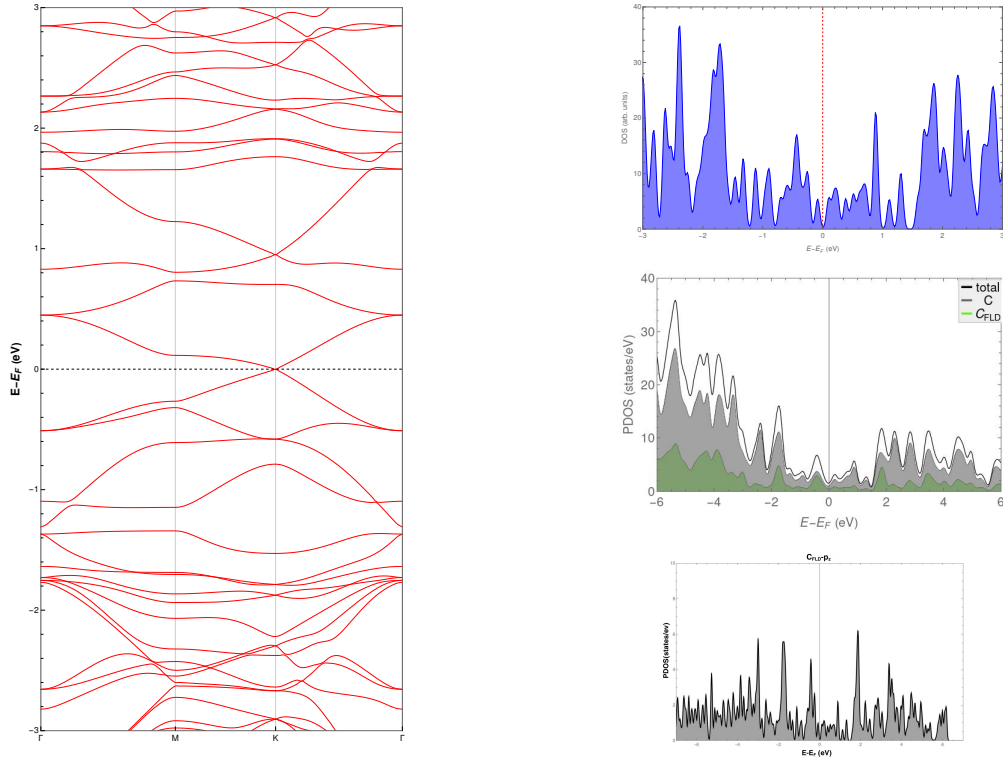


Figure 7: Fitted energy EOS for superlattice.

Figure 8: Left: Band structure of  $7 \times 7$  FLD superlattice. Right: (Top) Density of states (DOS), (Middle) Contribution of FLD carbon atoms to the density of states and (Bottom) Main contribution from  $p_z$  orbitals around Fermi level from the FLD carbon atoms.

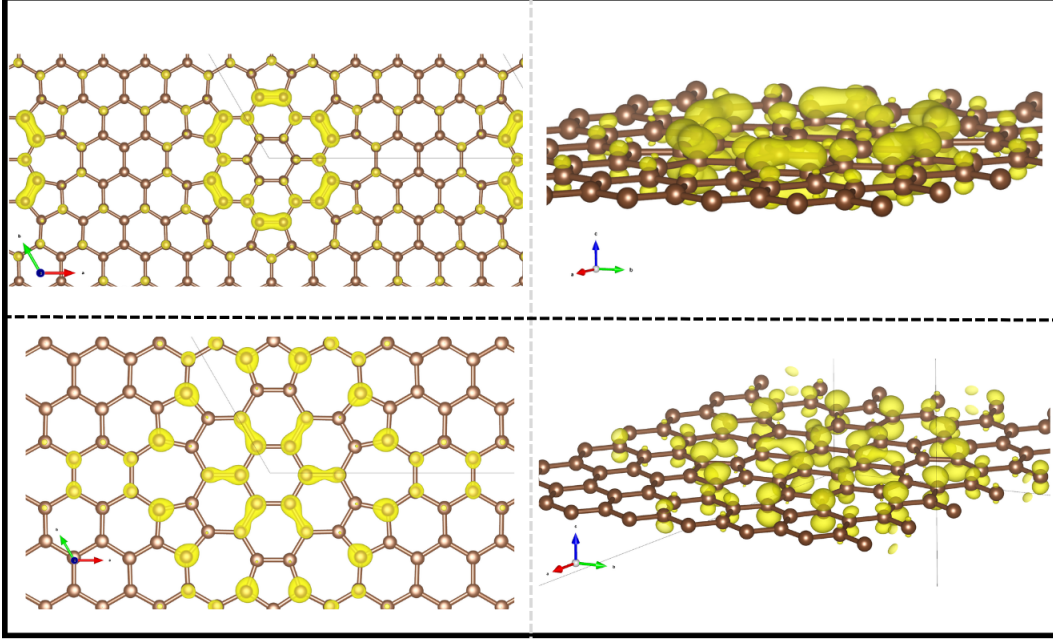


Figure 9: Top: Isosurface images of partial charge density of last occupied band. Bottom: Isosurface images of partial charge density of first unoccupied band.

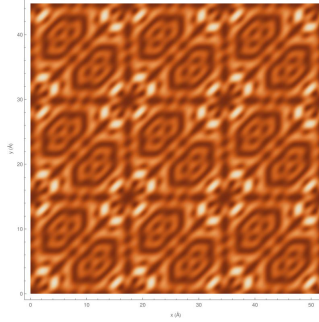


Figure 10: Simulated STM image of the  $7 \times 7$  FLD superlattice at a bias voltage of  $V_{\text{bias}} = -0.3$  eV.

## 4 Conclusion and Future Work

In this study, we have provided a detailed analysis of the electronic properties of a  $7 \times 7$  graphene superlattice containing topological defects, highlighting the preservation of its semimetallic character and the role of localized states around the Fermi level. Our findings contribute to the growing body of knowledge on how periodic defect patterns can be used to engineer the electronic behavior of graphene-based systems.

Future work will aim to extend this investigation by introducing atomic vacancies within the defect arrangement to explore their impact on electronic localization and potential magnetic behavior. Additionally, we plan to incorporate transition metal adatoms at various non-equivalent sites across the superlattice to study their influence on spin-dependent electronic properties and possible emergence of magnetic moments. Finally, we will investigate the effects of stacking an additional graphene layer in distinct non-equivalent configurations, with the goal of understanding interlayer coupling and its consequences for band structure modifications.

## References

- [1] E. Cockayne, G. M. Rutter, N. P. Guisinger, J. N. Crain, P. N. First, and J. A. Stroscio. Grain boundary loops in graphene. *Physical Review B*, 83(19):195425, 2011.

- [2] H. P. Pinto and J. Leszczynski. Fundamental properties of graphene. In F. D’Souza and K. M. Kadish, editors, *Handbook of Carbon Nanomaterials: Volume 5. Graphene—Fundamental Properties*, pages 1–37. World Scientific, 2014.
- [3] G. Kresse and J. Furthmüller. Efficiency of ab-initio total energy calculations for metals and semiconductors using a plane-wave basis set. *Computational Materials Science*, 6(1):15–50, 1996.
- [4] J. W. Furness, A. D. Kaplan, J. Ning, J. P. Perdew, and J. Sun. Accurate and numerically efficient r2scan meta-generalized gradient approximation. *Journal of Physical Chemistry Letters*, 11(19):8208–8215, 2020.
- [5] K. Momma and F. Izumi. Vesta 3 for three-dimensional visualization of crystal, volumetric and morphology data. *Journal of Applied Crystallography*, 44(6):1272–1276, 2011.
- [6] R. C. Andrew, R. E. Mapasha, A. M. Ukpong, and N. Chetty. Mechanical properties of graphene and boronitrene. *Physical Review B - Condensed Matter and Materials Physics*, 85:125428, 3 2012.