CLASSIFICATION VIA QUANTUM MACHINE LEARNING

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ABSTRACT

Classification is a key component of various scientific, technological and industrial domains, from biomedical diagnostics and computational materials science to finance, climate modeling, and sociology. However, classical machine learning (ML) approaches often face limitations in computational efficiency, especially for high-dimensional and complex datasets, where quantum computing has been proposed as a promising breakthrough. Quantum machine learning (QML) has recently attracted much interest, intending to leverage the potential of quantum computing to achieve computational advantages over classical methods. Notable quantum algorithms, such as the Harrow-Hassidim-Lloyd (HHL) solver for linear systems and Shor's algorithm for integer factorization, demonstrate exponential speedups for specific tasks, suggesting the potential of quantum computing to revolutionize the computational landscape. In this mini-review, we explore the current state of the art of quantum classification algorithms, focusing on quantum support vector machines (OSVMs) and Quantum Neural Networks (QNNs), their implementations using the Qiskit software framework and their performance. By critically evaluating their advantages and limitations, we evaluate whether QML represents a transformative paradigm or remains constrained by challenges in hardware, scalability, and decoherence. Finally, we will highlight the role of hybrid classical-quantum approaches and the advancements needed to realize quantum-enhanced classification in practical applications.

Introduction

Classification is probably the most essential component of any activity, regardless of whether it is for scientific purposes. Its wide-ranging applications include finance [1], climate modelling [2], medical diagnostics [3], computational materials science [4], sociology [5] and human behaviour itself [6]. Data is categorized into distinct groups to generate precise predictive models through classification. Typically, these issues are grouped into two primary categories: binary classification and multi-class classification. The binary classification process entails dividing data into two categories, such as identifying spam versus non-spam emails or differentiating between cancerous and non-cancerous tissues in medical diagnosis. In contrast, multi-classification encompasses additional categories, such as identifying skin lesion types associated with cancerous conditions [7].

ML is a branch of computer science focused on identifying patterns in data attributes to make predictions about previously unseen inputs. It involves creating algorithms that enable computers to learn from data and make decisions autonomously, without being explicitly programmed for specific tasks. These algorithms are generally categorized into three main types: supervised, unsupervised, and reinforcement learning [8].

Supervised learning relies on a labeled training dataset, where input-output relationships are clearly defined, allowing the algorithm to learn and classify new data based on these examples. Unsupervised learning, on the other hand, aims to uncover hidden structures, clusters, or groupings within unlabeled data [9]. In both cases, the core task is pattern classification, which involves assigning new input data to predefined categories or classes.

Reinforcement learning, which mimics aspects of human learning, operates within a framework of rules and objectives. Here, the algorithm receives rewards or penalties based on the actions it takes to achieve a goal. Rewards reinforce successful strategies, while penalties prompt adjustments to improve decision-making. While reinforcement learning is a powerful approach, this work will not focus on it, as the primary application under review is classification.

A significant challenge in ML is the computational time and storage required, especially when dealing with large datasets. Additionally, training these models is time-intensive as the main challenges lie in the problem of finding the right parameters that lead to an optimal solution. To address these limitations, researchers have turned to quantum computing as a promising alternative. Quantum methods have the potential to significantly reduce both storage requirements and computational time, offering a new direction for overcoming the constraints of classical approaches [10].

The most noticeable advantage of quantum computing is the ability of manipulate quantum states in superposition in order to speed up computational tasks in terms of complexity, as these operations would be executed on many states at the same time. In a formal way, quantum computers surpass classical ones by using qubits, which exist in an exponentially larger space, $\mathbb{SU}(2^n)$, compared to classical bits in Boolean space, $\mathbb{B}^{\otimes n}$. While an n-bit classical register holds one n-digit binary string, a quantum register of the same size can represent all possible strings simultaneously, offering an exponential advantage [11]. Then, quantum algorithms are developed such that the modified quantum state has a high amplitude for states representing solutions for a given problem. However, while quantum supremacy has been demonstrated for specific problems [12], achieving it in data science remains uncertain, even theoretically. Nonetheless, this is a key objective in QML.

Usually, QML is considered for four main tasks as shown in Fig.1, where CC tasks refers to classical computers using quantum computing inspired algorithms to process classical data, such as recommendation system algorithms [13]. CQ refers to processing classical data using QML algorithms [14]. QC setting asks how classical learning techniques may help in quantum tasks and this is an active area of investigation, with classical machine learning algorithms used in many areas in the quantum computing, such as qubit characterization [15], control [16] and readout[17]. Finally, QQ, a field remaining in its early stages, involves the processing of quantum data with quantum machine learning algorithms, for instance, analyzing molecular ground state energy directly in quantum computers using QML to optimize processes.

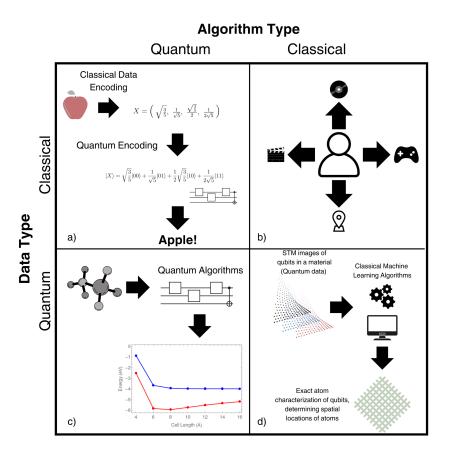


Figure 1: QML tasks from different perspectives. a) QC. b) CC. c) QQ. d) CQ.

In this work, we provide a comprehensive review of the current state of quantum classification algorithms, specifically emphasizing the implementation of QSVMs and QNNs. We critically assess the potential of these algorithms to revolutionize classification tasks in practical applications by evaluating their advantages and limitations. This work aims to determine whether QML is a transformative paradigm or if existing technological challenges still constrain it by analyzing the interaction between quantum computing and machine learning. In Table 1 and Figure 2 we provide an overview of the topics covered in this work, as well as the relevant literature reviewed.

Table 1.	Overview	of quantum	machine	learning	classification	methods
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Method	Key Idea	Algorithm	Hardware	References
Quantum k-Nearest Neighbors (QkNN)	Quantum state overlap for distance metrics	Grover-based search, State fidelity	Gate-based	
Quantum Neural Networks (QNNs)	Parametrized quantum cir- cuits as classifiers	Variational circuits, Backpropagation	NISQ devices	
Quantum Decision Trees	Superposition for parallel split evaluation	Amplitude amplification	Gate- based/Annealing	
Quantum SVM (QSVM)	Quantum kernels for high-dim spaces	HHL algorithm, Kernel estimation	Gate-based + QRAM	
Variational Quantum Classifiers (VQC)	Hybrid quantum-classical optimization	Parameter optimization loops	NISQ devices	

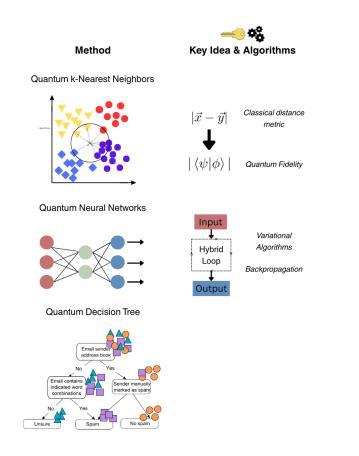


Figure 2: Overview of quantum machine learning classification methods

Quantum Classification Algorithms

Quantum k-nearest neighbours

The classical k-nearest neighbours algorithm assigns a class to an unclassified object by comparing its vector \vec{v} to previously classified training samples. This is done using a distance metric, typically Euclidean or Hamming distance, to identify the k-nearest neighbours in the multidimensional space. The steps of the algorithm can be summarized as follows:

- 1. Choose a distance metric and compute the distance between the unclassified object vector \vec{v} and each training sample.
- 2. Identify the k training samples closest to \vec{v} based on the chosen metric.
- 3. Assign the class with the highest frequency among the k nearest samples to the object \vec{v} .

This approach relies on the assumption that objects close to each other in the multidimensional space share similar properties. Now, the most expensive step in these algorithms is determining the distance between the test sample and the train states and by the aforementioned properties of quantum computing, this task is a good instance to use QML. Translating this concept into a quantum framework requires redefining distance metrics in quantum terms and consider the fidelity or overlap $|\langle x|y\rangle|$ as a measure of similarity between states.

Then, building on the data representation proposed by Lloyd et al. [18], as shown in Eq. 1, to evaluate the distance from a given $\vec{x} \in \mathbb{R}^N$ to the centroid of a given set V_j , $\vec{y_j}$, one can calculate the inner product of the state $|\psi\rangle = \frac{\sqrt{2}}{Z}(|0,x\rangle + |1,y_j\rangle)$, constructed for the system qubits and an adjoined ancilla, with the state $|\phi\rangle = \frac{\sqrt{Z}}{Z}(|\vec{x}|\,|0\rangle - |\vec{y_j}|\,|1\rangle)$, where $Z = |\vec{x}|^2 + |\vec{y_j}|^2$ ensures normalization. This leads to the identity in Eq. 2, which provides a way to compute the distance between the vectors.

$$|x\rangle = |x|^{-\frac{1}{2}}\vec{x} \tag{1}$$

$$|\vec{x} - \vec{y}|^2 = Z |\langle \psi | \phi \rangle|^2 \tag{2}$$

The overlap $|\langle \psi | \phi \rangle|^2$ in Eq. 2 can be physically retrieved using a routine known as the swap test [19] show in Figure 3, performing a projection on the ancilla alone. The probability of measuring the initial state $|\xi\rangle = |x,y_j,0_{anc}\rangle$ in this test is given by Eq. 3, where the overlap appears explicitly.

$$P(|\xi\rangle) = \frac{1 + |\langle\psi|\phi\rangle|^2}{2} \tag{3}$$

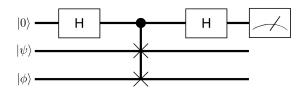


Figure 3: Swap Circuit

The authors argue that this quantum method, including the construction of quantum states, achieves greater efficiency than the classical polynomial runtime while preserving quantum coherence during the state creation. Using these principles, a quantum version of the nearest centroid algorithm can be constructed. Here, \vec{x} represents the sample to be classified, and $\vec{y_j} = \frac{\sum_p \vec{v_j}^p}{N_j}$ is the centroid of the given class V_j .

Quantum Neural Networks (QNNs)

Classical neural networks (NNs) are computational models inspired by biological neurons, processing input data through layered architectures of interconnected nodes to produce a desired classification output. As illustrated in Fig. 4, these models adjust their parameters via backpropagation to minimize a predefined loss function, optimizing their predictive

performance through iterative training. On the other hand, QNNs are a specialized subclass of variational quantum algorithms, implemented using parameterized quantum circuits. These circuits employ tunable unitary rotation gates and entangling operations to perform numerical tasks such as optimization, approximation, and classification [20].

The operational workflow of a common QNN involves the stages shown in Fig. 4. First, classical input data is encoded into a quantum state using a feature map [21], initializing the qubit register. Next, a variational circuit transforms this initial encoded quantum state across multiple layers. The final quantum state is then measured by evaluating the expectation value of a Hamiltonian operator, typically represented by Pauli gates [22]. These quantum measurements are decoded into classical outputs, which are used to compute the loss function. The variational parameters are optimized to minimize this loss, analogous to classical training but within a quantum computational framework. This hybrid structure positions QNNs at the intersection of classical deep learning and parameterized quantum circuits, offering potential advantages in certain machine learning tasks while remaining subject to ongoing research and design refinements. [23].

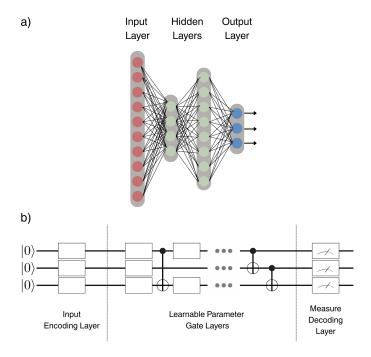


Figure 4: a) Main components of classical neural networks. b) Components in proposed ONN

Now, the previously described QNN structure is usually modified to match the specific needs of the problem. For instance, the feature map can be done in different ways like basis encoding, amplitude encoding, product encoding, angle encoding, etc. In a similar way, the variational quantum algorithm will be designed according to the problem and there are several ways to do it [24]. It has been demonstrated that Quantum Neural Networks (QNNs), implemented as variational quantum circuits with classical optimizers for tuning the parameters, can outperform NNs on relatively small datasets, despite their significantly lower complexity and fewer parameters [25]. For instance, QNNs achieved an average accuracy improvement of 7% over classical NNs in experiments, even with orders of magnitude fewer parameters. These advantages were also noticed in medical image classification [7, 26]. However, these advantages were observed under the constraints of current noisy intermediate-scale quantum (NISQ) hardware, which limits problem sizes due to qubit counts and error rates. As quantum hardware advances, it is expected that QNNs will scale to larger problem sizes, though challenges such as error mitigation, circuit depth limitations, and optimal entanglement strategies must first be addressed.

Quantum Decision Trees (QDTs)

References

[1] Jasmina Smailović, Miha Grčar, Nada Lavrač, and Martin Žnidaršič. Stream-based active learning for sentiment analysis in the financial domain. *Information Sciences*, 285:181–203, 2014. Processing and Mining Complex Data Streams.

- [2] C. O. de Burgh-Day and T. Leeuwenburg. Machine learning for numerical weather and climate modelling: a review. *Geoscientific Model Development*, 16(22):6433–6477, 2023.
- [3] Bradley J. Erickson, Panagiotis Korfiatis, Zeynettin Akkus, and Timothy L. Kline. Machine learning for medical imaging. *RadioGraphics*, 37(2):505–515, 2017. PMID: 28212054.
- [4] Yue Liu, Tianlu Zhao, Wangwei Ju, and Siqi Shi. Materials discovery and design using machine learning. *Journal of Materiomics*, 3(3):159–177, 2017. High-throughput Experimental and Modeling Research toward Advanced Batteries.
- [5] Giovanni Di Franco and Michele Santurro. Machine learning, artificial neural networks and social research. 55:1007–1025, 2021.
- [6] Blake A. Richards, Timothy P. Lillicrap, Philippe Beaudoin, Yoshua Bengio, Rafal Bogacz, Amelia Christensen, Claudia Clopath, Rui Ponte Costa, Archy de Berker, Surya Ganguli, Colleen J. Gillon, Danijar Hafner, Adam Kepecs, Nikolaus Kriegeskorte, Peter Latham, Grace W. Lindsay, Kenneth D. Miller, Richard Naud, Christopher C. Pack, Panayiota Poirazi, Pieter Roelfsema, João Sacramento, Andrew Saxe, Benjamin Scellier, Anna C. Schapiro, Walter Senn, Greg Wayne, Daniel Yamins, Friedemann Zenke, Joel Zylberberg, Denis Therien, and Konrad P. Kording. A deep learning framework for neuroscience. Nature Neuroscience 2019 22:11, 22:1761–1770, 10 2019.
- [7] S. Sofana Reka, H. Leela Karthikeyan, A. Jack Shakil, Prakash Venugopal, and Manigandan Muniraj. Exploring quantum machine learning for enhanced skin lesion classification: A comparative study of implementation methods. *IEEE Access*, 12:104568–104584, 2024.
- [8] Taiwo Oladipupo Ayodele. Types of machine learning algorithms. In Yagang Zhang, editor, *New Advances in Machine Learning*, chapter 3. IntechOpen, Rijeka, 2010.
- [9] Vratika Gupta, Vinay Kumar Mishra, Priyank Singhal, and Amit Kumar. An overview of supervised machine learning algorithm. In 2022 11th International Conference on System Modeling & Advancement in Research Trends (SMART), pages 87–92, Dec 2022.
- [10] Siddhartha Bhattacharyya. 1. Introduction to quantum machine learning degruyter.com. https://www.degruyter.com/document/doi/10.1515/9783110670707-001/html?lang=en&srsltid= AfmBOooSaEWc-Lhu5Q72P5vuHWm_Y-YgM6DHeMRsIa9RGnSxPbyiBfNP. [Accessed 09-03-2025].
- [11] Michael A. Nielsen and Isaac L. Chuang. *Quantum Computation and Quantum Information: 10th Anniversary Edition.* Cambridge University Press, 2010.
- [12] Frank Arute, Kunal Arya, Ryan Babbush, Dave Bacon, Joseph C. Bardin, Rami Barends, Rupak Biswas, Sergio Boixo, Fernando G.S.L. Brandao, David A. Buell, Brian Burkett, Yu Chen, Zijun Chen, Ben Chiaro, Roberto Collins, William Courtney, Andrew Dunsworth, Edward Farhi, Brooks Foxen, Austin Fowler, Craig Gidney, Marissa Giustina, Rob Graff, Keith Guerin, Steve Habegger, Matthew P. Harrigan, Michael J. Hartmann, Alan Ho, Markus Hoffmann, Trent Huang, Travis S. Humble, Sergei V. Isakov, Evan Jeffrey, Zhang Jiang, Dvir Kafri, Kostyantyn Kechedzhi, Julian Kelly, Paul V. Klimov, Sergey Knysh, Alexander Korotkov, Fedor Kostritsa, David Landhuis, Mike Lindmark, Erik Lucero, Dmitry Lyakh, Salvatore Mandrà, Jarrod R. McClean, Matthew McEwen, Anthony Megrant, Xiao Mi, Kristel Michielsen, Masoud Mohseni, Josh Mutus, Ofer Naaman, Matthew Neeley, Charles Neill, Murphy Yuezhen Niu, Eric Ostby, Andre Petukhov, John C. Platt, Chris Quintana, Eleanor G. Rieffel, Pedram Roushan, Nicholas C. Rubin, Daniel Sank, Kevin J. Satzinger, Vadim Smelyanskiy, Kevin J. Sung, Matthew D. Trevithick, Amit Vainsencher, Benjamin Villalonga, Theodore White, Z. Jamie Yao, Ping Yeh, Adam Zalcman, Hartmut Neven, and John M. Martinis. Quantum supremacy using a programmable superconducting processor. *Nature* 2019 574:7779, 574(7779):505–510, oct 2019.
- [13] Ewin Tang. A quantum-inspired classical algorithm for recommendation systems. In *Proceedings of the 51st Annual ACM SIGACT Symposium on Theory of Computing*, STOC 2019, page 217–228, New York, NY, USA, 2019. Association for Computing Machinery.
- [14] Esma Aïmeur, Gilles Brassard, and Sébastien Gambs. Quantum speed-up for unsupervised learning. *Machine Learning*, 90(2):261–287, feb 2013.
- [15] Muhammad Usman, Yi Zheng Wong, Charles D. Hill, and Lloyd C.L. Hollenberg. Framework for atomic-level characterisation of quantum computer arrays by machine learning. *npj Computational Materials* 2020 6:1, 6(1):1–8, mar 2020.
- [16] Murphy Yuezhen Niu, Sergio Boixo, Vadim N. Smelyanskiy, and Hartmut Neven. Universal quantum control through deep reinforcement learning. *npj Quantum Information* 2019 5:1, 5(1):1–8, apr 2019.
- [17] Easwar Magesan, Jay M. Gambetta, A. D. Córcoles, and Jerry M. Chow. Machine Learning for Discriminating Quantum Measurement Trajectories and Improving Readout. *Physical Review Letters*, 114(20):200501, may 2015.

- [18] Seth Lloyd, Masoud Mohseni, Patrick Rebentrost, Seth Lloyd, Masoud Mohseni, and Patrick Rebentrost. Quantum algorithms for supervised and unsupervised machine learning. *arXiv*, page arXiv:1307.0411, 2013.
- [19] Harry Buhrman, Richard Cleve, John Watrous, and Ronald de Wolf. Quantum fingerprinting. *Physical Review Letters*, 87:167902, 9 2001.
- [20] Yunseok Kwak, Won Joon Yun, Soyi Jung, and Joongheon Kim. Quantum neural networks: Concepts, applications, and challenges, 2021.
- [21] Hyeokjea Kwon, Hojun Lee, and Joonwoo Bae. Feature map for quantum data in classification, 2024.
- [22] Edward Farhi and Hartmut Neven. Classification with quantum neural networks on near term processors, 2018.
- [23] Quantum Neural Networks Qiskit Machine Learning 0.8.2 qiskit-community.github.io. https://qiskit-community.github.io/qiskit-machine-learning/tutorials/01_neural_networks.html. [Accessed 26-03-2025].
- [24] Yunseok Kwak, Won Joon Yun, Soyi Jung, and Joongheon Kim. Quantum neural networks: Concepts, applications, and challenges. In 2021 Twelfth International Conference on Ubiquitous and Future Networks (ICUFN), pages 413–416, 2021.
- [25] Ricardo Daniel Monteiro Simões, Patrick Huber, Nicola Meier, Nikita Smailov, Rudolf M. Füchslin, and Kurt Stockinger. Experimental evaluation of quantum machine learning algorithms. *IEEE Access*, 11:6197–6208, 2023.
- [26] Dong Yumin, Mingqiu Wu, and Jinlei Zhang. Recognition of pneumonia image based on improved quantum neural network. *IEEE Access*, 8:224500–224512, 2020.