



Set 9: Image Compression

Lecturer Arto Kaarna

Lappeenranta University of Technology (LUT)
School of Engineering Science (LENS)
Machine Vision and Pattern Recognition (MVPR)

Arto.Kaarna@lut.fi

<http://www.lut.fi/web/en/school-of-engineering-science/research/machine-vision-and-pattern-recognition>



Contents

- Introduction and Background
- Image Coding
- Image Compression
- Wavelet Transform



Introduction

- Data compression is a process of reducing the amount of data required to represent the given information.
- Data redundancy is a central issue in image compression.

$$R_D = 1 - \frac{1}{C_R}, C_R = \frac{n_1}{n_2} = \frac{\text{original}}{\text{compressed}}$$

- If $n_1 = n_2, C_R = 1$ and $R_D = 0$ *no redundancy*
 - If $n_1 \gg n_2, C_R \rightarrow \infty$ and $R_D \rightarrow 1$ *high redundancy*
 - If $n_1 \ll n_2, C_R \rightarrow 0$ and $R_D \rightarrow -\infty$ *undesirable*
-
- Redundancy types: coding, interpixel (spatial), psychovisual redundancies



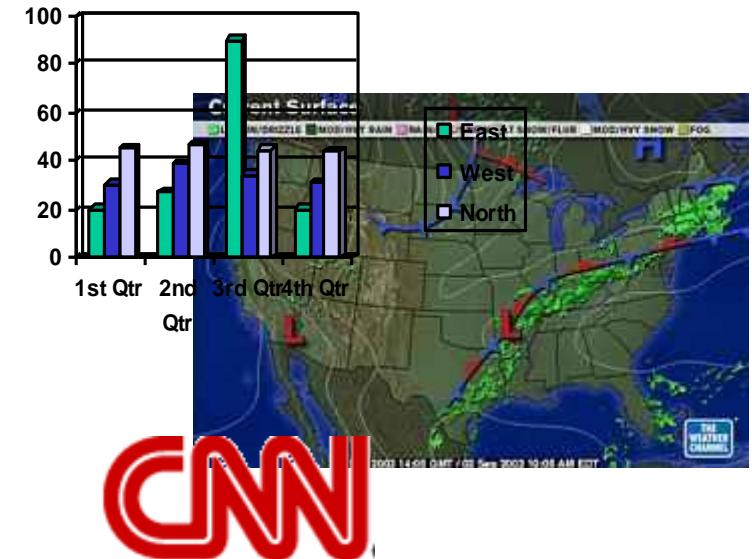
Introduction

- 1) Storage: local, cloud, services
- 2) Transmission: wired/wireless, application?
- 3) Data access, 1990 -> 201x
 - Capacities : 100MB -> TeraBytes
 - Seek time : 15 milliseconds -> 10 milliseconds
 - Transfer rate: 1MB/sec -> 1 GB/sec
 - Price \$/MB : 4 -> 0.0000283
 - Compression improves overall response time in some applications



Background: Digital Data

- Everyday an enormous amount of information need to be stored, processed, and transmitted
- Sources of data: multiple, e.g.
 - Financial data,
 - Reports, Inventory,
 - Cable TV,
 - Online Ordering and tracking
- Processing of Digital Data
 - Coding, compression
 - Data analytics: patterns, classes/clusters





Background: Data from Imaging

- Sources
 - Digital camera, video camera
 - Image scanner
 - Ultra-sound (US), Computer Tomography (CT), Magnetic resonance image (MRI), digital X-ray (XR), Infrared
 - Etc.
- Application areas, e.g.
 - Medical imaging
 - Remote sensing
 - Consumer applications: digital TV, mobile terminals, etc.



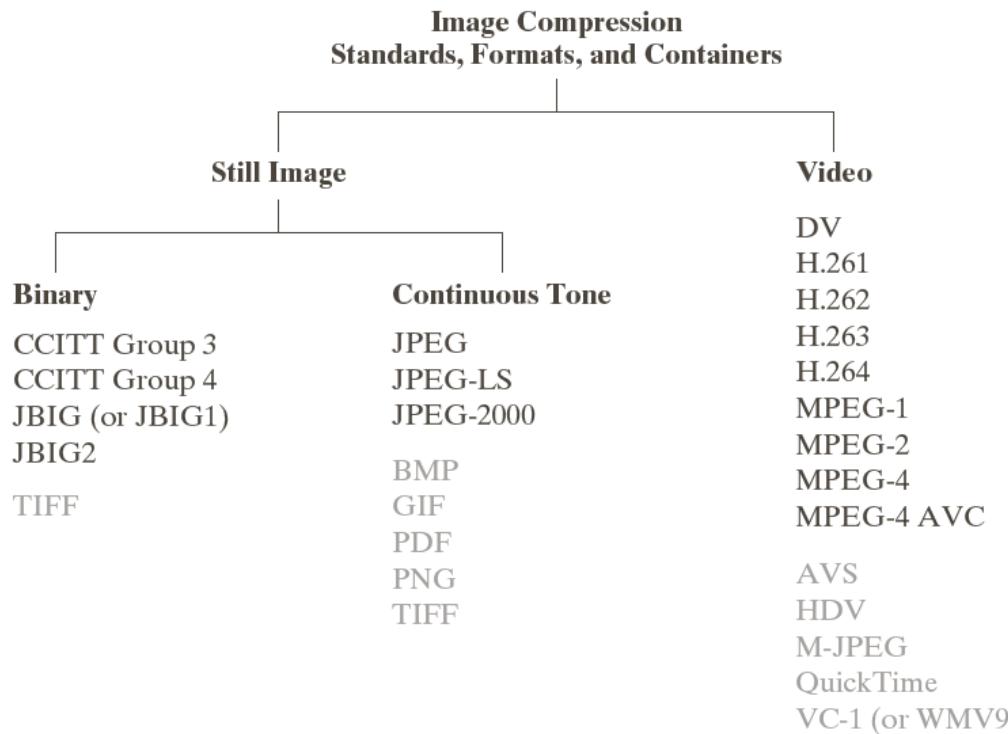
Basic Concepts: Data Rates

- Still images:
 - One page of A4 format at 600 dpi is > 100 MB
 - One color image in a digital camera generates 10-30 MB
 - Scanned 3"×7" photograph at 300 dpi is 30 MB
- Digital TV, HDTV/4K/8K
 - Resolutions: 1920×1080/3840×2160/7680×4320
 - Bitplanes: 8-12, Frame rate: 30-300
- Digital cinema $4K \times 2K \times 3 \times 12 \text{ bits/pel} = 48 \text{ MB/frame}$ or 1 GB/sec or 70 GB/min
- Spectral images: $n * m * p * r$, per satellite per day, multiple scanners, continuous scanning



Compression standards

- Still images and video sequences



© 1992–2008 R. C. Gonzalez & R. E. Woods



Basic Concepts

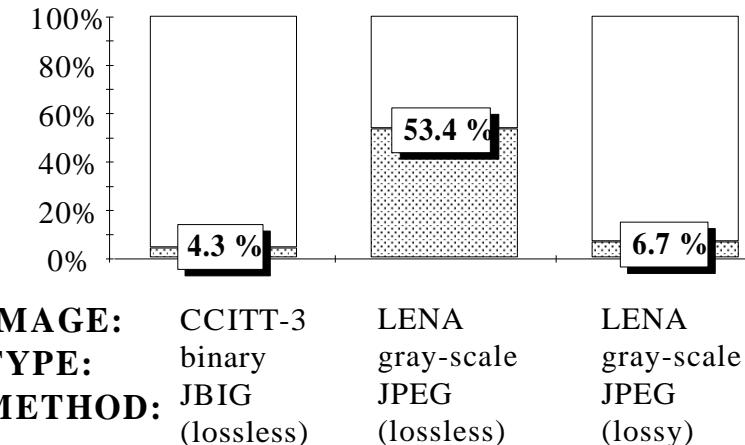
- Why do we need to compress images?
- Image types
- Parameters of digital images
- Lossless vs. lossy compression
- Quality measures: rate, distortion, computational, perceptual, etc.
- Compression is an enabling technology for HDTV, mobile communications, etc.





Basic Concepts: Approaches

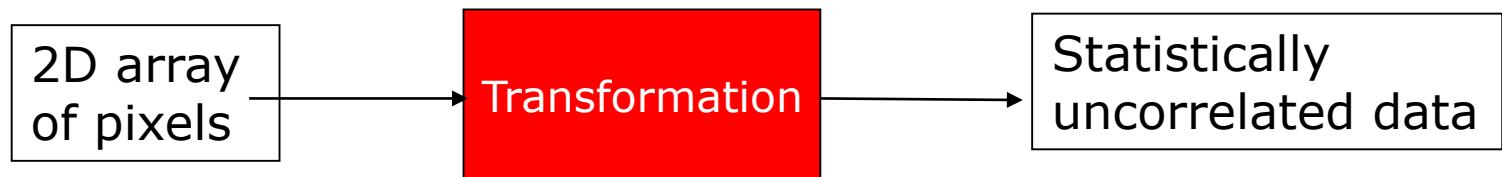
- Lossless compression: reversible, information preserving
 - text compression algorithms,
 - binary images, palette images.
- Lossy compression: irreversible
 - grayscale, color, video.
- Near-lossless compression:
 - medical imaging, remote sensing.





Basic Concepts: Approaches

- Data compression is the art and science of representing information in a compact form: we want to remove redundancy from the data

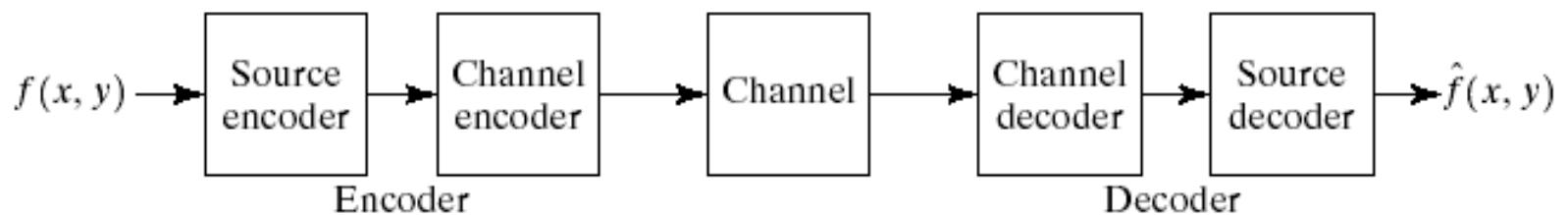


- Data is a sequence of symbols taken from a discrete alphabet
- Still image data: a collection of 2-D arrays (one for each color plane) of values representing intensity (color) of the point in corresponding spatial location (pixel)



Basic Concepts: Approaches

- The coding depends both on the source and for the channel



- The source encoder is responsible for removing redundancy (coding, inter-pixel, psycho-visual)
- The channel encoder ensures robustness against channel noise or other errors.

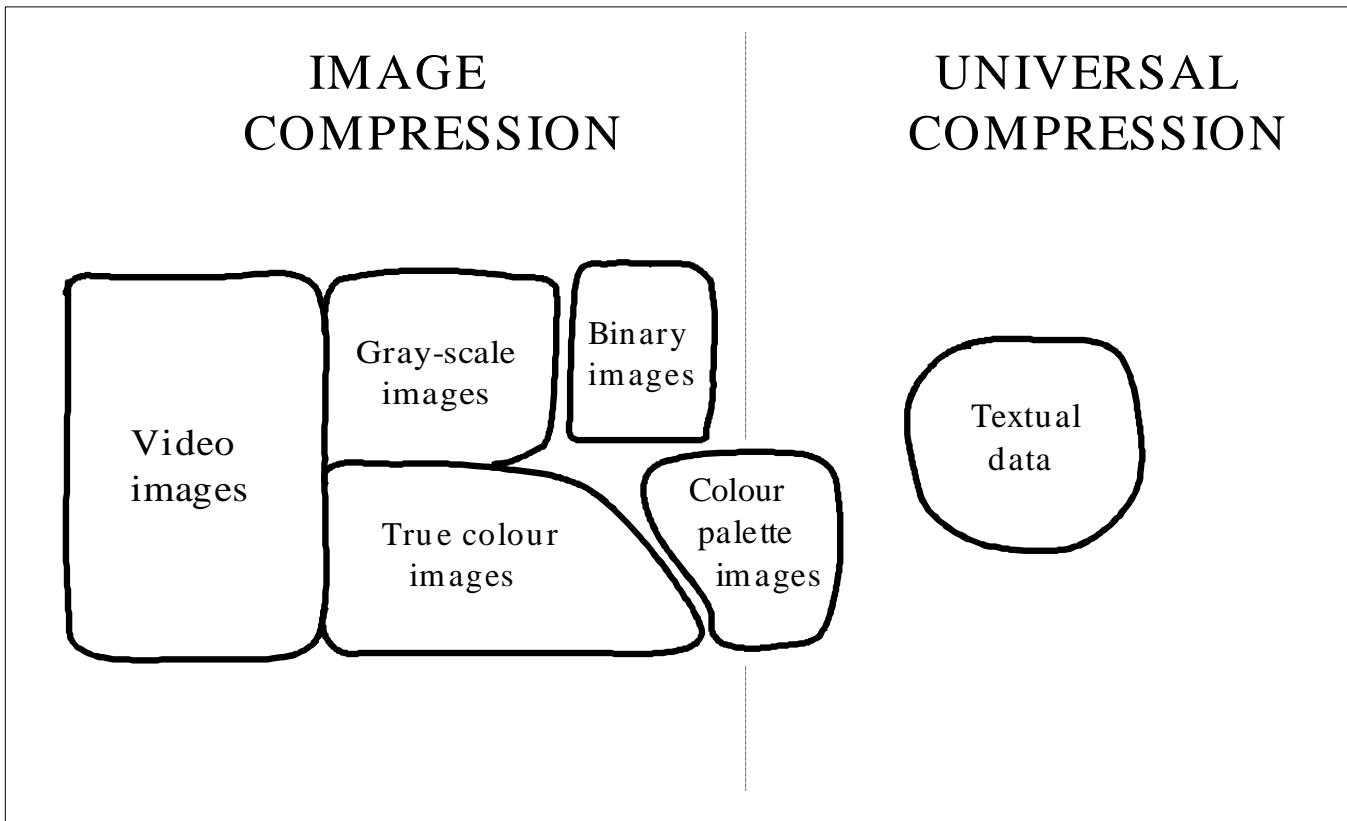


Basic Concepts: Approaches

- Statistical redundancy:
 1. Spatial correlation
 - a) Local: pixels at neighboring locations have similar intensities
 - b) Global: reoccurring patterns
 2. Spectral correlation – between color planes
 3. Temporal correlation – between consecutive frames (for videos, store only the parts that change)
- Tolerance to fidelity:
 1. Perceptual redundancy
 2. Limitation of rendering hardware



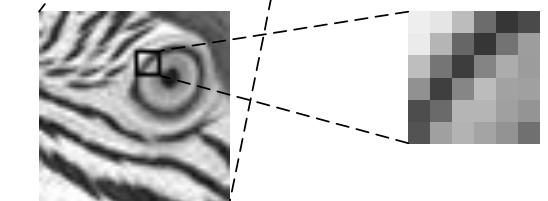
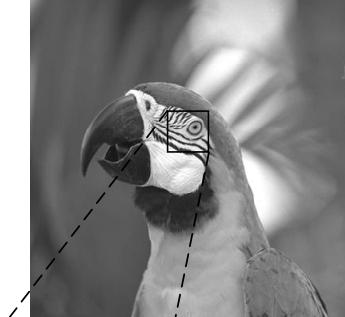
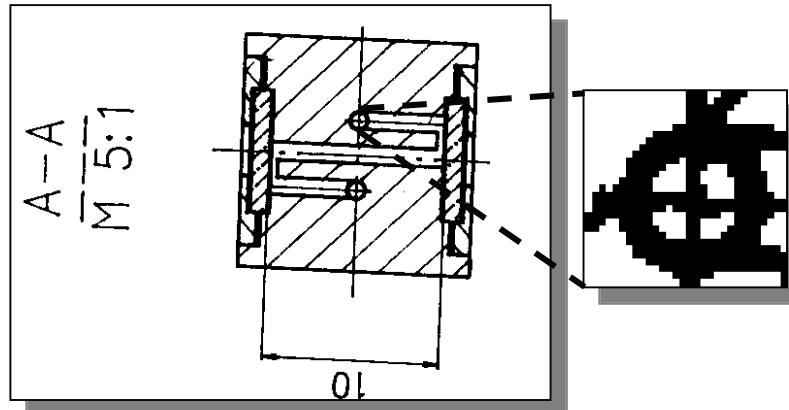
Basic Concepts: Approaches



- Why specific algorithms for images are needed?



Basic Concepts: Image types



Y-U-V components





Basic Concepts: Color

$$Y = 0.3 \cdot R + 0.6 \cdot G + 0.1 \cdot B$$

$$U = B - Y$$

$$V = R - Y$$

R, G, B -- red, green, blue

Y -- the luminance

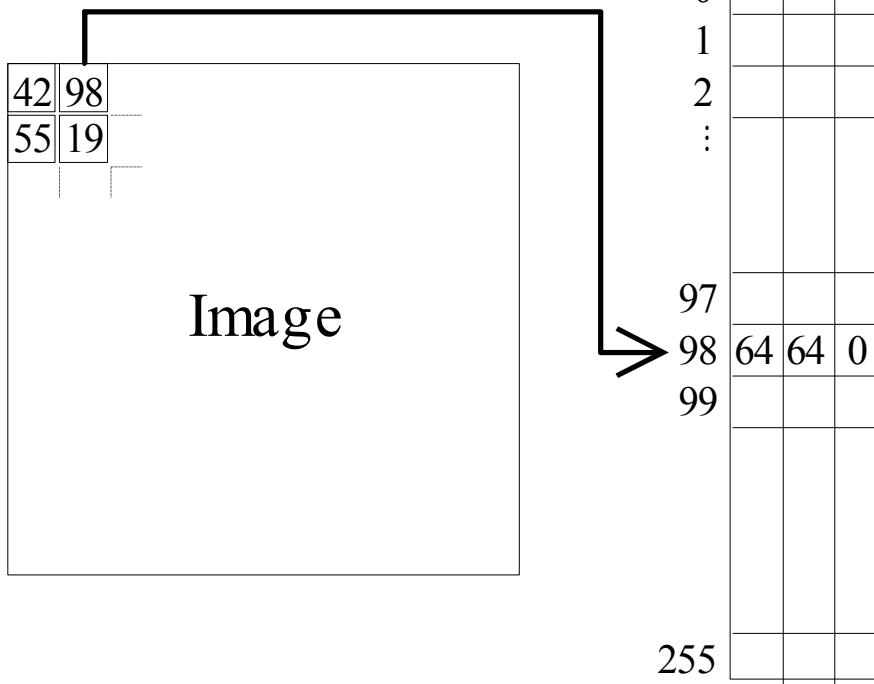
U, V -- the chrominance components

Most of the information is collected to the Y component, while the information content in the U and V is less.



Look-up Tables in Compression

- Benefits, limitations?



RGB look-up-table

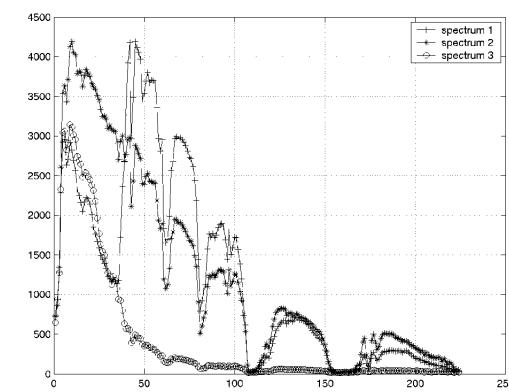
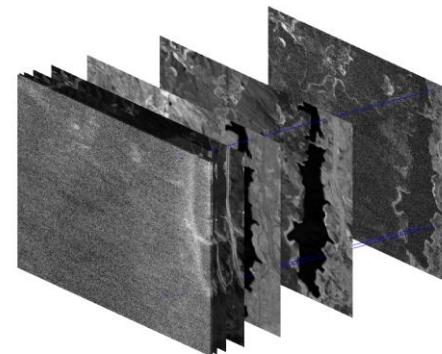
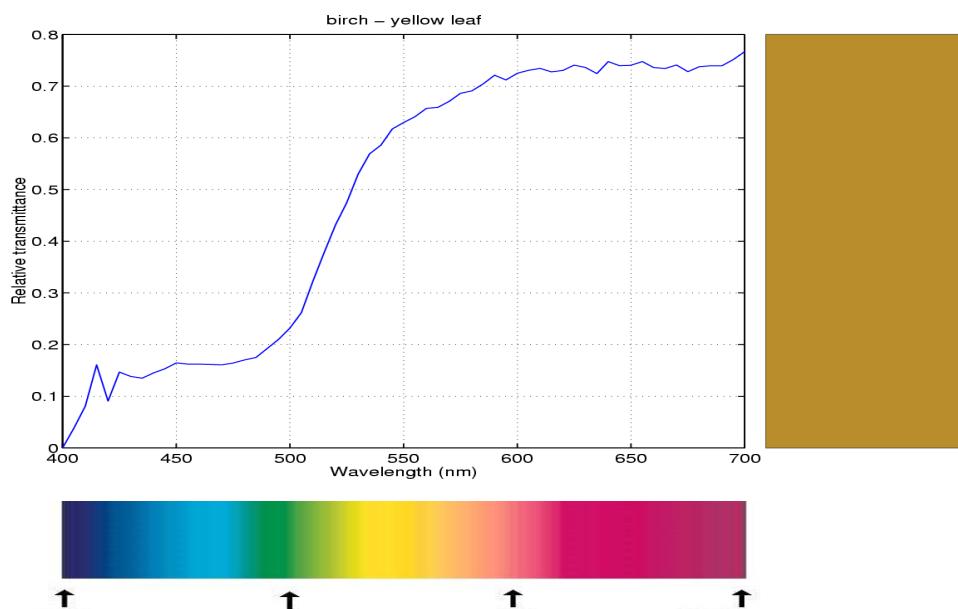
$$[R, G, B] = LUT[index]$$

$$\text{E.g.: } [64, 64, 0] = LUT[98]$$



Spectral Images

- Spectral image: n components according to wavelengths.
- Three components R, G, B => “usual” color image.





Quality Measures

- Bit rate: How much data per pixel?
- Compression ratio: How much smaller?
- Computation time: How fast?
- Distortion: How much error in the presentation?
- Bit rate bits/pixel:

$$\frac{\text{size of the compressed file}}{\text{pixels in the image}} = \frac{D}{N}$$

- Compression ratio:

$$C = \frac{\text{size of the original file}}{\text{size of the compressed file}} = \frac{N \cdot k}{D}$$

k = the number of bits per pixel in the original image
 D/N = the bit rate of the compressed image



Quality Measures

- The data redundancy is computed as $R = 1 - \frac{1}{c}$
- If the size of the image is $M * N$, the intensities of the image are r_k , and k :th intensity appears n_k times, then the probability for a symbol is

$$p_k(r_k) = \frac{n_k}{NM}$$

- The average number of bits required for each pixel is

$$L_{avg} = \sum_{k=0}^{L-1} l(r_k)p_k(r_k)$$

where $l(r_k)$ is the number of bits needed to represent r_k



Quality Measures

- Mean average error (MAE):

$$\text{MAE} = \frac{1}{N} \sum_{i=1}^N |y_i - x_i|$$

- Mean square error (MSE):

$$\text{MSE} = \frac{1}{N} \sum_{i=1}^N (y_i - x_i)^2$$

- Signal-to-noise ratio (SNR):

- decibels

$$\text{SNR} = 10 \cdot \log_{10} [\sigma^2 / \text{MSE}]$$

- Peak-signal-to-noise ratio (PSNR):

$$\text{PSNR} = 10 \cdot \log_{10} [A^2 / \text{MSE}]$$

- A is the amplitude of the signal, for an 8-bit signal

$$A = 2^8 - 1 = 255$$



Quality Measures

- Visual quality metrics
 - Computational metrics developed such that they match with subjects, e.g. visual quality

Rating scale of the
Television
Allocations Study
Organization.
(Frendendall and
Behrend.)

Value	Rating	Description
1	Excellent	An image of extremely high quality, as good as you could desire.
2	Fine	An image of high quality, providing enjoyable viewing. Interference is not objectionable.
3	Passable	An image of acceptable quality. Interference is not objectionable.
4	Marginal	An image of poor quality; you wish you could improve it. Interference is somewhat objectionable.
5	Inferior	A very poor image, but you could watch it. Objectionable interference is definitely present.
6	Unusable	An image so bad that you could not watch it.



Coding: General Aspects

- Coder and decoder computation complexity
- Memory requirements
- Fixed rate or variable rate
- Error resilience (sensitivity)
- Symmetric or asymmetric
- Decompress at multiple resolutions, decompress at various bit rates; decompress with lost data?
- Standard or proprietary (application based)
- In coding, $C_R = 2$ to 10 can be expected.
- Make use of coding redundancy and inter-pixel redundancy.



Coding: Role of modeling

- Modeling and coding:
 - How, and in what order the image is processed?
 - What are the symbols (pixels, blocks) to be coded?
 - What is the statistical model of these symbols?
- Requirement:
 - Uniquely decodable: different input => different output.
 - Instantaneously decodable: the symbol can be recognized after its last bit has been received



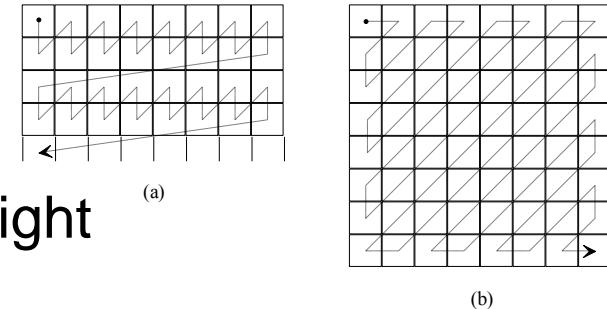
Coding: Role of modeling

- Segmentation:
 - Local (pixels) or global (fractal compression)
 - Compromise: block coding
- Order of processing:
 - In what order the blocks (or pixels) are processed?
 - In what order are pixels inside the block processed?



Coding: Role of modeling

- Order of processing:
 - Row-major order: top-to-down, left-to-right
- Zigzag scanning:
 - Pixel-wise processing (a)
 - DCT-transformed block (Discrete Cosine Transform) (b)
- Progressive modeling:
 - The quality of an image quality increases gradually as data are received
 - For example in pyramid coding: first the low resolution version, then increasing the resolution

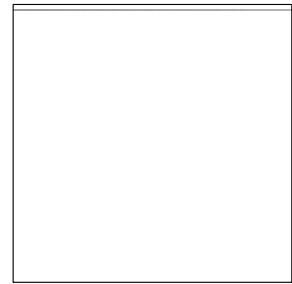




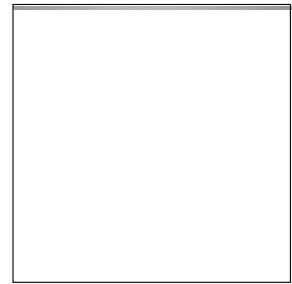
Progressive reconstruction

- Reconstruction quality

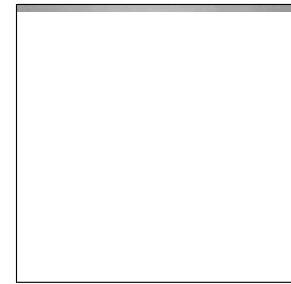
0.1 %



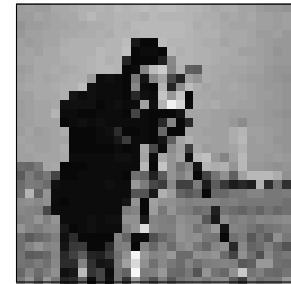
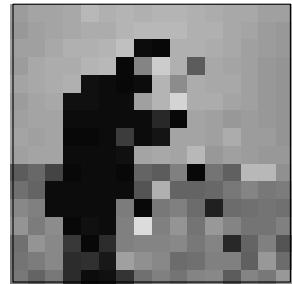
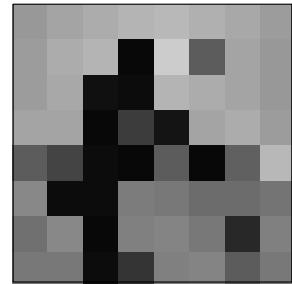
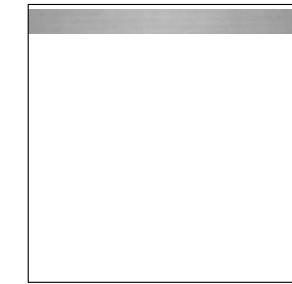
0.5 %



2.1 %



8.3 %





Statistical Modeling

- Set of symbols (alphabet) $S = \{s_1, s_2, \dots, s_N\}$
 - N is number of symbols in the alphabet.
- Probability distribution of the symbols: $P = \{p_1, p_2, \dots, p_N\}$
- The (Shannon) **entropy** H (and the average number of bits) of an information source S is defined as

$$H = -\sum_{i=1}^N p_i \cdot \log_2(p_i)$$

- The amount of information in symbol s_i , i.e., the number of bits to code or code length for the symbol s_i :

$$H(s_i) = -\log_2(p_i)$$



Statistical Modeling

- Static modeling:
 - Static model (code table)
 - One-pass method: encoding
 - ASCII data: $p('e')=10\%$, $p('t')=8\%$
- Semi-adaptive modeling
 - Two-pass method: (1) analysis, (2) encoding
- Adaptive (or dynamic) modeling:
 - Symbol by symbol on-line adaptation during coding/encoding
 - One-pass method: analysis and encoding



Statistical Modeling

- Context modeling:
 - Spatial dependencies between the pixels
 - For example, what is the most probable symbol after a known sequence of symbols?
- Predictive modeling (for coding prediction errors):
 - Prediction of the current pixel value
 - Calculating the prediction error
 - Modeling the error distribution
 - E.g. differential pulse code modulation (DPCM)

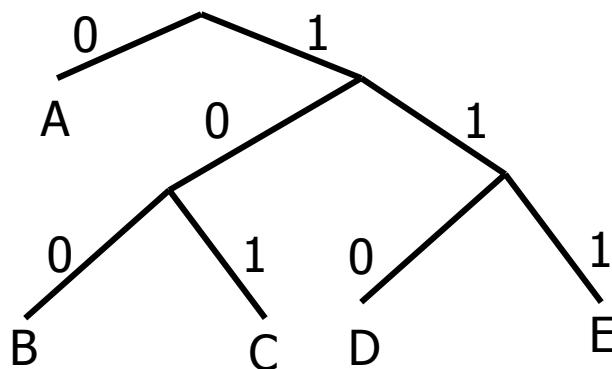


Huffman Coding

- INIT:
 - Put all nodes in an OPEN list and keep it sorted all times according to their probabilities
- REPEAT
 - a) From OPEN pick *two* nodes having the *lowest* probabilities, create a parent node of them
 - b) Assign the sum of the children's probabilities to the parent node and inset it into OPEN
 - c) Assign code 0 and 1 to the two branches of the tree, and delete the children from OPEN

Huffman Coding

Symbol	p_i	$-\log_2(p_i)$	Code	Subtotal
A	15/39	1.38	0	1*15
B	7/39	2.48	100	3*7
C	6/39	2.70	101	3*6
D	6/39	2.70	110	3*6
E	5/39	2.96	111	3*5
Total:				87 bits



Binary tree

$$H = 2.19 \text{ bits}$$

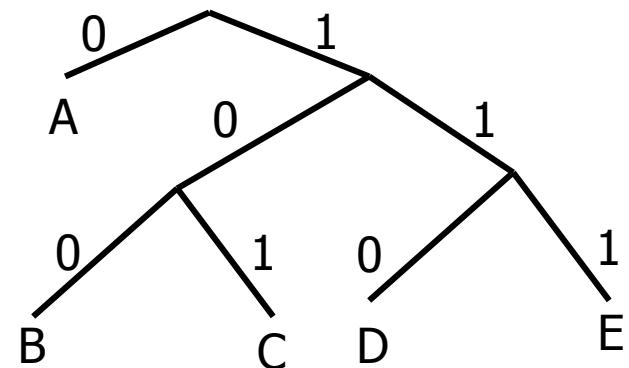
$$L = 87/39 = 2.23 \text{ bits}$$



Huffman Coding

- Bit codes: A – 0; B – 100; C – 101; D – 110; E - 111
- Input bit stream (22 bits):

1000100010101010110111



- Extracted codes:

100 0 100 0 101 0 101 0 110 111

- Decoded message:

B A B A C A C A D E



Huffman Coding

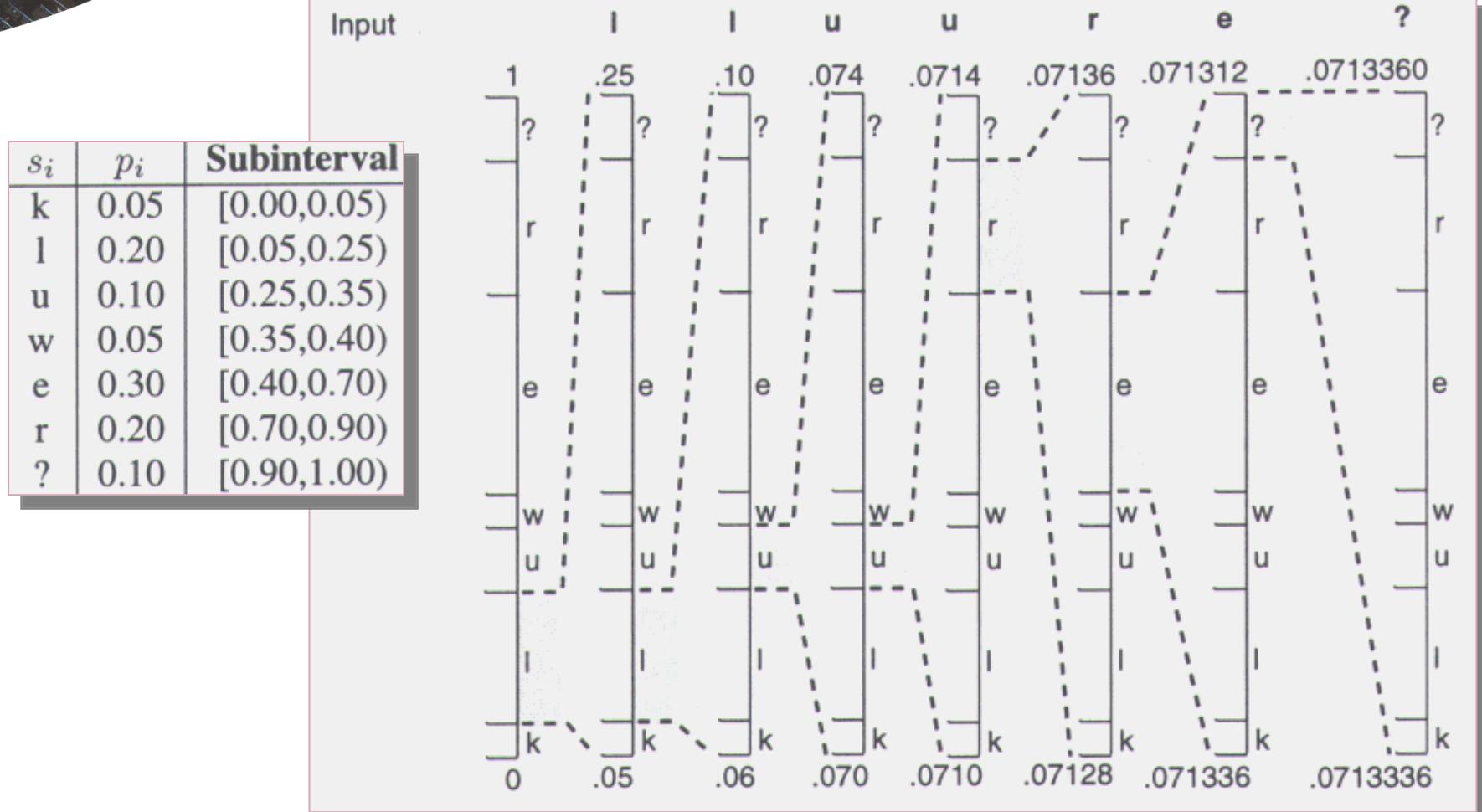
- Optimum code for a given data set requires two passes
- Code construction complexity $O(N \log N)$
- Fast lookup table based implementation
- Requires at least one bit per symbol
- Average codeword length is within one bit of zero-order entropy (Tighter bounds are known): $H \leq R \leq H + 1$ bit
- Susceptible to bit errors



Arithmetic Coding

- Alphabet extension (blocking symbols) can lead to coding efficiency
- How about treating entire sequence as one symbol!
- Not practical with Huffman coding
- Arithmetic coding allows you to do precisely this
- Basic idea: map data sequences to sub-intervals in $[0,1)$ with lengths equal to the probability of corresponding sequence
- QM-coder is an arithmetic coding tailored for binary data
 - 1) Huffman coder: $H \leq R \leq H + 1$ bit/pel
 - 2) Block coder: $H_n \leq R_n \leq H_n + 1/n$ bit/pel
 - 3) Arithmetic coder: $H \leq R \leq H + 1$ bit/message

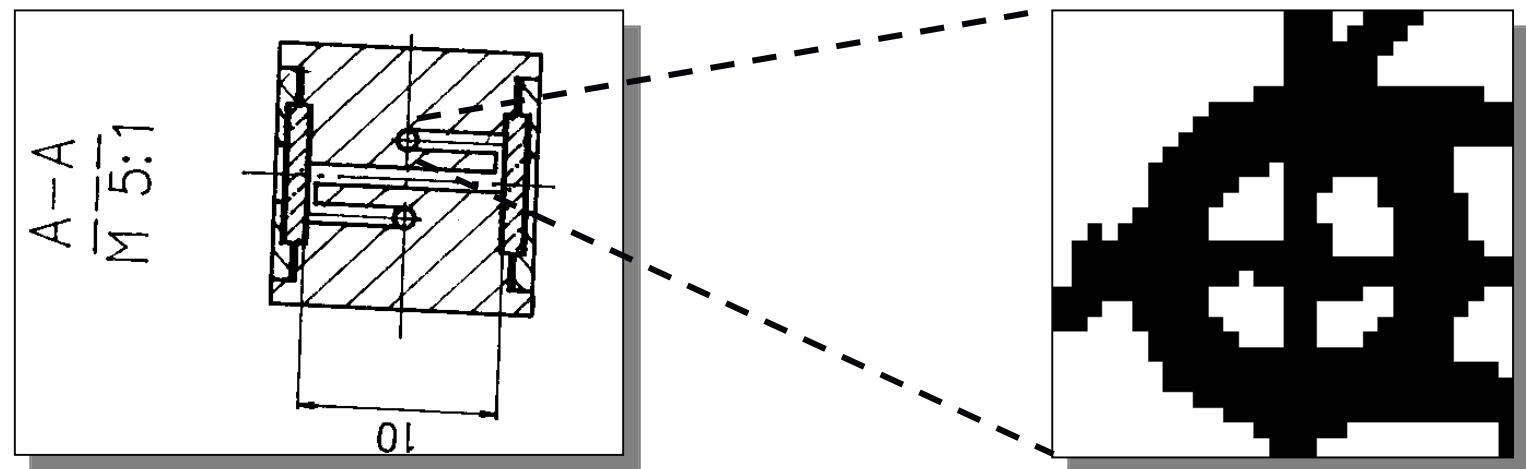
Arithmetic Coding





Binary Images

- Binary images consist only of two colors, black and white
- The probability distribution of the alphabet is often very skewed, e.g. $p(\text{white})=0.98$, and $p(\text{black})=0.02$
- Moreover, the images usually have large homogenous areas of the same color





Binary Images

- Run-length encoding
- Predictive encoding
- CCITT group 3 and group 4 standards
 - READ code (2D, Relative Element Address Designate)
- Block transform coding
- JBIG, JBIG2 (Joint Bilevel Image Experts Group)
 - Standard by CCITT and ISO
 - Context-based compression pixel by pixel
 - QM-coder (arithmetic coder)



Binary Images: RLE

- Pre-processing method, good when one symbol occurs with high probability or when symbols are dependent
- Count how many repeated symbol occur
- Source 'symbol' = length of run



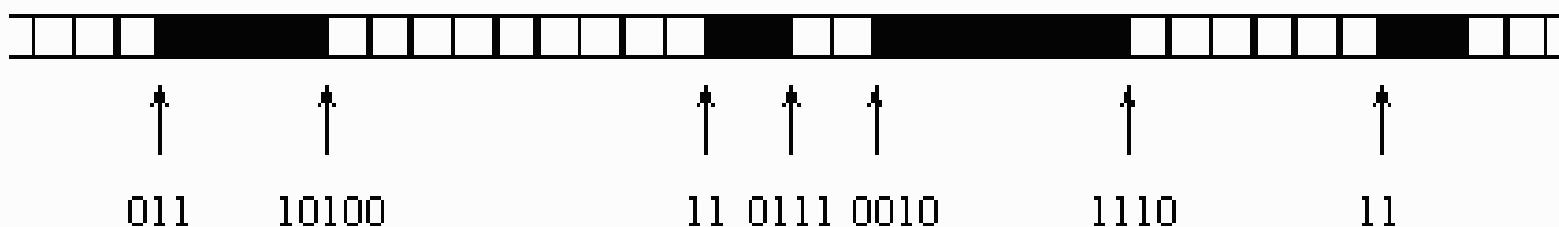
- Example: ..., 4b, 9w, 2b, 2w, 6b, 6w, 2b, ...



Binary Images: RLE

- Huffman code table

n	white runs	black runs
0	00110101	0000110111
1	000111	010
2	0111	11
3	1000	10
4	1011	011
5	1100	0011
6	1110	0010
7	1111	00011
8	10011	000101
9	10100	000100
10	00111	0000100
11	01000	0000101
12	001000	0000111





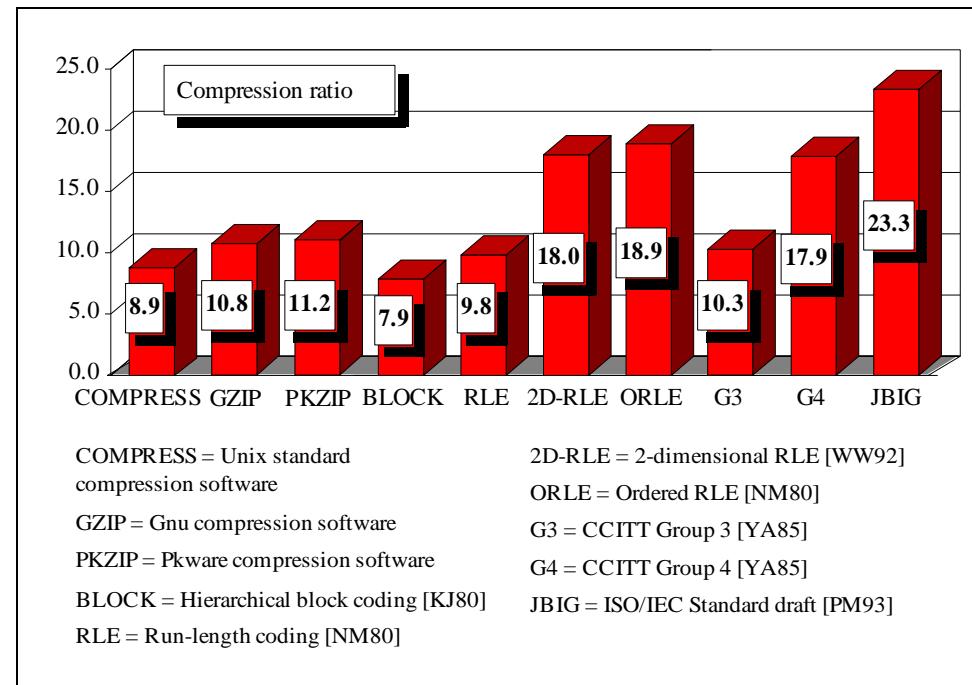
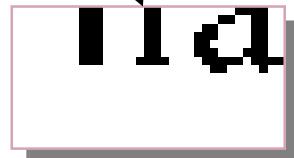
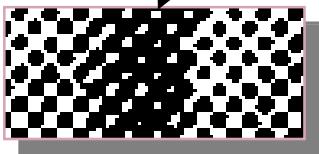
JBIG2

- Bilevel (binary) documents, like fax documents.
- Both graphic (line art) and pictures (halftone).



Mentoring li

To help lower care faced by women in Medicine's Institut has been selected nationally to participation program funded Health Services Of (PHSOWH). The direction of Dr Pa





Continuous Tone Images

- Lossless and near-lossless compression
 - Bit-plane coding: to bit-planes of a grayscale image
 - A series of binary images
 - Lossless and near-lossless JPEG
 - Joint Photographic Experts Group:
<https://jpeg.org/index.html>
 - Pixel by pixel by predicting the current pixel on the basis of the neighboring pixels
 - Prediction errors coded by Huffman or arithmetic coding (QM-coder)

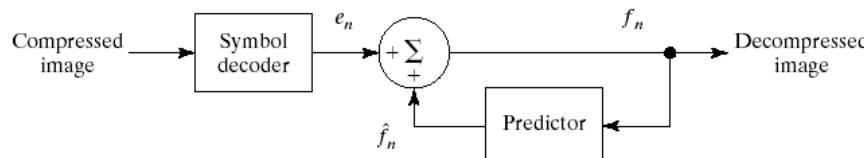
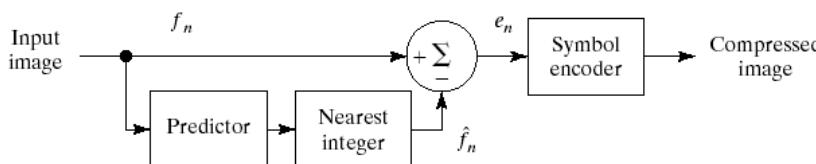


Continuous Tone Images

- Prediction to remove inter-pixel redundancy

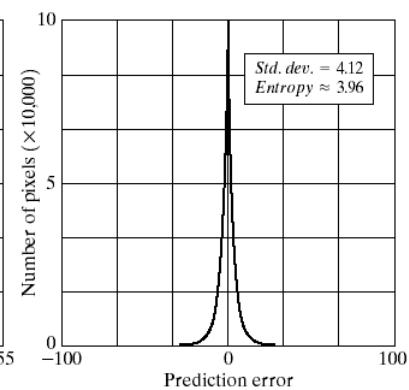
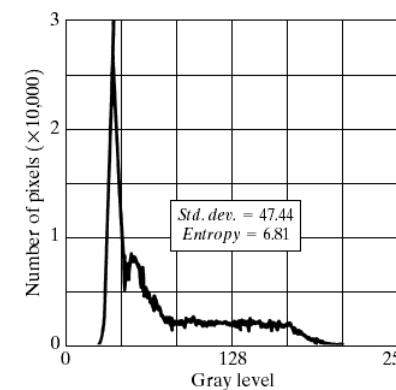
a
b

FIGURE 8.19 A lossless predictive coding model:
(a) encoder;
(b) decoder.



a
b c

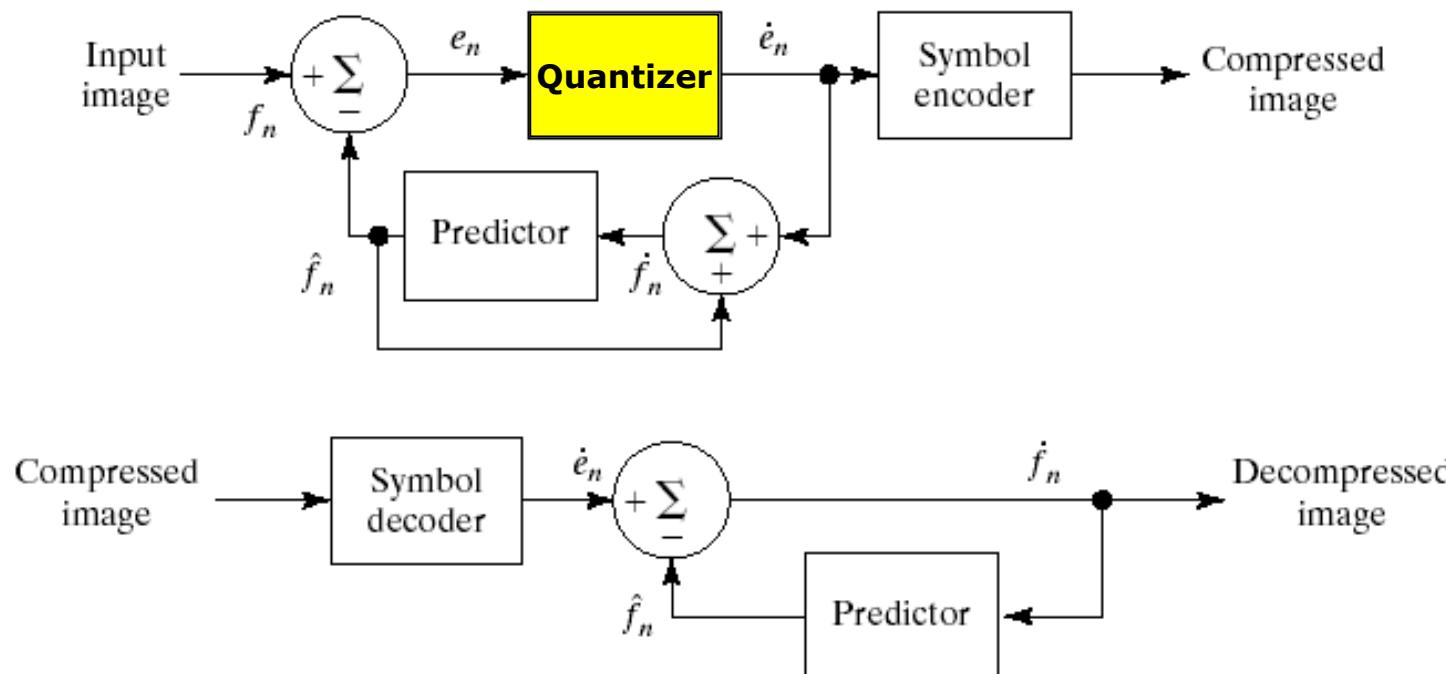
FIGURE 8.20
(a) The prediction error image resulting from Eq. (8.4-9).
(b) Gray-level histogram of the original image.
(c) Histogram of the prediction error.





Continuous Tone Images

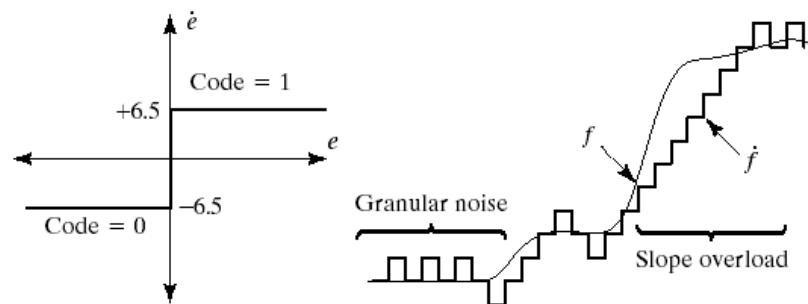
- Prediction in lossy compression





Continuous Tone Images

- Delta modulation



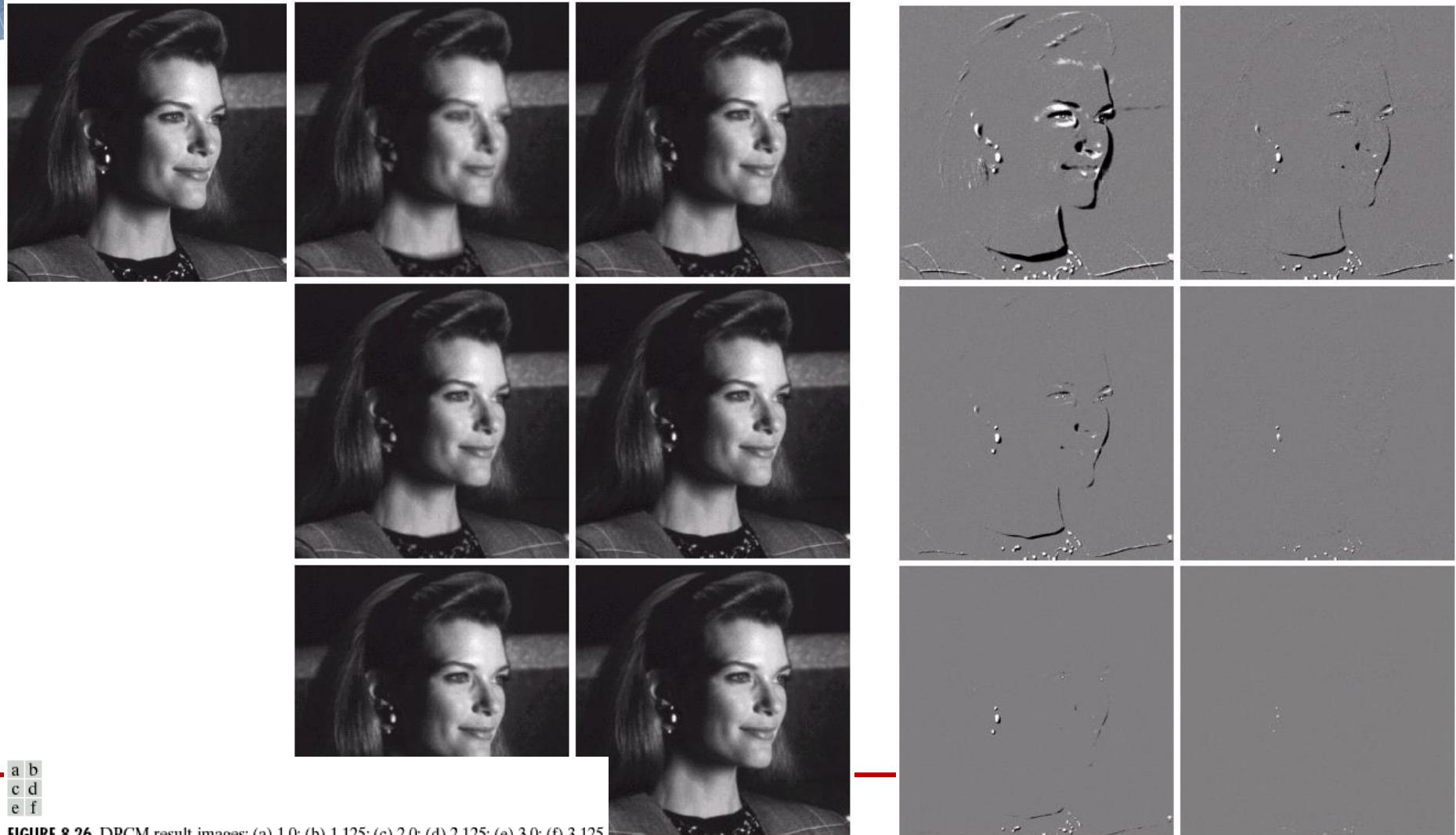
a
b
c

FIGURE 8.22 An example of delta modulation.

Input		Encoder				Decoder		Error
n	f	\hat{f}	e	\dot{e}	\hat{f}	\hat{f}	\dot{f}	$[f - \hat{f}]$
0	14	—	—	—	14.0	—	14.0	0.0
1	15	14.0	1.0	6.5	20.5	14.0	20.5	-5.5
2	14	20.5	-6.5	-6.5	14.0	20.5	14.0	0.0
3	15	14.0	1.0	6.5	20.5	14.0	20.5	-5.5
.
.
14	29	20.5	8.5	6.5	27.0	20.5	27.0	2.0
15	37	27.0	10.0	6.5	33.5	27.0	33.5	3.5
16	47	33.5	13.5	6.5	40.0	33.5	40.0	7.0
17	62	40.0	22.0	6.5	46.5	40.0	46.5	15.5
18	75	46.5	28.5	6.5	53.0	46.5	53.0	22.0
19	77	53.0	24.0	6.5	59.6	53.0	59.6	17.5
.
.



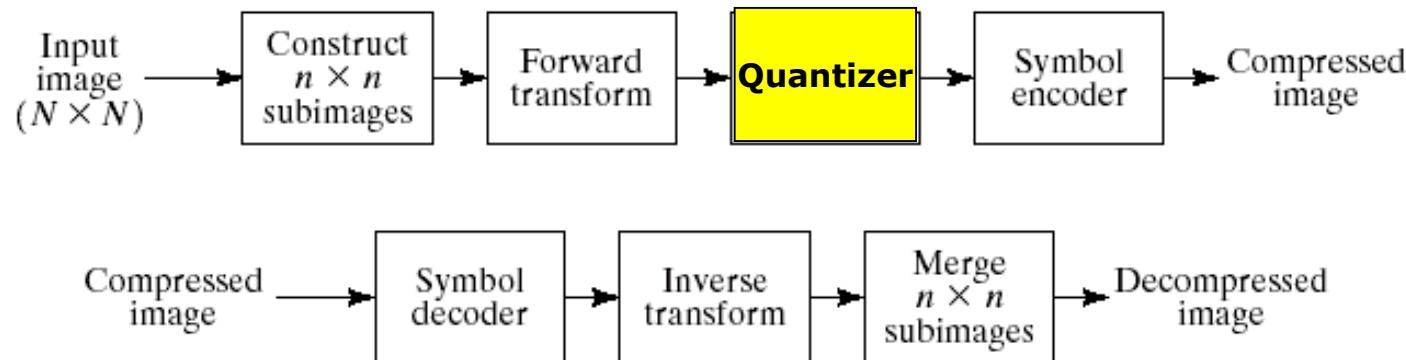
Continuous Tone Images, DPCM





Continuous Tone Images

- A reversible linear transform (such as Fourier Transform) is used to map the image into a set of transform coefficients; These coefficients are then quantized and coded.
- The goal of transform coding is to decorrelate pixels and pack information into small number of transform coefficients.





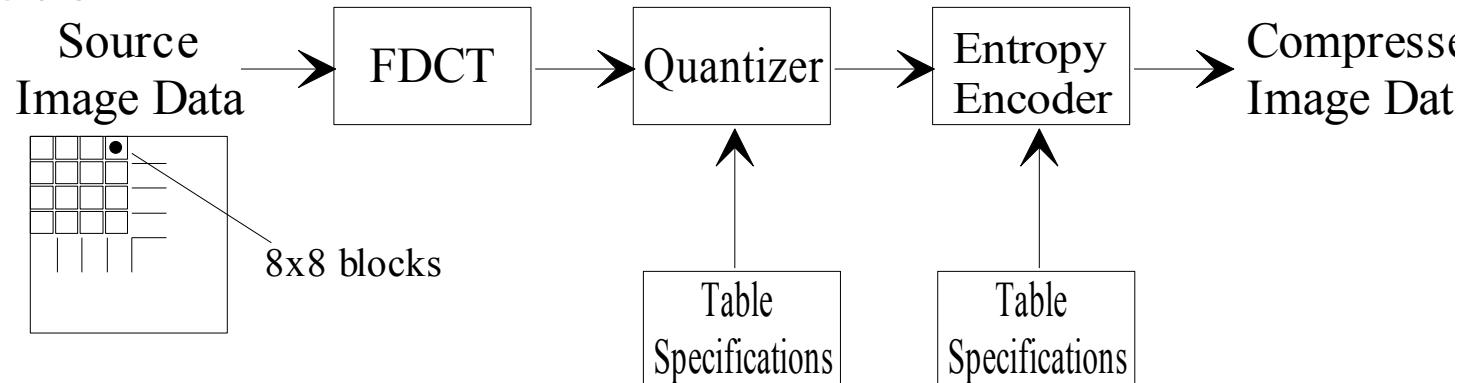
Continuous Tone Images: JPEG

- Vector quantization: codebooks
- JPEG (Joint Photographic Experts Group)
- Lossy coding of continuous tone still images, both color and grayscale
- Based on Discrete Cosine Transform (DCT):
 - 1) Image is divided into block $N \times N$.
 - 2) The blocks are transformed with 2-D DCT.
 - 3) DCT coefficients are quantized.
 - 4) The quantized coefficients are encoded.

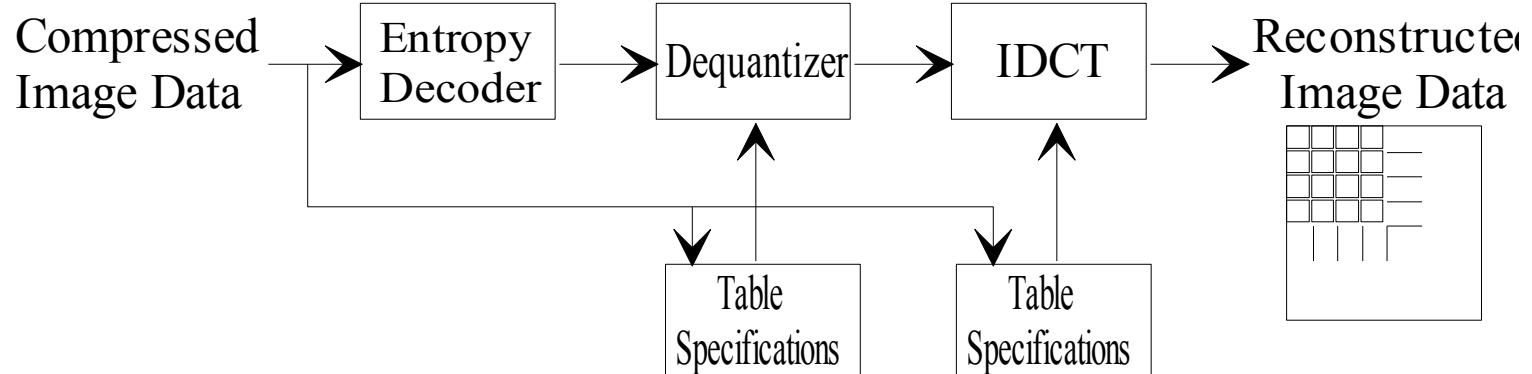


Continuous Tone Images: JPEG

- Encoder



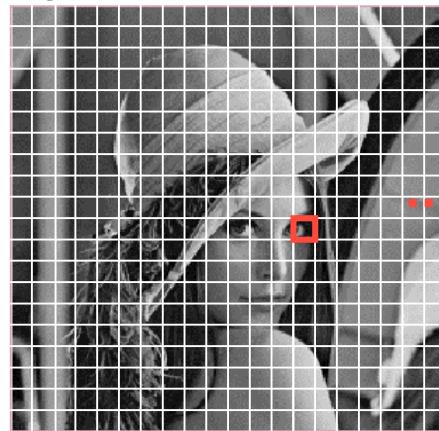
- Decoder



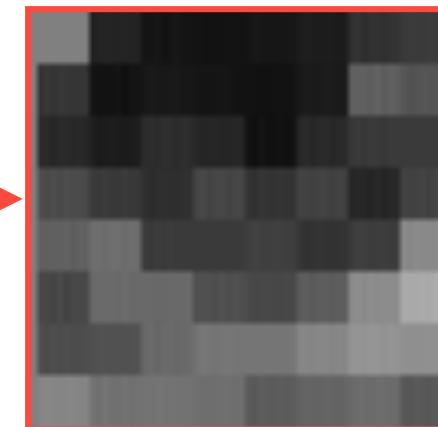


Continuous Tone Images: JPEG

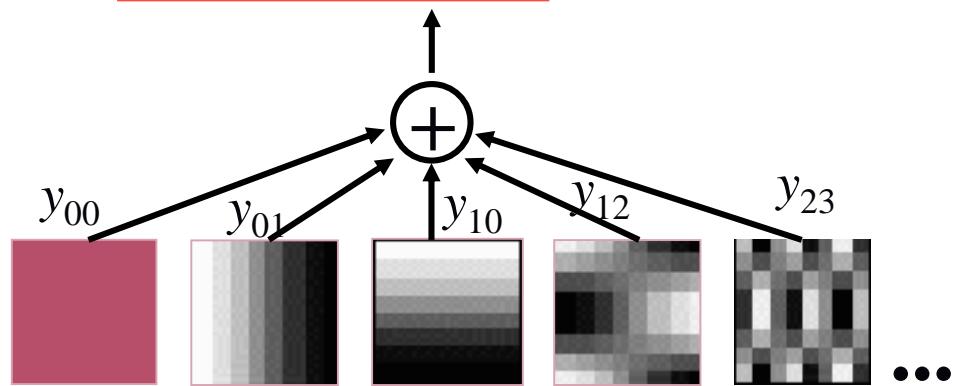
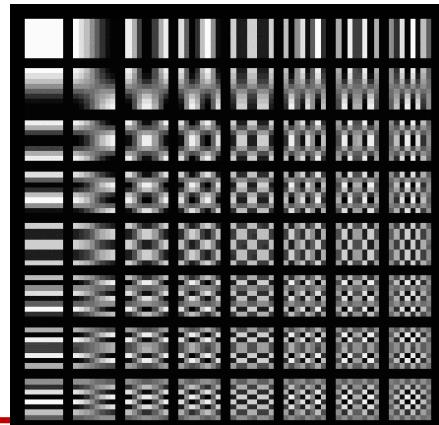
- Input image



8x8 block



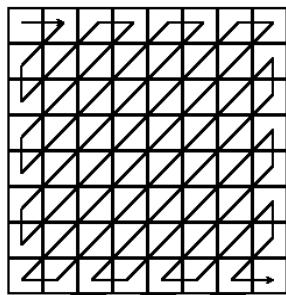
- DCT





Continuous Tone Images: JPEG

- Converting a 2-D matrix into a 1-D array, so that the frequency (horizontal and vertical) increases in this order and the coefficients variance are decreasing in this order.



0	1	5	6	14	15	27	28
2	4	7	13	16	26	29	42
3	8	12	17	25	30	41	43
9	11	18	24	31	40	44	53
10	19	23	32	39	45	52	54
20	22	33	38	46	51	55	60
21	34	37	47	50	56	59	61
35	36	48	49	57	58	62	63

DC

Direct current

Matlab: `y=dct(x);`

AC

Alternating current

$$\hat{T}(u, v) = \text{round} \left[\frac{T(u, v)}{Z(u, v)} \right]$$

Original block								Transformed block							
139	144	149	153	155	155	155	155	235.6	-1.0	-12.1	-5.2	2.1	-1.7	-2.7	1.3
144	151	153	156	159	156	156	156	-22.6	-17.5	-6.2	-3.2	-2.9	-0.1	0.4	-1.2
150	155	160	163	158	156	156	156	-10.9	-9.3	-1.6	1.5	0.2	-0.9	-0.6	-0.1
159	161	162	160	160	159	159	159	-7.1	-1.9	0.2	1.5	0.9	-0.1	0.0	0.3
159	160	161	162	162	155	155	155	-0.6	-0.8	1.5	1.6	-0.1	-0.7	0.6	1.3
161	161	161	161	160	157	157	157	1.8	-0.2	1.6	-0.3	-0.8	1.5	1.0	-1.0
162	162	161	163	162	157	157	157	-1.3	-0.4	-0.3	-1.5	-0.5	1.7	1.1	-0.8
162	162	161	161	163	158	158	158	-2.6	1.6	-3.8	-1.8	1.9	1.2	-0.6	-0.4

16	11	10	16	24	40	51	61
12	12	14	19	26	58	60	55
14	13	16	24	40	57	69	56
14	17	22	29	51	87	80	62
18	22	37	56	68	109	103	77
24	35	55	64	81	104	113	92
49	64	78	87	103	121	120	101
72	92	95	98	112	100	103	99



JPEG vs. JPEG2000

- Fractal coding
- Pyramid coding
- Wavelet transform, e.g. JPEG 2000

JPEG: 0.25 bpp



JPEG2000: 0.25 bpp





Continuous Wavelet Transform

- CWT is analysing signal $f(x)$ as with a transform

$$W_\psi(s, t) = \int_{-\infty}^{\infty} f(x) \psi_{s,t}(x) dx$$

where $\psi_{s,t}(x) = \frac{1}{\sqrt{s}} \psi\left(\frac{x-t}{s}\right)$

- The inverse transform has the perfect reconstruction feature

$$f(x) = \frac{1}{C_\psi} \int_0^{\infty} \int_{-\infty}^{\infty} W_\psi(s, t) \frac{\psi_{s,t}(x)}{s^2} dt ds$$

with the admissibility condition $C_\psi = \int_{-\infty}^{\infty} \frac{|\Psi(\mu)|^2}{|\mu|} d\mu < \infty$



Discrete Wavelet Transform

- The signal $f(x)$ as a combination of expansion functions is

$$f(x) = \sum_k \alpha_k \varphi_k(x)$$

where $\varphi_k(x)$ are the expansion functions.

- In DWT the $\varphi_k(x)$ discretized as

$$\varphi_{j,k}(x) = 2^{\frac{j}{2}} \varphi(2^j x - k), \quad j, k \in \mathbb{Z}, \varphi(x) \in L^2(\mathbb{R})$$

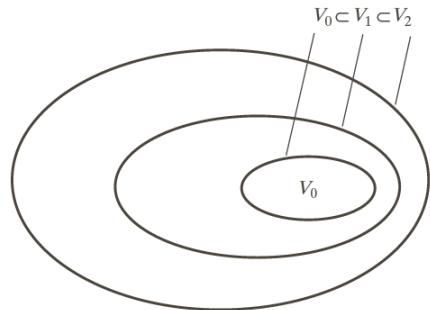
- E.g. Haar scaling function

$$\varphi(x) = \begin{cases} 1, & 0 \leq x < 1 \\ 0, & \text{otherwise} \end{cases}$$



Discrete Wavelet Transform

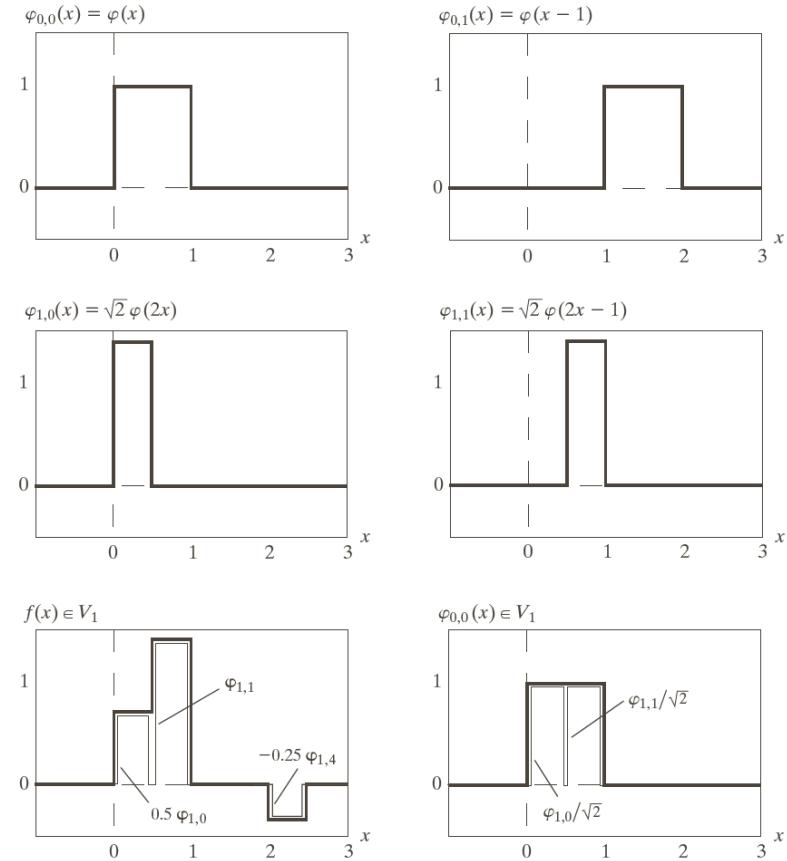
- Haar transform, scaling functions in V_0 and V_1



- The wavelet function $\psi(x)$ describes the differences

$$V_{j+1} = V_j \oplus W_j$$

$$\langle \varphi_{j,k}, \psi_{j,l}(x) \rangle = 0$$





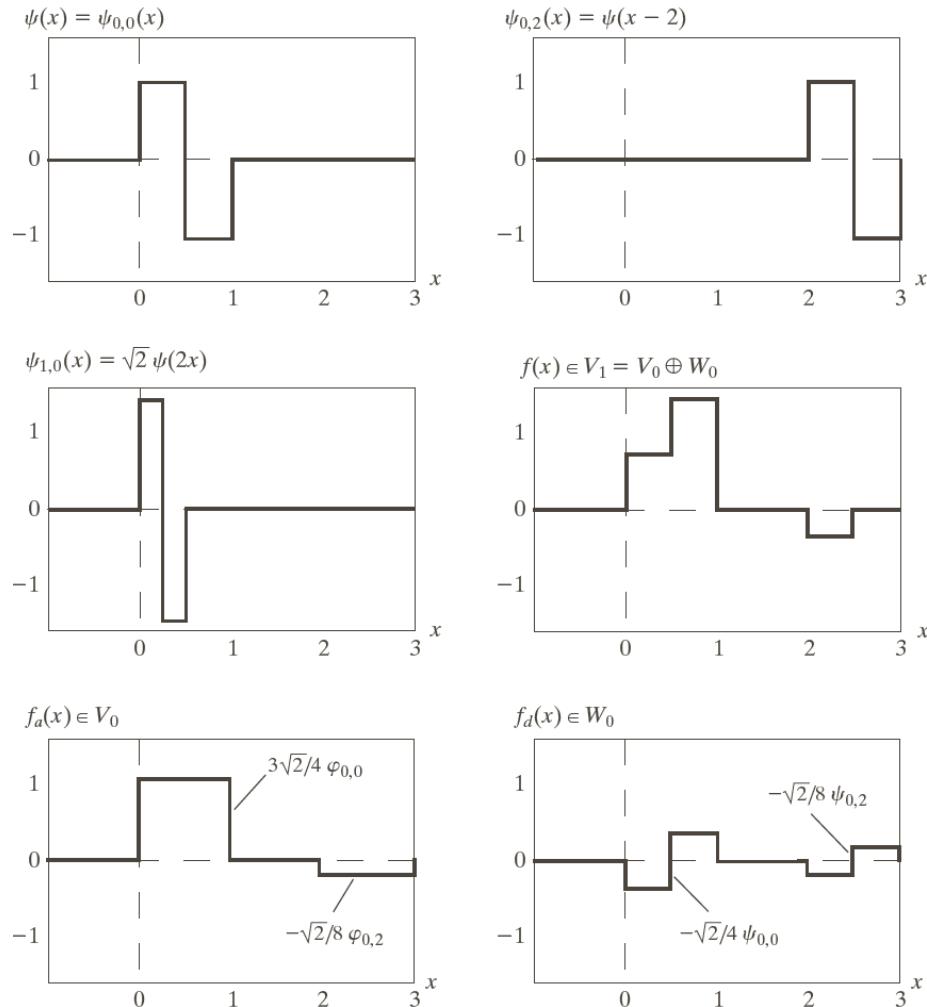
Discrete Wavelet Transform

- E.g. Haar wavelet function is

$$\psi(x) = \begin{cases} 1, & 0 \leq x < 0.5 \\ -1, & 0.5 \leq x < 1 \\ 0, & \text{elsewhere} \end{cases}$$

- As the result

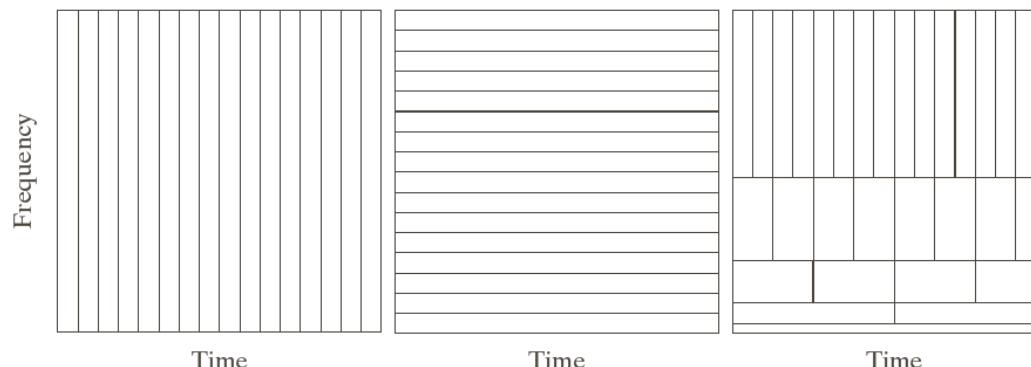
$$f(x) = f_a(x) + f_d(x)$$



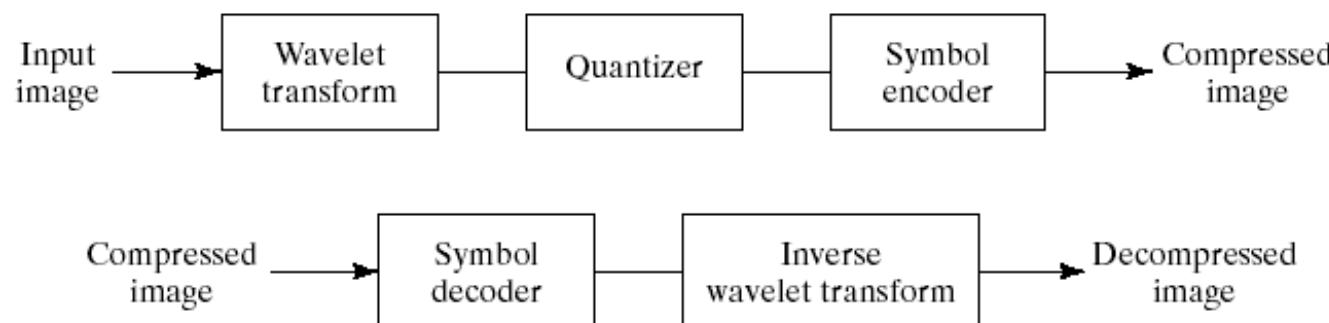


Wavelet Compression

- FT vs. WT: time-frequency tilings (time domain, FD, WD)



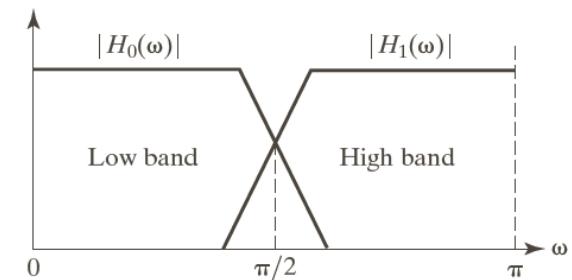
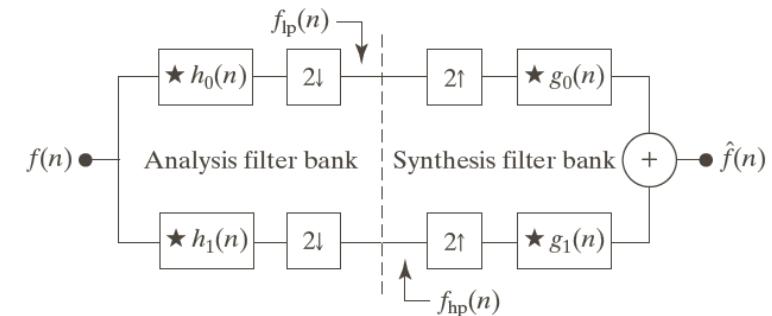
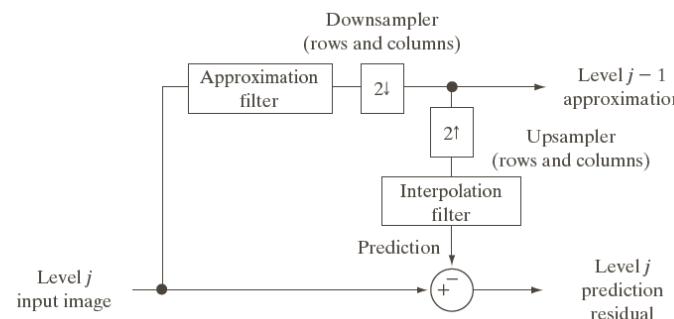
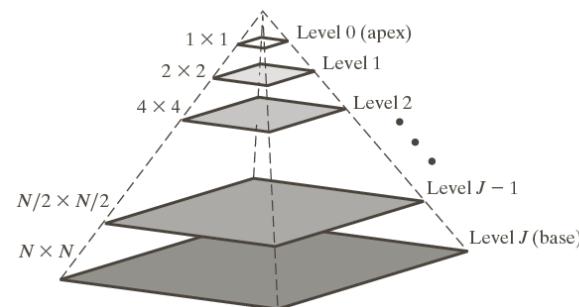
- In practice





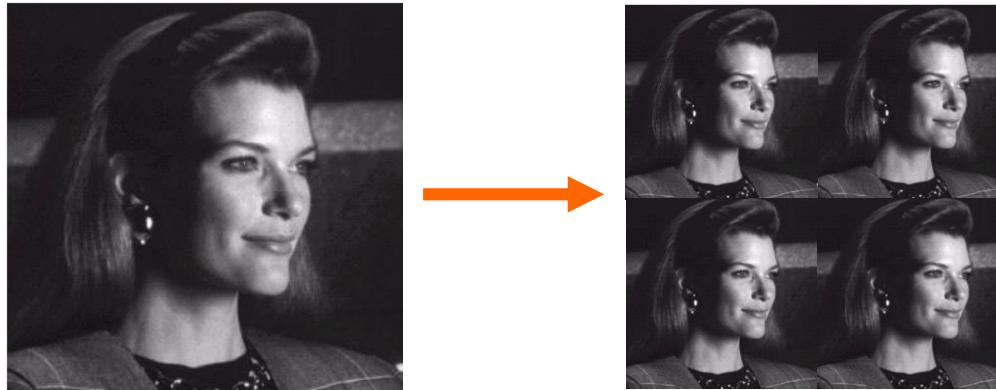
Wavelet Compression

- Wavelet transform is constructing an approximating image pyramid and differences (details) between them

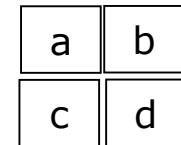
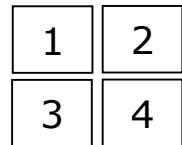




Wavelet Compression



Put a pixel in each quadrant → No size change



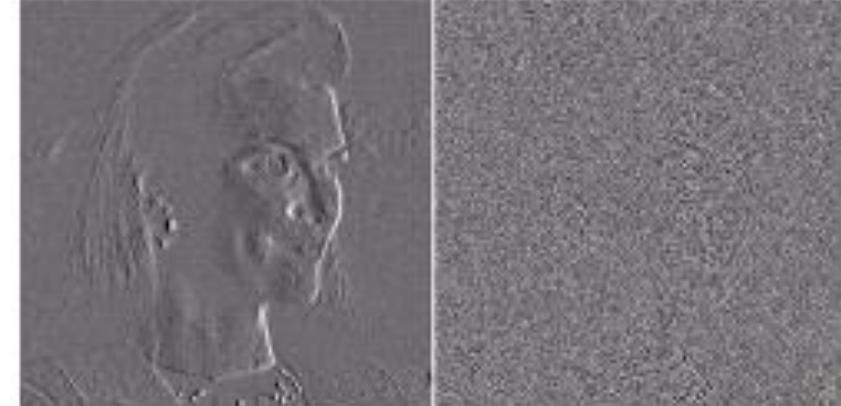
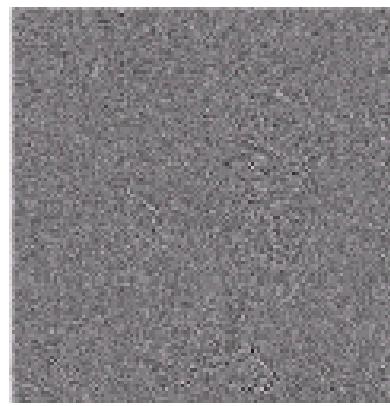
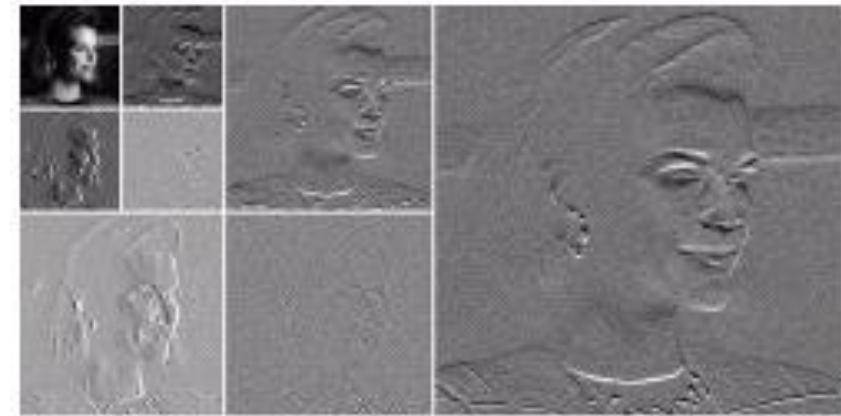
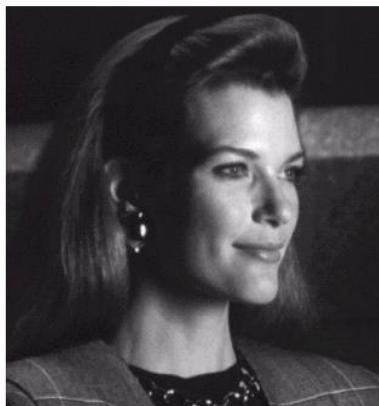
$$\begin{aligned}a &= (x_1+x_2+x_3+x_4)/4 \\b &= (x_1+x_2-x_3-x_4)/4 \\c &= (x_1+x_3-x_2-x_4)/4 \\d &= (x_1+x_4-x_2-x_3)/4\end{aligned}$$

$$\begin{bmatrix} a \\ b \\ c \\ d \end{bmatrix} = \frac{1}{4} \begin{bmatrix} 1 & 1 & 1 & 1 \\ 1 & 1 & -1 & -1 \\ 1 & -1 & 1 & -1 \\ -1 & -1 & 1 & 1 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \\ x_3 \\ x_4 \end{bmatrix}$$

$$\begin{bmatrix} x_1 \\ x_2 \\ x_3 \\ x_4 \end{bmatrix} = \begin{bmatrix} 1 & 1 & 1 & 1 \\ 1 & 1 & -1 & -1 \\ 1 & -1 & 1 & -1 \\ -1 & -1 & 1 & 1 \end{bmatrix} \begin{bmatrix} a \\ b \\ c \\ d \end{bmatrix}$$



Wavelet Compression





Wavelet Compression

- Large set of filters defined with various features
 - Orthonormal
 - Biorthogonal (orthogonal)
 - Overcomplete (frame)

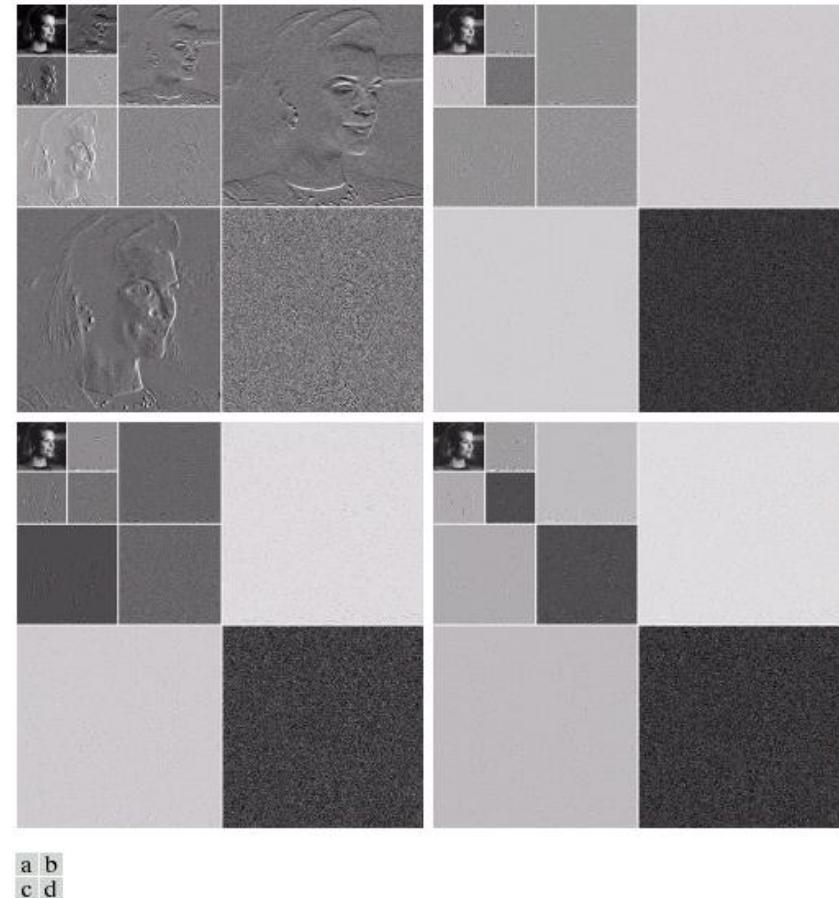


FIGURE 8.42 Wavelet transforms of Fig. 8.23 with respect to (a) Haar wavelets, (b) Daubechies wavelets, (c) symlets, and (d) Cohen-Daubechies-Feauveau biorthogonal wavelets.

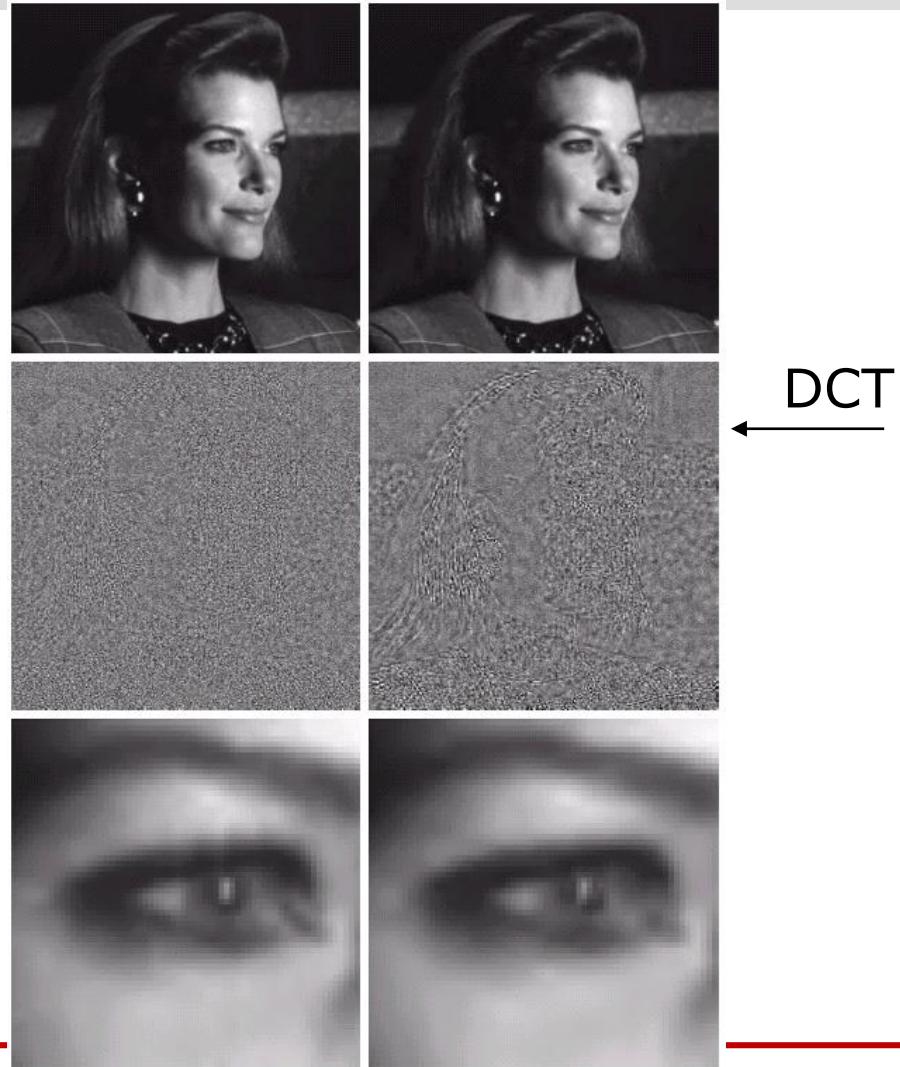


Wavelet Compression

- High Frequency coefficients tend to be very small $\rightarrow 0$

Wavelet
→

- They can be quantized very effectively without distorting the results





Video Sequences

- Video images are three-dimensional generalization of still images (spatial correlation) where the third dimension is time (spatial and temporal correlation)
- Each frame of a video sequence can be compressed by any image compression algorithm
- Motion JPEG (M-JPEG)
 - Images separately JPEG coded
- MPEG (Moving Pictures Expert Group)
 - Temporal correlations used
 - Two basic techniques:
 - Block based motion compensation
 - DCT based compression



Video Sequences

- Compression ratios for various channels

Channel	Bit rate	NTSC TV 168 Mb/s	HDTV 933 Mb/s	Film quality 2300 Mb/s
PC LAN	30 kb/s	5,600:1	31,000:1	76,000:1
Modems	56 kb/s	3,000:1	17,000:1	41,000:1
ISDN	64 - 144 kb/s	1,166:1	6,400:1	16,000:1
T-1, DSL	1.5 Mb/s	112:1	622:1	1,500:1
Ethernet	10 Mb/s	17:1	93:1	230:1
T-3	42 Mb/s	4:1	22:1	54:1
Fiber optic	200 Mb/s	1:1	5:1	11:1



MPEG-family

- MPEG-1 (1992): VideoCD
- MPEG-2 (1994): DVD, digital TV, SVCD
 - about 50:1 compression, typically 3-10 Mbps
- MPEG-3: was abandoned
- MPEG-4 (1999+): DivX (starting from Version 5)
 - designed specially for low-bandwidth
- MPEG-7 (>1998):
 - searching and indexing of a/v data, using Description Tools



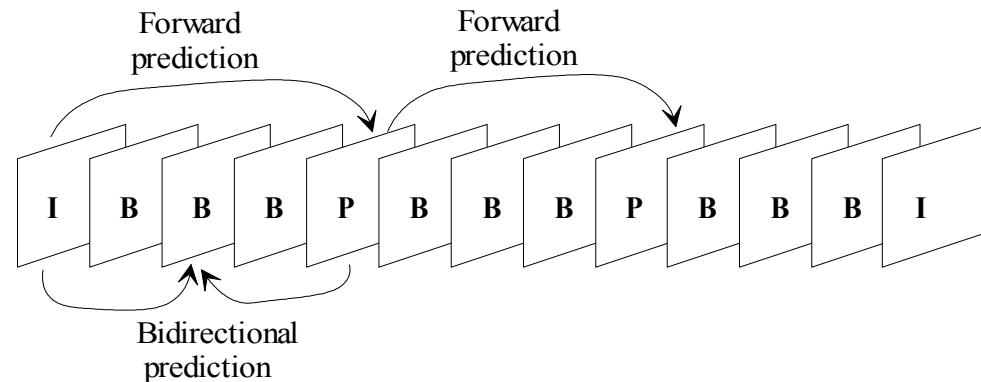
MPEG-1: Blocks

- The pictures are divided into 16x16 macroblocks, each consisting of four 8x8 elementary blocks
- The choice of the prediction method is chosen for each macroblock separately
- The intra-coded blocks are quantized differently from the predicted blocks:
 - Intra-coded blocks contain information in all frequencies and are quantized differently from the predicted blocks
 - The predicted blocks, contain mostly high frequencies and can be quantized with more coarse quantization tables.



MPEG-1: Inter-block Prediction

- Bidirectional prediction, Forward prediction, Backward prediction; Intra coding
 - I: *Intra pictures* are coded as still images by DCT
 - P: *Predicted pictures* are coded with reference to a past picture. The difference between the prediction and the original picture is then compressed by DCT
 - B: *Bidirectional pictures*, the prediction can be made both to a past and a future frame. Bidirectional pictures are never used as reference





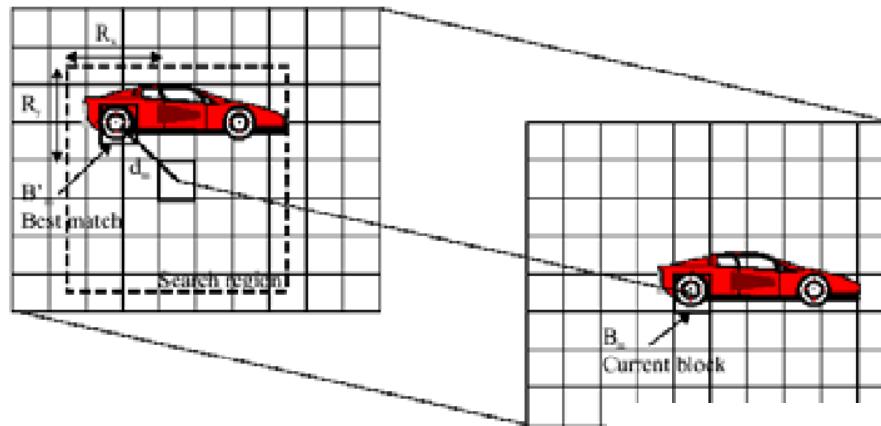
MPEG-1: Motion

- The prediction block in the reference frame is not necessarily in the same coordinates than the block in the current frame
- Because of motion in the image sequence, the most suitable predictor for the current block may exist anywhere in the reference frame
- The *motion estimation* specifies where the best prediction (best match) is found
- *Motion compensation* consists of calculating the difference between the reference and the current block



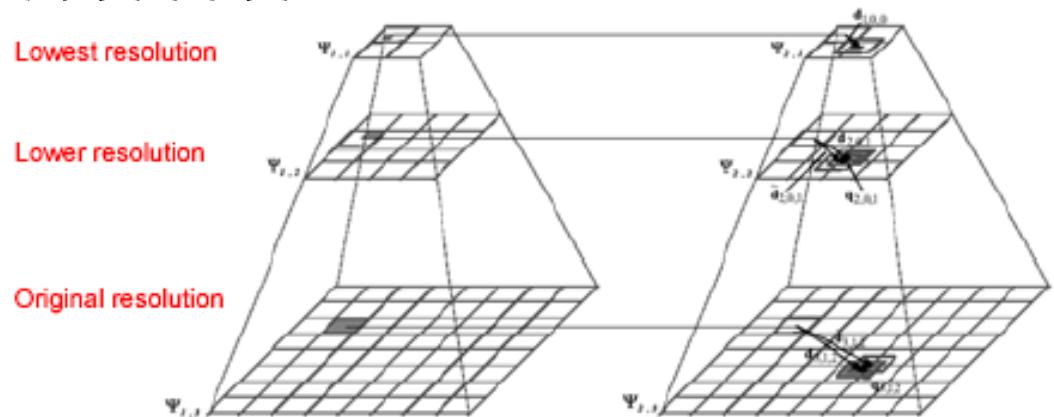
MPEG-1: Motion

- Exhaustive search block matching.



Slow !

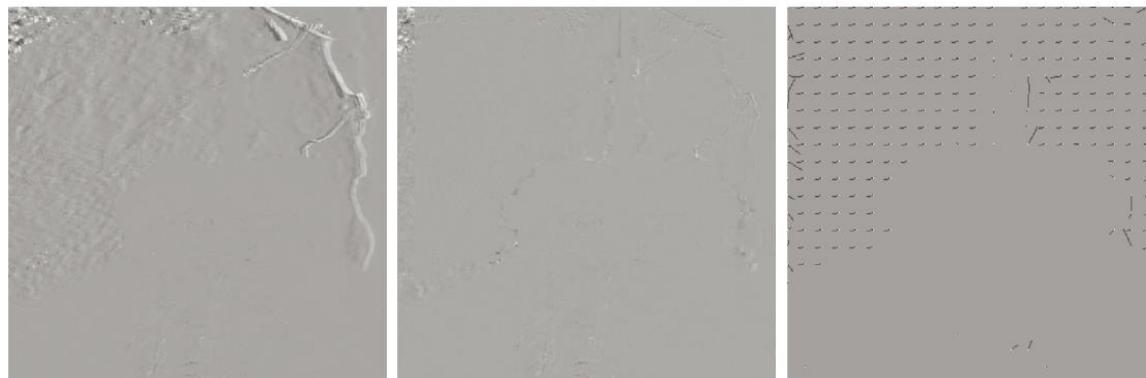
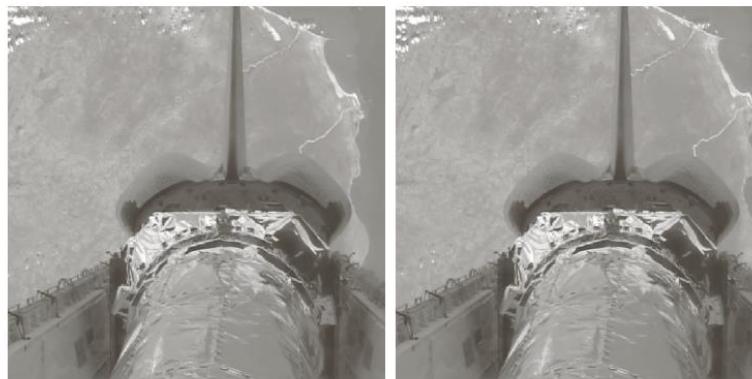
- Hierarchical block matching.





MPEG-1: Motion

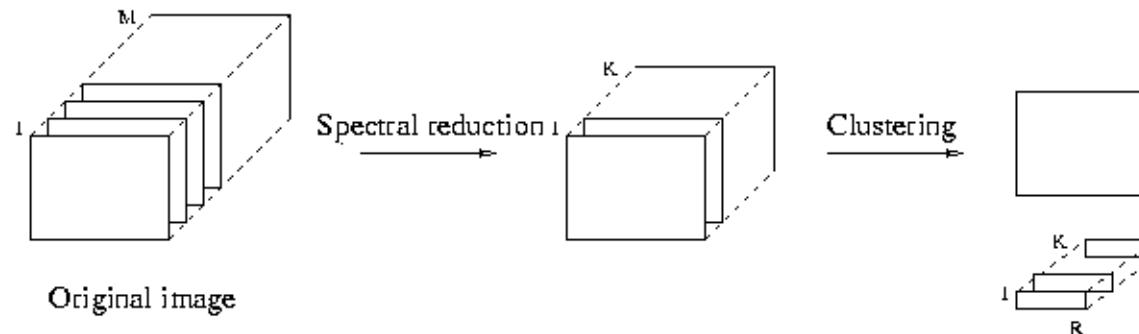
- Motion compensation; two frames (13 frames apart), difference, motion compensation applied, motion vectors





Spectral Images

- Approach 1



- Approach 2

- Clustering replaced with transform coding, quantization, and arithmetic coding.
- Results in lossy compression.



Summary

- Compression approaches contain lots of details in
 - Modelling
 - Transforms
 - Algorithms, Implementations
- Not any one solution good for various types of data
 - Images: Binary, color, spectral, video
 - Text, other data
 - Application?
- Still, how to handle the exponential increase in the amount of data?