

ENVM 1502 -River Basin Hydrology and Water Management (2022/23 Q3)

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loading packages

```
In [1]: import os
import glob
import math
import warnings
import datetime
import regionmask
import numpy as np
import pandas as pd
import xarray as xr
import matplotlib as mpl
import matplotlib.pyplot as plt
from scipy.optimize import root
from scipy.stats import theilslopes
from scipy.optimize import fmin

# webscraping Q data
import json
import urllib
from bs4 import BeautifulSoup
from urllib.request import urlopen

# plotting/mapmaking
import rasterio
import cartopy
import cartopy.crs as ccrs
import geopandas as gpd
from rasterio.plot import show as rioshow
from ismn.interface import ISMN_Interface
from cartopy.io.img_tiles import OSM
```

```
from cartopy.mpl.gridliner import LONGITUDE_FORMATTER, LATITUDE_FORMATTER

# own geospatial functions
from geospatial_functions import get_background_map
from geospatial_functions import reproject_raster
from geospatial_functions import remove_below_0

import warnings
warnings.filterwarnings('ignore')
```

specifying directories

In [2]:

```
path = os.getcwd()
home_path = os.path.dirname(path)
data_folder = f'{home_path}\\Data'
gis_folder = f'{home_path}\\GIS'
data_folder_grace = f'{home_path}\\Data\\Grace'
soil_moisture_path = f'{os.path.dirname(path)}\\Data\\Soilmoisture'
ENVM1502_link_path = os.path.dirname(os.path.dirname(os.path.dirname(path)))
ENVM1502_data_path = f'{ENVM1502_link_path}\\Unit 2\\Ex3 - Soil moisture\\'
```

loading needed geospatial layers

these are prepared using data from hydrosheds and dem data

In [3]:

```
# Loading other layers
outline      = gpd.read_file(f'{gis_folder}\\hudson_basin_26918.gpkg", driver="GPKG", crs="EPSG:26918")
main_rivers   = gpd.read_file(f'{gis_folder}\\main_rivers_hudson_basin.gpkg", driver="GPKG", crs="EPSG:26918")
all_rivers    = gpd.read_file(f'{gis_folder}\\rivers_hudson_basin.gpkg", driver="GPKG", crs="EPSG:26918")
gdf_thiessen = gpd.read_file(f'{gis_folder}\\Thiessen_prcp.shp', crs="EPSG:26918")
outline_buffered = gpd.read_file(f'{gis_folder}\\hudson_basin_buffered.gpkg", crs="EPSG:26918")

# fixing crs
for layer in [outline, main_rivers, all_rivers, gdf_thiessen, outline_buffered]:
    layer.geometry = layer.geometry.to_crs("EPSG:4326")
```

More indepth analyses & data can be found on [github](#)

0. Dataset

0.1.1 & 0.1.2 - P

All data is downloaded from: <https://www.ncei.noaa.gov/cdo-web/>. The raw data file is too large to be stored, individual station data can be found [here](#) in the repo.

Initially the mean over the whole area was taken, however this removes the peaks. To combat this thiessen polygons were made to make a better representation of the data. This can be found in notebook [0.1.2](#)

load in station data:

```
In [6]: # define variable to store data
df_lst_input = []
station_lst = []
station_index_dict= {}

# read in all precipitation files
files = glob.glob(f"{data_folder}\P\data per station\*_prcp.csv")
for index, file in enumerate(files):
    df = pd.read_csv(file, index_col='DATE', usecols=['DATE', 'PRCP', 'STATION', 'LATITUDE', 'LONGITUDE'], delimiter=',', parse_dates=['DATE'])
    station_lst.append([df.iloc[0].STATION, df.iloc[0].LATITUDE, df.iloc[0].LONGITUDE])
    df_lst_input.append(df)
    station_index_dict[f"{df.iloc[0].STATION}"] = index
```

combine raw data into layer

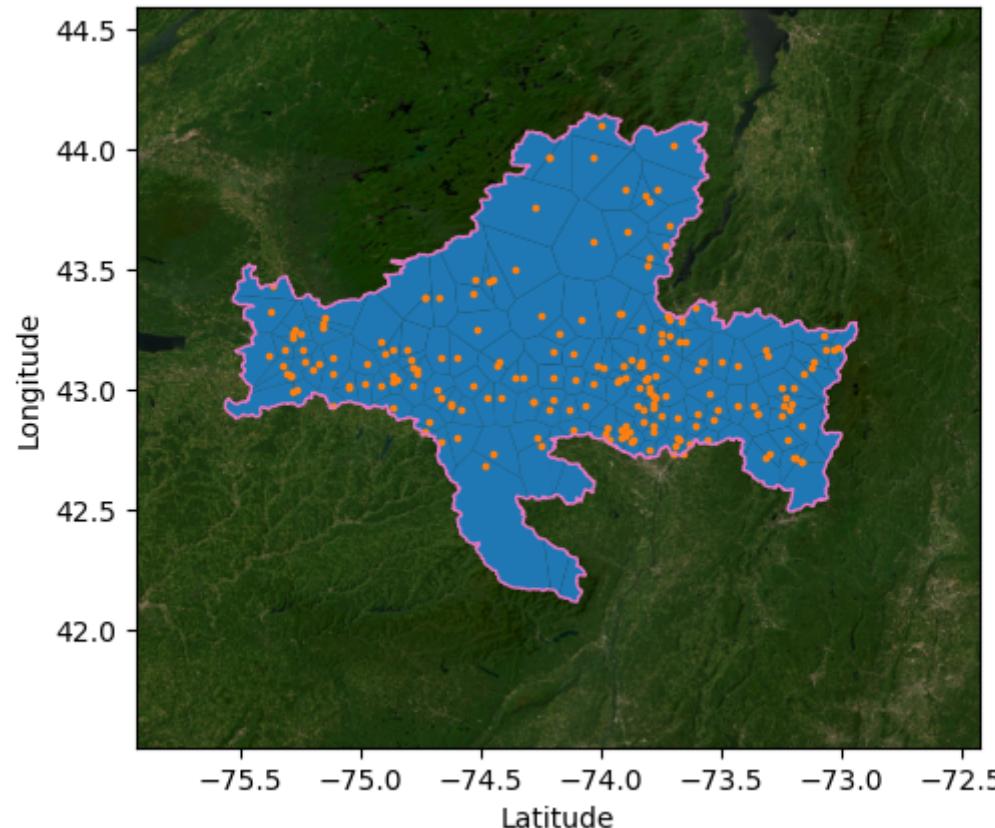
```
In [7]: # make a df of the ids
station_arr = np.array(station_lst)
df_stations = pd.DataFrame(data=list(zip(station_arr[:,0], station_arr[:,1], station_arr[:,2]))),
                           columns = ['STATION', 'LATITUDE', 'LONGITUDE'],)
```

```
# combine the points into a geodataframe to be plotted
geom = gpd.points_from_xy(df_stations.LONGITUDE,df_stations.LATITUDE)
gdf_stations = gpd.GeoDataFrame(data=df_stations,geometry=geom, crs="EPSG:4326")
gdf_stations_in_area = gdf_stations[gdf_stations.within(outline.iloc[0].geometry)]
```

```
In [6]: # plot the stations & polygons
fig, ax = plt.subplots(1)
gdf_thiessen.plot(ax=ax)
gdf_stations_in_area.plot(ax=ax,color="C1",markersize=3) .plot()
outline.plot(ax=ax,edgecolor="C6",facecolor="None")
ax.set_title(f"example of what all {len(gdf_stations_in_area)} stations with thiessen polygons would look like")
ax.set_xlabel("Latitude")
ax.set_ylabel("Longitude")

# add background
bounds_stations = (ax.get_xlim()[0], ax.get_ylim()[0], ax.get_xlim()[1], ax.get_ylim()[1])
with rasterio.open(get_background_map("P_stations", bounds_stations)) as r:
    rio.show(r, ax=ax,zorder=-10);
```

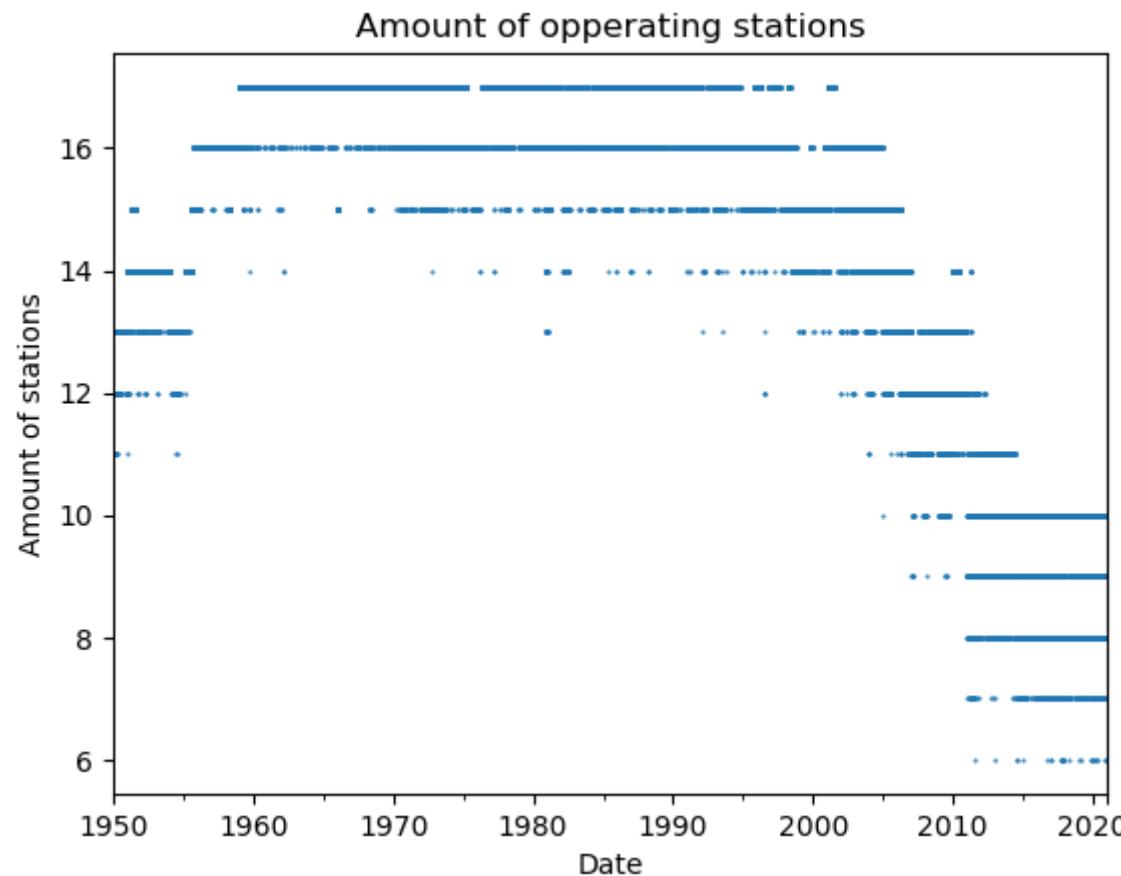
example of what all 205 stations with thiessen polygons would look like



In reality not all stations have data at once, only 4 stations stand between 1950 and 2020, to combat this, we create thiessen polygons for all combinations of stations

```
In [7]: gdf_joined = gdf_stations_in_area.sjoin(gdf_thiessen)
lst_dfs_concat = []
for i in gdf_joined.index:
    station_name = gdf_joined.loc[i,"STATION"]
    station_area = gdf_joined.loc[i,"area"]
    df = df_lst_input[station_index_dict[station_name]][["PRCP"]].copy()
    df.rename(columns={'PRCP':f'{station_name}'},inplace=True)
    lst_dfs_concat.append(df)
df_combined = pd.concat(lst_dfs_concat, axis=1)
```

```
In [8]: n_year = 50 # threshold for the number of years to be operating
# drop columns depending on the threshold
df_selected_combined = df_combined.loc["1950":"2020"].dropna(axis=1, thresh=365*n_year)
# count the amount of nan values
count_nans = df_selected_combined.apply(lambda x: np.isnan([x.loc[col] for col in x.index])).sum(axis=1)
# plot the amount of not-nan-values
(len(df_selected_combined.columns)- count_nans).plot(lw=0,marker=". ",ms=1)
# beautify
plt.title("Amount of operating stations")
plt.ylabel("Amount of stations")
plt.xlabel("Date");
```



to speed thing up the threshold was lowered in this case, but a threshold of 20 continous years was used to generate the data set. An example is given below of how the polygon code looks

```
In [9]: # code to create thiessen polygons
from longsgis import voronoiDiagram4plg
def draw_thiessen_polygons(stations, boundary):
    """https://pypi.org/project/voronoi-diagram-for-polygons/
    warnings.filterwarnings("ignore", category=FutureWarning)
    vd = voronoiDiagram4plg(stations, boundary)
    return vd
```

```
In [10]: # make a list of columns in th df
columns = np.array(df_selected_combined.columns.to_list())
# create a list of stations in a given row: this is to reduce the number of theissen combinations to make
series_stations_not_na_txt = df_selected_combined.apply(lambda x: ','.join(columns[~np.isnan([x.loc[col] for col in x.index])]))
# load this isnto a df
df_stations_not_na_txt = pd.DataFrame(data=series_stations_not_na_txt,columns=["names_station"])
# obtain the total area
total_area = outline.to_crs("EPSG:26918").area.sum()
# lists to store data being generated
lst_df_joined = []
dict_df_joined = {}
# loop over all the combinations of thiessen polygons - to demonstrate we just do one
for index, combination in enumerate(df_stations_not_na_txt['names_station'].unique()[:1]):
    # split the ids we joined in line 4
    ids_to_thiessen = combination.split(",")
    # get the data for each station
    df_station_to_thiessen = gdf_stations_in_area.set_index("STATION").loc[ids_to_thiessen]
    # draw the polygons
    thiessen_polygons = draw_thiessen_polygons(df_station_to_thiessen, outline)
    # fix crs issues for plotting
    thiessen_polygons = thiessen_polygons.to_crs("epsg:26918")
    df_station_to_thiessen = df_station_to_thiessen.to_crs("epsg:26918")
    # only importance is the area
    thiessen_polygons["Area_m2"] = thiessen_polygons.area
    # ensure the stataion has this area attribute
    df_joined = df_station_to_thiessen.sjoin(thiessen_polygons)
    # save the outputs to be used later, dict to get the index, list to store the data
    lst_df_joined.append(df_joined)
    dict_df_joined[combination] = index
```

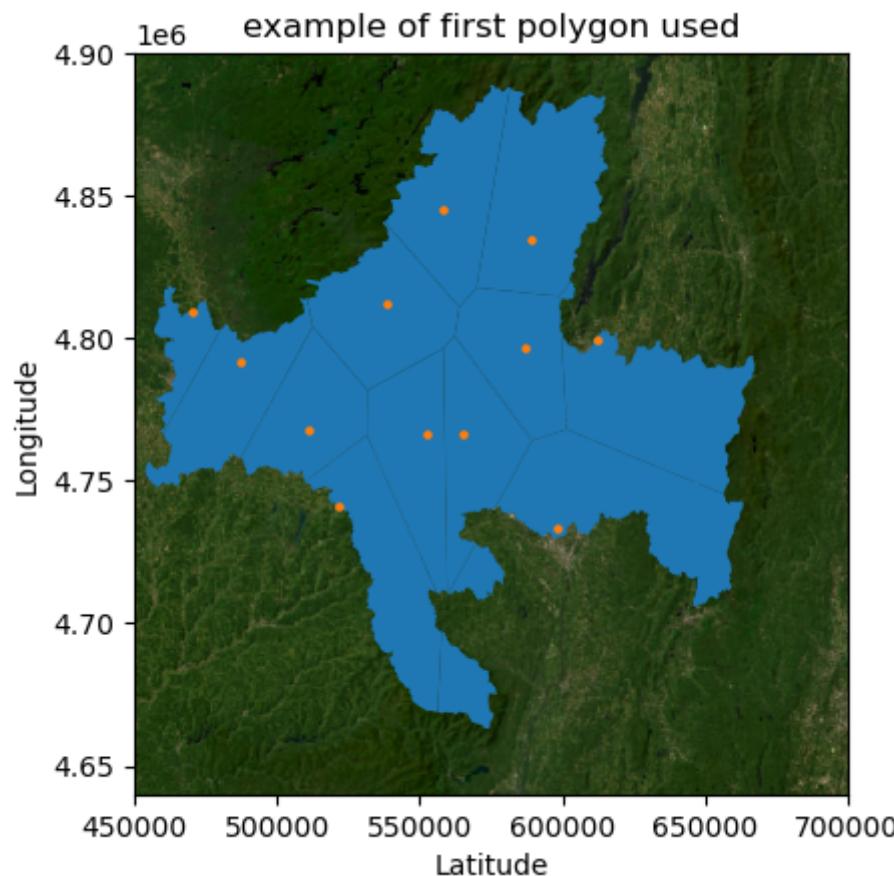
```
In [11]: # plot the result
fig, ax = plt.subplots(1)
df_station_to_thiessen.plot(ax=ax, color="C1", zorder=10, markersize=5)
thiessen_polygons.plot(ax=ax)
ax.set_title("example of first polygon used")

# add background
old_outline_path = get_background_map("outline", bounds_stations)
background_epsg26918 = reproject_raster(old_outline_path, "epsg:26918", ending=".tif")
with rasterio.open(background_epsg26918) as r:
```

```
rioshow(r, ax=ax, zorder=-10)

ax.set_xlim((4.5e5,7e5))
ax.set_ylim((4.64e6,4.9e6))

ax.set_xlabel("Latitude")
ax.set_ylabel("Longitude");
```

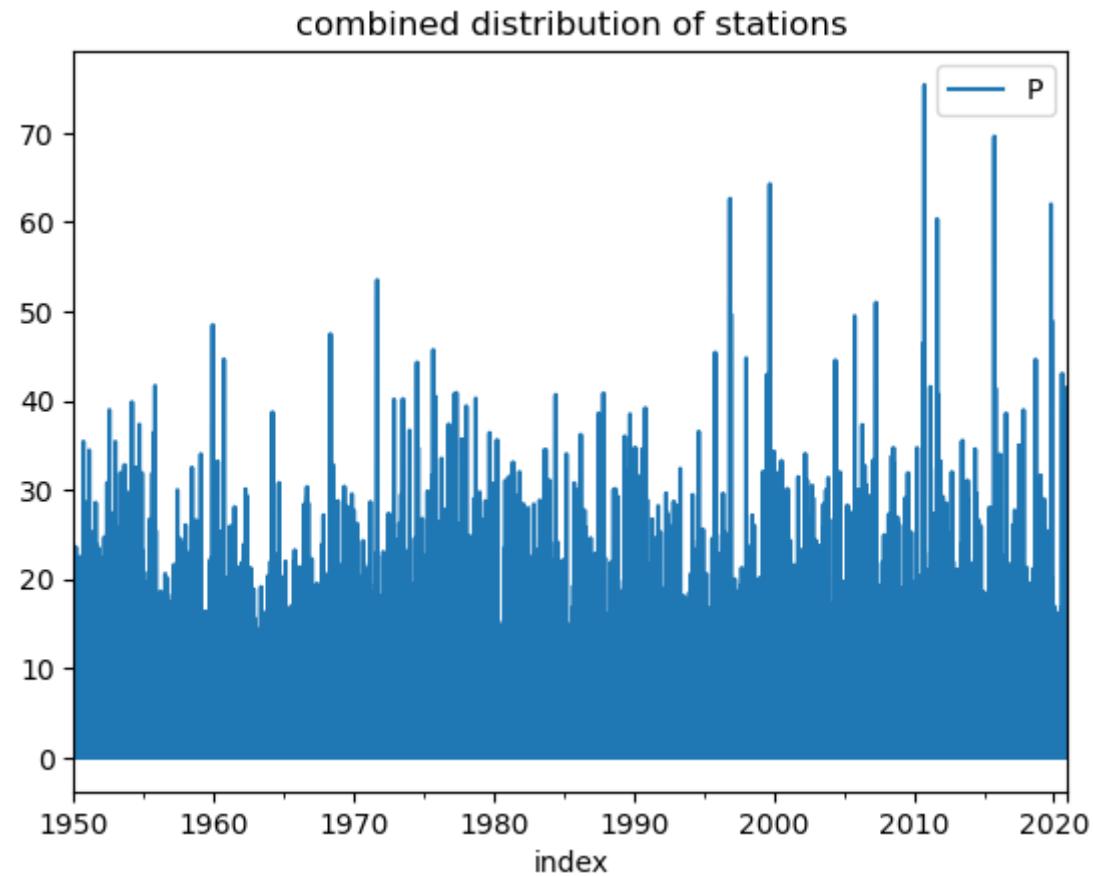


With the polygons generated the data can then be added by multiplying P with the fraction & summing

```
In [12]: df_p = pd.read_parquet(f"{data_folder}\P\weighted_average_P.parquet")

fig, ax = plt.subplots(1)
```

```
df_p.plot(ax=ax)
ax.set_title("combined distribution of stations");
```



0.1.3 - T

Similar to P, T was loaded in from station data obtained from <https://www.ncei.noaa.gov/cdo-web/>. More info in notebook 0.1.3

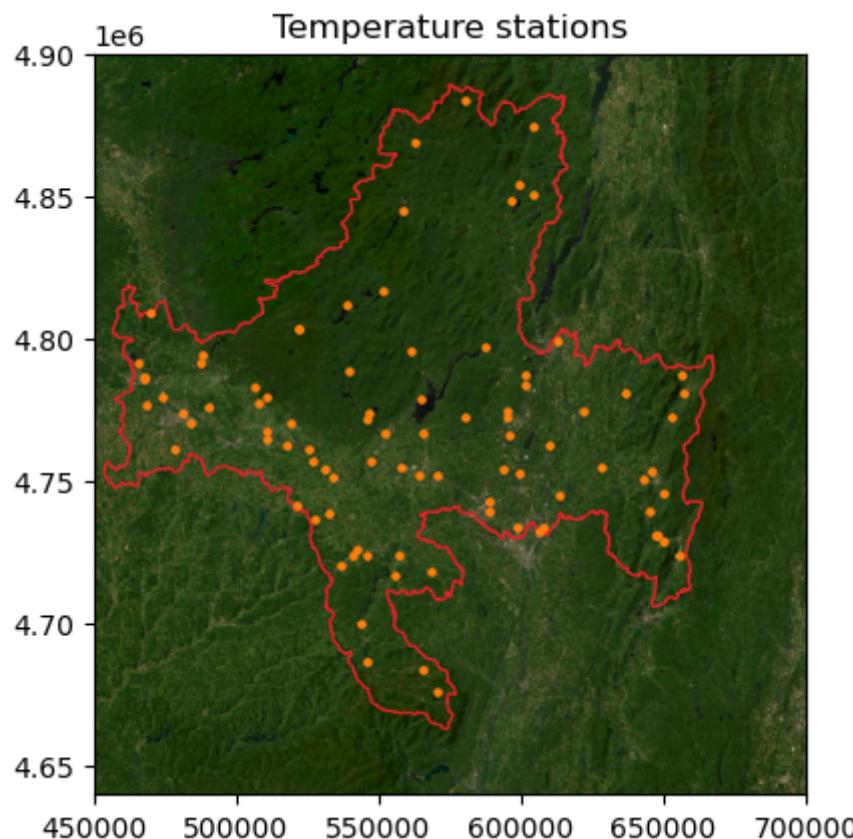
```
In [13]: gdf_stations = gpd.read_file(f'{gis_folder}\\\location_temperature_stations_upperbains_26918.gpkg')
```

```
In [14]: fig, ax = plt.subplots(1)
gdf_stations.plot(ax=ax, color="C1", zorder=10, markersize=5)
```

```
outline.to_crs("epsg:26918").plot(ax=ax, edgecolor='C3', facecolor="none")
ax.set_title("Temperature stations")

# add background
old_outline_path = get_background_map("outline", bounds_stations)
background_epsg26918 = reproject_raster(old_outline_path, "epsg:26918", ending=".tif")
with rasterio.open(background_epsg26918) as r:
    rio.show(r, ax=ax, zorder=-10)

ax.set_xlim((4.5e5,7e5))
ax.set_ylim((4.64e6,4.9e6));
```



In [15]: # turn df into gdf
df_station_ids = gdf_stations[["station ID"]].rename(columns={"station ID": "station_id"})

```
# Lists to store data
lst_t_dfs_max = []
lst_t_dfs_min = []
lst_elevation = []
# Loop over all lists
for ids in df_station_ids.station_id.values:
    # read & store ids
    df_in = pd.read_parquet(f"{data_folder}\\T\\data parquet basin\\temp_{ids}.parquet")
    lst_elevation.append([ids,df_in["ELEVATION"].iloc[0]])
    # fix indexing
    df_in["DATE"] = pd.to_datetime(df_in["DATE"])
    df_in = df_in.set_index("DATE")
    # remove unrealistic/error data
    df_in["TMAX"] = df_in["TMAX"].apply(lambda x: x if (x < 100) else np.nan)
    df_in["TMIN"] = df_in["TMIN"].apply(lambda x: x if (x < 100) else np.nan)
    df_in = df_in.rename(columns={"TMAX":f"TMAX_{ids}", "TMIN":f"TMIN_{ids}"})
    # store data
    df_in_max = df_in.drop(columns=['STATION', 'NAME', 'LATITUDE', 'LONGITUDE', 'ELEVATION', f"TMIN_{ids}"])
    df_in_min = df_in.drop(columns=['STATION', 'NAME', 'LATITUDE', 'LONGITUDE', 'ELEVATION', f"TMAX_{ids}"])
    lst_t_dfs_max.append(df_in_max)
    lst_t_dfs_min.append(df_in_min)
```

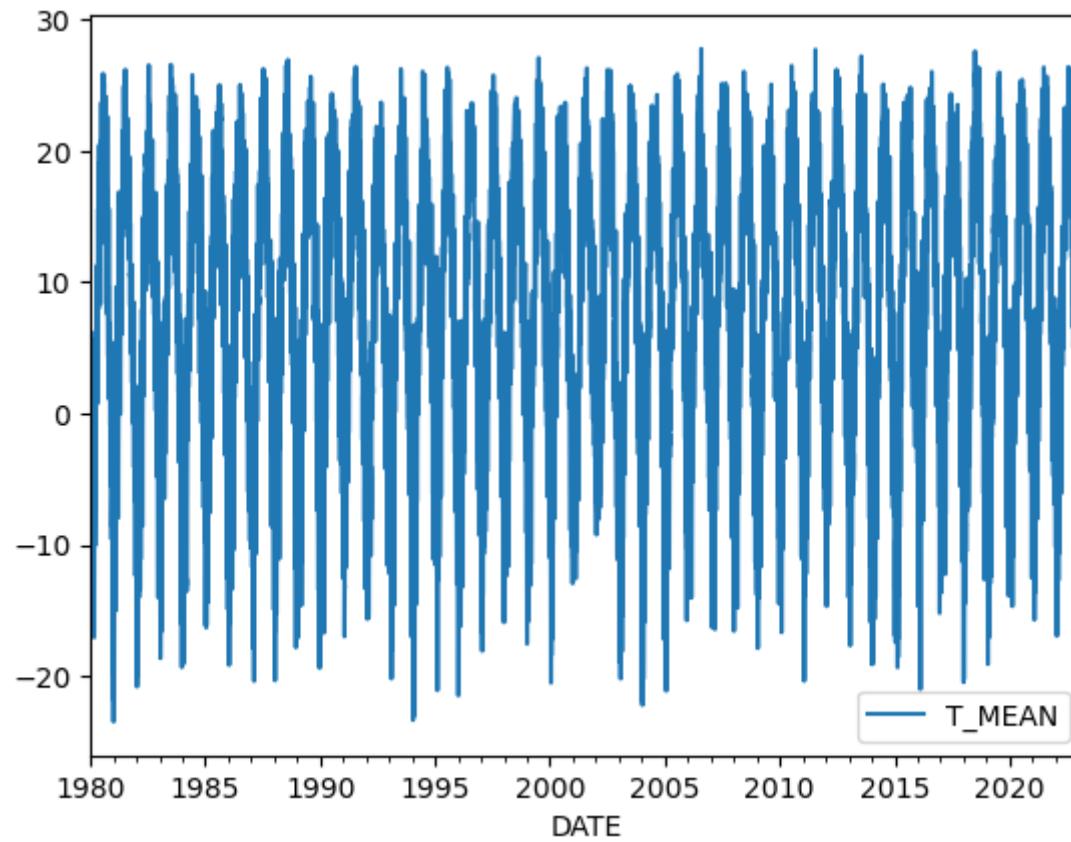
In [16]:

```
df_combined_max = pd.concat(lst_t_dfs_max, axis=1)
df_combined_mean_max = df_combined_max.mean(axis=1)

df_combined_min = pd.concat(lst_t_dfs_min, axis=1)
df_combined_mean_min = df_combined_min.mean(axis=1)
```

In [17]:

```
temp_mean_series = (df_combined_mean_max + df_combined_mean_min) /2
df_t = pd.DataFrame(data=temp_mean_series, columns=[ "T_MEAN"])
df_t.loc["1980":].plot();
```



0.2 Q

From the USGS website we can extract hydrological units for the basin

USGS Watershed Boundary Dataset (WBD) for 2-digit Hydrologic Unit - 02 (published 20230306) GeoPackage using [USGS TNM Download \(v2.0\)](#)



The ids shown on the map can be loaded in

```
In [12]: gdf_wbdhu = gpd.read_file(f'{gis_folder}\WBDHU8-hudson.gpkg', driver="GPKG", crs="EPSG:4326")
huc8_ids = ",".join(gdf_wbdhu.huc8.values)
# However we only take the northern part
huc8_ids = ",".join(gdf_wbdhu.iloc[[0,2,3,4,8]].huc8.values)
huc8_ids
```

```
Out[12]: '02020002,02020003,02020004,02020001,02020005'
```

Which we can query

```
In [13]: station_id_rest_query = f"https://waterservices.usgs.gov/nwis/dv/?format=rdb&huc={huc8_ids}&parameterCd=00060&siteType=ST&site
page = urlopen(station_id_rest_query)
html_bytes = page.read()
html = html_bytes.decode("utf-8")
```

& process

```
In [14]: # the 15th Line contains the number of sites:
skip_rows = 15
line = html.split("\n")[skip_rows]
print(line)
n = int(line[line.find("following ")+len("following "):line.find(" site")].strip())

data = html.split("\n")[skip_rows+1:skip_rows+1+n]
data_ordered = []
for line in data:
    words = line[line.find("USGS"):] .split(" ")
    type_id_name = words[:2] + [" ".join(words[2:])]
    data_ordered.append(type_id_name)
df_sites = pd.DataFrame(data=data_ordered,columns=["provider","site_no","name"])
df_sites.site_no = df_sites.site_no.astype(int)

df_sites.head(4)
```

```
# Data for the following 109 site(s) are contained in this file
```

Out[14]:

	provider	site_no	name
0	USGS	131199050	FISHING BROOK (COUNTY LINE FLOW OUTLET) NR NEW...
1	USGS	1311992	ARBUTUS POND OUTLET NEAR NEWCOMB NY
2	USGS	1312000	HUDSON RIVER NEAR NEWCOMB NY
3	USGS	1313500	CEDAR R BELOW CHAIN LAKES NR INDIAN LAKE NY

for these site numbers we can get the location & plot them, see notebook [0.2.2](#)

In [15]:

```
def plot_map(gdf_station, ax):
    legend_field = []

    # stations
    gdf_station.plot(ax=ax, markersize=2, color="C1")
    legend_field.append(mpl.lines.Line2D([],[],color='C1', linewidth=0, marker=".", label='station'))

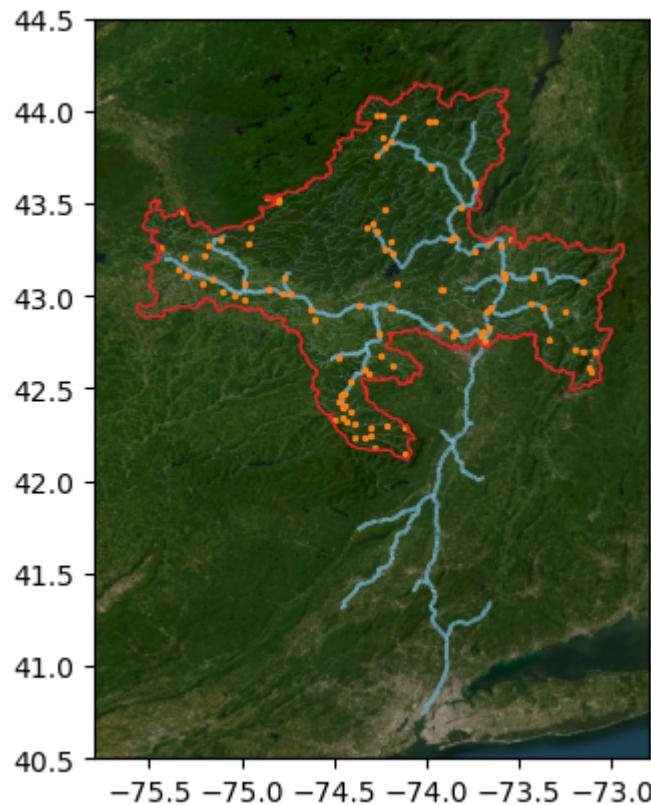
    outline.plot(ax=ax, edgecolor="C3", facecolor="None")
    main_rivers.plot(ax=ax, color="lightskyblue", alpha=0.6, zorder=-1, lw=1.5)
    all_rivers.plot(ax=ax, color="lightskyblue", alpha=0.2, zorder=-2, lw=0.4)
    # add background
    bounds_stations = (ax.get_xlim()[0], ax.get_ylim()[0], ax.get_xlim()[1], ax.get_ylim()[1])
    with rasterio.open(get_background_map("outline", bounds_stations)) as r:
        rioshow(r, ax=ax, zorder=-10)
    ax.set_xlim(-75.8, -72.8)
    ax.set_ylim(40.5, 44.5)
```

In [16]:

```
gdf_station = gpd.read_file(f"{gis_folder}\\discharge_stations.gpk", driver="GPKG")
# fixing indexing
gdf_station.index = gdf_station.apply(lambda x: int(x.site_no[1:]), axis=1)
gdf_station = gdf_station.drop(columns=["site_no"])
```

In [17]:

```
fig, ax = plt.subplots(1)
plot_map(gdf_station, ax)
```



These sites can then be loaded in, which can be found in notebook [0.2.3](#).

We focussed on station 1358000 as this was at the bottom of the catchement closest to the outflow.

```
In [18]: begin_end_date_csv = f"{data_folder}\Q_ids_with_begin-end-date.csv"
df_id_dates = pd.read_csv(begin_end_date_csv,index_col=0)
df_id_dates.set_index("ID",inplace=True)

lst_data = []
lst_errors = []
found_ids = []

for path in glob.glob(f"{data_folder}\Q\1*.parquet"):
    df = pd.read_parquet(path)
    # check columns integrity, else this will fail
```

```

df = df[['agency_cd', 'site_no', 'Data_codes', 'Q_m3_s_mean', 'date']]
df.index = pd.to_datetime(df.date)
df = df[df["Q_m3_s_mean"] > -999]
site_no = int(str(df['site_no'].iloc[0])[1:])
found_ids.append(site_no)
area = df_id_dates.loc[site_no, "Area_m2"]
df["Area_USGS"] = area
df["Q_mm_d"] = df["Q_m3_s_mean"] * 86400 / area * 1000 # s -> d, m3 -> mm
lst_data.append(df)

```

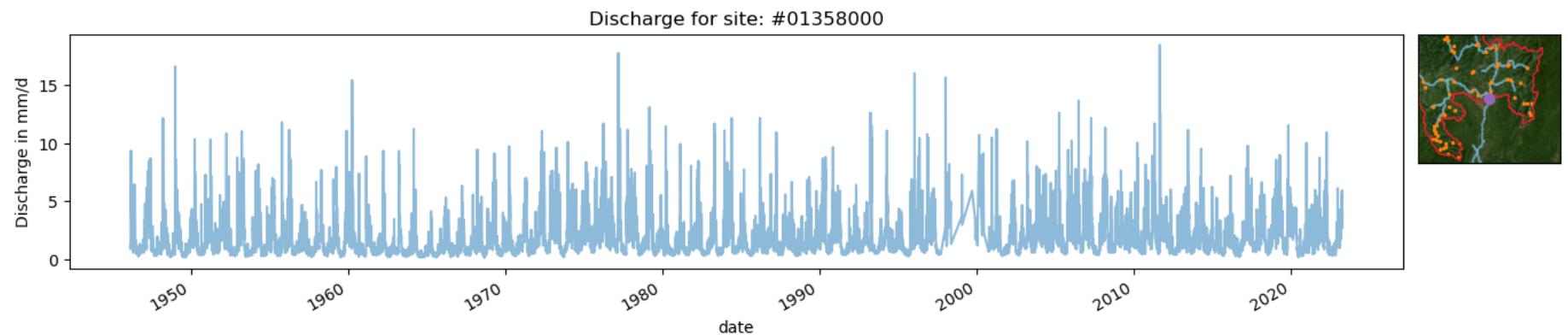
In [19]: wanted_index = list(found_ids).index(1358000)
wanted_index

Out[19]: 107

In [20]: `def plot_map(ax, station_id):`
 `legend_field = []`
 `# stations`
 `gdf_station.plot(ax=ax, markersize=2, color="C1")`
 `legend_field.append(mpl.lines.Line2D([],[],color='C1', linewidth=0, marker=".", label='station'))`
 `outline.plot(ax=ax, edgecolor="C3", facecolor="None")`
 `main_rivers.plot(ax=ax, color="lightskyblue", alpha=0.6, zorder=-1, lw=1.5)`
 `all_rivers.plot(ax=ax, color="lightskyblue", alpha=0.2, zorder=-2, lw=0.4)`
 `bounds_stations = (ax.get_xlim()[0], ax.get_ylim()[0], ax.get_xlim()[1], ax.get_ylim()[1])`
 `# add background`
 `with rasterio.open(get_background_map("outline", bounds_stations)) as r:`
 `rioshow(r, ax=ax, zorder=-10)`
 `# remove lat/lon markers`
 `ax.set_xticks([])`
 `ax.set_yticks([])`
 `# zoom on one station`
 `given_station = gdf_station.loc[[station_id]]`
 `given_station.plot(ax=ax, color="C4", markersize=40)`
 `x, y = given_station.geometry.x.iloc[0], given_station.geometry.y.iloc[0]`

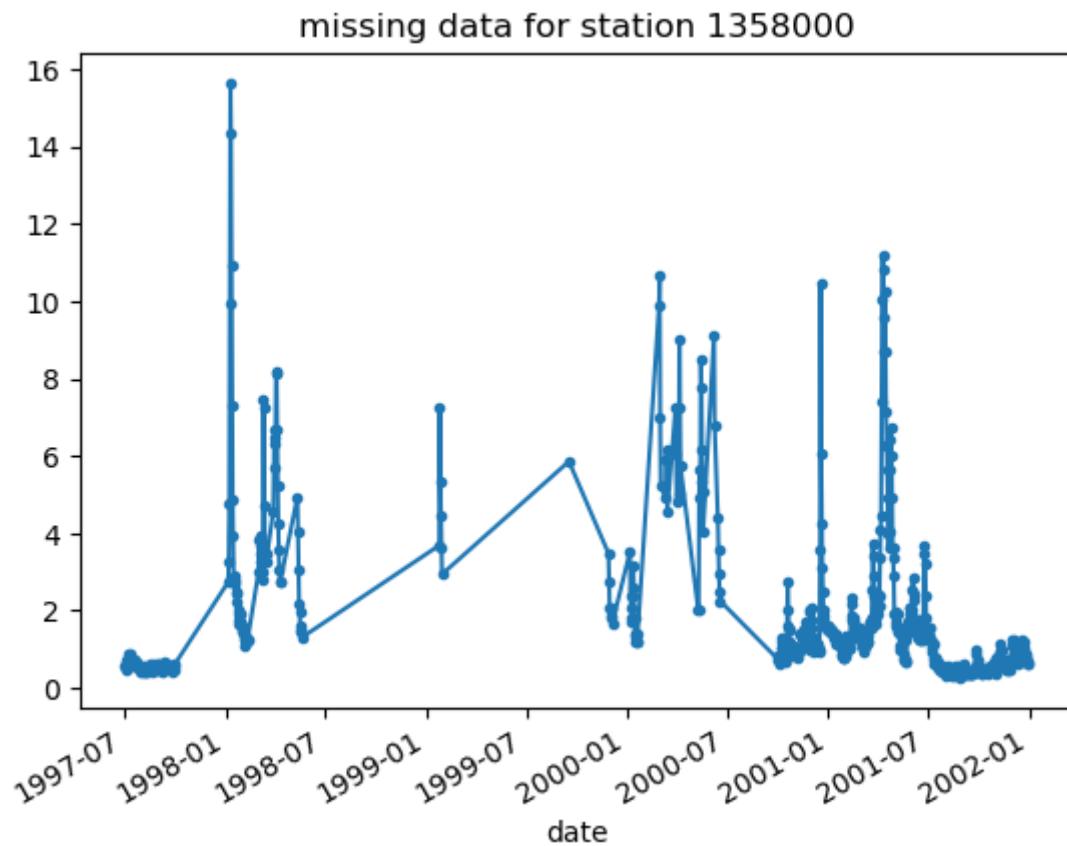
```
n = 1
ax.set_xlim(x- n,x + n)
ax.set_ylim(y -(2*n/3),y +(2*n/3))
```

```
In [21]: df = lst_data[wanted_index]
fig, ax = plt.subplots(1,figsize=(15,3))
ax2 = ax.inset_axes([.79,.45, 0.55,0.55])
plot_map(ax2, int(df["site_no"].iloc[0]))
df[['Q_mm_d']].plot(ax=ax, alpha=0.5)
ax.set_title(f'Discharge for site: #{df["site_no"].iloc[0]}')
ax.legend().remove()
ax.set_ylabel("Discharge in mm/d");
```



after a closer look this gaues seems to be missing some data between 1997 & 2001

```
In [28]: lst_data[wanted_index][ "Q_mm_d"].loc[ "1997-07": "2001"].plot(marker=".")
plt.title("missing data for station 1358000");
```



Instead opt for adding two gauges together: 01357500 & 01335754

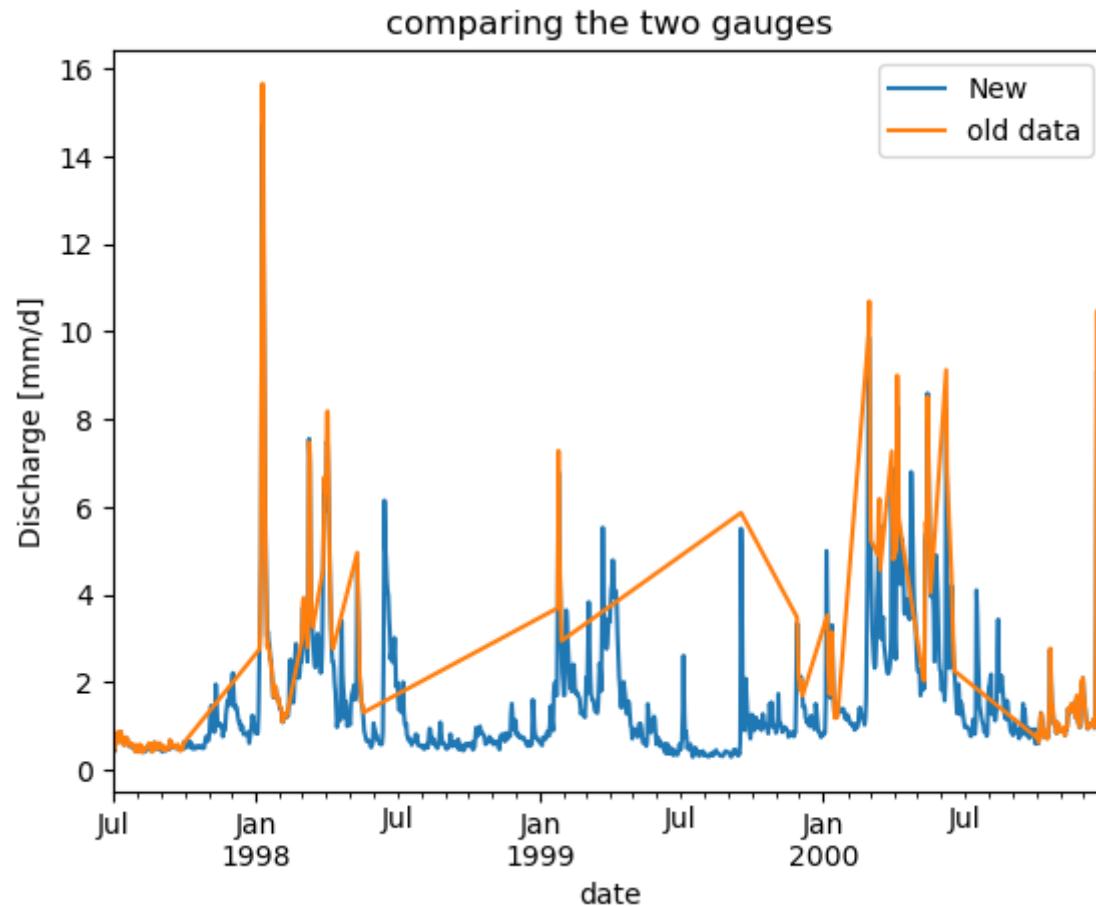


```
In [29]: # the flows have been added in m^3/s then divided by the total area
df_combined_E_W_path = glob.glob(f"{data_folder}\Q\combining_1357500_1335754.parquet")

df_combined_E_W = pd.read_parquet(df_combined_E_W_path[0], columns=['Q_mm_d_hydro', 'date'])
df_combined_E_W.index = pd.to_datetime(df_combined_E_W.date)
df_combined_E_W.rename(columns={'Q_mm_d_hydro': 'Q'}, inplace=True)
```

```
In [31]: ax = df_combined_E_W["Q"].loc["1997-07":"2000"].plot(label="New")
lst_data[wanted_index]["Q_mm_d"].loc["1997-07":"2000"].plot(ax=ax, label="old data")
```

```
ax.legend()  
ax.set_ylabel('Discharge [mm/d]')  
ax.set_title("comparing the two gauges");
```



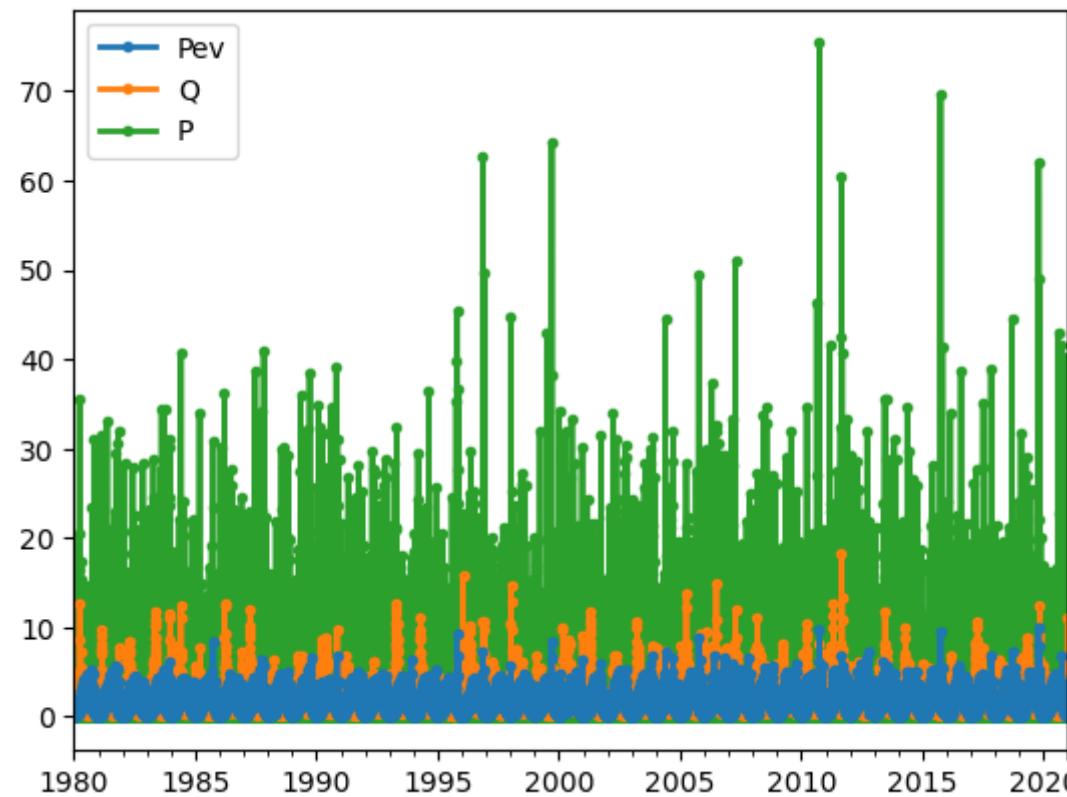
0.3 E_pot

-> handled in 2.5 & 2.6

0.4 Combining these four variables

The gleam data is only available from the 1980s so this is taken as the begin of the data period, full details in notebook [0.4](#)

```
In [3]: combined_forcing = pd.read_parquet(f"{data_folder}\\combined_data.parquet")
combined_forcing = combined_forcing.loc["1980":"2020"]
for i, col in enumerate(["Pev","Q","P"]):
    combined_forcing[col].plot(lw=2,marker=".",zorder=2-i,label=col)
plt.legend();
```



1.1 - Budyko

```
In [32]: def budyko(df_data_1, show=True):
    df_data_1.dropna(inplace=True)
    df_data = df_data_1.copy()
    fig, ax = plt.subplots()

    #Calculate mean
    p_mean = df_data_1.P.mean()
    q_mean = df_data_1.Q.mean()
    ep_mean = df_data_1.Pev.mean()

    df_data_1['Ea_P'] = 1 - df_data_1['Q'] / df_data_1['P']

    EA_P = 1 - q_mean / p_mean
    EP_P = ep_mean / p_mean

    EP_P_max = int(EP_P + 5)
    EP_P_array = np.linspace(1e-9, EP_P_max, EP_P_max*10)

    #Calculate theoretical Budyko
    budyko = (EP_P_array * np.tanh(1 / EP_P_array) * (1 - np.exp(-EP_P_array))) ** 0.5
    budyko_EP = (EP_P * np.tanh(1 / EP_P) * (1 - np.exp(-EP_P))) ** 0.5
    budyko_EA = budyko_EP * p_mean

    dS_dt = p_mean - q_mean - budyko_EA

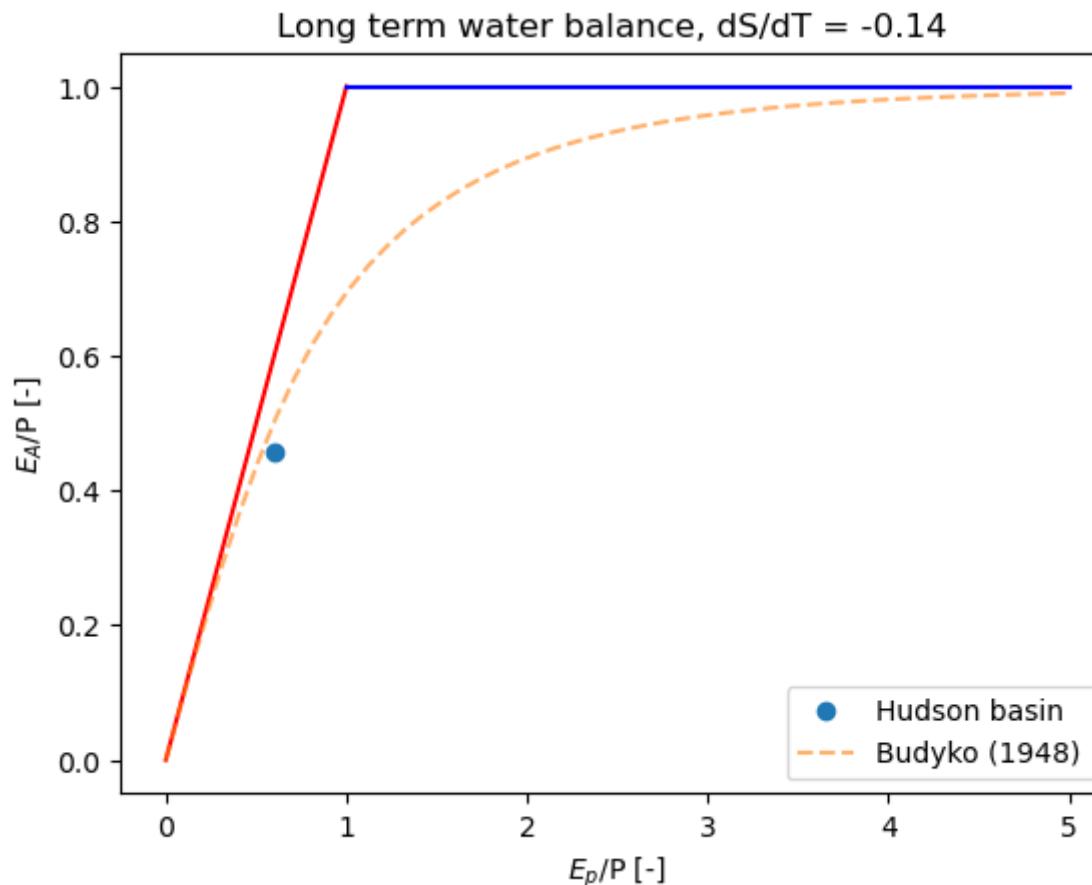
    #Make figure
    ax.plot([0,1], [0,1], 'r')
    ax.plot([1, EP_P_max], [1, 1], 'b')
    ax.set_xlabel('$E_p/P [-]')
    ax.set_ylabel('$E_A/P [-]$')

    ax.set_title(f'Long term water balance, dS/dT = {dS_dt:.2f} ')
    ax.plot(EP_P, EA_P, 'o', label=f'Hudson basin')
    ax.plot(EP_P_array, budyko, '--', alpha=0.6, label=f'Budyko (1948) ')
    ax.legend()

    if show != True:
        plt.close()
```

```
    return df_data, dS_dt
```

```
In [33]: long_term, dS_dt = budyko(combined_forcing)
```



As the partitioning point for this catchment lies close to the budyko curve this shows a good start. (section 2.6 made this possible)

```
In [34]: def flow_duration(df, ax, show=True):  
  
    df['Q'].dropna(inplace=True) #Drop the nan values  
    df_q = df[["Q"]].rename(columns={"Q": "R"})
```

```

# sort values in descending order
df_q.sort_values("R", ascending=False, inplace=True)
# by resetting the index we number them 1 to n
df_q = df_q.reset_index().reset_index()
df_q.set_index("index", inplace=True)
# this defaults to level_0 by pandas this is our m
df_q.rename(columns={"level_0": "m"}, inplace=True)
n = len(df_q) # number of observations
# we want to start at 1, not 0 so shift the numbering
df_q['m'] = df_q.apply(lambda x: x.m+1, axis=1)
# calculate p
df_q['p'] = df_q.apply(lambda x: x.m / (n+1), axis=1)

ax[0].set_ylabel("Runoff Q in [mm/d$]")
ax[0].set_xlabel("Date")
ax[0].set_title('Discharge Hudson River')
df[['Q']].plot(ax = ax[0], color="C0", xlabel='Date')

ax[1].set_ylabel("Runoff Q in [mm/d$]")
ax[1].set_xlabel("Exceedance probability [-]")
ax[1].set_title(f"Run off exceedance probability ")
ax[1].set_yscale("log")
ax[1].grid()
ax[1].plot(df_q.p, df_q.R, color="C0")

if show != True:
    plt.close()

return df_q

```

In [35]:

```

def auto_correlation(df, ax, show=True):
    df.dropna(inplace=True)
    lag = range(50)
    corr_coeff_1 = []
    #calculate correlation coefficient for different time Lags
    for i in lag:
        corr_coeff_1.append(df['Q'].autocorr(lag=i))
    # create a plot
    df['Q'].plot(ax=ax[0],color="C0")
    ax[0].set_ylabel("Runoff Q in [mm/d$]")

```

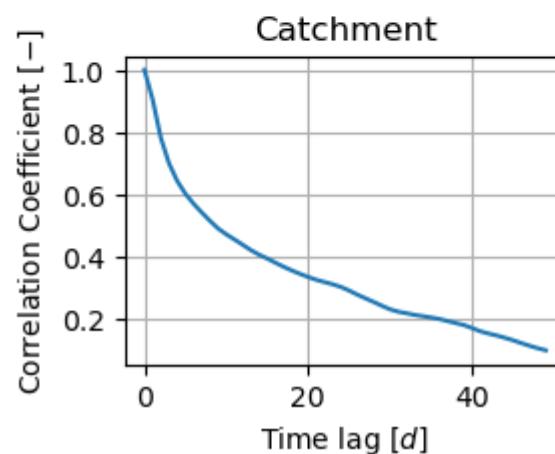
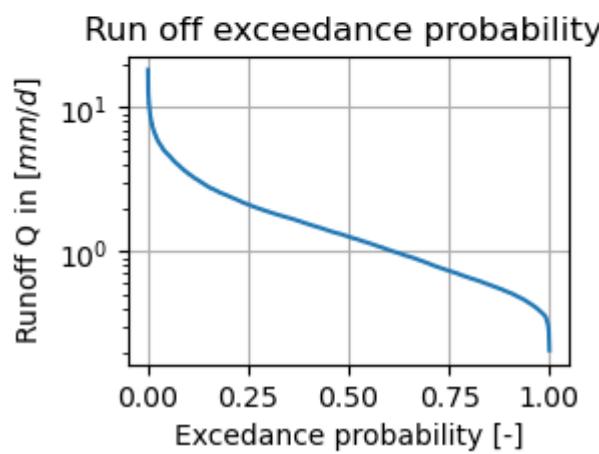
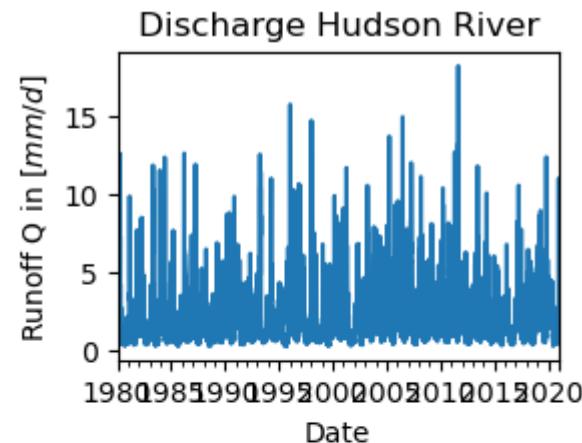
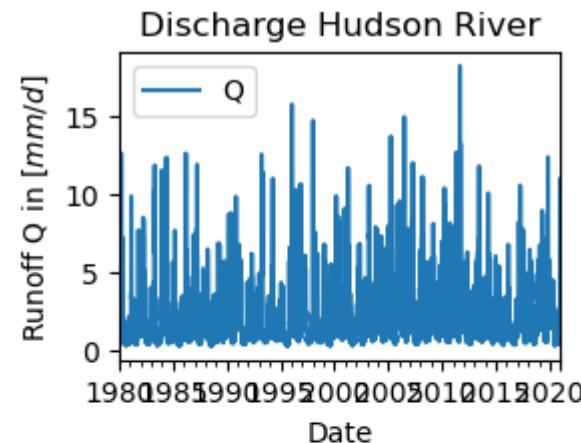
```
ax[0].set_xlabel("Date")
ax[0].set_title('Discharge Hudson River')

ax[1].plot(lag, corr_coeff_1, color="C0")
ax[1].set_ylabel("Correlation Coefficient $[-]$")
ax[1].set_xlabel("Time lag $[d]$")
ax[1].set_title(f"Catchment")
ax[1].grid()

if show != True:
    plt.close()

return corr_coeff_1
```

```
In [36]: fig, ax = plt.subplots(2,2)
fig.tight_layout(h_pad=6, w_pad=6)
_ = flow_duration(combined_forcing, [ax[0][0],ax[1][0]])
_ = auto_correlation(combined_forcing,[ax[0][1],ax[1][1]])
```



1.2 - Extreme value analysis

prepare the data

```
In [37]: prcp_df = combined_forcing[["P"]].copy()
prcp_df.dropna()
```

```
prcp_df.rename(columns={"P": "PRCP"}, inplace=True)
prcp_df = prcp_df[prcp_df.index > pd.Timestamp("1892-08-01")] # skip gap in data
```

In [38]:

```
def annual_maxima(data):
    """function to generate annual maxima by returning list ids belonging to yearly max"""
    idx_max = data.groupby(data.index.year)[['PRCP']].idxmax()
    max_list = data.loc[idx_max]
    return max_list
```

In [39]:

```
df_prcp_maxima = annual_maxima(prcp_df).sort_values("PRCP", ascending=False)
df_prcp_maxima.index.name = "time"
df_prcp_maxima.head()
```

Out[39]:

	PRCP
	time
2010-10-01	75.381120
2015-09-30	69.611906
1999-09-17	64.277034
1996-11-09	62.635524
2019-10-17	62.010101

Calculate empirical statistics for these maxima

In [40]:

```
# exercise, calculate N and expand your annual maxima dataframe with the columns i, p, q, y, T_a
M = len(df_prcp_maxima)

# indexing tricks to obtain i
df_prcp_maxima_ranked = df_prcp_maxima.copy().reset_index().reset_index()
df_prcp_maxima_ranked.set_index("time", inplace=True)
df_prcp_maxima_ranked['i'] = df_prcp_maxima_ranked.apply(lambda x: int(x['index']) + 1, axis=1)
df_prcp_maxima_ranked.drop(columns=['index'], inplace=True)

# use i to obtain p
df_prcp_maxima_ranked['p'] = df_prcp_maxima_ranked.apply(lambda x: int(x.i) / (M+1), axis=1)
```

```
# q = 1-p
df_prcp_maxima_ranked['q'] = df_prcp_maxima_ranked.apply(lambda x: 1 - x.p, axis=1)

# to compute y = -ln(-ln(q))
df_prcp_maxima_ranked['y'] = df_prcp_maxima_ranked.apply(lambda x: -np.log(-np.log(x.q)), axis=1)

# obtain T_a with 1/p
df_prcp_maxima_ranked['T_a'] = df_prcp_maxima_ranked.apply(lambda x: 1 / x.p, axis=1)
```

Calculate statistics for gumbel & fit

In [41]:

```
# exercise: compute Gumbel parameters (name them sigma and mu)
annual_maxima_df_sorted = df_prcp_maxima_ranked.copy()
s_R = annual_maxima_df_sorted['PRCP'].std()
s_y = annual_maxima_df_sorted['y'].std()
y_gem = annual_maxima_df_sorted['y'].mean()
R_max_gem = annual_maxima_df_sorted['PRCP'].mean()

sigma = s_R / s_y
mu = R_max_gem - s_R * y_gem / s_y

print(f'scale parameter σ = {sigma:.3f}')
print(f'location parameter μ = {mu:.3f}')
```

scale parameter σ = 10.490
location parameter μ = 35.052

In [42]:

```
# Now we can construct the Gumbel fit and plot the Gumbel line
dummy_y = np.arange(-2, 6.01, 0.2)
R_Gumbel = sigma * dummy_y + mu

fig, [ax, ax2] = plt.subplots(1, 2, figsize=(10, 5))
fig.tight_layout(w_pad=3)

ax.plot(annual_maxima_df_sorted['y'].values, annual_maxima_df_sorted['PRCP'].values, \
        'xk', markersize=7, label='Observed Annual Maxima')
ax.plot(dummy_y, R_Gumbel, \
        ':og', label = 'Gumbel Estimate')
ax.set_xlabel('Reduced variate y')
ax.set_ylabel('Precipitation (mm/day)')
```

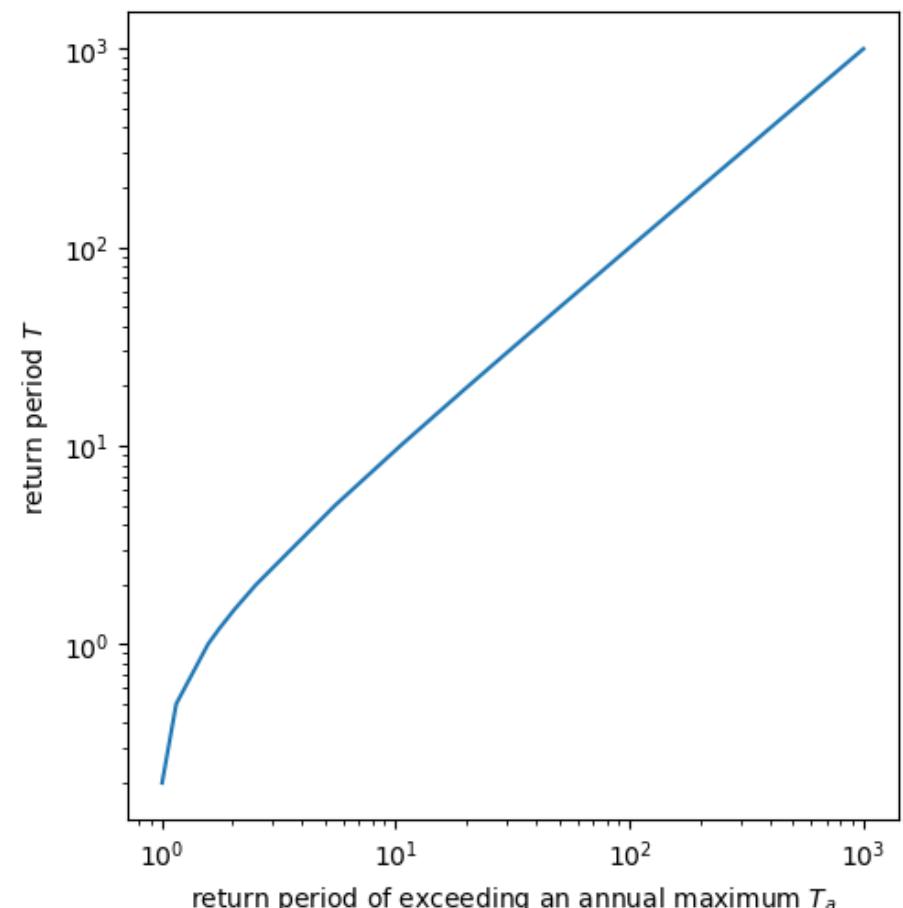
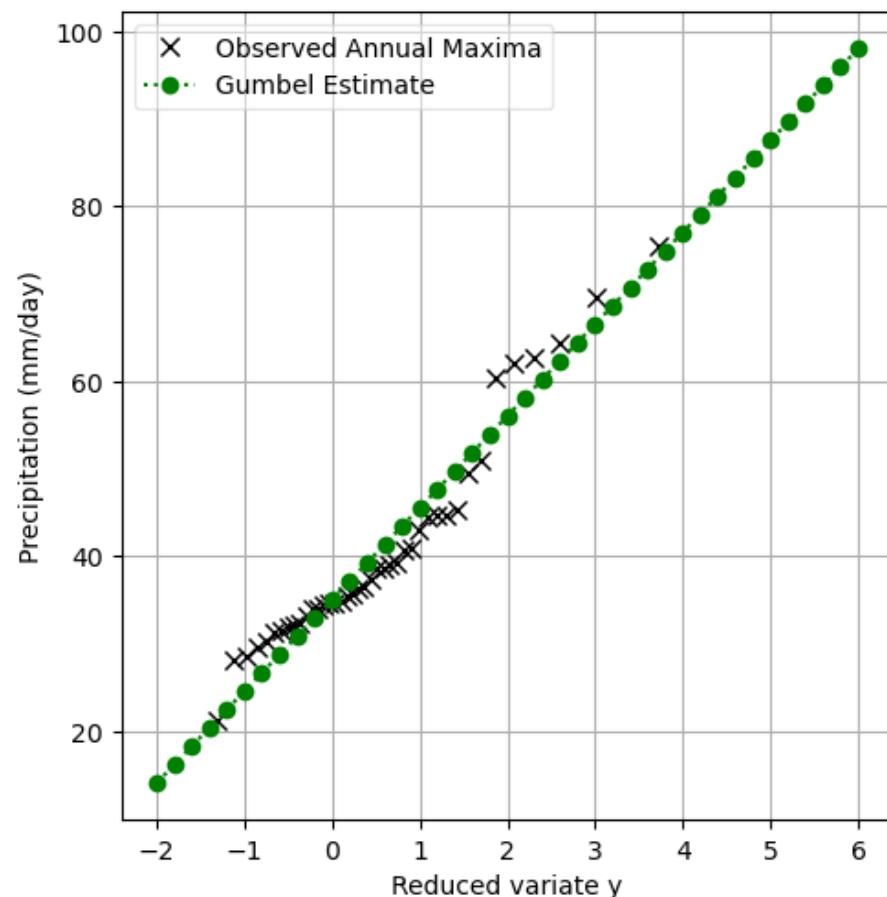
```

ax.legend(loc='best', framealpha=0.5)
ax.grid(True)

# Here we define the return periods and we inspect the difference between the two return periods
T_interest = np.asarray([0.2, 0.5, 1, 1.2, 1.5, 2, 5, 10, 20, 35, 50, 100, 200, 500, 1000])
T_a_interest = 1 / (1-np.exp(-1/T_interest))
ax2.loglog(T_a_interest,T_interest)
ax2.set_xlabel('return period of exceeding an annual maximum $T_a$')
ax2.set_ylabel('return period $T$')

# real return period for the observed annual maxima
annual_maxima_df_sorted['T'] = df_prcp_maxima_ranked.apply(lambda x: -1 / np.log(1 - (1/ x["T_a"])), axis=1)

```



Looks fairly straight forward, we continue with the MEV

```
In [43]: gumbel_estimate = sigma * (- np.log(1/T_interest)) + mu
T = annual_maxima_df_sorted['T'].values
```

```
In [44]: import mevpy as mev # only works when this "Mevpy" folder is in the folder of this .ipnyb-file (https://github.com/EnricoZorze)
```

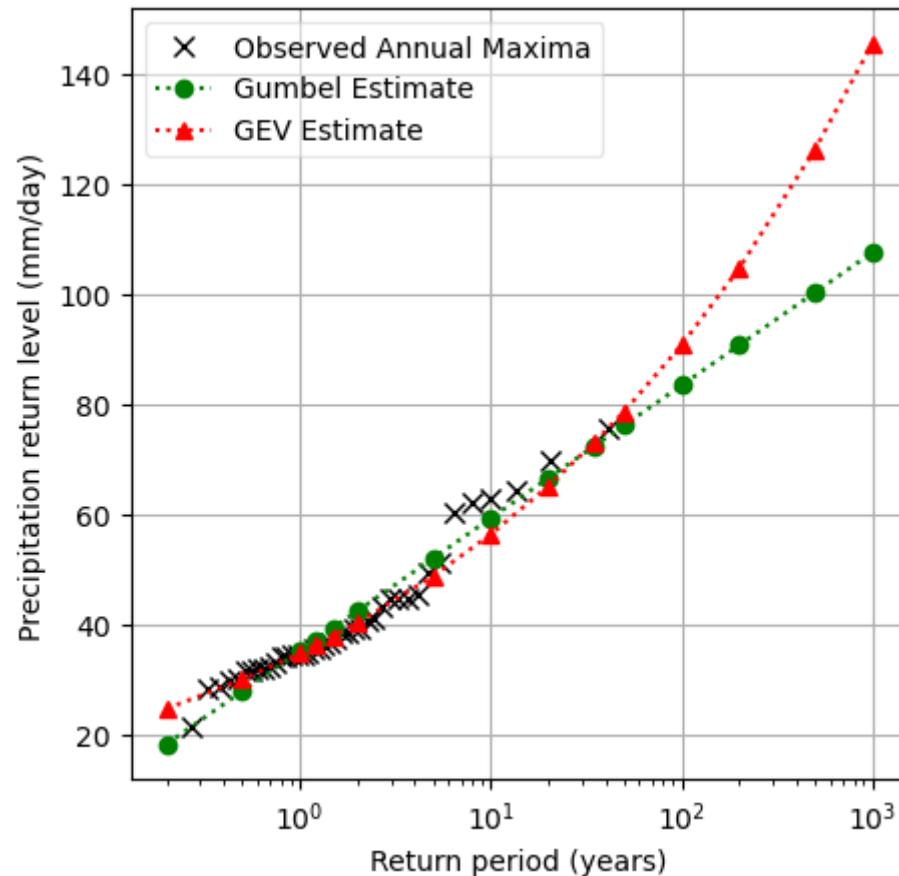
```
In [45]: # fit GEV parameters (without overwriting the sigma and mu from Gumbel)
AMS = annual_maxima_df_sorted['PRCP'].values
xi, sigma_gev, mu_gev = mev.gev_fit(AMS)

F_interest = np.exp(-(1/T_interest))*(1/T_interest)**0

# calculate the GEV estimate for our return periods of interest
gev_estimate = mev.gev_quant(F_interest, xi, sigma_gev, mu_gev)

# convert to dataframe and make a nice table
df_gev_estimate = pd.DataFrame(gev_estimate, columns=['GEV estimate (mm/day)'])
df_gev_estimate.index = T_interest # Return Period
```

```
In [46]: # create the figure
fig, ax = plt.subplots(figsize=(5,5))
ax.plot(T, annual_maxima_df_sorted['PRCP'].values, \
        'xk', markersize=7, label='Observed Annual Maxima')
# ax.plot(T_interest[:-4], full_series, ':Pb', markersize=7, label = 'Full series')
ax.plot(T_interest, gumbel_estimate, ':og', label = 'Gumbel Estimate')
ax.plot(T_interest, gev_estimate, ':^r', label='GEV Estimate')
ax.set_xlabel('Return period (years)')
ax.set_ylabel('Precipitation return level (mm/day)')
ax.set_xscale('log')
ax.legend(loc='best', framealpha=0.5)
ax.grid(True)
```



Looks similar to the gumbel but fits the data less and instead takes its own route

```
In [47]: prcp_df["YEAR"] = prcp_df.index.year
```

```
In [48]: # fit mev parameters for each year
N, C, W = mev.mev_fit(prcp_df, threshold=1)

# put this into a nice dataframe
df_params_mev = pd.DataFrame([N,C,W]).transpose()
df_params_mev.columns = ['N', 'C', 'W']

# plotting the CDF curves
```

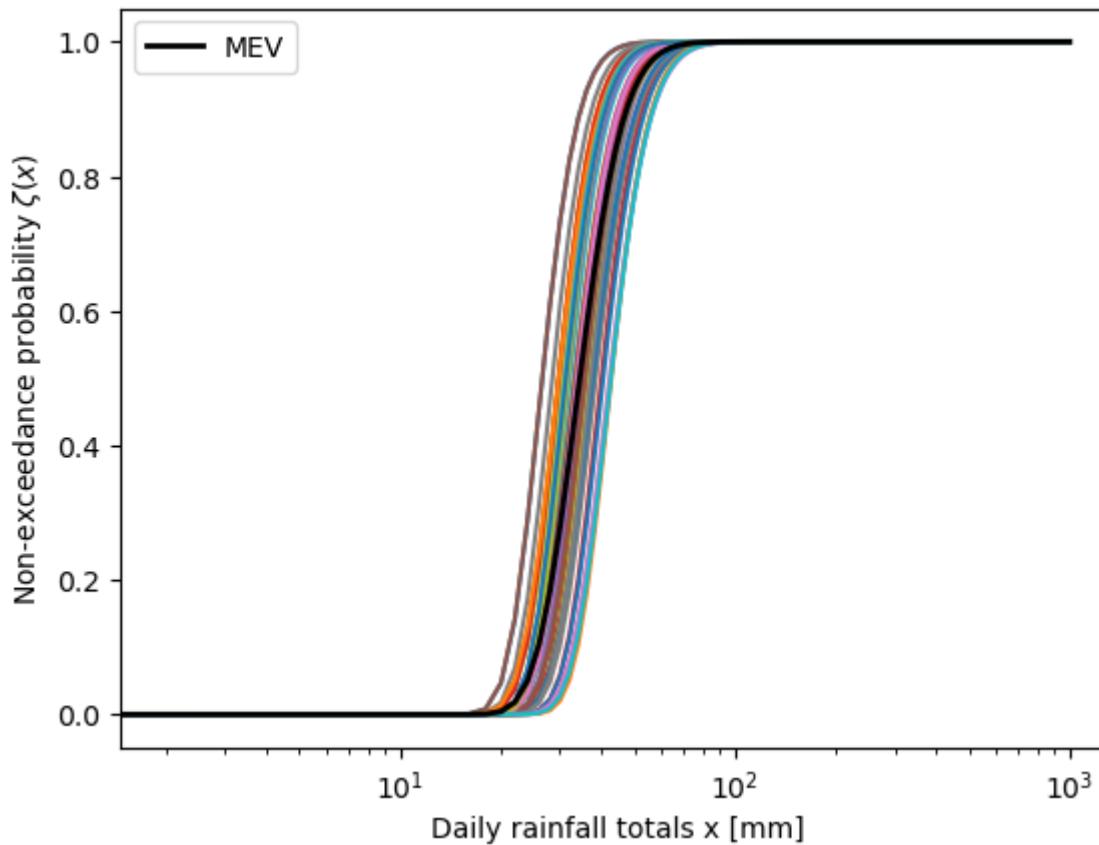
```
dummy_X = np.arange(0,1000,2)

# non-exceedance probability for individual years (here defined as H)
H = np.zeros((len(dummy_X),M))
zeta = np.zeros((len(dummy_X)))

# continue with your own code here:
for i in range(len(zeta)):
    x = dummy_X[i]
    lst = []
    for j in range(len(W)):
        lst.append((1 - np.exp(-(x/C[j])**W[j]))**N[j])
    zeta[i] = 1 / M * np.sum(lst)

# x = dummy_X[0]
for j in range(M):
    for i in range(len(H)):
        x = dummy_X[i]
        H[i,j] = (1 - np.exp(-(x/C[j])**W[j]))**N[j]

# plot figure like in Enrico's paper
fig, ax = plt.subplots()
ax.plot(dummy_X, H)
ax.plot(dummy_X, zeta, 'k', linewidth=2, label='MEV')
ax.set_xlabel('Daily rainfall totals x [mm]')
ax.set_ylabel('Non-exceedance probability $\zeta(x)$')
ax.set_xscale('log')
ax.legend();
```



```
In [49]: # obtain the MEV solution
x0 = np.mean(AMS)
mev_estimate, flags = mev.mev_quant(F_interest, x0, N, C, W)

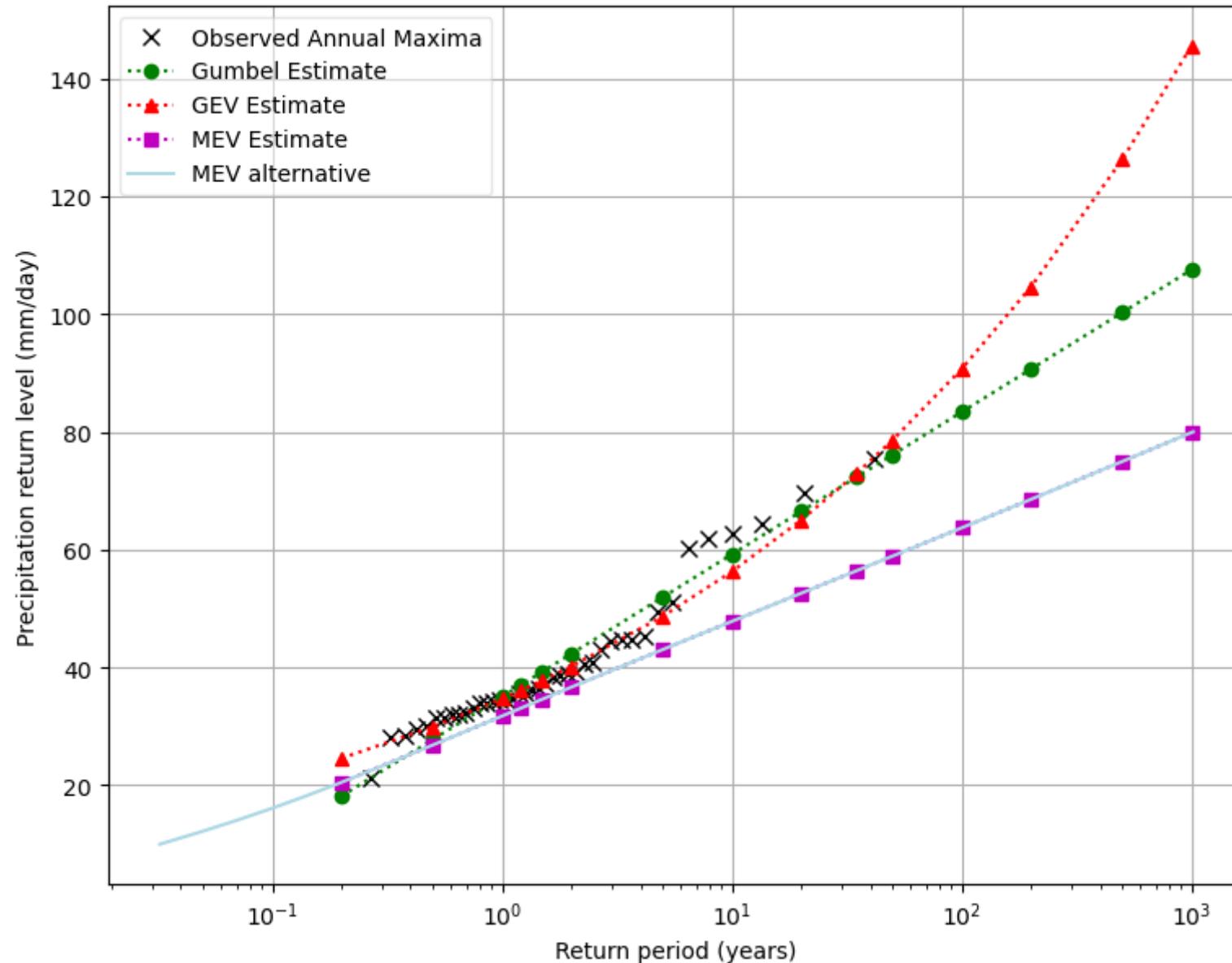
if any(flags) == True:
    print('Change starting guess for the numerical solution x0')
elif any(flags) == False:
    print('No errors have been raised, continue the exercise')
```

No errors have been raised, continue the exercise

```
In [50]: warnings.filterwarnings("ignore", category=RuntimeWarning)
# & including the MEV alternative:
# return periods for the CDF curves
```

```
Ta_c = 1/(1-zeta)
T_c = -1/(np.log(1-(1/Ta_c)))

fig, ax = plt.subplots(figsize=(9,7))
ax.plot(T, annual_maxima_df_sorted['PRCP'].values, \
         'xk', markersize=7, label='Observed Annual Maxima')
ax.plot(T_interest, gumbel_estimate, ':og', label = 'Gumbel Estimate')
ax.plot(T_interest, gev_estimate, ':^r', label='GEV Estimate')
ax.plot(T_interest, mev_estimate, ':sm', label='MEV Estimate')
mask = (T_c<1100) & (T_c > 0)
ax.plot(T_c[mask], dummy_X[mask], 'lightblue', label='MEV alternative')
ax.set_xlabel('Return period (years)')
ax.set_ylabel('Precipitation return level (mm/day)')
ax.set_xscale('log')
ax.legend(loc='best',framealpha=0.5)
ax.grid(True);
```



1.3 - Vegetation

```
In [51]: def water_balance(P, EP, Si_max):
```

```
    Si = np.zeros(len(P))
    Pe = np.zeros(len(P))
    for i in range(1, len(P)):
        Si[i] = Si[i-1] + P[i]
```

```
        if Si[i] > Si_max:
            Pe[i] = Si[i] - Si_max
            Si[i] = Si[i] - Pe[i]
```

```
        Si[i] = Si[i] - EP[i]
        if Si[i] < 0:
            Si[i] = 0
```

```
    df = pd.DataFrame()
    df['P'] = P
    df['EP'] = EP
    df['Si'] = Si
    df['Pe'] = Pe
    return df
```

```
def vegetation(df_in, show=True):
```

```
    df = df_in.copy()
    df.dropna(inplace=True)
```

```
    Si_max = 2.5 # mm
```

```
    df_wb = water_balance(df.P, df.Pev, Si_max)
```

```
    mean_P = df_wb['P'].mean()
    mean_Pe = df_wb['Pe'].mean()
    ratio = mean_Pe / mean_P
```

```
#Plot results
```

```
fig, ax = plt.subplots(2, figsize=(10,6))
df_wb['P'].plot(ax=ax[1])
df_wb['Pe'].plot(ax=ax[1], ylabel='[mm/d]')
```

```
df['P'].plot(ax=ax[0], xlabel='Date', ylabel='[mm/d]')
df['Pev'].plot(ax=ax[0], xlabel='Date', ylabel='[mm/d]')
df['Q'].plot(ax=ax[0], xlabel='Date', ylabel='[mm/d]')

ax[0].legend()
ax[0].set_title(f'Precipitation, Potential Evaporation and Discharge Hudson Basin')

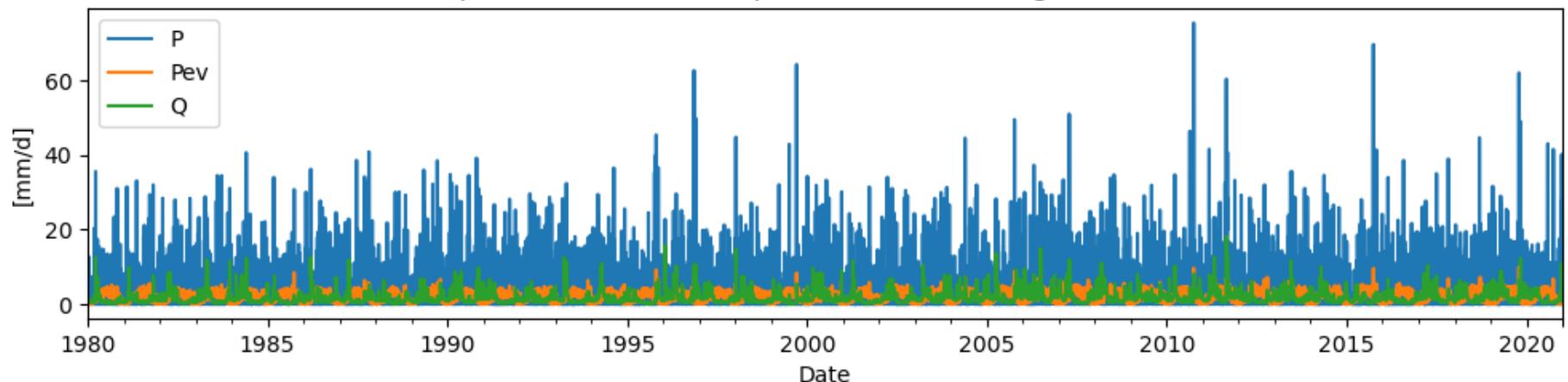
ax[1].set_xlabel('Date')
ax[1].set_title(f'Interception, with a throughfall ratio of {ratio:.2f}')
ax[1].legend()
fig.tight_layout(h_pad=4)

if show != True:
    plt.close()

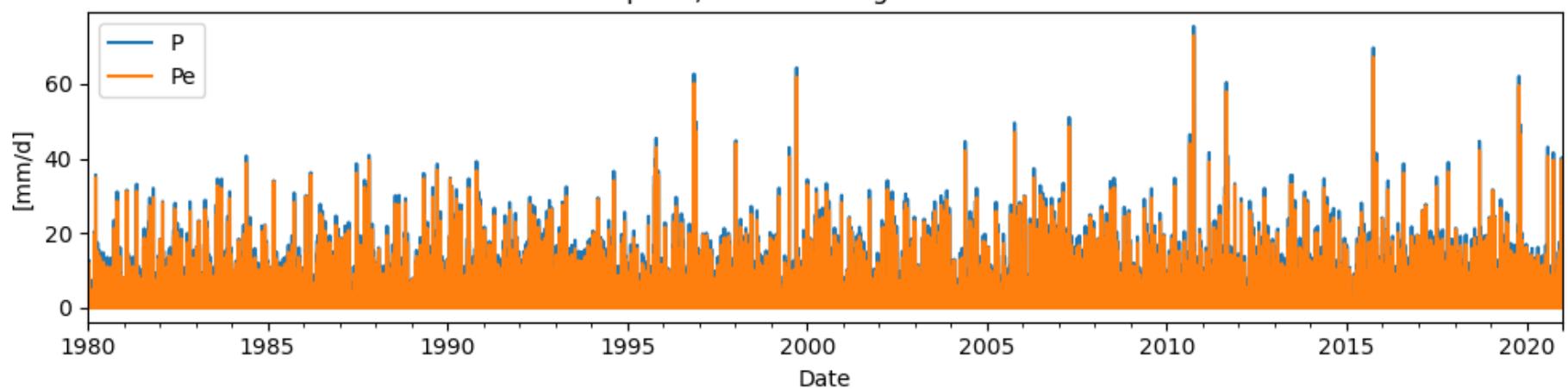
return ratio, df_wb
```

```
In [52]: ratio, df = vegetation(combined_forcing)
```

Precipitation, Potential Evaporation and Discharge Hudson Basin



Interception, with a throughfall ratio of 0.71



```
In [53]: def plant_transpiration(df_in, show=True):
    df = df_in.copy()
    df.dropna(inplace=True)

    P_mean = df['P'].mean()
    Q_mean = df['Q'].mean()
    Et_dash = P_mean - Q_mean
```

```
EP_mean = df['Pev'].mean()

df['Et'] = df['Pev'] / EP_mean * Et_dash
df['Sd'] = np.zeros(len(df['P']))

cumsum = 0

for i in df['Et'].index:
    cumsum += (df.loc[i,"P"] - df.loc[i,'Et'])
    if cumsum > 0:
        cumsum = 0
    df.loc[i,"Sd"] = np.minimum(0, cumsum)

unique_years = len(df.index.year.unique())

Sr = min(df['Sd'])
Sr_index = df['Sd'].idxmin()

EP_P = EP_mean / P_mean
Et_P = df['Et'].mean() / P_mean

fig, ax = plt.subplots(2,figsize=(8,8))
fig.tight_layout(h_pad=4)
#ax2 = ax[0].twinx()
df['P'].plot(ax=ax[0], label='Precipitation')
df['Pev'].plot(ax=ax[0], color='C1', label='Evaporation')

ax[0].legend()
#ax2.legend()
ax[0].set_xlabel('Time')
ax[0].set_ylabel('[mm/d]');

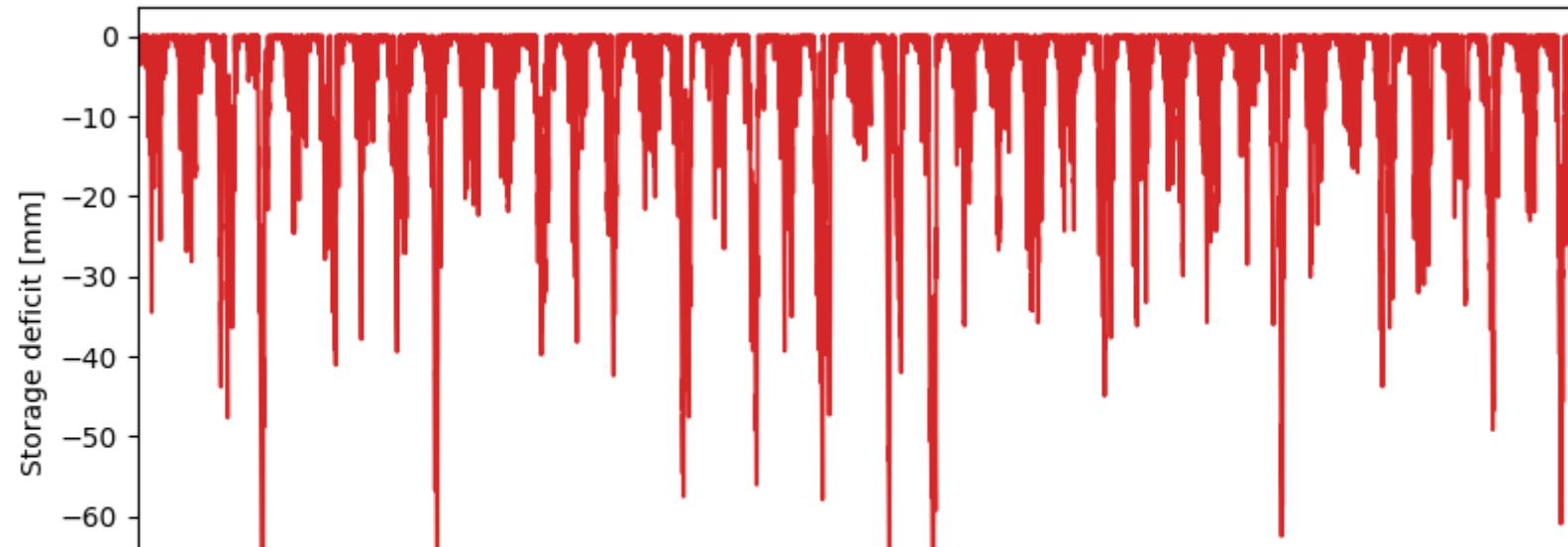
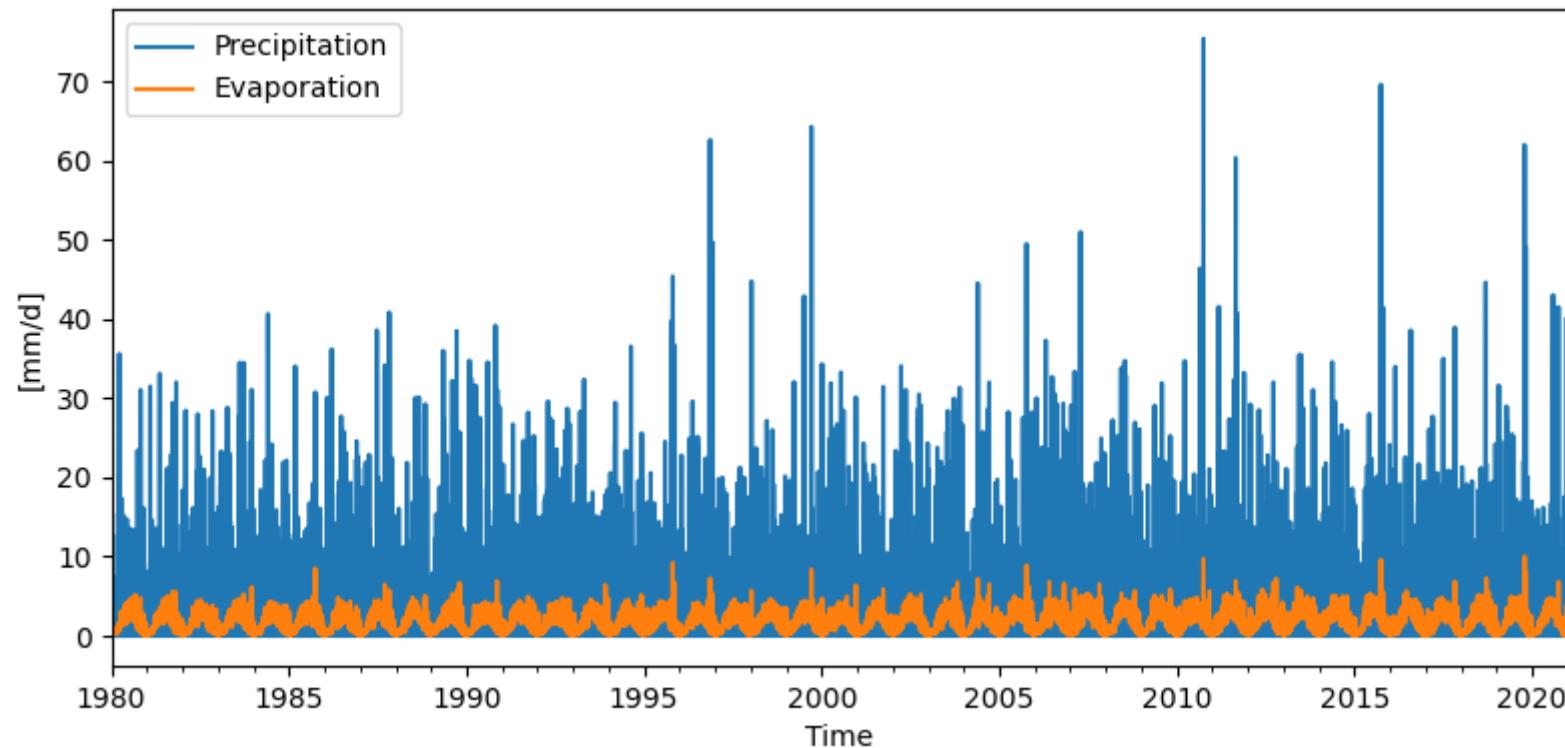
df['Sd'].plot(ax=ax[1], color='C3')
ax[1].plot(Sr_index, Sr, 'ro')
ax[1].text(Sr_index+datetime.timedelta(100), Sr, f'SR,{unique_years}y', fontsize=9)
ax[1].legend()
ax[1].set_xlabel('Time')
ax[1].set_ylabel('Storage deficit [mm]');

if show == True:
```

```
        print(f'The vegetation-accessible water storage volume (or root-zone storage capacity) SR,y is {-Sr:.2f} [mm] over the  
else:  
    plt.close()  
  
return df, Sr, Et_P, EP_P
```

In [54]: `df, Sr, Et_P, EP_P = plant_transpiration(combined_forcing)`

The vegetation-accessible water storage volume (or root-zone storage capacity) SR,y is 73.86 [mm] over the preceding 41 years



1.4

This only take from 1894, due to missing days and to remove the remove gap between 1988 and 1892

```
In [55]: def align_zeros(axes):
    ylims_current = {} # Current ylims
    ylims_mod = {} # Modified ylims
    deltas = {} # ymax - ymin for ylims_current
    ratios = {} # ratio of the zero point within deltas
    for ax in axes:
        ylims_current[ax] = list(ax.get_ylimits())
            # Need to convert a tuple to a list to manipulate elements.
        deltas[ax] = ylims_current[ax][1] - ylims_current[ax][0]
        ratios[ax] = -ylims_current[ax][0]/deltas[ax]

    for ax in axes: # Loop through all axes to ensure each ax fits in others.
        ylims_mod[ax] = [np.nan,np.nan] # Construct a blank list
        ylims_mod[ax][1] = max(deltas[ax] * (1-np.array(list(ratios.values()))))
            # Choose the max value among (delta for ax)*(1-ratios),
            # and apply it to ymax for ax
        ylims_mod[ax][0] = min(-deltas[ax] * np.array(list(ratios.values())))
            # Do the same for ymin
        ax.set_ylimits(tuple(ylims_mod[ax]))
```

```
In [56]: df_all_data_snow_model = combined_forcing.loc[pd.Timestamp("1894-01-01"):]
```

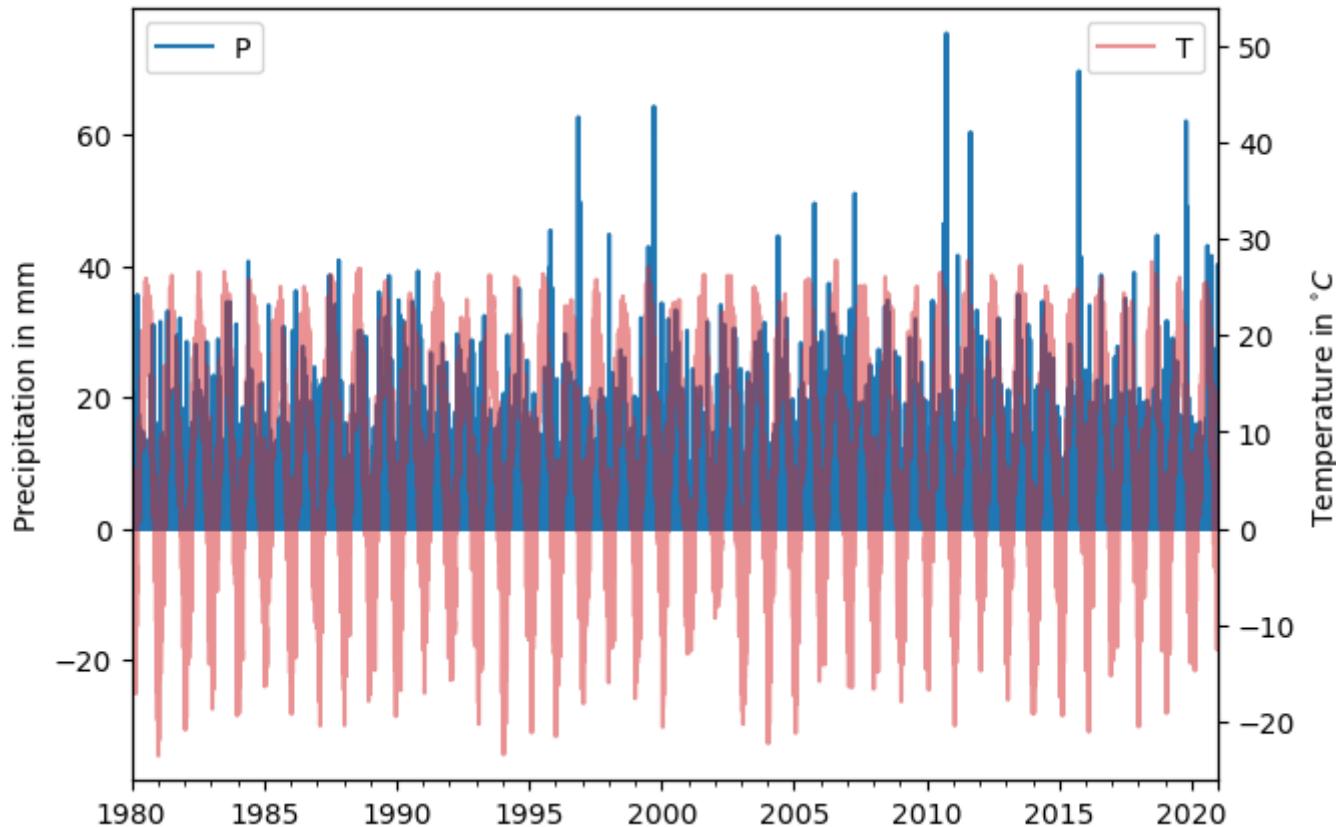
```
In [57]: df_T_P = df_all_data_snow_model[["T", "P"]].dropna(axis=0)

fig, ax = plt.subplots(1,1, figsize=(7,5), sharex=True)
df_T_P[['P']].plot(ax=ax, alpha=1)
```

```
ax.set_ylabel("Precipitation in mm")
ax.legend(loc="upper left")

ax2 = ax.twinx()
df_T_P[["T"]].plot(ax=ax2,color="C3",alpha=0.5,zorder=-10)
ax2.legend(loc="upper right")
ax2.set_ylabel("Temperature in  $^{\circ}\text{C}$ ")

align_zeros([ax,ax2]);
```

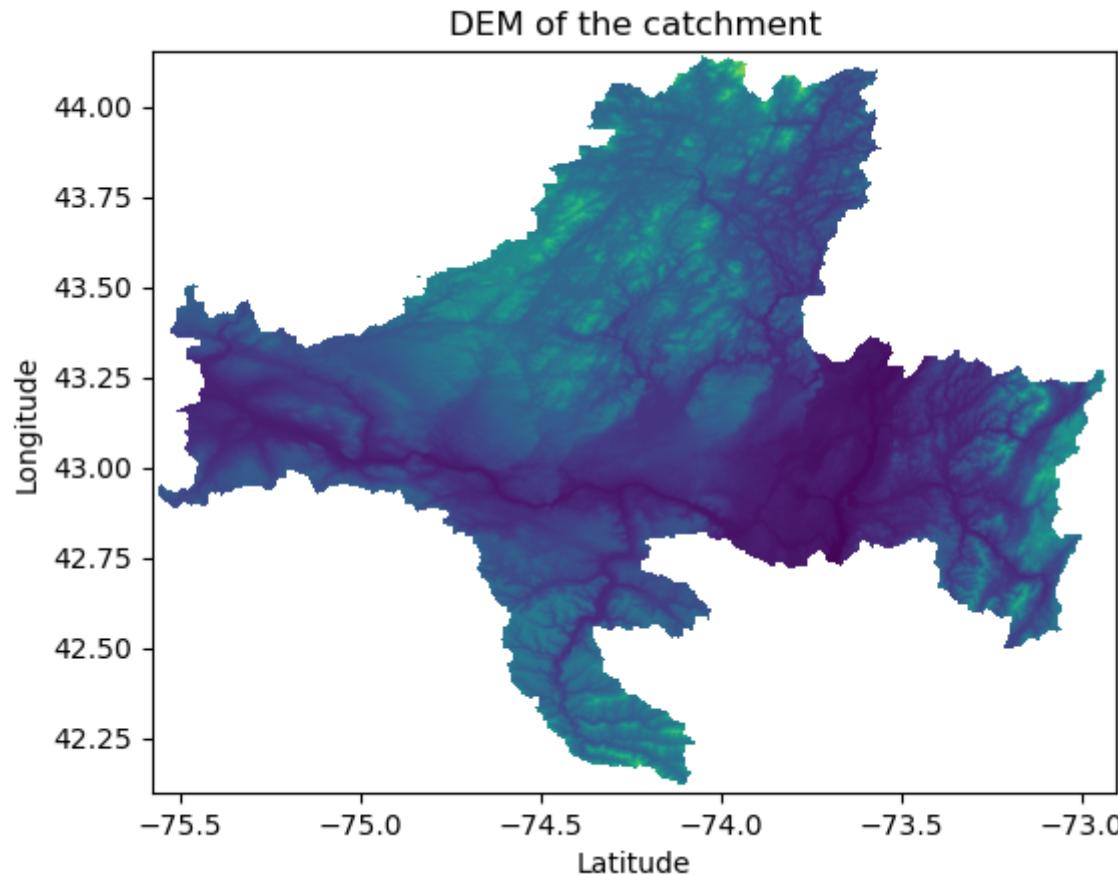


Consider elevation data as this correlates with snow

In [58]:

```
fig, ax = plt.subplots(1)
path = f'{gis_folder}\\basin_dem_SRTM.tif'
```

```
new_path = reproject_raster(path, "EPSG:4326")
with rasterio.open(new_path, driver='GTiff') as r:
    rioshow(r, ax=ax)
ax.set_title("DEM of the catchment")
ax.set_xlabel("Latitude")
ax.set_ylabel("Longitude");
```



In [59]:

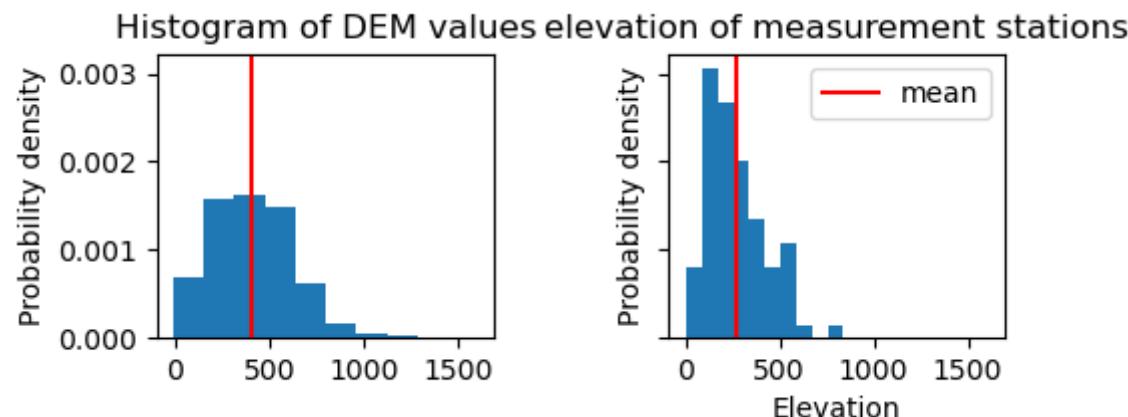
```
with rasterio.open(
    new_path,
    driver='GTiff',
    count=1,
    crs='EPSG:4326'
```

```
) as r:  
dem_data = r.read(1)
```

From the station data where the temperature is measured

```
In [60]: load_lst_elevation = np.loadtxt(f'{data_folder}\\T\\elevation_stations.txt', delimiter=";", dtype=str)  
lst_elevation = load_lst_elevation[:,1].astype(np.float64)
```

```
In [61]: fig, [ax,ax2] = plt.subplots(1,2,sharex=True,sharey=True,figsize=(5,2))  
fig.tight_layout(w_pad=4)  
  
dem_data_in_basin = dem_data[dem_data>-999]  
_, __, ___ = ax.hist(np.sort(dem_data_in_basin),density=True);  
ax.axvline(np.mean(dem_data_in_basin),color="r")  
ax.set_title("Histogram of DEM values")  
ax.set_ylabel("Probability density")  
  
_, __, ___ = ax2.hist(lst_elevation,density=True)  
ax2.axvline(np.mean(lst_elevation),color="r",label="mean")  
ax2.legend()  
ax2.set_title("elevation of measurement stations");  
ax2.set_ylabel("Probability density")  
ax2.set_xlabel("Elevation");
```



The two histograms above show the distribution of the different elevations. In red the mean is shown. The dem and station measurements are fairly similar, though the stations measure a bit lower

Start by taking the mean heights and the mean temperature as one flat plane

```
In [62]: def prev_date(date, days=1):
    subtracted_date = pd.to_datetime(date) - datetime.timedelta(days=days)
    subtracted_date = subtracted_date.strftime("%Y-%m-%d")
    return subtracted_date
```

```
In [63]: df = df_T_P.copy()

Er = lst_elevation.mean() #m
Tt = -0.5 # degc
FM = 3 # mm/deg/d
S_0 = 0 # mm - no snow at start

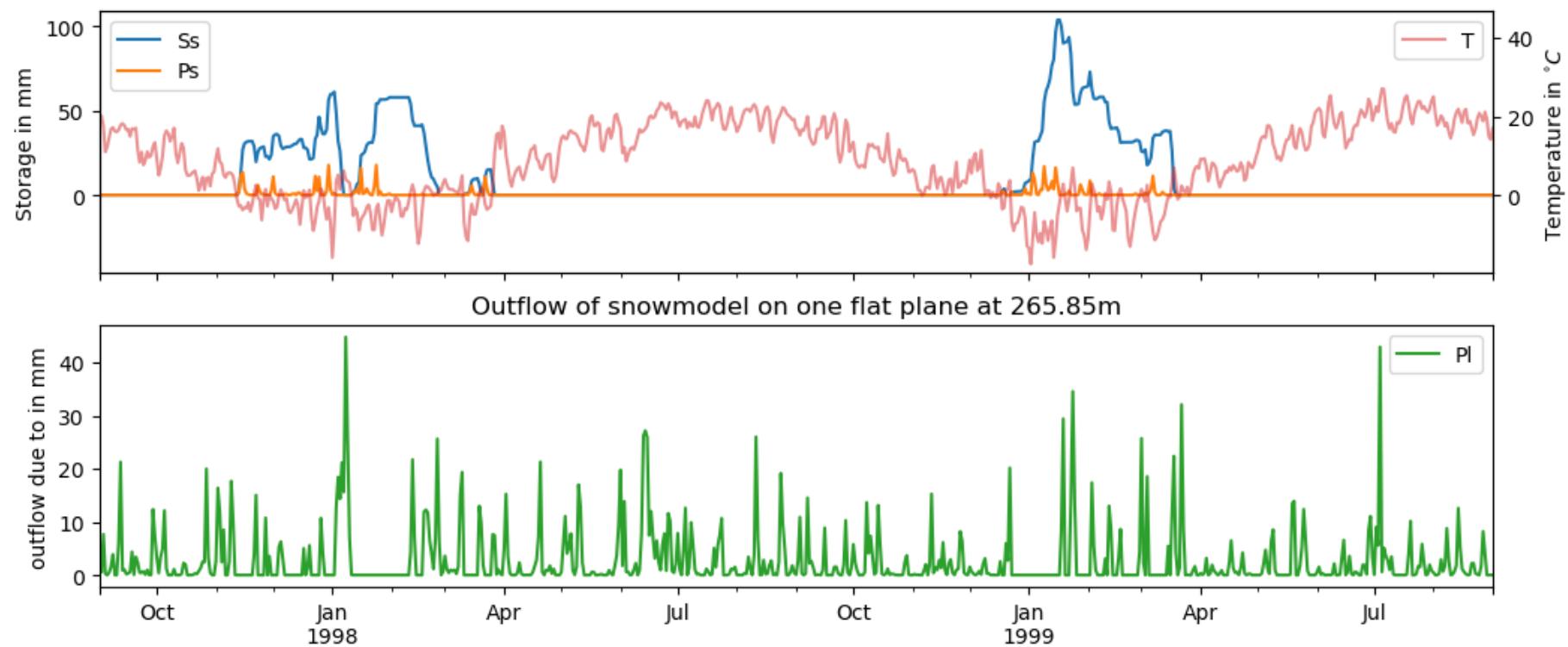
# for every day:
dt = 1
for i, date in enumerate(df.index):
    P = df.loc[date,"P"]
    TR = df.loc[date,"T"]
    if i == 0:
        df.loc[prev_date(date),"Ss"] = S_0 # initial amount snow (0) for non existing day

    # if below threshold temperature, assume not first day for similiicity
    if TR < Tt and i != 0:
        df.loc[date,"Pr"] = 0 # no rainfall
        df.loc[date,"Ps"] = P # precipitation is snow
        df.loc[date,"M"] = 0 # Too cold for melt
        df.loc[date,"Ss"] = df.loc[prev_date(date),"Ss"] + df.loc[date,"Ps"] * dt # add snow to the prev day
        df.loc[date,"Pl"] = 0 # no outflow as too cold
    # then must be above
    else:
        df.loc[date,"Pr"] = P # all precip is rainfall
        df.loc[date,"Ps"] = 0 # no snow
        df.loc[date,"M"] = min(df.loc[prev_date(date),"Ss"]/dt, FM * (TR - Tt)) # calculate melt
        df.loc[date,"Ss"] = df.loc[prev_date(date),"Ss"] - df.loc[date,"M"] * dt # remove melted snow
        df.loc[date,"Pl"] = df.loc[date,"Pr"] + df.loc[date,"M"] # outflow = rain + melt
```

```
if i == 0:  
    df.drop(index=prev_date(date),inplace=True) # remove initial amount snow for non existing day  
  
df_case1 = df.copy()
```

plot for 1997-1999

```
In [64]: fig, [ax,ax3] = plt.subplots(2,1,figsize=(12,5),sharex=True)  
df_plot = df_case1.loc["1997-09-01":"1999-09-01"]  
df_plot[['Ss','Ps']].plot(ax=ax)  
ax.set_ylabel("Storage in mm")  
ax.legend(loc="upper left")  
  
ax2 = ax.twinx()  
df_plot[['T']].plot(ax=ax2,color="C3",alpha=0.5,zorder=-10)  
ax2.legend(loc="upper right")  
ax2.set_ylabel("Temperature in  $^{\circ}\text{C}$ ")  
  
align_zeros([ax,ax2])  
  
df_plot[['Pl']].plot(ax=ax3,color="C2")  
ax3.set_ylabel("outflow due to in mm")  
ax3.set_title(f"Outflow of snowmodel on one flat plane at {E:.2f}m");
```



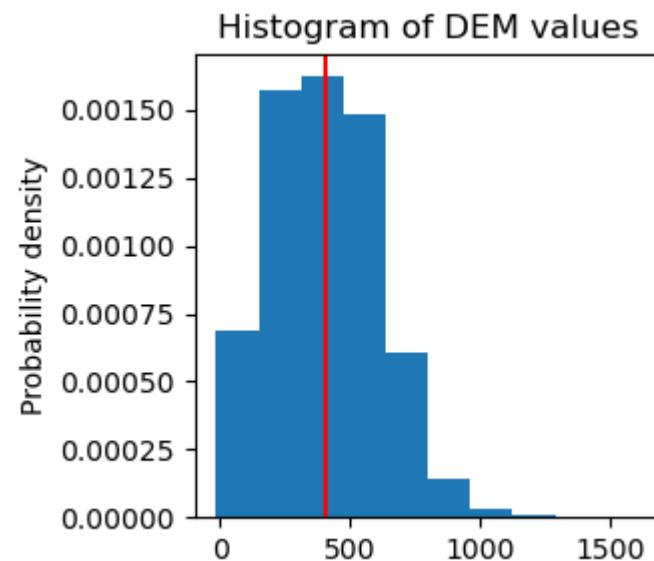
repeat but with different elevation bands As we can see below, there is a spread of elevation from 0 to around 1000. these can be split into 4 bands:

1. `elevation < 250`
2. `250 < elevation < 500`
3. `500 < elevation < 750`
4. `750 < elevation`

```
In [65]: fig, ax = plt.subplots(1,sharex=True,sharey=True,figsize=(3,3))

dem_data_in_basin = dem_data[dem_data>-999]
_, __, ___ = ax.hist(np.sort(dem_data_in_basin),density=True);
ax.axvline(np.mean(dem_data_in_basin),color="r")
ax.set_title("Histogram of DEM values")
```

```
ax.set_ylabel("Probability density")
ax.annotate(f"$\mu$ = {np.mean(dem_data_in_basin):.1f}m", (np.mean(dem_data_in_basin)+12, 0.002), color="red");
```



```
In [66]: A1 = len(dem_data_in_basin[dem_data_in_basin<=250])/ len(dem_data_in_basin)
A2 = len(dem_data_in_basin[(dem_data_in_basin>250) & (dem_data_in_basin <=500)]) / len(dem_data_in_basin)
A3 = len(dem_data_in_basin[(dem_data_in_basin>500) & (dem_data_in_basin <=750)]) / len(dem_data_in_basin)
A4 = len(dem_data_in_basin[(dem_data_in_basin>750)]) / len(dem_data_in_basin)
print(f'A1:\t{A1:.2f}\nA2:\t{A2:.2f}\nA3:\t{A3:.2f}\nA4:\t{A4:.2f}\nΣ:\t{A1 + A2 + A3 + A4:.2f}' )
```

```
A1:    0.26
A2:    0.40
A3:    0.28
A4:    0.05
Σ:    1.00
```

```
In [67]: # for every day:
dt = 1

Er = 331 # m

heights = [125, 375, 625, 875] # m
A_lst = [A1, A2, A3, A4]
A = sum(A_lst)
```

```

lst_df      = []
lst_df_storage = []
for A_index, Ei in enumerate(heights):
    df = df_T_P.copy()
    # compute for each day
    for i, date in enumerate(df.index):
        P = df.loc[date,"P"]
        TR = df.loc[date,"T"]
        Ti = TR - 0.6 * (Ei-Er) / 100

        if i == 0:
            df.loc[prev_date(date),"Ss"] = S_0 # initial amount snow (0) for non existing day

        # if below threshold temperature, assume not first day for similitude
        if Ti < Tt and i != 0:
            df.loc[date,"Pr"] = 0                                # no rainfall
            df.loc[date,"Ps"] = P                               # precipitation is snow
            df.loc[date,"M"] = 0                               # Too cold for melt
            df.loc[date,"Ss"] = df.loc[prev_date(date),"Ss"] + df.loc[date,"Ps"] * dt # add snow to the prev day
            df.loc[date,"Pl"] = 0                               # no outflow as too cold
        # then must be above
        else:
            df.loc[date,"Pr"] = P                                # all precip is rainfall
            df.loc[date,"Ps"] = 0                               # no snow
            df.loc[date,"M"] = min(df.loc[prev_date(date),"Ss"]/dt, FM * (Ti - Tt)) # calculate melt
            df.loc[date,"Ss"] = df.loc[prev_date(date),"Ss"] - df.loc[date,"M"] * dt # remove melted snow
            df.loc[date,"Pl"] = df.loc[date,"Pr"] + df.loc[date,"M"]                # outflow = rain + melt
            if i == 0:
                df.drop(index=prev_date(date),inplace=True) # remove initial amount snow for non existing day
        # for each height aggregate:
        fi = A_lst[A_index]/A
        df["Pl"] = df.apply(lambda x : x.Pl * fi, axis=1)
        df_out = df[["Pl"]].rename(columns={"Pl":f"Pl_{A_index+1}"})
        lst_df.append(df_out)

        df["Ss_scaled"] = df.apply(lambda x : x.Ss * fi, axis=1)
        df_storage_out = df[["Ss","Ss_scaled"]].rename(columns={"Ss":f"Ss_{A_index+1}", "Ss_scaled":f"Ss_scaled_{A_index+1}"})
        lst_df_storage.append(df_storage_out)

```

```
df_case2 = pd.concat(lst_df + lst_df_storage, axis=1)
df_case2["Pl_tot"] = df_case2.apply(lambda x : x.Pl_1 + x.Pl_2 + x.Pl_3 + x.Pl_4, axis=1)
df_case2["Ss_tot"] = df_case2.apply(lambda x : x.Ss_scaled_1 + x.Ss_scaled_2 + x.Ss_scaled_3 + x.Ss_scaled_4, axis=1)
```

```
In [68]: fig, ax = plt.subplots(1,2,sharey=True,figsize=(10,3))
fig.suptitle("Snow melt in four segments",y=1.04)

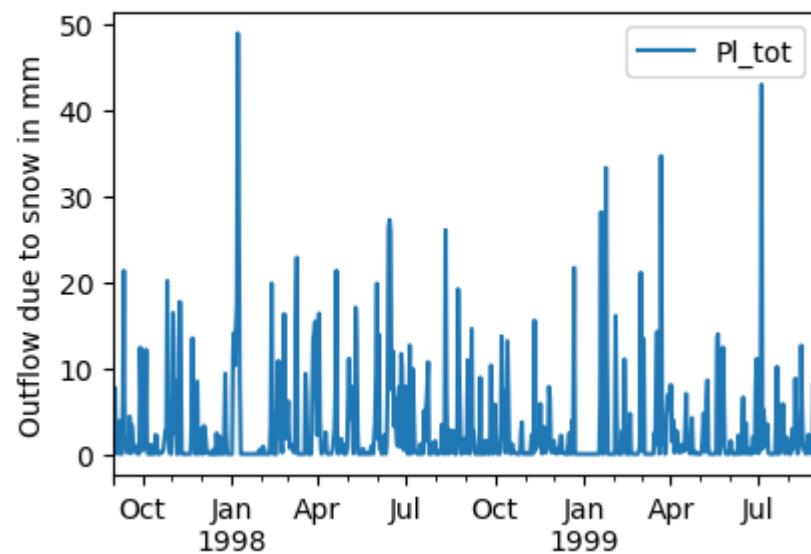
df_plot = df_case2.loc["1997-09-01":"1999-09-01"]
df_plot[['Pl_tot']].plot(ax=ax[0])
ax[0].set_ylabel("Outflow due to snow in mm")
ax[0].set_title("Summed outflow")
df_plot[['Pl_1','Pl_2','Pl_3','Pl_4']].plot(ax=ax[1])
ax[1].legend(heights, bbox_to_anchor=(1,1),title="Contribution \nheight(m)")
ax[1].set_title("individual contributions");

fig, ax = plt.subplots(1,2,sharey=True,figsize=(10,3))
fig.suptitle("Snow storage in four segments",y=1.04)

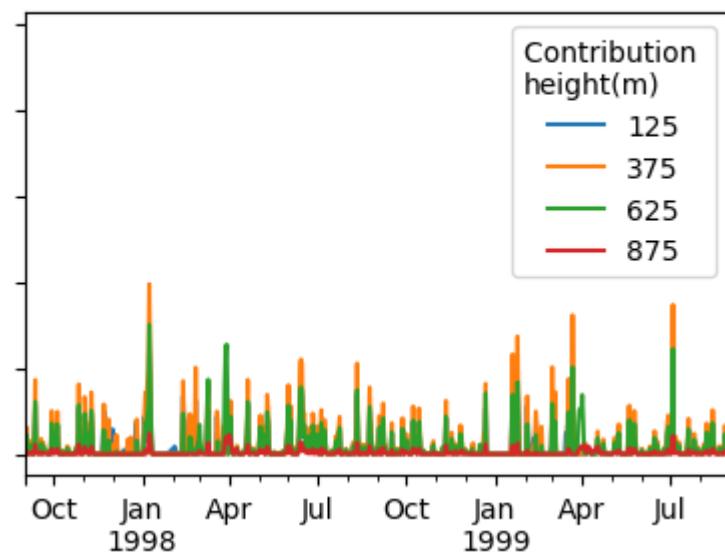
df_plot = df_case2.loc["1997-09-01":"1999-09-01"]
df_plot[['Ss_tot']].plot(ax=ax[0])
ax[0].set_ylabel("Outflow due to snow in mm")
ax[0].set_title("Summed storage")
df_plot[['Ss_scaled_1','Ss_scaled_2','Ss_scaled_3','Ss_scaled_4']].plot(ax=ax[1])
ax[1].legend(heights, bbox_to_anchor=(1,1),title="Contribution \nheight(m)")
ax[1].set_title("scaled individual contributions");
```

Snow melt in four segments

Summed outflow

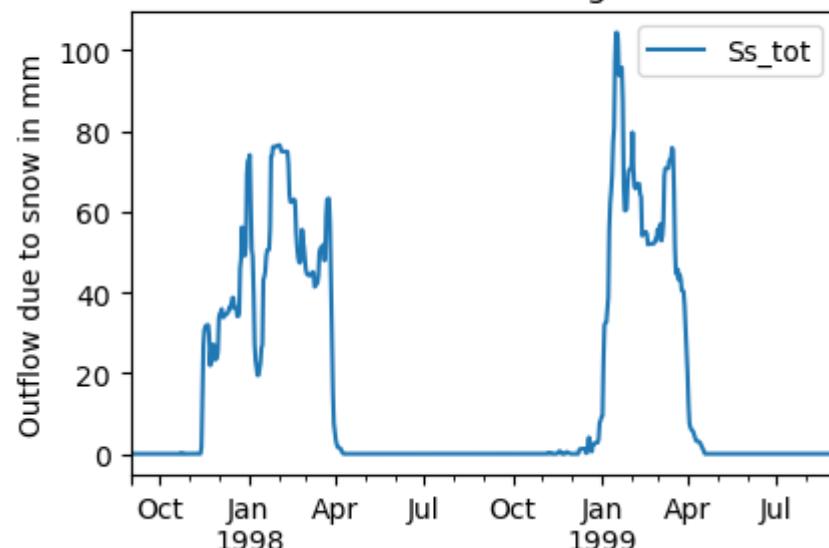


individual contributions

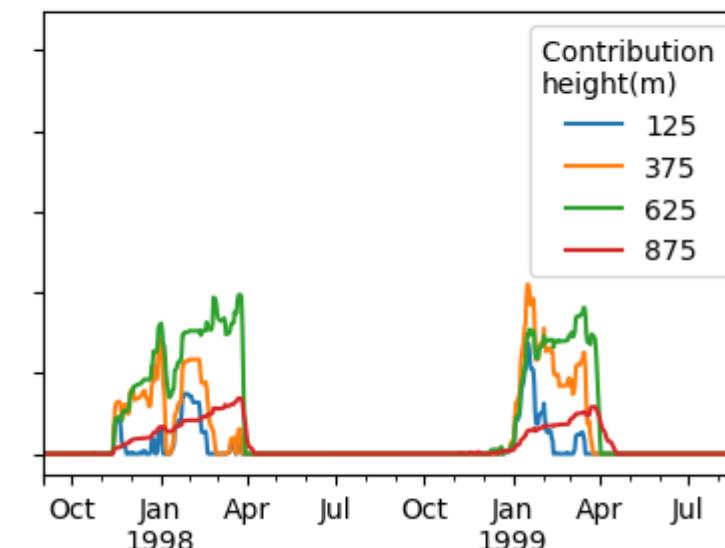


Snow storage in four segments

Summed storage



scaled individual contributions



You nicely see the storages increase and the difference per elevation band can also be seen nicely. The january melt in the 375m band shows up strongly in the the outflow peak.

1.5 - Flood routing

Can be found in notebook [1.5](#) takes long to run due to large data set. An example of the fit is given below:



There is no delay (time lag) in the peaks, and the objective function was not able to get success.

1.6 - Moisture recycling

Can be found in notebook [1.6](#), no large insights, most of the moisture in the eastern united states comes from the ocean, likely also due to the gulfstream which passes by.

2.1 - Surface water classification

Landsat data can be downlaoded from <https://earthexplorer.usgs.gov/>, using landsat 8 level 2 in this case.

This data is unprocessed datset very large and thus is not included, the results will be included.

Analysis is done in QGIS with the [Semi-Automatic Classification Plugin](#)

The data from landsat can be imported, merged into one multiband layer and clipped to the basin area. The bands are remaped as shown in the legend to make water more visible (black). *Note: not all areas area covered, but optted for best fit*

This result is left below:



The result of the plugin classification using 10 examples of water and 10 of not water results in the following image:

```
In [69]: cmap = mpl.colormaps["winter"]
# Loading the data in in 28918 crs
outline      = gpd.read_file(f'{gis_folder}\\hudson_basin_26918.gpkg', driver="SHP", crs="EPSG:26918")
main_rivers   = gpd.read_file(f'{gis_folder}\\main_rivers_hudson_basin.gpkg', driver="GPKG", crs="EPSG:26918")
all_rivers    = gpd.read_file(f'{gis_folder}\\rivers_hudson_basin.gpkg', driver="GPKG", crs="EPSG:26918")
```

```
In [70]: fixed_nans_path = remove_below_0(f'{gis_folder}\\classification_of_waterbodies_26918.tif', ending="tif")
fig, ax = plt.subplots(1)
with rasterio.open(fixed_nans_path, driver='GTiff') as r:
    img = rio.show(r, ax=ax, cmap=cmap, zorder=100, alpha=0.8)
ax.set_title("Classification of surface water in northern part of the catchment")
ax.set_xlabel("Latitude $(epsg:26918, unit m)$")
ax.set_ylabel("Longitude $(epsg:26918)$")

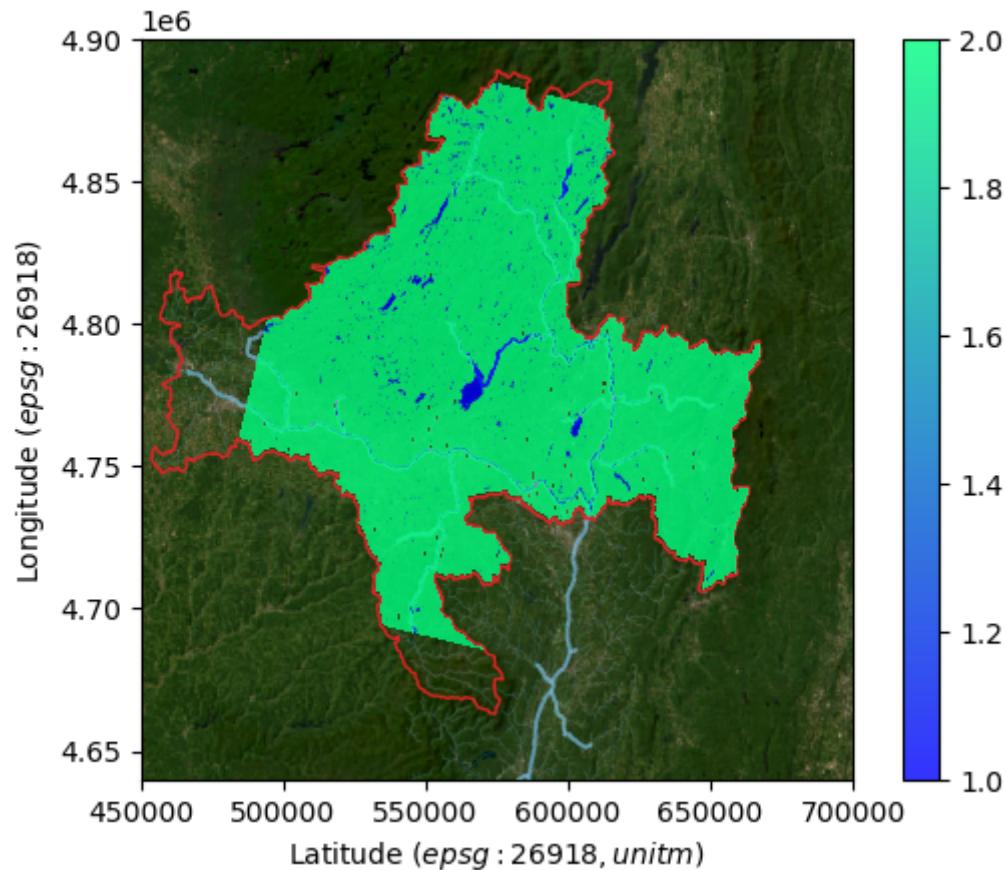
# add other features
outline.plot(ax=ax, edgecolor="C3", facecolor="None")
main_rivers.plot(ax=ax, color="lightskyblue", alpha=0.6, zorder=-1, lw=1.5)
all_rivers.plot(ax=ax, color="lightskyblue", alpha=0.2, zorder=-2, lw=0.4)

# add background
with rasterio.open(background_epsg26918) as r:
    rio.show(r, ax=ax, zorder=-100)

# fix color bar
im = img.get_images()[0]
fig.colorbar(im, ax=ax, cmap=cmap);

ax.set_xlim((4.5e5, 7e5))
ax.set_ylim((4.64e6, 4.9e6));
```

Classification of surface water in northern part of the catchment



as some overlap with rivers and some very small areas so these can be removed by only taking those larger than 10ha, the overlap remaining is merely the reservoirs built on the river rather than the actual course of the river. This can be further filtered to yield:

```
In [71]: df_all_water_more10ha = gpd.read_file(f"{gis_folder}\\\waterbodies_polygon_above10ha_excluding_river.gpkg")
fig, ax = plt.subplots(1)
df_all_water_more10ha.plot(facecolor="C0",ax=ax,edgecolor="w")

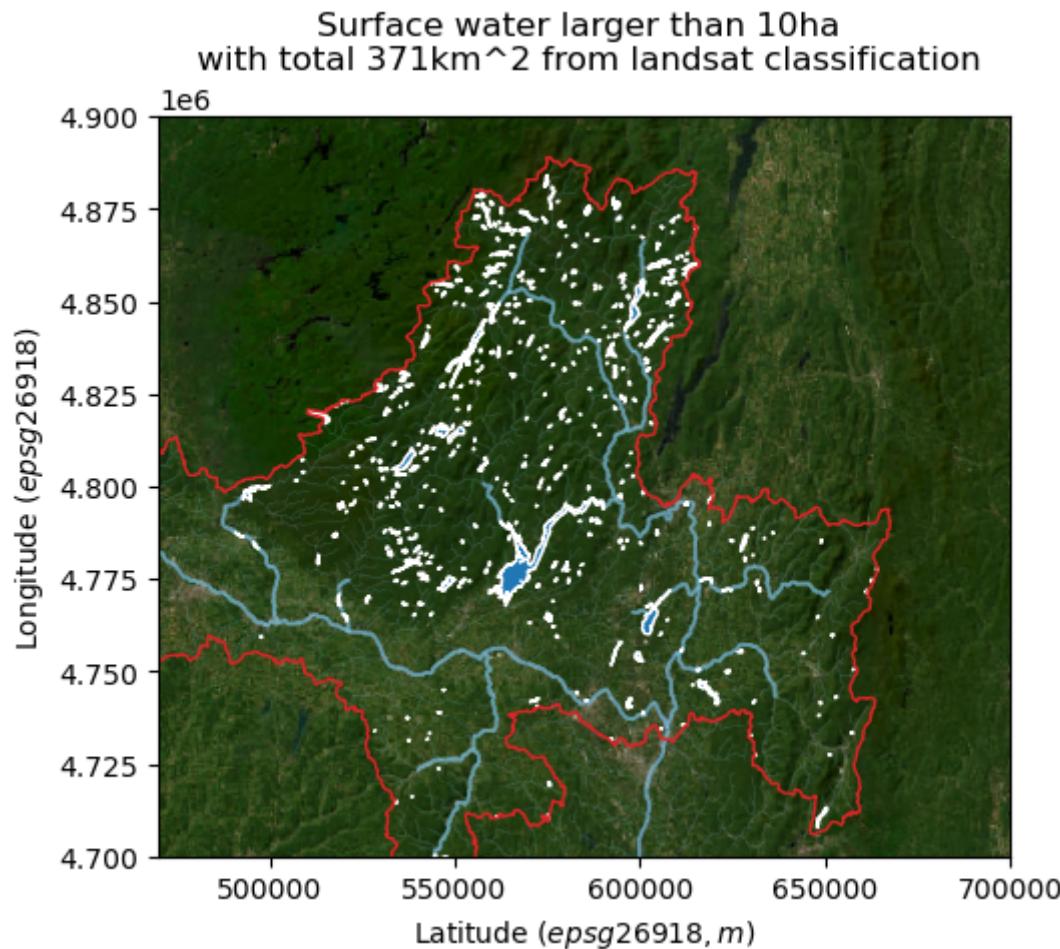
# add other features
outline.plot(ax=ax, edgecolor="C3", facecolor="None")
main_rivers.plot(ax=ax, color="lightskyblue",alpha=0.6,zorder=-1,lw=1.5)
all_rivers.plot(ax=ax, color="lightskyblue",alpha=0.2,zorder=-2,lw=0.4)
```

```
# add background
with rasterio.open(background_epsg26918) as r:
    rioshow(r, ax=ax, zorder=-100)

ax.set_title(f"Surface water larger than 10ha \n with total {df_all_water_more10ha.area.sum()/10**6:.0f}km^2 from landsat clas
ax.set_xlabel("Latitude $(epsg26918, m)$")
ax.set_ylabel("Longitude $(epsg26918)$")

ax.set_xlim((4.7e5,7e5))
ax.set_ylim((4.70e6,4.9e6));

# fig.savefig(r"Figures/surfacewater_image.png")
```



2.2 - Remote Precipitation measurement

Not done due to time constraints, complexity in finding data & plenty of other available precipitation data sources used to fulfill learning goals, see 2.6

2.3 - Soil moisture

In situ

Initial parts for in situ soil measurement, downloaded from <https://ismn.earth/en/data/>, site Lye Brook 2042

```
In [72]: request = OSM()

ismn = ISMN_Interface(soil_moisture_path)
stems = None

depth = (0.05, 2)
def read_ismn(depth):
    min_depth, max_depth = depth

    fig = plt.figure(figsize=(15,4), constrained_layout=True)
    gs = fig.add_gridspec(1, 3)
    map_ax, ts_ax = fig.add_subplot(gs[0, 0], projection=ccrs.PlateCarree()), fig.add_subplot(gs[0, 1:])

    # Plot a small overview map with station locations over Open Street Map
    ismn.plot_station_locations(variable='soil_moisture', min_depth=min_depth, max_depth=max_depth, markersize=5, text_scalefactor=0.5)
    map_ax.set_extent([-77,-70,40,47])
    map_ax.add_image(request, 6)
    outline.plot(ax=map_ax, edgecolor="C3", facecolor="None")
    main_rivers.plot(ax=map_ax, color="lightskyblue", alpha=0.6, zorder=-1, lw=1.5)
    all_rivers.plot(ax=map_ax, color="lightskyblue", alpha=0.2, zorder=-2, lw=0.4)

    # Extract the sensors in the chosen depths at the locations and store their data
    sensors = []
    for network, station, sensor in ismn.collection.iter_sensors(variable='soil_moisture', depth=(min_depth, max_depth)):
        data = sensor.read_data()
        data.loc[data['soil_moisture_flag'] != 'G', 'soil_moisture'] = np.nan
        data = data['soil_moisture']
        if sensor.depth[0] == sensor.depth[1]:
            depth = f"{sensor.depth[0]}"
        else:
```

```

        depth = f"{sensor.depth[0]}-{sensor.depth[1]}"
        data.name = f"{station.name} ({depth} m)"
        sensors.append(data)

    global stems
    stems = pd.concat(sensors, axis=1)

    stems_plot = stems.loc['2017-01-01':,:]

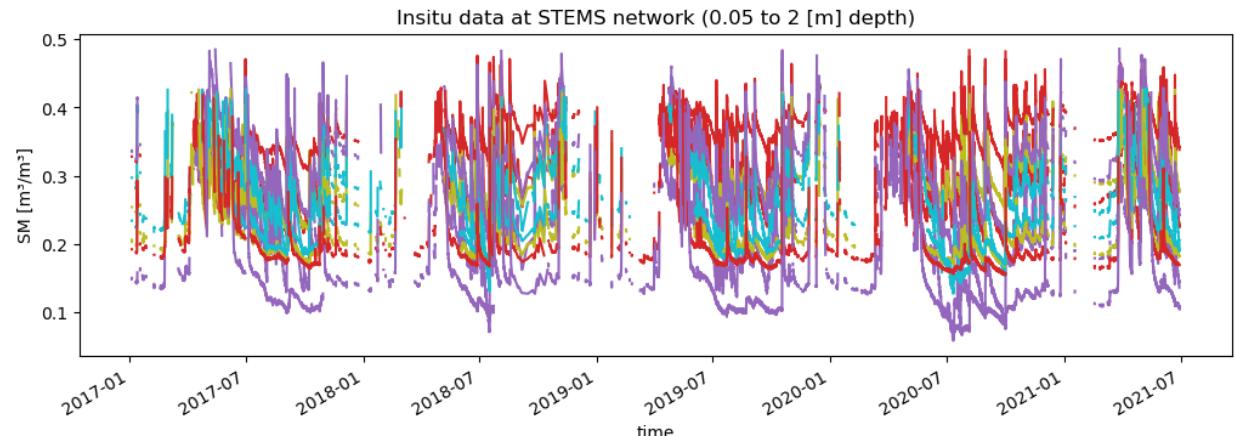
    p = stems_plot.plot(ax=ts_ax, xlabel='time', ylabel='SM [m³/m³]', title=f'Insitu data at STEMS network ({min_depth} to {max_depth} m)', legend().remove()

read_ismn(depth);

```

Found existing ismn metadata in C:\Users\david\Documents\@@ Python\Jaar 5\Q3\ENVM1502\Git\ENVM1502-Catchment-model\Data\Soilmoisture\python_metadata\Soilmoisture.csv.

25 valid sensors in 1 stations in 1 networks (of 1 potential networks)
for variable soil_moisture between 0.05 and 2 m

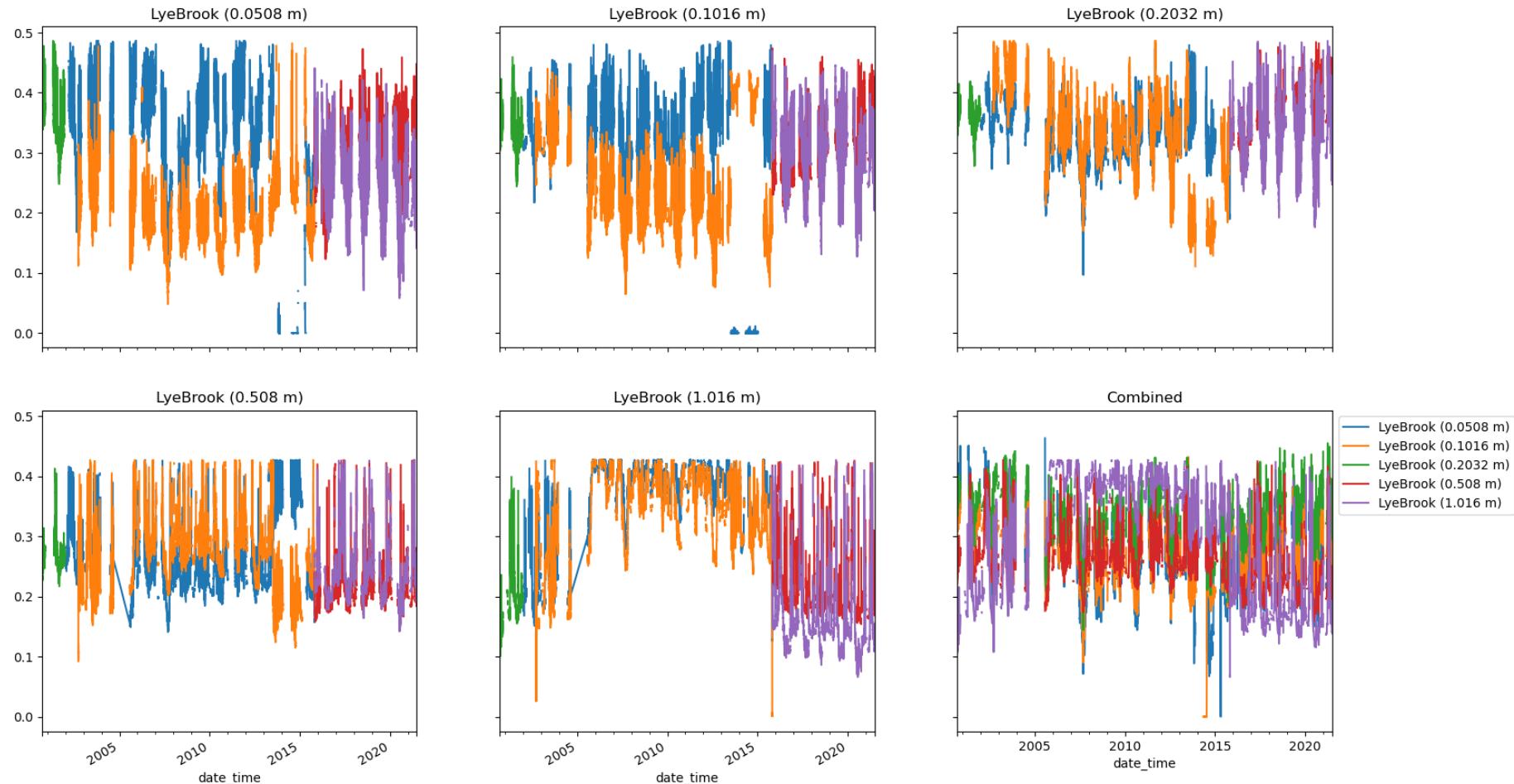


```
In [73]: unique_val_cols = stems.columns.unique()
n = len(unique_val_cols)
fig, ax = plt.subplots(int((n+1)/3),3, figsize=(15,10), sharex=True, sharey=True)
fig.tight_layout(w_pad=5, h_pad=5)
lst_dfs = []
ax = ax.flatten()
for index, col in enumerate(unique_val_cols):
    df_depth = stems[col]
    lst_dfs.append(pd.DataFrame(data=df_depth.mean(axis=1).resample("d").mean(), columns=[col]))
```

```

df_depth.plot(ax=ax[index])
ax[index].legend().remove()
ax[index].set_title(col)
stems_merged = pd.concat(lst_dfs, axis=1)
stems_merged.plot(ax=ax[-1])
ax[-1].legend(bbox_to_anchor=(1,1))
ax[-1].set_title("Combined");

```



The plot above shows the uncertainty in the data as different sensors report differently over time. Daily averages can be obtained by taking the mean of the observations and then resampling on a daily basis.

Microwave remote sensing - Soil Moisture Active Passive Mission (SMAP)

In [74]:

```
year,month,day = 2021, 7, 3
date = f'{year}-{month:02}-{day:02}'

y = 40.48908101650877
x = -74.0305856727883
n_x = 5
n_y = n_x

smap_raw = xr.open_dataset(f'{ENVM1502_data_path}/LTC_DATA/SMAP_raw_202107.nc').sel(lon=slice(x - n_x, x + n_x),
                                lat=slice(y + n_y, y - n_y))
smap_lprm = xr.open_dataset(f'{ENVM1502_data_path}/LTC_DATA/SMAP_LPRM_202107.nc').sel(lon=slice(x - n_x, x + n_x),
                                lat=slice(y - n_y, y + n_y))

def plot_lprm(day):
    """
    Select and visualise SMAP data at a given time
    """
    date = f'2021-07-{day:02}'

    fig, axs = plt.subplots(1, 2, figsize=(15,3), subplot_kw={'projection': ccrs.Robinson()})

    fig.suptitle("SMAP data from passive remote sensing", fontsize=18, y=1.08)
    p1 = smap_raw['tbh'].sel(time=date).plot(transform=ccrs.PlateCarree(), ax=axs[0], cmap=plt.get_cmap('plasma'), vmin=200,
    axs[0].set_title(f"{date} ${T}_{B,H}$")
    p2 = smap_raw['tbv'].sel(time=date).plot(transform=ccrs.PlateCarree(), ax=axs[1], cmap=plt.get_cmap('plasma'), vmin=200,
    axs[1].set_title(f"{date} ${T}_{B,V}$")

    for p in [p1, p2]:
        p.axes.coastlines()

    fig, axs = plt.subplots(1, 3, figsize=(18,3), subplot_kw={'projection': ccrs.Robinson()})

    p3 = smap_lprm['temperature'].sel(time=date).plot(transform=ccrs.PlateCarree(), ax=axs[0], cmap=plt.get_cmap('hot_r'), vmi
    axs[0].set_title(f"{date} Surface Temperature")

    p4 = smap_lprm['vod'].sel(time=date).plot(transform=ccrs.PlateCarree(), ax=axs[1], cmap=plt.get_cmap('Greens'), vmin=0, v
```

```

    axs[1].set_title(f"{date} Vegetation Optical Depth")

    p5 = smap_lprm['soil_moisture'].sel(time=date).plot(transform=ccrs.PlateCarree(), ax=axs[2], cmap=plt.get_cmap('Blues'), v
    axis[2].set_title(f"{date} Soil Moisture")

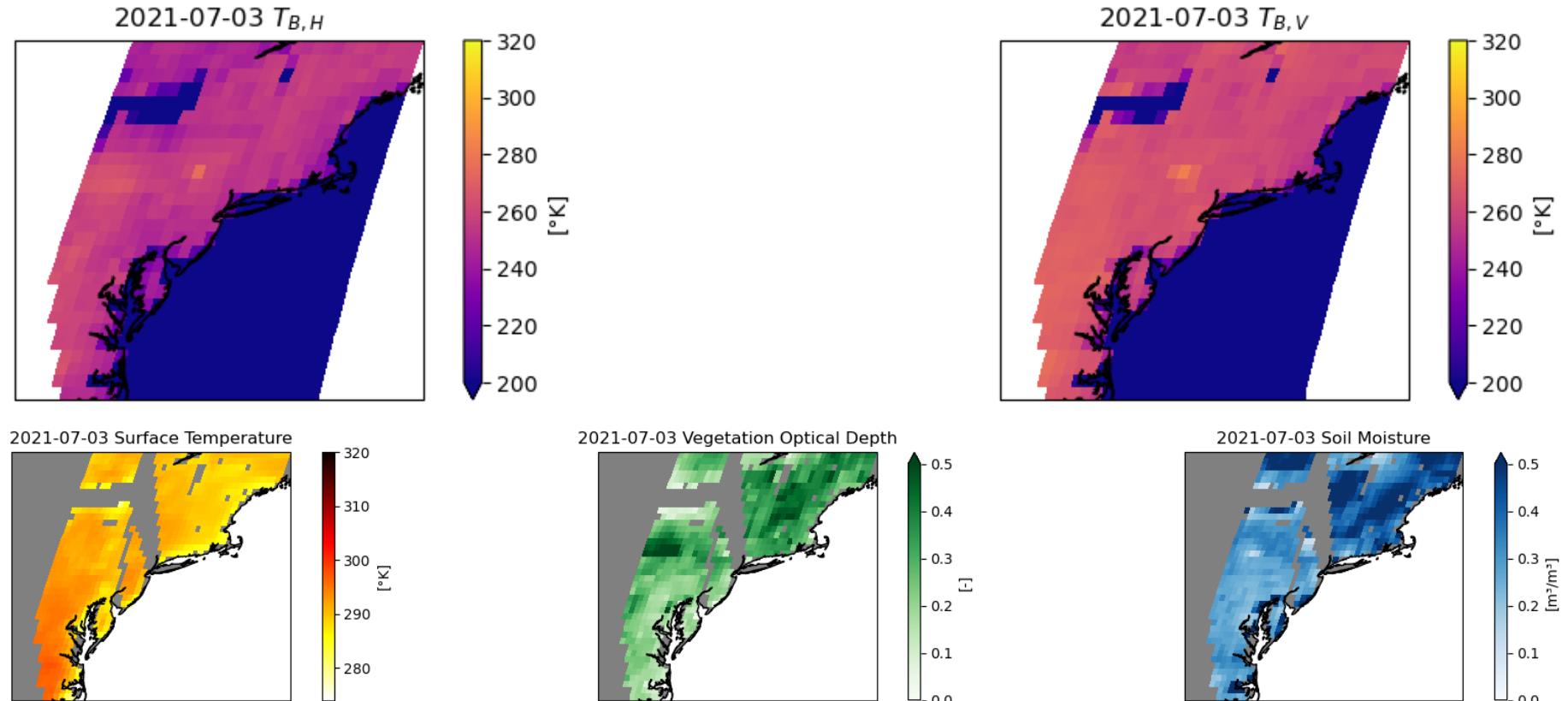
    for p in [p3, p4, p5]:
        p.axes.add_feature(cartopy.feature.LAND, zorder=0, facecolor='gray')
        p.axes.coastlines()

    plt.tight_layout()

plot_lprm(3)

```

SMAP data from passive remote sensing



Combining passive & active -Copernicus Climate Data Service CCDS

Load esa data

This takes quite long

```
In [75]: filelist=glob.glob(f'{ENVM1502_data_path}/CDS_DATA/cds_data_esa/C3S*.nc')

dt=[datetime.datetime.strptime(x.split('/')[-1].split('-')[-3], '%Y%m%d%H%M%S') for x in filelist]
df = pd.DataFrame({'filepath':filelist}, index=dt).sort_index()
stack = xr.open_mfdataset(df.filepath.values, engine='netcdf4', combine='nested', concat_dim='time')
dslon = stack['lon'].compute()
dslat = stack['lat'].compute()
dssm = stack['sm'].compute()
# dssm
```

```
In [76]: year  = 2018
month = 6
day   = 3
date  = f'{year}-{month:02}-{day:02}'

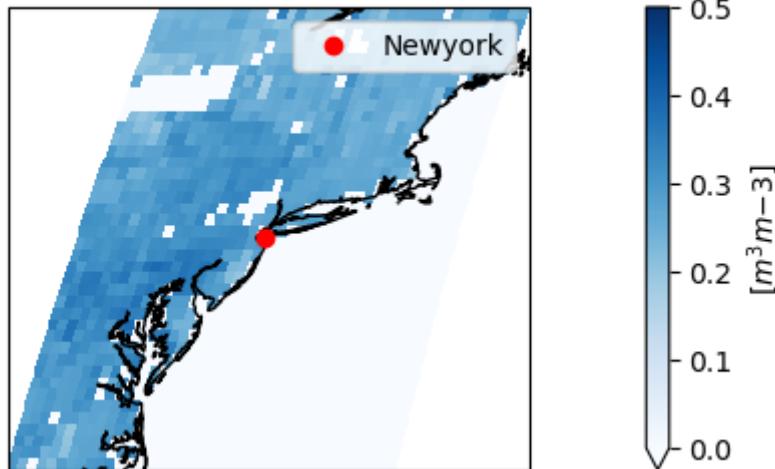
y = 40.48908101650877
x = -74.0305856727883
n_x = 5
n_y = n_x
ny = dssm.sel(lon=slice(x - n_x, x + n_x),
               lat=slice(y + n_y, y - n_y), time=date)

fig, axs = plt.subplots(1, 1, figsize=(15,3), subplot_kw={'projection': ccrs.Robinson()})
ny.plot(transform=ccrs.PlateCarree(), ax=axs, cmap=plt.get_cmap('Blues'), vmin=0, vmax=0.5, cbar_kwargs={'label': '[\$m^{3}] m{-3}'})
axs.plot(x,y,"ro",transform=ccrs.PlateCarree(),label="Newyork")

for p in axs:
    # p.axes.add_feature(cartopy.feature.LAND, zorder=0, facecolor='gray')
    p.axes.coastlines()

axs.legend();
axs.set_title(f"Capurnicus Data from esa for {date}");
```

Capurnicus Data from esa for 2018-06-03



```
In [77]: mask = regionmask.mask_geopandas(outline_buffered,
                                         smap_lprm['soil_moisture'].lon.to_numpy(),
                                         smap_lprm['soil_moisture'].lat.to_numpy(),
                                         lon_name="lon",
                                         lat_name="lat")

cropped_ds_smap = smap_lprm.where(mask==0)
cropped_ds_ccds = dssm.where(mask==0)

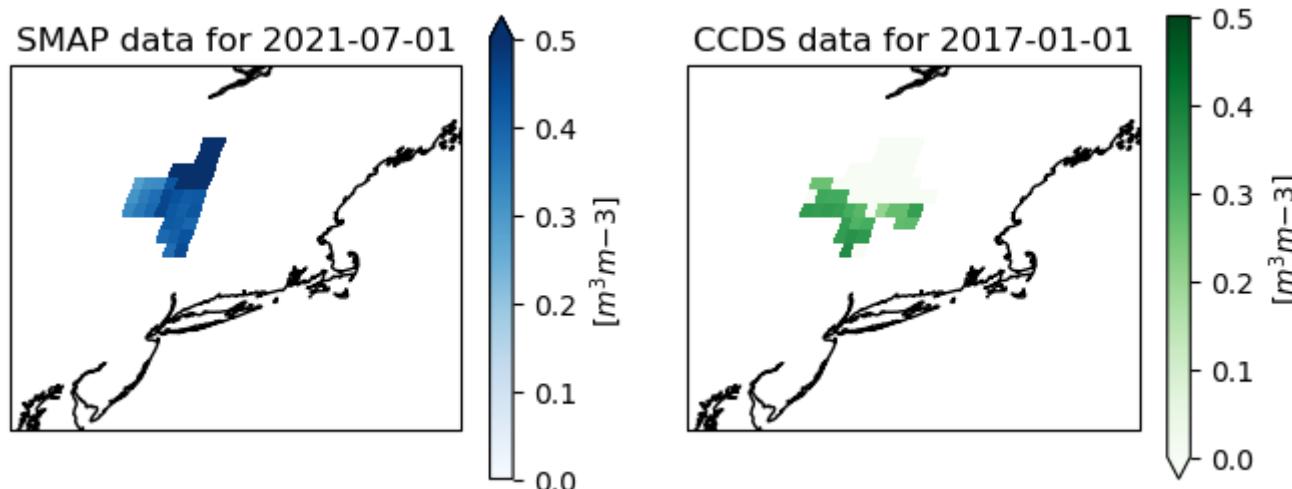
plot_ds_smap = cropped_ds_smap["soil_moisture"].isel(time=0)
plot_ds_ccds = cropped_ds_ccds.isel(time=0)

fig, [axs, axs2] = plt.subplots(1, 2, figsize=(8,3), subplot_kw={'projection': ccrs.Robinson()})
plot_ds_smap.plot(transform=ccrs.PlateCarree(), ax=axs, cmap=plt.get_cmap('Blues'), vmin=0, vmax=0.5, cbar_kwargs={'label': '[%]'})
time = cropped_ds_smap.isel(time=0).time.values
axs.set_title(f"SMAP data for {str(time)[:10]}")

plot_ds_ccds.plot(transform=ccrs.PlateCarree(), ax=axs2, cmap=plt.get_cmap('Greens'), vmin=0, vmax=0.5, cbar_kwargs={'label': '[%]'})
time = cropped_ds_ccds.isel(time=0).time.values
axs2.set_title(f"CCDS data for {str(time)[:10]}")

for p in [axs, axs2]:
    p.axes.coastlines()
```

```
outline.plot(ax=p, edgecolor="C3", facecolor="None", transform=ccrs.PlateCarree())
p.set_xlim((p.get_xlim()[0]+300000,p.get_xlim()[1]))
p.set_ylim((p.get_ylim()[0]+350000,p.get_ylim()[1]+10000));
```

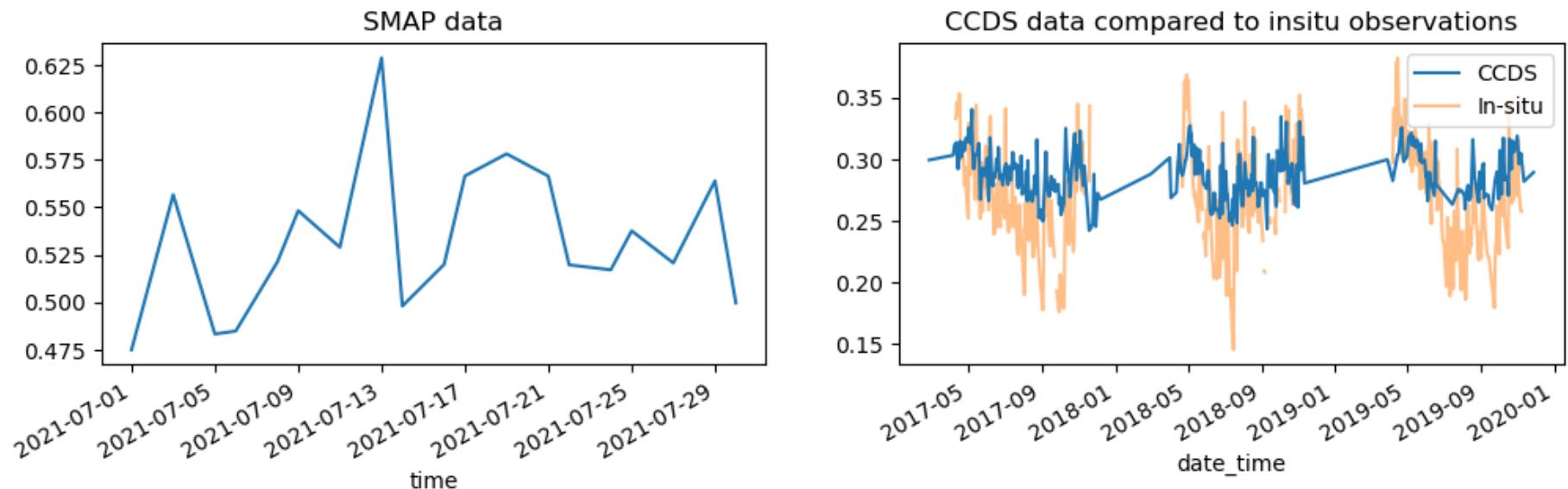


```
In [78]: ds_mean_smap = cropped_ds_smap.mean(dim=["lat","lon"])
series_smap_sm = ds_mean_smap["soil_moisture"].to_pandas()
series_smap_sm_pos = series_smap_sm[series_smap_sm> 0]

ds_mean_ccds = cropped_ds_ccds.mean(dim=["lat","lon"])
series_ccds_sm = ds_mean_ccds.to_pandas()
series_ccds_sm_pos = series_ccds_sm[series_ccds_sm> 0]

fig, [ax, ax2] = plt.subplots(1,2,figsize=(12,3))
series_smap_sm_pos.plot(ax=ax)
ax.set_title('SMAP data')

series_ccds_sm_pos.plot(ax=ax2,label="CCDS")
stems_merged.loc[series_ccds_sm_pos.index.min():series_ccds_sm_pos.index.max()]["LyeBrook (0.0508 m)"].plot(ax=ax2, alpha=0.5,
ax2.legend()
ax2.set_title('CCDS data compared to insitu observations');
```



The plots above show the different products. The ccds show some promising data when compared with the ground obersvation data. Obtaining SMAP data for the same period wasn't possible.

2.4 - Grace data & DEMs

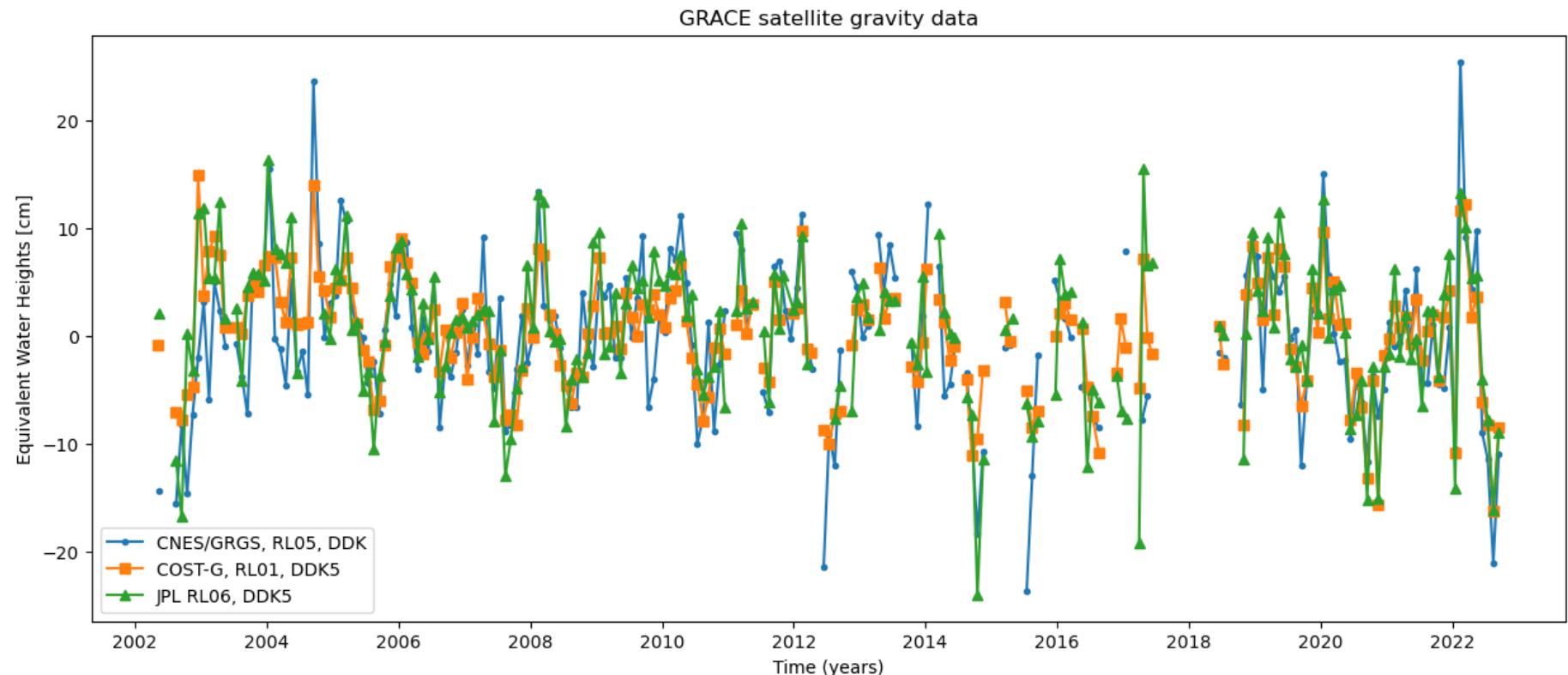
Dems have been used throughout, see GIS images

```
In [79]: files = glob.glob(f"{data_folder_grace}\\\*.txt")
cnes_grcs = pd.read_csv(files[1], skiprows=45, skipinitialspace=True, delimiter=' ', index_col=['Time (years)'],
                        names=['Time (seconds since 1970/01/01)', 'Time (days since 1950/01/01)', 'Time (years)', 'Equivalent Water Height (cm)', 'Linear model (cm)', 'Periodic model (cm)'])
cost_g = pd.read_csv(files[2], skiprows=45, skipinitialspace=True, delimiter=' ', index_col=['Time (years)'],
                     names=['Time (seconds since 1970/01/01)', 'Time (days since 1950/01/01)', 'Time (years)', 'Equivalent Water Height (cm)', 'Linear model (cm)', 'Periodic model (cm)'])
jpl = pd.read_csv(files[3], skiprows=45, skipinitialspace=True, delimiter=' ', index_col=['Time (years)'],
                  names=['Time (seconds since 1970/01/01)', 'Time_days_since', 'Time (years)', 'Equivalent Water Heights (cm)', 'Linear model (cm)', 'Periodic model (cm)'])

jpl['Time days'] = jpl.apply(lambda x: pd.Timestamp('1950-01-01') + datetime.timedelta(x.Time_days_since), axis=1)
```

```
jpl_1 = jpl.copy()
jpl_1.set_index(['Time days'], inplace=True)
jpl_1.drop(inplace=True, columns=['Time (seconds since 1970/01/01)', 'Time_days_since', 'Linear model (cm)', 'Periodic model (cm)'])
jpl_1['Storage [mm]'] = jpl_1['Equivalent Water Heights (cm)'] * 10
jpl_1.drop(inplace=True, columns=['Equivalent Water Heights (cm)'])
jpl_1.to_parquet(f'{data_folder_grace}\jplStorage.parquet')
```

```
In [80]: fig, ax = plt.subplots(figsize=(15,6))
cnes_grgs['Equivalent Water Heights (cm)'].plot(marker='.', label='CNES/GRGS, RL05, DDK')
ax.xaxis.set_major_locator(mpl.ticker.MaxNLocator(nbins=12, integer=True))
ax.set_ylabel('Equivalent Water Heights [cm]')
cost_g['Equivalent Water Heights (cm)'].plot(marker='s', label='COST-G, RL01, DDK5')
jpl['Equivalent Water Heights (cm)'].plot(marker='^', label='JPL RL06, DDK5')
ax.set_title('GRACE satellite gravity data')
ax.legend();
```



GRACE (Gravity Recovery And Climate Experiment)

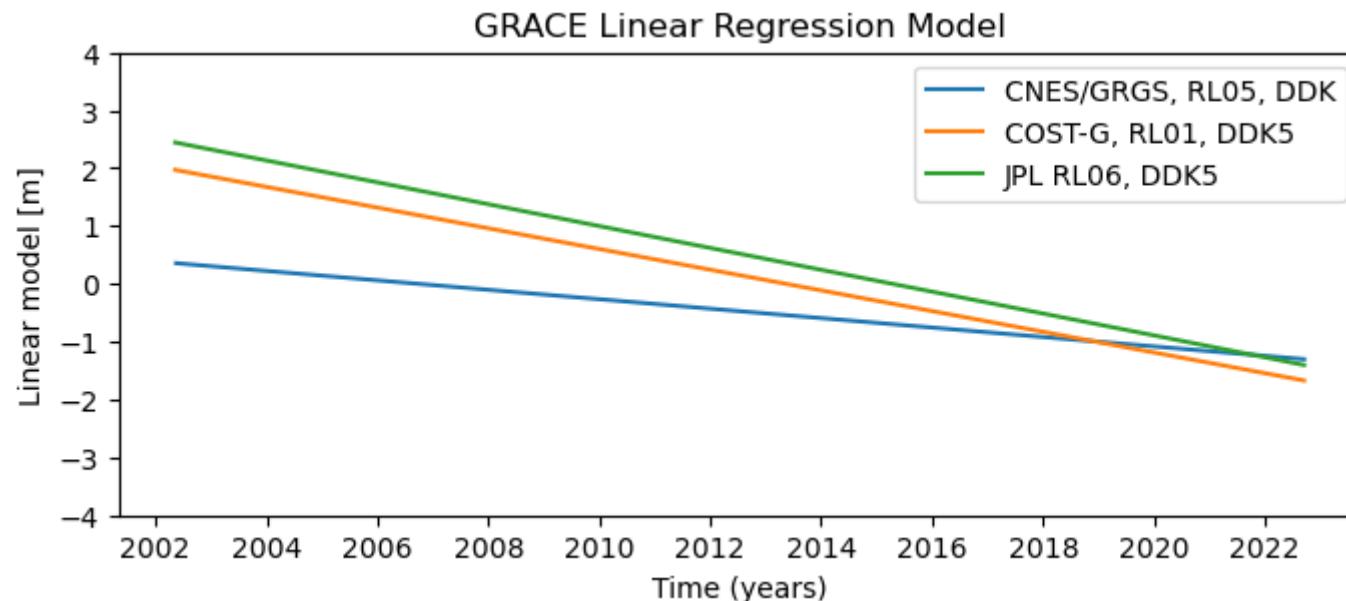
Grace data is obtained by a pair of satellites which follows each other on a polar orbit. The satellites are situated on a altitude of 500km and a distance of 220 km from each other. The plotted time series are created by three different groups.

- CNES/GRGS: French National Space Center/ Research Group for Space Geodesy in Toulouse
- COST-G: Combination Service for Time-variable Gravity Fields consortium
- JPL: Jet Propulsion Laboratory, in Pasadena, California

As can be seen, the COST-G model shows peaks with less magnitude compared to the other 2 models.

Overall, the water height is changing within a year.

```
In [81]: fig, ax = plt.subplots(figsize=(8,3))
cngrgs['Linear model (cm)'].plot(label='CNES/GRGS, RL05, DDK')
ax.xaxis.set_major_locator(mpl.ticker.MaxNLocator(nbins=12, integer=True))
ax.set_ylabel('Linear model [m]')
cost_g['Linear model (cm)'].plot(label='COST-G, RL01, DDK5')
jpl['Linear model (cm)'].plot(label='JPL RL06, DDK5')
ax.set_title('GRACE Linear Regression Model')
ax.legend()
ax.set_ylim((-4, 4));
```



All three models show a decreasing trend in water height over past 20 years.

2.5- Evaporation from Remote sensing

landsat was tried first

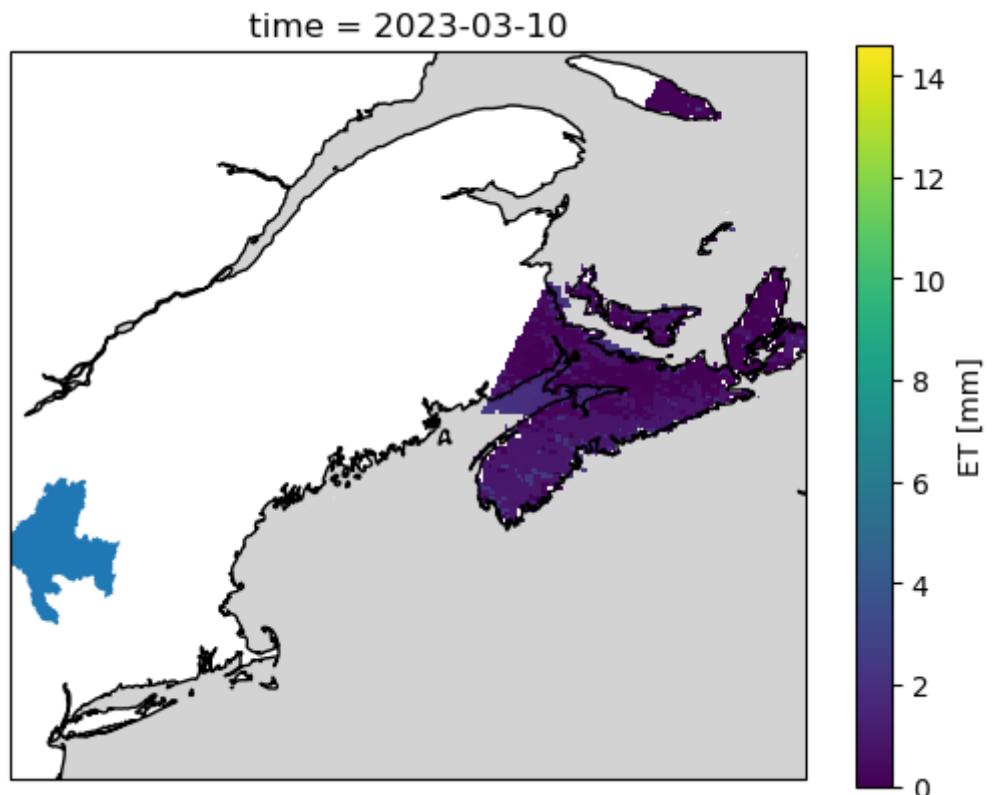
```
In [82]: outline = gpd.read_file(f"{gis_folder}\\\hudson_basin.gpkg", driver="GPKG", crs="EPSG:26918")
outline_buffered = gpd.read_file(f"{gis_folder}\\\hudson_basin_buffered.gpkg", crs="EPSG:26918")
for layer in [outline, outline_buffered]:
    layer.geometry = layer.geometry.to_crs("EPSG:4326")
```

```
In [83]: ds = xr.open_dataset(data_folder + '\\EP\\landsat.nc')
```

```
In [84]: # to avoid showing warnings of cartopy
import warnings
warnings.filterwarnings('ignore')

pvar = ds.ET.isel(time=0)
```

```
ax = plt.axes(projection=ccrs.PlateCarree())      # to use simple Lat/Lon
pvar.plot.imshow(ax=ax, transform=ccrs.PlateCarree(), interpolation='nearest')
ax.coastlines()
ax.add_feature(cartopy.feature.OCEAN, facecolor='lightgray')
ax.set_xlim((-75, -60))
ax.set_ylim((40, 50))
outline.plot(ax=ax);
```



clearly falls outside our area, thus try another product

Use era5 data:

code for automatic data retrieval is available in notebook [2.5](#) but was omitted for space reason

These are large files so are not in the project folder, but processed data is available

```
In [85]: year = ['2001', '2002', '2003', '2004', '2005', '2006', '2007', '2008', '2009', '2010']
path = f"C:\\\\Users\\\\david\\\\Documents\\\\EP_data_ENVM1502\\\\Era5_{year[0]}-{year[-1]}.nc"
ds = xr.open_dataset(path)
ds.pev.values[ds.pev.values > 0] = 0
cmap = mpl.colormaps["RdBu"]
```

We want to crop our region out of the mask as it currently includes a lot of ocean, when we take the mean, this causes discrepancies

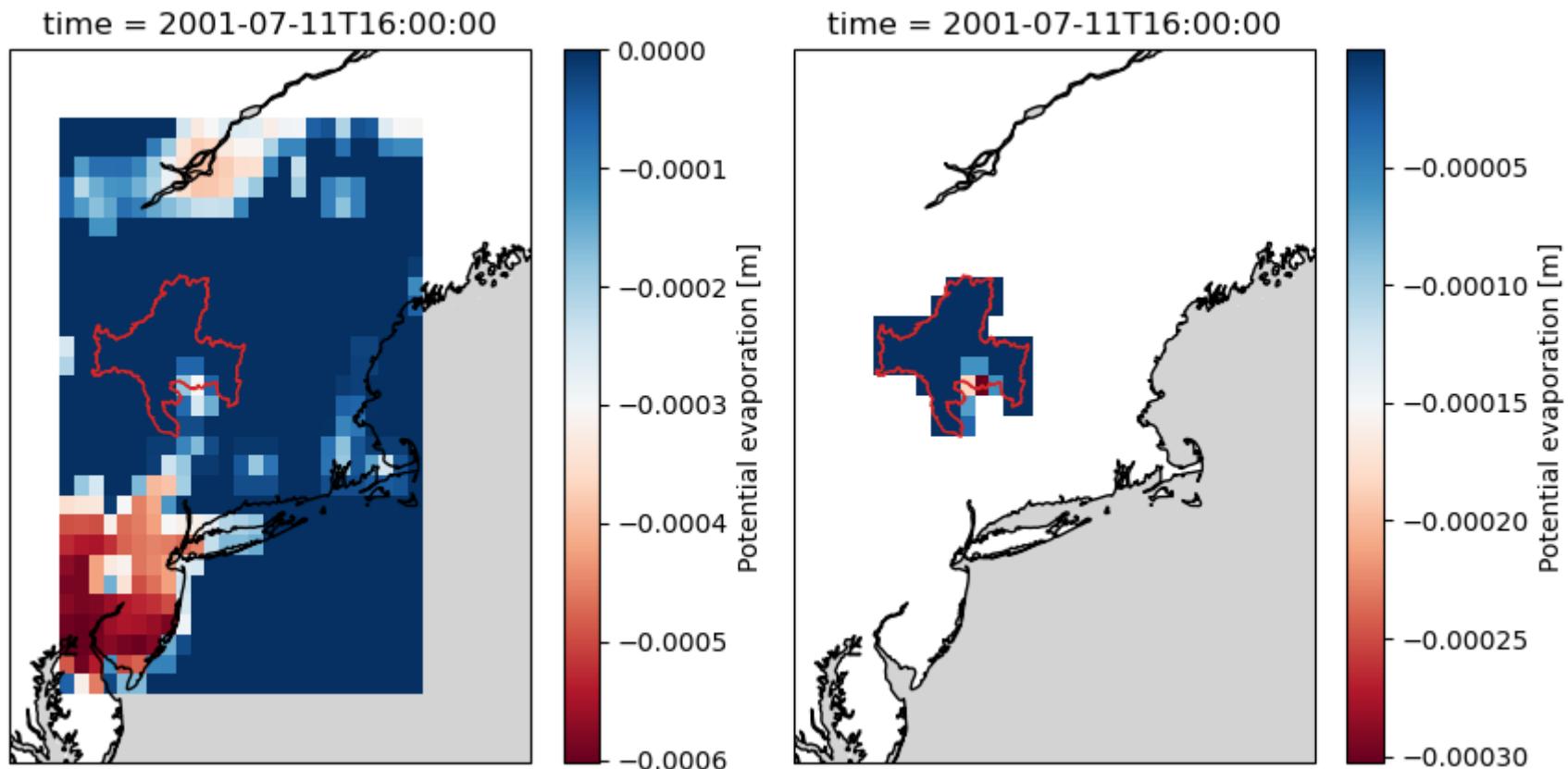
```
In [86]: pvar = ds.pev.isel(time=4600)
# ax = plt.axes(projection=ccrs.Orthographic(0, 0)) # to use the Orthographic projection

fig = plt.figure(figsize=(10,5))
ax = fig.add_subplot(121,projection=ccrs.PlateCarree())
ax2 = fig.add_subplot(122,projection=ccrs.PlateCarree())

pvar.plot.imshow(ax=ax, transform=ccrs.PlateCarree(),interpolation='nearest',cmap=cmap)
ax.coastlines()
ax.add_feature(cartopy.feature.OCEAN, facecolor='lightgray')
ax.set_xlim((-77,-68))
ax.set_ylim((38,47))
outline.plot(ax=ax, edgecolor="C3", facecolor="None")

# cropping
lon = np.arange(-76, -70+0.25, 0.25)
lat = np.arange( 39, 46+0.25, 0.25)
mask = regionmask.mask_geopandas(outline_buffered, lon, lat,lon_name="longitude",lat_name="latitude")
cropped_ds = ds.where(mask==0)

pvar = cropped_ds.pev.isel(time=4600)
pvar.plot.imshow(ax=ax2, transform=ccrs.PlateCarree(),interpolation='nearest',cmap=cmap)
ax2.coastlines()
ax2.add_feature(cartopy.feature.OCEAN, facecolor='lightgray')
ax2.set_xlim((-77,-68))
ax2.set_ylim((38,47))
outline.plot(ax=ax2, edgecolor="C3", facecolor="None");
```



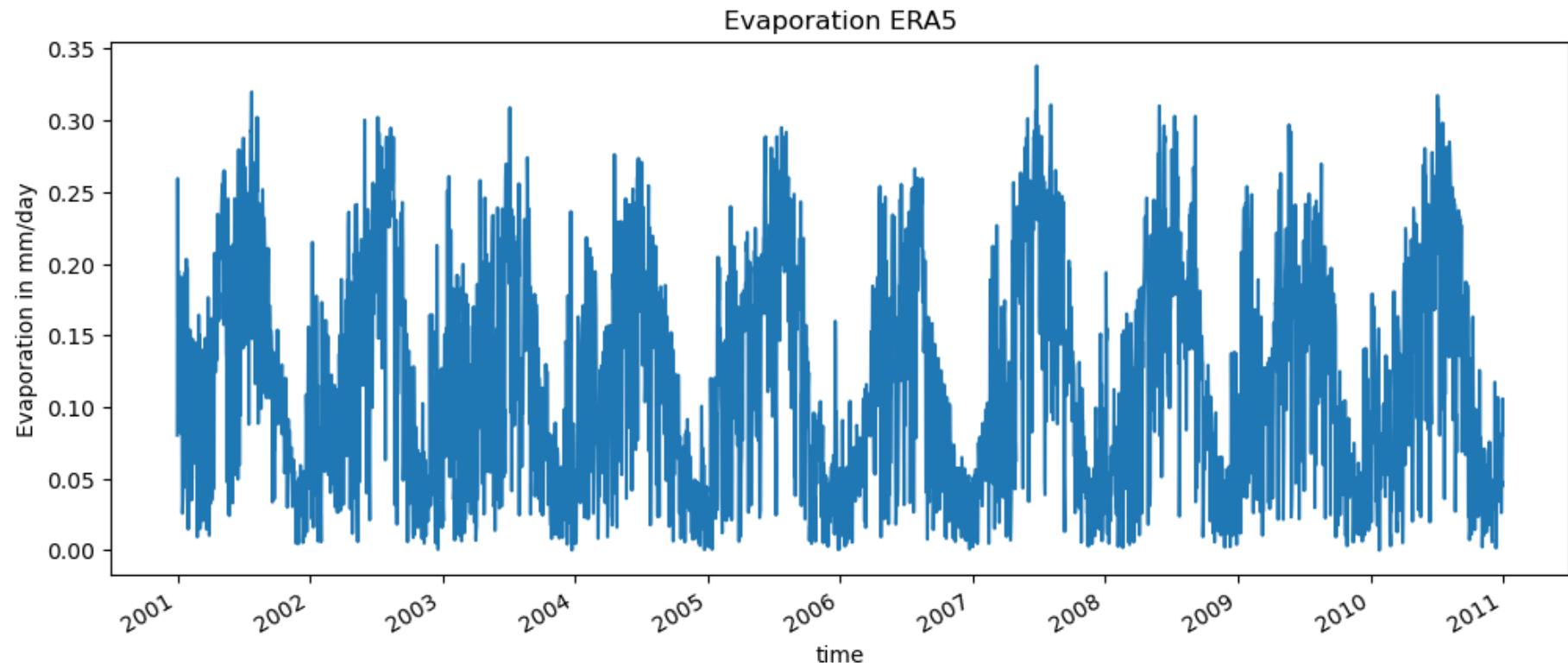
Take mean & resample

```
In [87]: ds_combine_mean = cropped_ds.mean(dim=["latitude","longitude"])
ds_combine_daily = ds_combine_mean.resample(time="1D").sum()
```

Export to df to be used & repeat for all years

```
In [88]: series_pev = ds_combine_daily.pev.to_pandas()
df_pev = pd.DataFrame(data=series_pev,columns=["Pev"])
df_pev.Pev = df_pev.Pev * - 1000 # m -> m & evap is evaporation is negative as it leaves the earth
df_pev.index = df_pev.index - datetime.timedelta(hours=6)
```

```
In [89]: fig, ax = plt.subplots(1, figsize=(12,5))
df_pev["Pev"].plot(ax=ax)
ax.set_title("Evaporation ERA5")
ax.set_ylabel("Evaporation in mm/day");
```



Era5 seems very low which we dont fully understand, explored more in 2.6

2.6 - Data assimilation

quite a bit of work has been done to prepare all the data:

- [2.6.0](#) collects all the data using the google earth engine for IMERG, MODIS & GRACE
- [2.6.1](#) loads in monthly GLEAM evaporation data obtained from their sstp server between 1980-2020

- [2.6.2](#) repeats this process for all the daily gleam data between 1980 - 2020, this data is large (17Gbs) thus only the processed data is included.

Only the results are shown here (still reproducible), see notebook [2.6.7](#) for more detail.

load data

limit to 2010-2015 due to storage constraints

P - ERA 5 obtained from ESMValTool - Forcings for the HBVmountain hydrological model: *with thanks to Rolf Hut*

```
In [90]: ds_era5 = xr.load_dataset(f"{data_folder}\ERA5_Group18_2010_2015.nc")
mask = regionmask.mask_geopandas(outline_buffered,
                                  ds_era5['pr'].lon.to_numpy(),
                                  ds_era5['pr'].lat.to_numpy(),
                                  lon_name="lon",
                                  lat_name="lat")
cropped_ds_era5 = ds_era5.where(mask==0)

# Pr in "kg m-2 s-1" -> *86400 mm/d
pr_series = cropped_ds_era5["pr"].mean(dim=["lat","lon"]).to_pandas() * 86400
df_era5_P = pd.DataFrame(pr_series,columns=["pr"]).rename(columns={"pr":"era5"})
```

```
In [91]: IMERG = pd.read_parquet(f"{data_folder}\P\IMERG.parquet").rename(columns={"P":"IMERG"})
```

```
In [92]: files = glob.glob(f"{data_folder}\combined*.parquet")
df_all_data = pd.read_parquet(files[0]).loc["2010":"2015"]
station_data = df_all_data[[ "P"]].rename(columns={"P":"station"})
```

```
In [93]: monlthy_p = [df_era5_P.resample("m").sum(), IMERG.resample("m").sum(), station_data.resample("m").sum()]
df_p = pd.concat(monlthy_p, axis = 1).loc["2010-03":"2014"]

# Compute monthly mean mP and variance vP of precipitation
df_p["mp"] = df_p.apply(lambda x: np.mean([x[f'{col}'] for col in x.index]),axis=1)
df_p["vp"] = df_p.apply(lambda x: (np.sum([(x[f'{col}'] - x.mp)**2 for col in x.index]))/(len(x.index)-1), axis=1)
df_p["sp"] = df_p.apply(lambda x: np.sqrt(x.vp) ,axis=1)
```

E - Load in EP from data collected already

```
In [94]: ERA5_E = pd.read_parquet(f"{data_folder}\EP\combined_PE.parquet").rename(columns={"Pev":"Era5"}).resample('m').sum()
```

```
In [95]: MODIS = pd.read_parquet(f"{data_folder}\EP\MODIS.parquet").dropna()
MODIS["PET"] = MODIS["PET"] * 0.1 # "kg/m^2/8day" -> mm: scale factor 0.1
```

```
In [96]: MODIS_monthly = MODIS.resample('m').sum()
MODIS_monthly.rename(columns={"PET":"MODIS"},inplace=True)
```

```
In [97]: GLEAM = pd.read_parquet(f"{data_folder}\EP\GLEAM.parquet").loc["2010":"2015"].rename(columns={"Pe":"GLEAM"})
```

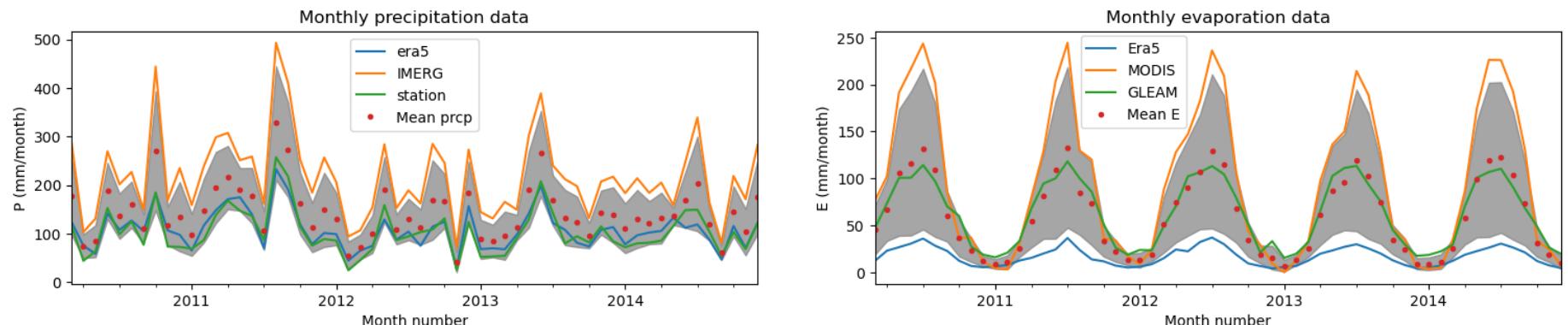
```
In [98]: df_e = pd.concat([ERA5_E,MODIS_monthly, GLEAM],axis=1).loc["2010-03":"2014"]

# Compute monthly mean mE and variance vE of evaporation
df_e["me"] = df_e.apply(lambda x: np.mean([x[f"{col}"] for col in x.index]),axis=1)
df_e["ve"] = df_e.apply(lambda x: (np.sum([(x[f"{col}"] - x.me)**2 for col in x.index]))/(len(x.index)-1), axis=1)
df_e["se"] = df_e.apply(lambda x: np.sqrt(x.ve),axis=1)
```

```
In [99]: fig, [ax2, ax] = plt.subplots(1,2, figsize=(15,3))
fig.tight_layout(w_pad=5)

df_e[['Era5','MODIS','GLEAM']].plot(ax=ax)
df_e['me'].plot(ax=ax, lw=0, color="C3", marker=".", label="Mean E")
ax.fill_between(df_e.index,(df_e["me"]+df_e["se"]).values,(df_e["me"]-df_e["se"]).values,color="grey",alpha=0.7)
ax.set_title("Monthly evaporation data")
ax.set_ylabel("E (mm/month)")
ax.set_xlabel("Month number");
ax.legend(bbox_to_anchor=(0.464,0.588))

df_p[['era5','IMERG','station']].plot(ax=ax2)
df_p['mp'].plot(ax=ax2, lw=0, color="C3", marker=".", label="Mean prcp")
ax2.fill_between(df_p.index,(df_p["mp"]+df_p["sp"]).values,(df_p["mp"]-df_p["sp"]).values,color="grey",alpha=0.7)
ax2.set_title("Monthly precipitation data")
ax2.set_ylabel("P (mm/month)")
ax2.set_xlabel("Month number")
ax2.legend();
```



Here we see the issue with the era 5 evaporation data

Q - station data already prepared

```
In [100...]: df_q = df_all_data[["Q"]].resample("m").sum().loc["2010-03":"2014"]
# Compute monthly mean mq and variance vq of river discharge
df_q["mq"] = df_q.apply(lambda x: np.mean([x[f"{col}"] for col in x.index]),axis=1)
df_q["vq"] = df_q.apply(lambda x: 0.1 * x.mq, axis=1)
df_q["sq"] = df_q.apply(lambda x: np.sqrt(x.vq),axis=1)
```

S - from Earth engine

```
In [101...]: df_GRACE = pd.read_parquet(f"{data_folder}\Grace\GRACE.parquet").loc["2010-03":"2014"]
df_GRACE_error = pd.read_parquet(f"{data_folder}\GRace\GRACE_error.parquet").loc["2010-03":"2014-12"]
```

Bit of data management & magic to get it working with the others. Due to missing data there is some uncertainty in this method

```
In [102...]: df_s_in = pd.concat([df_GRACE,df_GRACE_error],axis=1).resample("m").mean()
wanted_index = df_q.apply(lambda x: f'{x.name.year}-{x.name.month}', axis=1).copy()
current_index = df_s_in.apply(lambda x: f'{x.name.year}-{x.name.month}', axis=1)
df_index = pd.DataFrame(wanted_index).reset_index().set_index(0).rename(columns={"index":"fulldate"})
df_missing = df_index.loc[list(set(wanted_index.values).difference(set(current_index.values)))].sort_values("fulldate").set_index(0)
df_missing['graceJPL'] = 0
df_missing['graceJPLerror'] = 10**9
df_s = pd.concat([df_s_in,df_missing[['graceJPL','graceJPLerror']]])
```

```
df_s["graceJPL"] = df_s.apply(lambda x: 0 if np.isnan(x.graceJPL) else x.graceJPL, axis=1)
df_s["graceJPLerror"] = df_s.apply(lambda x: 10**9 if np.isnan(x.graceJPLerror) else x.graceJPLerror, axis=1)
```

In [103...]

```
# Compute monthly mean mS and variance vS of water storage
df_s["ms"] = df_s.apply(lambda x: x.graceJPL if not np.isnan(x.graceJPL) else 0, axis=1) # 0
df_s["ss"] = df_s.apply(lambda x: x.graceJPLerror if x.graceJPLerror > -9999 else np.nan, axis=1) #10**9 if np.isnan(x.graceJPLerror)
df_s["vs"] = df_s.apply(lambda x: x.graceJPLerror**2 if x.graceJPLerror > -9999 else 10**9, axis=1) #10**9 if np.isnan(x.graceJPLerror)
```

then run the algorithm

In [104...]

```
def gaussian_product(m1, v1, m2, v2):
    w1 = v2 / (v1 + v2)
    w2 = v1 / (v1 + v2)
    m = w1 * m1 + w2 * m2
    v = w1 * v1
    # print(v, w2*v2)
    if not np.isclose(v, w2 * v2):
        print(f"Issue with V2, should be same {v}, {w2 * v2}")
        raise AssertionError
    return m, v
```

In [105...]

```
def close_water_balance(mP, vP, mE, vE, mQ, vQ, mS, vS):
    # Specify prior mean and variance for initial storage S0 (first month)
    mS0 = 0
    vS0 = 200 * 200#large variance to indicate large uncertainty
    # print([len(mP), len(vP),len(mE), len(vE), len(mQ), len(vQ), len(mS), len(vS)])
    # Initialize posteriors
    # We compute these in forward Loop (filtering posteriors) and then update them in backward Loop (smoothing posteriors)
    nt = len(mP)#number of months in time-series
    mPostP = np.zeros(nt)#posterior mean of precipitation in each month
    vPostP = np.zeros(nt)#posterior variance of precipitation in each month
    mPostE = np.zeros(nt)#etc...
    vPostE = np.zeros(nt)
    mPostQ = np.zeros(nt)
    vPostQ = np.zeros(nt)
    mPostS = np.zeros(nt)
    vPostS = np.zeros(nt)

    # Forward Loop (filtering)
```

```

for t in range(nt):
    if t != 0: # Step 1: predict - compute forward distribution to S
        mS0, vS0 = mPostS[t-1], vPostS[t-1]
        mS_1 = mP[t] + mS0 - mE[t] - mQ[t]
        vS_1 = vP[t] + vS0 + vE[t] + vQ[t]
        mPostS[t], vPostS[t] = gaussian_product(mS_1, vS_1, mS[t], vS[t]) # Step 2: update - compute filtering posterior of S

    # Backward Loop (smoothing)
    mToS, vToS = 0.0, 1e+9#represents backward distribution to S - initialize to wide Gaussian for last month
    for t in reversed(range(nt)):
        mPostS[t], vPostS[t] = gaussian_product(mPostS[t], vPostS[t], mToS, vToS) # Step 1: smoothing posterior of S

        mBackS, vBackS = gaussian_product(mToS, vToS, mS[t], vS[t]) # Step 2: posteriors of P, E, and Q ### bac
        if t != 0:
            mS0, vS0 = mPostS[t-1], vPostS[t-1]
        else:
            mS0, vS0 = 0, 200*200
        # Q = P - S + S0 - E
        mQ_1 = mP[t] - mBackS + mS0 - mE[t]
        vQ_1 = vP[t] + vBackS + vS0 + vE[t]
        mPostQ[t], vPostQ[t] = gaussian_product(mQ[t], vQ[t], mQ_1, vQ_1)
        # P = S - S0 + E + Q
        mP_1 = + mBackS - mS0 + mE[t] + mQ[t]
        vP_1 = + vBackS + vS0 + vE[t] + vQ[t]
        mPostP[t], vPostP[t] = gaussian_product(mP[t], vP[t], mP_1, vP_1)
        # E = P + S0 - Q - S
        mE_1 = mP[t] - mBackS + mS0 - mQ[t]
        vE_1 = vP[t] + vBackS + vS0 + vQ[t]
        mPostE[t], vPostE[t] = gaussian_product(mE[t], vE[t], mE_1, vE_1)

        mToS = mBackS - mP[t] + mE[t] + mQ[t] # Step 3: backward distribution to S0
        vToS = vBackS + vP[t] + vE[t] + vQ[t]

    mPostS0, vPostS0 = gaussian_product(mToS, vToS, mS0, vS0) # After backward loop: compute posterior mean and variance of S0
    return mPostP, vPostP, mPostE, vPostE, mPostQ, vPostQ, mPostS, vPostS, mPostS0, vPostS0 # Return final water balance estin

```

In [106...]

```

vals = close_water_balance(df_p["mp"].values, df_p["vp"].values, df_e["me"].values, df_e["ve"].values, df_q["mq"].values, df_c
mPostP, vPostP, mPostE, vPostE, mPostQ, vPostQ, mPostS, vPostS, mPostS0, vPostS0 = vals

```

```
In [107...]: df_p["mPostP"],df_p["vPostP"],df_e["mPostE"],df_e["vPostE"] = mPostP,vPostP,mPostE,vPostE
df_q["mPostQ"],df_q["vPostQ"],df_s["mPostS"],df_s["vPostS"] = mPostQ,vPostQ,mPostS,vPostS
```

Due to small errors in the numerical methods the water balance has some errors but they are close enough to zero to call it a success (Top plot).

Right shows that the gleam data is the best overall when closing the monthly waterbalance. This has already been done above & this is why the basin falls so nicely on the budyko curve. The station data looks very similar to the era5 precipitation data showing the data collection went well ;).

```
In [108...]: water_balance = np.zeros(len(mPostP))
storage_final = np.zeros(len(mPostP))

fig, ax_l = plt.subplots(1,figsize=(5,5))
for t in range(len(mPostP)):
    if t == 0:
        S0 = mPostS0
    else:
        S0 = mPostS[t-1]
    water_balance[t] = mPostS[t] - mPostP[t] + mPostE[t] + mPostQ[t] - S0
    storage_final[t] = mPostP[t] - mPostE[t] - mPostQ[t] + S0
ax_l.plot(water_balance,"ro")
ax_l.axhline(0)
ax_l.set_title("Error in the water balance")

# The plt.fill_between() function is useful for plotting an uncertainty interval.
fig, [ax2, ax] = plt.subplots(1,2,figsize=(20,5))
fig.tight_layout()

df_p['mp'].plot(ax=ax2,lw=0,color="C3",marker=".", alpha=0.3,label="initial mean")
ax2.fill_between(df_p.index,(df_p["mp"]+df_p["sp"]).values,(df_p["mp"]-df_p["sp"]).values,color="grey",alpha=0.3, label="initial uncertainty")

df_p['mPostP'].plot(ax=ax2,lw=0,color="k",marker=".",label="post mean")
ax2.fill_between(df_p.index,(df_p["mPostP"]+np.sqrt(df_p["vPostP"]).values),(df_p["mPostP"]-np.sqrt(df_p["vPostP"]).values),color="grey",alpha=0.3, label="post uncertainty")

df_p[['era5","IMERG","station']].plot(ax=ax2)

ax2.legend()
ax2.set_title("Mean monthly precipitation data with uncertainty bounds")
```

```
ax2.set_ylabel("P (mm/month)")
ax2.set_xlabel("Date")

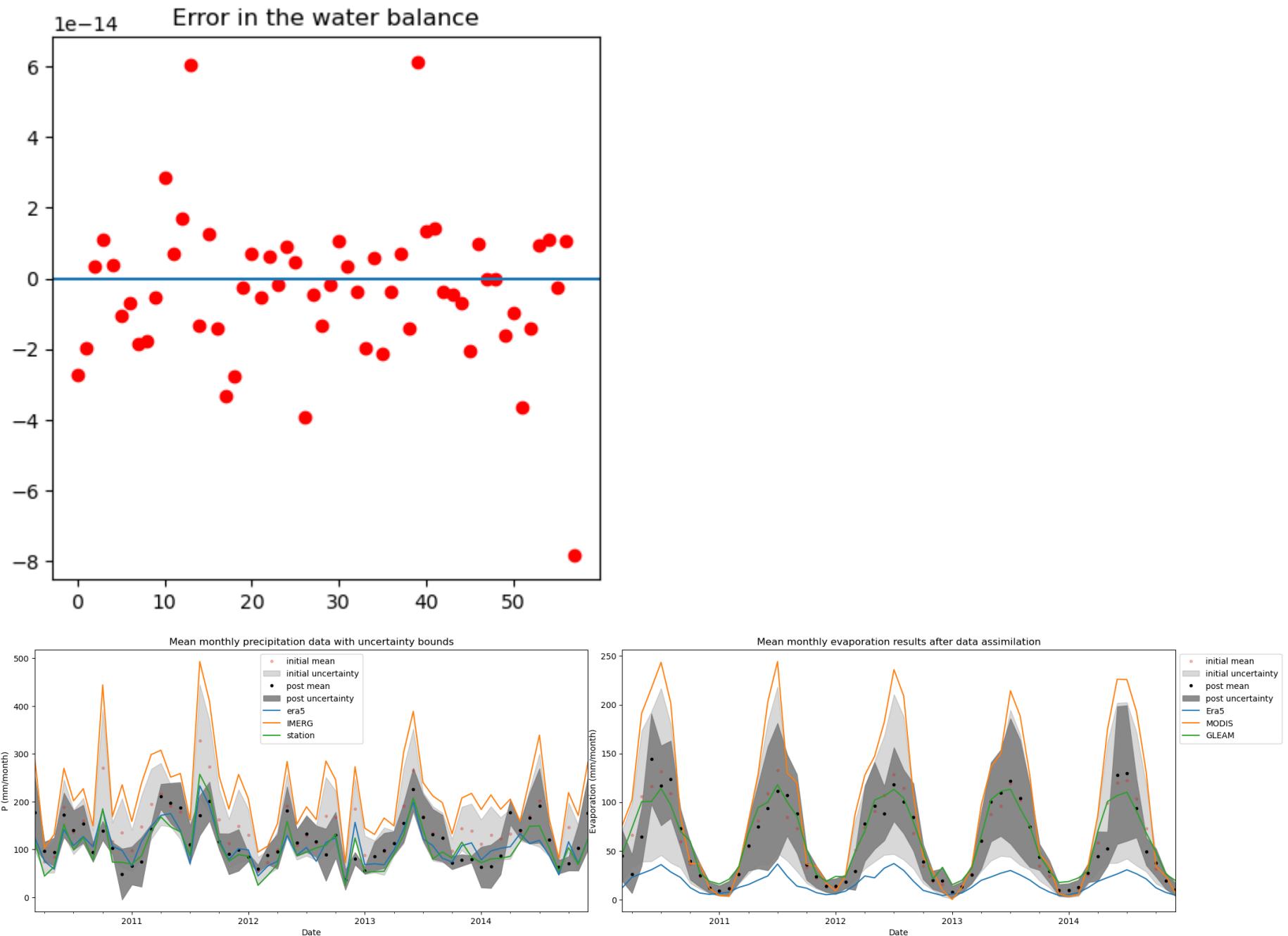
df_e['me'].plot(ax=ax, lw=0, color="C3", marker=".", alpha=0.3, label="initial mean")
ax.fill_between(df_e.index, (df_e["me"]+df_e["se"]).values, (df_e["me"]-df_e["se"]).values, color="grey", alpha=0.3, label="initial se")

df_e['mPostE'].plot(ax=ax, lw=0, color="k", marker=".", label="post mean")
ax.fill_between(df_e.index, (df_e["mPostE"]+np.sqrt(df_e["vPostE"])).values, (df_e["mPostE"]-np.sqrt(df_e["vPostE"])).values, color="grey", alpha=0.3, label="post se")

df_e[['Era5', "MODIS", "GLEAM"]].plot(ax=ax)

ax.legend(bbox_to_anchor=(1,1))
ax.set_title("Mean monthly evaporation results after data assimilation")
ax.set_ylabel("Evaporation (mm/month)")
ax.set_xlabel("Date")

fig.savefig("Figures\data_assimilation.png");
```



2.8 - Climate data

notebook 2.8 provides an automated way to download data, we will simply load it here

In [109...]

```
# This code shows one map
ifile = glob.glob(f'{data_folder}\\Climate Predictions\\*.nc')
ds_534 = xr.open_mfdataset(ifile[0]) # open dataset as x-array
ds_585 = xr.open_mfdataset(ifile[1]) # open dataset as x-array
```

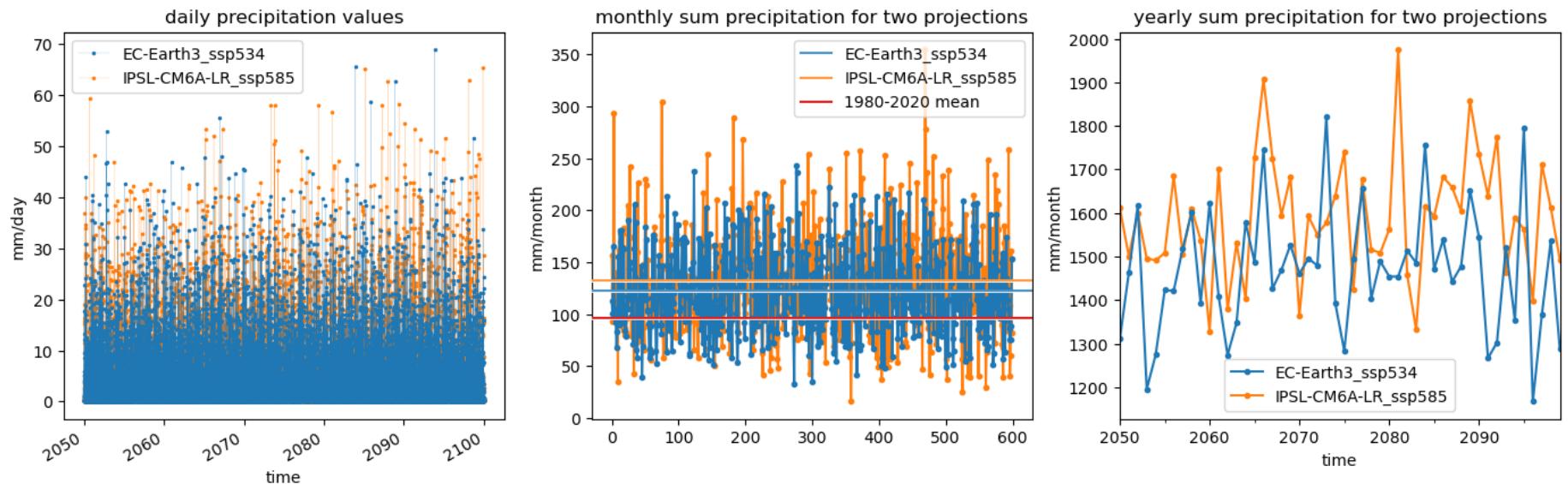
In [110...]

```
lst_series_out = []
names = ["EC-Earth3-ssp534", "IPSL-CM6A-LR-ssp585"]
fig, [ax, ax2, ax3] = plt.subplots(1,3,figsize=(17,5))
for index, ds in enumerate([ds_534,ds_585]):
    mean_lat = ds.mean(dim="lat")
    mean_lat_lon = mean_lat.mean(dim="lon")
    series_out = mean_lat_lon.pr.to_pandas() * 86400
    series_out.plot(ax=ax, marker=".", markersize=3, lw=0.1, label=names[index], zorder=1-index)
    ax.set_title("daily precipitation values")
    ax.set_ylabel("mm/day")
    ax.legend()
    lst_series_out.append(series_out)

for index, series_out in enumerate(lst_series_out):
    df = pd.DataFrame(data=series_out)
    ax2.axhline(df.resample("m").sum()[0].mean(), color=f"C{index}", label=names[index], alpha=0.8, lw=1.5, zorder=5)
    ax2.axhline(df.resample("m").sum()[0].mean(), color="w", lw=2, zorder=4)
    df = df.resample("m").sum()
    ax2.plot(df[0].values, marker=".", zorder=1-index, color=f"C{index}")
    ax2.set_ylabel("mm/month")
    ax2.set_title("monthly sum precipitation for two projections")
    ax2.axhline(combined_forcing[[ "P"]].resample("m").sum().mean().values, color="C3", lw=1.5, label="1980-2020 mean", zorder=5)
    ax2.axhline(combined_forcing[[ "P"]].resample("m").sum().mean().values, color="w", lw=2, zorder=4)
    ax2.legend()

for index, series_out in enumerate(lst_series_out):
    df = pd.DataFrame(data=series_out)
    df.resample("y").sum().plot(ax=ax3,marker=".", label=names[index], zorder=1-index)
```

```
ax3.set_ylabel("mm/month")
ax3.set_title("yearly sum precipitation for two projections")
ax3.legend(names);
```



SSP585 shows a higher level of monthly rainfall than SSP534, showing increasing flood peaks could be an issue to look out for. At the same time the lower peaks are also more extreme

3.1 Reservoir modeling

Before developing a HBV model, a reservoir model is made. With an objective function, the optimal parameters for k and α are determined.

$$Q = k \cdot S^\alpha$$

```
In [23]: def storage(S0, k, alpha, data):
    dt = 1
    S = np.zeros(len(data))
    S[0] = S0
    for i in range(len(data)-1):
```

```

        S[i+1] = S[i] - k * dt * S[i] ** alpha + data['P'].iloc[i] * dt - data['Prev'].iloc[i] * dt
        if S[i+1] < 0:
            S[i+1] = 0
    data['S'] = S
    return data

```

In [24]:

```

S0 = 75 #mm
t0 = 0 #days
tmax = 200 #days
dt = 1 #days

```

In [25]:

```

def fobj(p, S0, df):
    k, alpha = p
    df_s = storage(S0, k, alpha, df)
    df_s['Q'] = k * df_s['S'] ** alpha
    Q_mean = df_s.Q.mean()
    P_mean = df_s.P.mean()
    runoff = Q_mean / P_mean
    runoff_model = 0.54 #determined with long term water balance
    sse = np.sum((runoff - runoff_model) ** 2)
    return sse

popt = fmin(fobj, [0.005, 1], args=(S0, combined_forcing))
k_opt, alpha_opt = popt

print('Value for k', k_opt)
print('Value for alpha:', alpha_opt)

```

Optimization terminated successfully.
 Current function value: 0.000000
 Iterations: 49
 Function evaluations: 95
 Value for k 0.006568329614848229
 Value for alpha: 2.29074597887151

In [26]:

```

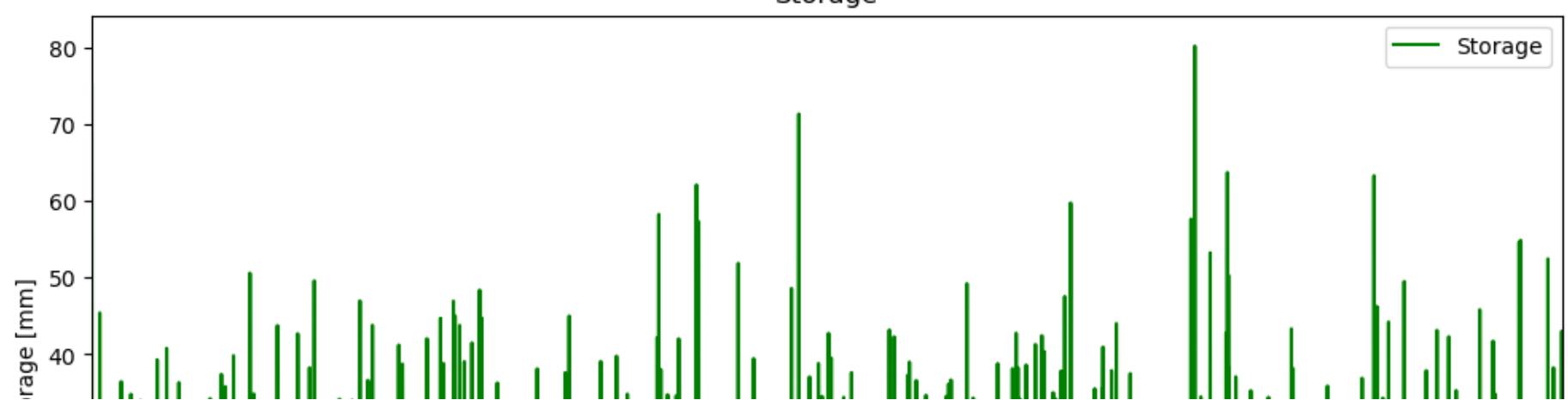
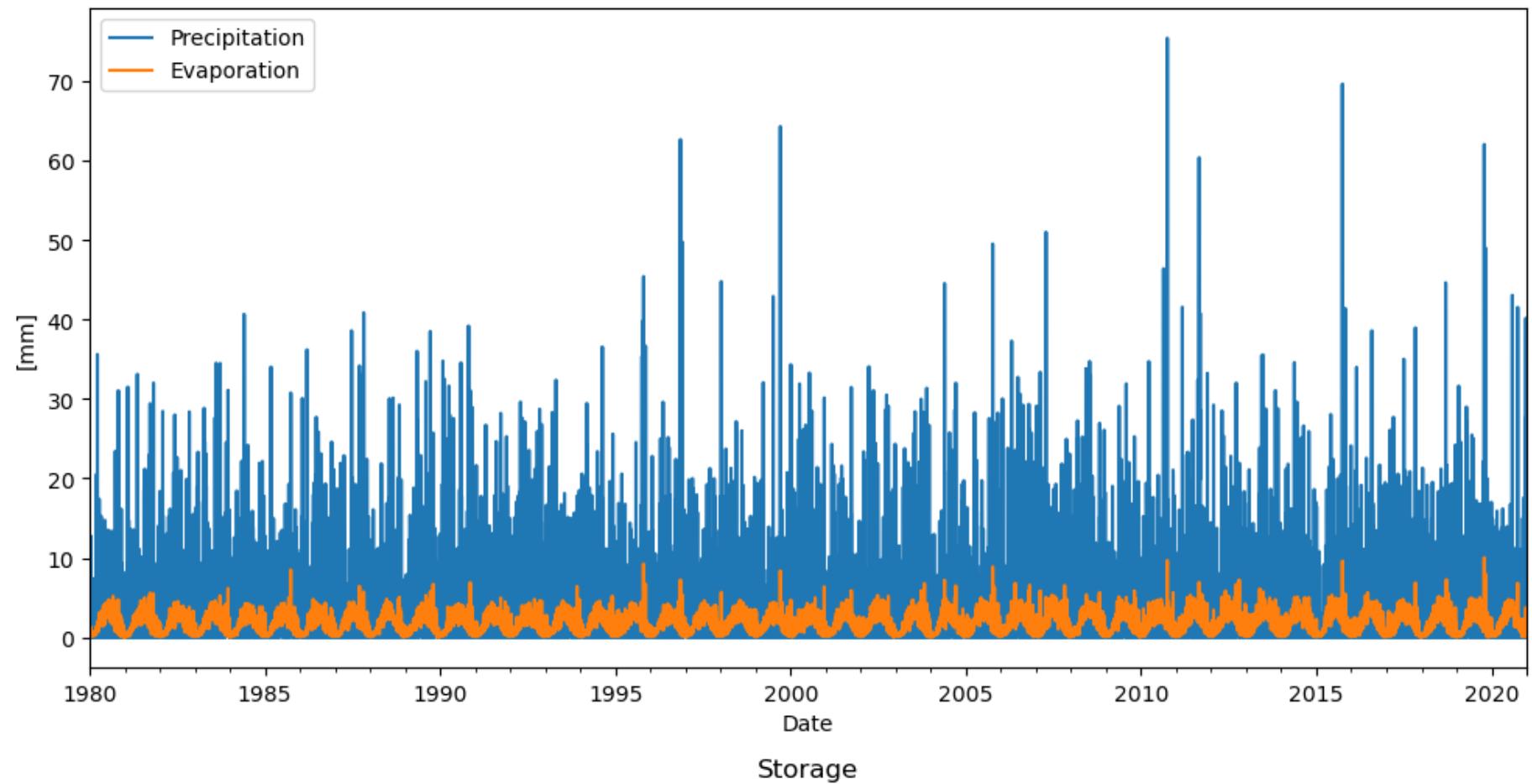
df_storage = storage(S0, k_opt, alpha_opt, combined_forcing)

fig, ax = plt.subplots(2, figsize=(10,10))
df_storage['P'].plot(ax=ax[0], ylabel='[mm]', label='Precipitation')

```

```
df_storage['Pev'].plot(ax=ax[0], label='Evaporation')
df_storage['S'].plot(ax=ax[1], label='Storage', color='green', ylabel='Storage [mm]', title='Storage')
ax[0].set_xlabel('Date')
ax[1].set_xlabel('Date')
fig.tight_layout()
ax[0].legend()
ax[1].legend()
```

Out[26]: <matplotlib.legend.Legend at 0x2495d293510>



3.2/3.3 Lumped model and calibration

To model the water cycle, the HBV model is used. First this is done as lumped model, taking the whole area as a homogeneous area.

In the HBV model, the snow storage is added. The data set is splitted in sets of 4 years. Each time the model is calibrated over data of 4 years, and after it is tested on the following 4 years. This is repeated 4 more times. Each time the NSE is calculated to see the predictive skill of the model.

```
In [4]: def Weigfun( Tlag):
    # WEIGFUN Summary of this function goes here
    #   Detailed explanation goes here
    nmax=int(np.ceil(Tlag))

    if nmax==1:
        Weights=float(1)
    else:
        Weights=np.zeros(nmax)

    th=Tlag/2
    nh=int(np.floor(th))
    for i in range(0,nh):
        Weights[i]=(float(i+1)-0.5)/th
    i=nh
```

```

Weights[i]=(1+(float(i+1)-1)/th)*(th-int(np.floor(th)))/2+(1+(Tlag-float(i+1))/th)*(int(np.floor(th))+1-th)/2
for i in range(nh+1, int(np.floor(Tlag))):
    Weights[i]=(Tlag-float(i+1)+.5)/th

if Tlag>int(np.floor(Tlag)):
    Weights[int(np.floor(Tlag))]=(Tlag-int(np.floor(Tlag)))**2/(2*th)

Weights=Weights/sum(Weights)

return(Weights)
# plot(Weights)

```

In [5]:

```

def HBVMod(Par, forcing, Sin, n_day, snow=True, mode='training'):
    #HBVpareto Calculates values of 3 objective functions for HBV model

    Imax = Par[0]
    Ce = Par[1]
    Sumax = Par[2]
    beta = Par[3]
    Pmax = Par[4]
    Tlag = Par[5]
    Kf = Par[6]
    Ks = Par[7]
    FM = 3 # mm/deg/d
    Tt = -0.5 # degc

    Prec = forcing['P'].values
    Qo = forcing['Q'].values
    Etp = forcing['Pev'].values
    temp = forcing['T'].values
    Psnow = np.zeros(len(Prec))
    Pldt = np.zeros(len(Prec))

    tmax = len(Prec)

    # allocate Si, Su, Sf, Ss, Eidt, Eadt, Qtotdt

    Si = np.zeros(tmax)
    Su = np.zeros(tmax)

```

```

Sf = np.zeros(tmax)
Ss = np.zeros(tmax)
Ssnow = np.zeros(tmax)
Eidt = np.zeros(tmax)
Eadt = np.zeros(tmax)
Qtotdt = np.zeros(tmax)
Qs = np.zeros(tmax)
Qf = np.zeros(tmax)

# initialize Si, Su, Sf, Ss, Ssnow
Si[0] = Sin[0]
Su[0] = Sin[1]
Sf[0] = Sin[2]
Ss[0] = Sin[3]
Ssnow[0] = Sin[4]

dt = 1
Er = 331 #m

# Model 1 SOFI
for i in range(0, tmax):
    Ept = Etp[i] * dt
    TR = temp[i] * dt

    #snow reservoirs
    Ti = TR #different elevations not taken into account
    if snow:
        if Ti < Tt and i != 0:
            Pdt = 0 # no rainfall
            Ps = Prec[i] * dt # precipitation is snow
            M = 0 # Too cold for melt
            Ssnow[i] = Ssnow[i-1] + Ps # add snow to the prev day
            Pldt[i] = 0 # no outflow as too cold
        # then must be above
    else:
        Pdt = Prec[i] * dt # all precip is rainfall
        Ps = 0 # no snow
        M = min(Ssnow[i-1] / dt, FM * (Ti - Tt)) # calculate melt

```

```

        Ssnow[i]           = Ssnow[i-1] - M * dt
        Pldt[i]           = M
    if i < tmax-1:
        Ssnow[i+1] = Ssnow[i]

    else:
        Pdt            = Prec[i] * dt
        Pldt[i] = 0
        Ps = 0

    # Interception Reservoir
    if Pdt > 0:
        Si[i] = Si[i] + Pdt
        Pedt = np.maximum(0, (Si[i] - Imax) / dt) + Pldt[i] #Outflow of snow storage is added here
        Si[i] = Si[i] - Pedt
        Eidt[i] = 0
    else:
        # Evaporation only when there is no rainfall
        Pedt = np.maximum(0, (Si[i] - Imax) / dt) + Pldt[i] #is zero, because of no rainfall
        Eidt[i] = np.minimum(Epdt, Si[i] / dt)
        Si[i] = Si[i] - Pedt - Eidt[i]

    if i < tmax-1:
        Si[i+1] = Si[i]

    # Split Pe into Unsaturated Reservoir and Preferential reservoir
    if Pedt > 0:
        Cr = (Su[i] / Sumax) ** beta
        Qiudt = (1 - Cr) * Pedt # flux from Ir to Ur
        Su[i] = Su[i] + Qiudt
        Qufdt = Cr * Pedt #flux from Su to Sf
    else:
        Qufdt = 0

    # Transpiration
    Epdt = max(0, Epdt - Eidt[i])
    Eadt[i] = Epdt * (Su[i] / (Sumax * Ce))
    Eadt[i] = min(Su[i] / dt, Eadt[i])
    Su[i] = Su[i] - Eadt[i]

```

```

# Percolation
Qusdt = Pmax * (Su[i] / Sumax) * dt # Flux from Su to Ss
Su[i] = Su[i] - Qusdt

if i < tmax - 1:
    Su[i+1] = Su[i]

# Fast Reservoir
Sf[i] = Sf[i] + Qufdt
Qfdt = dt * Kf * Sf[i]
Sf[i] = Sf[i] - Qfdt

if i < tmax-1:
    Sf[i+1] = Sf[i]

# Slow Reservoir
Ss[i] = Ss[i] + Qusdt
Qsdt = dt * Ks * Ss[i]
Ss[i] = Ss[i] - Qsdt
if i < tmax-1:
    Ss[i+1] = Ss[i]

Qtotdt[i] = Qsdt + Qfdt
Qs[i] = Qsdt
Qf[i] = Qfdt

Psnow[i] = Ps

# Check Water Balance
Sout = np.array([Si[-1], Su[-1], Sf[-1], Ss[-1], Ssnow[-1]]) # initialize Si, Su, Sf, Ss, Ssnow
Sf = Si[-1] + Ss[-1] + Sf[-1] + Su[-1] + Ssnow[-1] #final storage
Sin = sum(Sin) #initial storage
WB = sum(Prec) - sum(Eidt) - sum(Eadt) - sum(Qtotdt) - Sf + Sin

# Offset Q
Weigths = Weigfun(Tlag)

```

```

Qm = np.convolve(Qtotdt, Weights)
Qm = Qm[0:tmax]
forcing.loc[:, 'Qm'] = Qm
forcing.loc[:, 'PSnow'] = Psnow
forcing.loc[:, 'S_snow'] = Ssnow
forcing.loc[:, 'Pl_snow'] = Pldt

#Use n_days for spinoff to compensate for initial storage
if mode == 'training':
    Qo = Qo[n_day:]
    Qm = Qm[n_day:]

# Calculate objective
ind = np.where(Qo>=0)
QoAv = np.mean(Qo[ind])
ErrUp = np.sum((Qo - Qm) ** 2)
ErrDo = np.sum((Qo - QoAv) ** 2)
Obj = 1 - (ErrUp / ErrDo)

return forcing, Obj, Sout

# Leg['Qobs', 'Qmod']

```

I_{max} is based on grassland < 1mm and forest: 1-5 mm. S_{max} range is based on the Sr of 73 mm calculated in previous exercise.

```

In [6]:      #      Imax Ce Smax beta Pmax Tlag Kf Ks
ParMinn = np.array([0.1,    0.1,   40,     .1,    .001,    0.001,    .0001,    .001])
ParMaxn = np.array([5,      0.85,  100,    8,     10.0,    10,      0.1,     1])
Sin = np.array([0,      100,   0,      5,     0])

```

```

In [7]: def calibration(df, n_max, Par_Maxn, Par_Minn, S_in, snow=True, mode='Training'):
    # GLUE
    nmax = n_max
    A = np.zeros((nmax,9))
    Sout_lst = np.zeros((nmax, len(S_in)))
    n_feasible = 0

```

```

for n in range(1,nmax):
    Rnum = np.random.random(8) #generate a vector of random number

    Par = Rnum * (Par_Maxn - Par_Minn) + Par_Minn # calculate the random parameter set
    df, Obj, Sout = HBVMod(Par, df, Sin, 365+180, snow=snow, mode=mode) #call the model

    if Obj>0:
        A[n_feasible,0:8] = Par
        A[n_feasible,8] = Obj
        Sout_lst[n_feasible, :] = Sout
        n_feasible = n_feasible + 1

np.savetxt(f'{data_folder}\MC2_before.txt',A[0:n_feasible,:], delimiter =',',)

#find the optimum

Opt_obj = A.argmax(axis=0)[8]

#find the optimal parameter set
OptPar = A[Opt_obj, 0:8]
Sout = Sout_lst[Opt_obj, :]
NSE = A[Opt_obj, 8]

return OptPar, Sout, NSE

```

In [12]:

```

OptPar_lst = []
Sout_lst = []
NSE_lst = []
a=0
start = 1980

fig, ax = plt.subplots(5, 2, figsize=(15,15))
plt.tight_layout(h_pad=5, w_pad=3)

for i in range(10):
    end = start + 3

```

```
if (i % 2) == 0:
    OptPar, Sout, NSE = calibration(combined_forcing.loc[str(start):str(end)], 100000, ParMaxn, ParMinn, Sin)
    OptPar_lst.append(OptPar)
    Sout_lst.append(Sout)
    NSE_lst.append(NSE)
    df, Obj, _ = HBVMod(OptPar_lst[a], combined_forcing.loc[str(start):str(end)], Sout_lst[a], 0, snow=True, mode='Test')
    c = 0
    ax[a, c].set_title(f'Calibration, NSE ={Obj:.3f}')
else:
    df, Obj, _ = HBVMod(OptPar_lst[a], combined_forcing.loc[str(start):str(end)], Sout_lst[a], 0, snow=True, mode='Test')
    c = 1
    ax[a, c].set_title(f'Test, NSE ={Obj:.3f}')

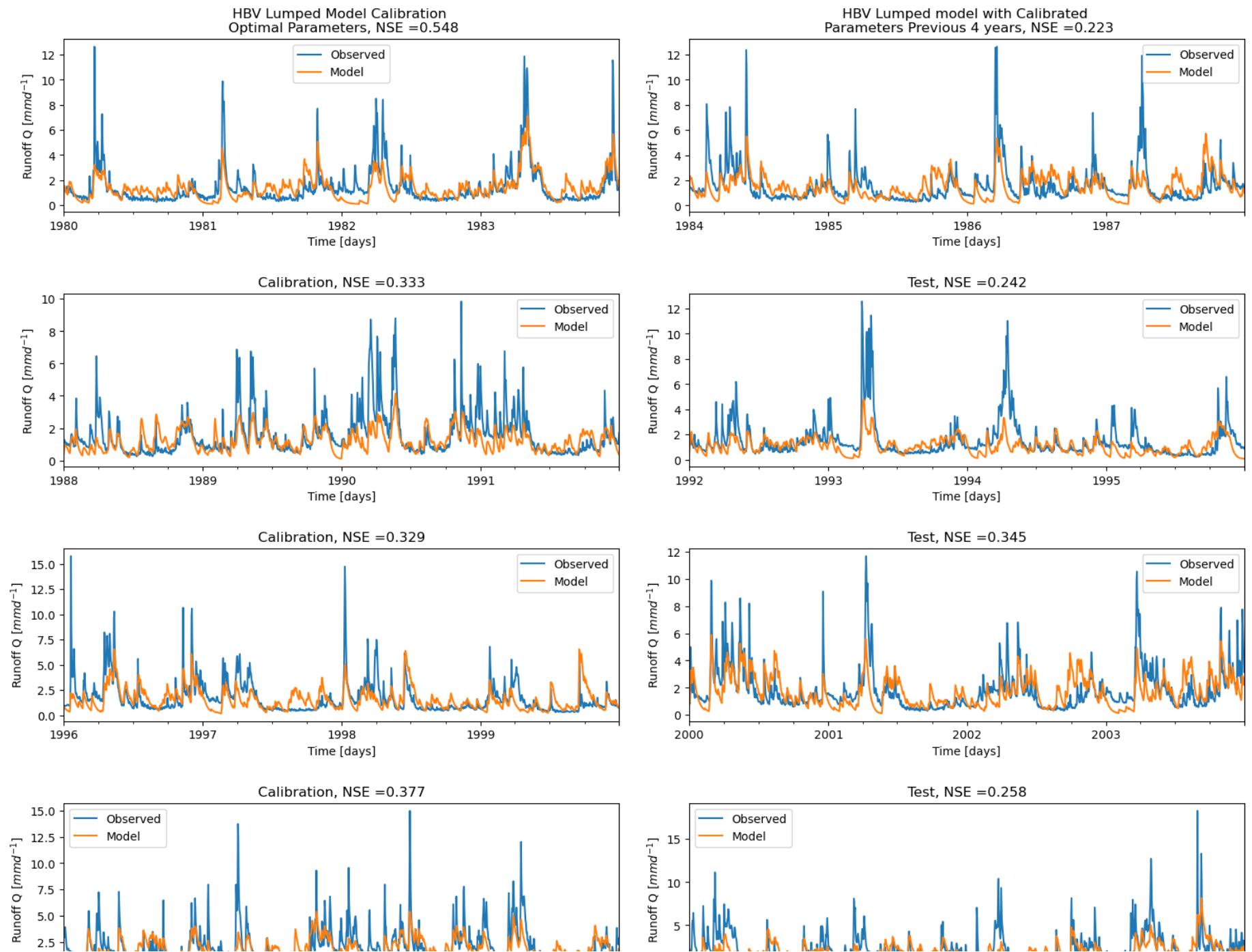
if i == 0:
    ax[a, c].set_title(f'HBV Lumped Model Calibration \n Optimal Parameters, NSE ={Obj:.3f}')
elif i== 1:
    ax[a, c].set_title(f'HBV Lumped model with Calibrated \n Parameters Previous 4 years, NSE ={Obj:.3f}')

df.Q.plot(label='Observed', ax=ax[a, c])
df.Qm.plot(label='Model', ax=ax[a, c])

ax[a, c].set_xlabel('Time [days]')
ax[a, c].set_ylabel('Runoff Q [$mm^3$]')

ax[a, c].legend()
start += 4
if (i % 2) != 0:
    a += 1

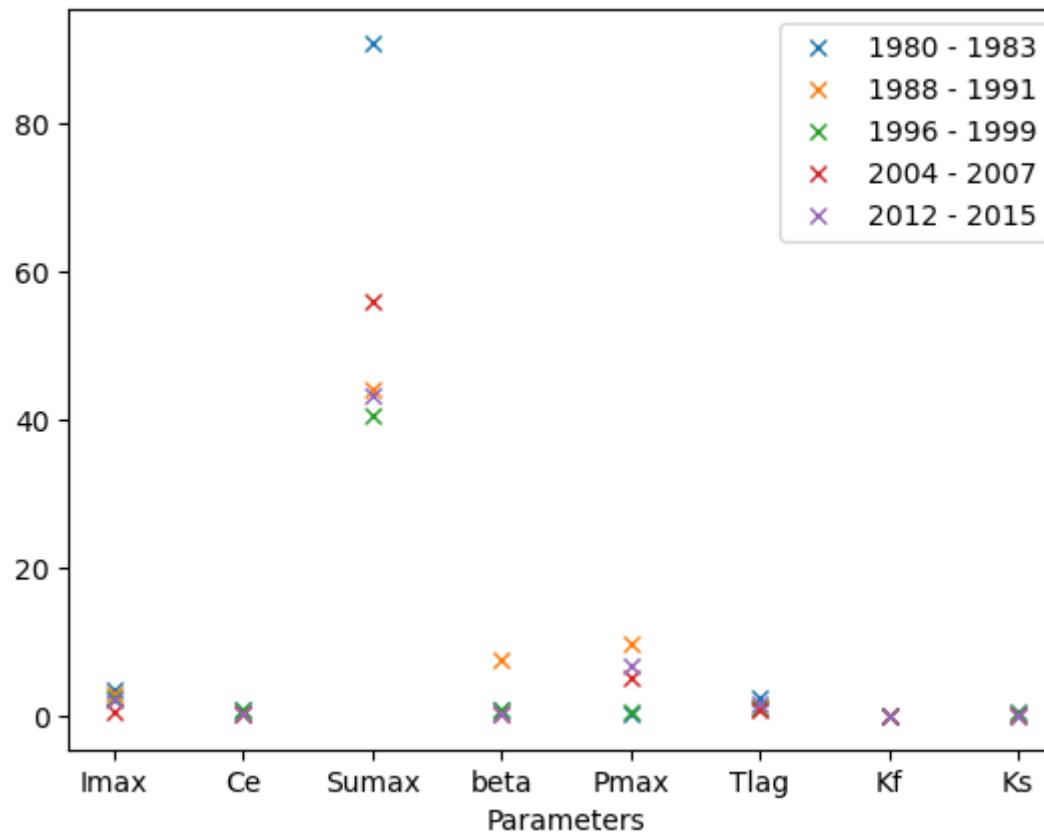
fig.savefig('Figures\\lumped_model.png', bbox_inches='tight')
```



To see how the different optimal parameters for the different sets, a plot is made.

```
In [14]: par = np.array(['Imax' , 'Ce' , 'Sumax' , 'beta', 'Pmax',      'Tlag',      'Kf',   'Ks' ])  
y=0  
  
fig, ax = plt.subplots()  
for i in range(5):  
    ax.plot(par, OptPar_lst[i], 'x', color=f'C{i}', label=f'{str(1980 + y)} - {str(1983 + y)}')  
    y += 8  
ax.legend()  
ax.set_xlabel('Parameters')  
  
ax.set_title('Optimal parameters after 100,000 runs');
```

Optimal parameters after 100,000 runs



If log NSE or sqrt NSE is desired, code below could be used in the HBV model.

```
In [ ]: # Calculate objective

ind    = np.where(Qm>0)
Qm    = Qm[ind]

if Obj_type == "NSE":
    Qo    = Qo[ind]

# in case other obj, use these
elif Obj_type == "NSE_log":
```

```
Qo = np.log(Qo[ind])
Qm = np.log(Qm)

elif Obj_type == "NSE_sqrt":
    Qo      = np.sqrt(Qo[ind])
    Qm      = np.sqrt(Qm)
```

3.4 Distributed model

As a last part, the basin is divided into three different landscape classification (hillslope, wetland and plateau). The HBV model from the previous exercise is adjusted depending on the characteristics of the landscape. For the snow parts, the area is divided into the different elevations as done in 1.4. Calibration is also executed, but this takes a long time and is very uncertain as there are 20 different parameters.

```
In [15]: files = glob.glob(f"{gis_folder}\\*.txt")
# Load files created in qgis
DEM=np.genfromtxt(files[0], dtype=float, autostrip=True)
slope=np.genfromtxt(files[3], dtype=float, autostrip=True)
hand=np.genfromtxt(files[1], dtype=float, autostrip=True)
basin = np.where(DEM >=0, 1, 0) #points inside basin 1, outside 0
```

```
In [16]: fig, ax = plt.subplots(1, 4, figsize=(15,3))
fig.tight_layout()

# plot DEM
ax[0].set_title("DEM")
DEM[DEM==9999]=np.nan # deal with nan values
img0 = ax[0].imshow(DEM, cmap='hsv') # plot
plt.colorbar(img0, ax=ax[0])

#plot HAND
ax[1].set_title("HAND")
hand[hand==9999]=np.nan
img1 = ax[1].imshow(hand, cmap="hsv") # plot
plt.colorbar(img1, ax=ax[1])

#plot slope
```

```
ax[2].set_title("slope")
slope[slope==9999]=np.nan
img2 = ax[2].imshow(slope, cmap="hsv") # plot
plt.colorbar(img2, ax=ax[2])

threshold_h = 90
threshold_s = 20

#make Landscape classification
hillslope = (np.array(slope) > threshold_s) & (np.array(hand) > threshold_h)
plateau = (np.array(hand) > threshold_h) & (np.array(slope) < threshold_s)
wetland = np.array(hand) <= threshold_h
basin = np.array(basin) > 0

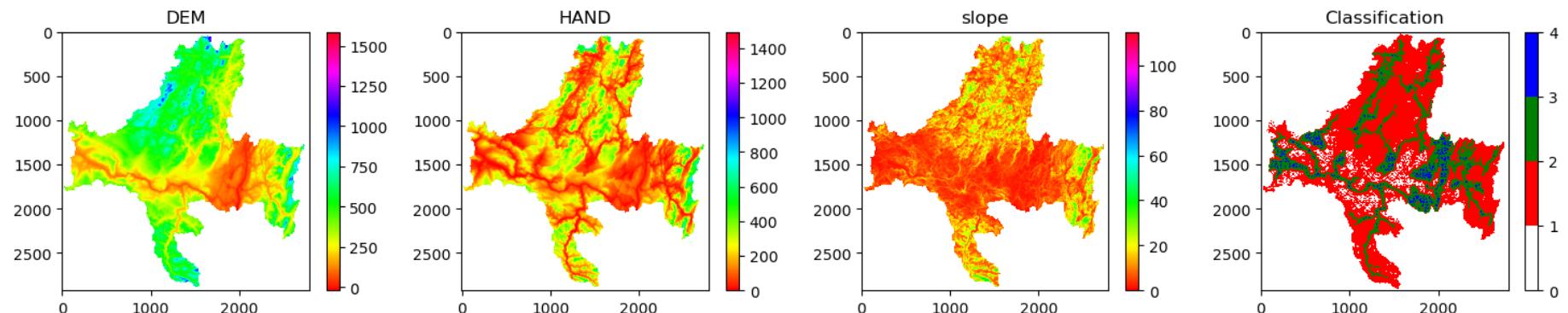
#calculate percentages
hillslope_per = float(np.sum(hillslope)) /np.sum(basin)
wetland_per = float(np.sum(wetland)) /np.sum(basin)
plateau_per = float(np.sum(plateau)) /np.sum(basin)

#landscape percentages
landscape_per= np.array([plateau_per, hillslope_per, wetland_per])

#matrics with Landscape classes
landscapes = np.zeros(DEM.shape)
landscapes[plateau] = 1
landscapes[hillslope] = 2
landscapes[wetland] = 3

#plot Landscapes
ax[3].set_title("Classification")
cmap = mpl.colors.ListedColormap(['white', 'red', 'green', 'blue'])
bounds=[0,1,2,3,4]
norm = mpl.colors.BoundaryNorm(bounds, cmap.N)
img3 = ax[3].imshow(landscapes, cmap=cmap, norm=norm)
plt.colorbar(img3,ax=ax[3])
```

Out[16]: <matplotlib.colorbar.Colorbar at 0x23f26a5d6d0>



```
In [17]: #Divide Landscape areas in different height categories
```

```
A_lst = []
for i in range(1,4):

    A1 = len(DEM[(landscapes==i) & (DEM<=250)]) / len(DEM[(landscapes==i)])
    A2 = len(DEM[(landscapes==i) & (DEM>250) & (DEM <=500)]) / len(DEM[(landscapes==i)])
    A3 = len(DEM[(landscapes==i) & (DEM>500) & (DEM <=750)]) / len(DEM[(landscapes==i)])
    A4 = len(DEM[(landscapes==i) & (DEM>750)]) / len(DEM[(landscapes==i)])

    A_lst.append([A1, A2, A3, A4])

heights = [125, 375, 625, 875] # m
```

```
In [18]: def FLEXtopo(ParPlateau, ParHillslope, ParWetland, ParCatchment, forcing, landscapes, snow=True):
```

```
#parameters and constants
Tlag=ParCatchment[1]
Ks=ParCatchment[0]
dt=1
tmax=len(forcing['P'].values)

#initialize states
States_plateau=np.zeros((tmax,4))
States_hillslope=np.zeros((tmax,4))
States_wetland=np.zeros((tmax,4))
Ss=np.zeros((tmax,1))
```

```

#initialize fluxes
Fluxes_plateau=np.zeros((tmax,4))
Fluxes_hillslope=np.zeros((tmax,4))
Fluxes_wetland=np.zeros((tmax,3))
Qsdt=np.zeros(tmax)
Qtotdt=np.zeros(tmax)

#initialize inbetween snow storages
Snow_A_plateau=np.zeros((tmax,4))
Snow_A_hillslope=np.zeros((tmax,4))
Snow_A_wetland=np.zeros((tmax,4))
#
#Loop over time
for t in range(0,tmax):

    #plateau
    Fluxes_plateau, States_plateau = plateau(t, ParPlateau, forcing, Fluxes_plateau, States_plateau, Snow_A_plateau, A_lst
    #hillslope
    Fluxes_hillslope, States_hillslope = hillslope(t, ParHillslope, forcing, Fluxes_hillslope, States_hillslope, Snow_A_hi

    #wetland
    Fluxes_wetland, States_wetland, Ss = wetland(t, ParWetland, forcing, Fluxes_wetland, States_wetland, Ss, landscapes[2]

    # Slow Reservoir
    Ss[t] = Ss[t] + Fluxes_plateau[t,3] * landscapes[0] + Fluxes_hillslope[t,3] * landscapes[1]
    Qsdt = dt*Ks*Ss[t]
    Ss[t] = Ss[t]-min(Qsdt,Ss[t])
    if t < tmax-1:
        Ss[t+1] = Ss[t]

    Qtotdt[t] = Qsdt + Fluxes_plateau[t,2] * landscapes[0] + Fluxes_hillslope[t,2] * landscapes[1] +   Fluxes_wetland[t, 2

    # Offset Q
    Weigths=Weigfun(Tlag)

    Qm = np.convolve(Qtotdt,Weigths)
    Qm = Qm[0:tmax]

```

```
    return(Qm)
```

```
In [19]: def hillslope(timestep, Par, forcing, Fluxes, States, Ssnow_A, A_lst, snow):
    #HBVpareto Calculates values of 3 objective functions for HBV model

    Imax=Par[0]
    Ce=Par[1]
    Sumax=Par[2]
    beta=Par[3]
    D=Par[4]
    Kf=Par[5]

    Prec = forcing['P'].values
    Qo = forcing['Q'].values
    Etp = forcing['Pev'].values
    temp = forcing['T'].values
    Psnow = np.zeros(len(Prec))
    Pldt = np.zeros(len(Prec))

    tmax=len(Prec)

    Si = States[:,0]
    Su = States[:,1]
    Sf = States[:,2]
    Ssnow = States[:,3]

    Eidt = Fluxes[:,0]
    Eadt = Fluxes[:,1]
    Qfdt = Fluxes[:,2]
    Qusdt = Fluxes[:,3]

    dt = 1
    t = timestep

    Er = 331 #m
    Tt = -0.5 # degc
    FM = 3.8    # mm/deg/d
```

```

Epdt = Etp[t] * dt
TR   = temp[t] * dt

Pldt_A_lst = []
Ssnow_lst = []

if snow:
    for A_index, Ei in enumerate(heights):

        Ti = TR - 0.6 * (Ei-Er) / 100

        if Ti < Tt and t != 0:
            Pdt              = 0                                # no rainfall
            Ps               = Prec[t] * dt                      # precipitation is snow
            M                = 0                                # Too cold for melt
            Ssnow_A[t, A_index] = Ssnow_A[t-1, A_index] + Ps  # add snow to the prev day
            Pldt_A           = 0                                # no outflow as too cold

        # then must be above
        else:
            Pdt              = Prec[t] * dt                  # all precip is rainfall
            Ps               = 0                                # no snow
            M                = min(Ssnow_A[t-1, A_index] / dt, FM * (Ti - Tt))  # calculate melt
            Ssnow_A[t, A_index] = Ssnow_A[t-1, A_index] - M * dt  # remove melted snow
            Pldt_A           = M                                # outflow = melt

        fi = A_lst[A_index]
        Pldt_A_lst.append(Pldt_A * fi)
        Ssnow_lst.append(Ssnow_A[t, A_index] * fi)

    Pldt[t] = np.sum(Pldt_A_lst)
    Ssnow[t] = np.sum(Ssnow_lst)

    if t < tmax-1:
        Ssnow[t+1] = Ssnow[t]

else:
    Pdt  = Prec[t] * dt
    Pldt[t] = 0
    Ps   = 0

```

```
# Interception Reservoir
if Pdt>0:
    Si[t]=Si[t]+Pdt
    Pedt=max(0,Si[t]-Imax) + Pldt[t]
    Si[t]=Si[t]-Pedt
    Eidt[t]=0
else:
    # Evaporation only when there is no rainfall
    Pedt= Pldt[t]
    Eidt[t]=min(Epdt,Si[t])
    Si[t]=Si[t]-Eidt[t]

if t<tmax-1:
    Si[t+1]=Si[t]

# Unsaturated Reservoir
if Pedt>0:
    rho = (Su[t] / Sumax) ** beta
    Su[t] = Su[t] + (1-rho) * Pedt
    Qufdt = rho*Pedt
else:
    Qufdt=0

# Transpiration
Epdt=max(0,Epdt-Eidt[t])
Eadt[t]=Epdt*(Su[t]/(Sumax*Ce))
Eadt[t]=min(Eadt[t],Su[t])
Su[t]=Su[t]-Eadt[t]

# Preferential Percolation

Qusdt = max(0, (Su[t]/Sumax) * D * dt - Sumax)
Su[t] = Su[t] - Qusdt

if t<tmax-1:
```

```

Su[t+1]=Su[t]

# Fast Reservoir
Sf[t] = Sf[t] + (1-D) * Qufdt * dt
Qfdt[t] = dt*Kf*Sf[t]
Sf[t]=Sf[t] - min(Qfdt[t],Sf[t])

if t<tmax-1:
    Sf[t+1]=Sf[t]

Psnow[i] = Ps

#save output
States[:,0] = Si
States[:,1] = Su
States[:,2] = Sf
States[:,3] = Ssnow

Fluxes[:,0] = Eidt
Fluxes[:,1] = Eadt
Fluxes[:,2] = Qfdt
Fluxes[:,3] = Qusdt

return(Fluxes, States)

```

In [20]:

```

def plateau( timestep, Par, forcing, Fluxes, States, Ssnow_A, A_lst, snow):
    #HBVpareto Calculates values of 3 objective functions for HBV model

    Imax=Par[0]
    Ce=Par[1]
    Sumax=Par[2]
    beta=Par[3]
    Pmax=Par[4]
    Kf=Par[5]

    Prec = forcing['P'].values
    Qo = forcing['Q'].values
    Etp = forcing['Pev'].values
    temp = forcing['T'].values

```

```

Psnow = np.zeros(len(Prec))
Pldt = np.zeros(len(Prec))

tmax=len(Prec)
Si=States[:,0]
Su=States[:,1]
Sf=States[:,2]
Ssnow = States[:,3]

Eidt=Fluxes[:,0]
Eadt=Fluxes[:,1]
Qfdt=Fluxes[:,2]
Qusdt=Fluxes[:,3]

dt=1
t=timestep

Er = 331 #m
Tt = -0.5 # degc
FM = 3.8 # mm/deg/d

Epdt = Etp[t] * dt
TR = temp[t] * dt

Pldt_A_lst = []
Ssnow_lst = []

if snow:
    for A_index, Ei in enumerate(heights):

        Ti = TR - 0.6 * (Ei-Er) / 100

        if Ti < Tt and t != 0:
            Pdt = 0 # no rainfall
            Ps = Prec[t] * dt # precipitation is snow
            M = 0 # Too cold for melt
            Ssnow_A[t, A_index] = Ssnow_A[t-1, A_index] + Ps # add snow to the prev day
            Pldt_A = 0 # no outflow as too cold
            # then must be above

```

```

else:
    Pdt = Prec[t] * dt
    Ps = 0
    M = min(Ssnow_A[t-1, A_index] / dt, FM * (Ti - Tt))
    Ssnow_A[t, A_index] = Ssnow_A[t-1, A_index] - M * dt
    Pldt_A = M

    fi = A_lst[A_index]
    Pldt_A_lst.append(Pldt_A * fi)
    Ssnow_lst.append(Ssnow_A[t, A_index] * fi)

    Pldt[t] = np.sum(Pldt_A_lst)
    Ssnow[t] = np.sum(Ssnow_lst)

    if t < tmax-1:
        Ssnow[t+1] = Ssnow[t]

else:
    Pdt = Prec[t] * dt
    Pldt[t] = 0
    Ps = 0

# Interception Reservoir
if Pdt>0:
    Si[t]=Si[t]+Pdt
    Pedt=max(0,Si[t]-Imax) + Pldt[t]
    Si[t]=Si[t]-Pedt
    Eidt[t]=0
else:
# Evaporation only when there is no rainfall
    Pedt= Pldt[t]
    Eidt[t]=min(Epd, Si[t])
    Si[t] = Si[t]-Eidt[t]

if t<tmax-1:
    Si[t+1]=Si[t]

# Unsaturated Reservoir
if Pedt>0:

```

```
rho = (Su[t] / Sumax) ** beta
Su[t] = Su[t] + (1-rho) * Pedt
Qufdt = rho*Pedt
else:
    Qufdt=0

# Transpiration
Epdt=max(0,Epdt-Eidt[t])
Eadt[t]=Epdt*(Su[t]/(Sumax*Ce))
Eadt[t]=min(Eadt[t],Su[t])
Su[t]=Su[t]-Eadt[t]

# Percolation
Qusdt=(Su[t]/Sumax)*Pmax*dt
Su[t]=Su[t]-min(Qusdt,Su[t])
if t<tmax-1:
    Su[t+1]=Su[t]

# Fast Reservoir
Sf[t]=Sf[t]+Qufdt
Qfdt[t]= dt*Kf*Sf[t]
Sf[t]=Sf[t]-min(Qfdt[t],Sf[t])
if t<tmax-1:
    Sf[t+1]=Sf[t]

Psnow[i] = Ps

#save output
States[:,0] = Si
States[:,1] = Su
States[:,2] = Sf
States[:,3] = Ssnow

Fluxes[:,0]=Eidt
Fluxes[:,1]=Eadt
Fluxes[:,2]=Qfdt
Fluxes[:,3]=Qusdt
```

```
    return(Fluxes, States)
```

```
In [21]: def wetland( timestep, Par, forcing, Fluxes, States, Ss, landscape_per, Ssnow_A, A_lst, snow):
    #HBVpareto Calculates values of 3 objective functions for HBV model

    Imax=Par[0]
    Ce=Par[1]
    Sumax=Par[2]
    beta=Par[3]
    Cmax=Par[4]
    Kf=Par[5]

    Prec = forcing['P'].values
    Qo = forcing['Q'].values
    Etp = forcing['Pev'].values
    temp = forcing['T'].values
    Psnow = np.zeros(len(Prec))
    Pldt = np.zeros(len(Prec))

    tmax=len(Prec)

    Si=States[:,0]
    Su=States[:,1]
    Sf=States[:,2]
    Ssnow = States[:,3]

    Eidt=Fluxes[:,0]
    Eadt=Fluxes[:,1]
    Qfdt=Fluxes[:,2]

    dt=1
    t=timestep
    Er = 331 #m
    Tt = -0.5 # degc
    FM = 3.8    # mm/deg/d

    Epdt = Etp[t] * dt
    TR    = temp[t] * dt
```

```

Pldt_A_lst = []
Ssnow_lst = []
if snow:
    for A_index, Ei in enumerate(heights):

        Ti = TR - 0.6 * (Ei-Er) / 100

        if Ti < Tt and t != 0:
            Pdt = 0
            Ps = Prec[t] * dt
            M = 0
            Ssnow_A[t, A_index] = Ssnow_A[t-1, A_index] + Ps
            Pldt_A = 0
            # then must be above
        else:
            Pdt = Prec[t] * dt
            Ps = 0
            M = min(Ssnow_A[t-1, A_index] / dt, FM * (Ti - Tt))
            Ssnow_A[t, A_index] = Ssnow_A[t-1, A_index] - M * dt
            Pldt_A = M
            # all precip is rainfall
            # no snow
            # calculate melt
            # remove melted snow
            # outflow = melt

        fi = A_lst[A_index]
        Pldt_A_lst.append(Pldt_A * fi)
        Ssnow_lst.append(Ssnow_A[t, A_index] * fi)

    Pldt[t] = np.sum(Pldt_A_lst)
    Ssnow[t] = np.sum(Ssnow_lst)

    if t < tmax-1:
        Ssnow[t+1] = Ssnow[t]

else:
    Pdt = Prec[t] * dt
    Pldt[t] = 0
    Ps = 0
    # Interception Reservoir

```

```

if Pdt>0:
    Si[t]=Si[t]+Pdt
    Pedt=max(0,Si[t]-Imax) + Pldt[t]
    Si[t]=Si[t]-Pedt
    Eidt[t]=0
else:
# Evaporation only when there is no rainfall
    Pedt=0 + Pldt[t]
    Eidt[t]=min(Epdt,Si[t])
    Si[t]=Si[t]-Eidt[t]

if t<tmax-1:
    Si[t+1]=Si[t]

# Unsaturated Reservoir
if Pedt>0:
    rho=(Su[t]/Sumax)**beta
    Su[t]=Su[t]+(1-rho)*Pedt
    Qufdt=rho*Pedt
else:
    Qufdt=0

# Transpiration
Epdt=max(0,Epdt-Eidt[t])
Eadt[t]=Epdt*(Su[t]/(Sumax*Ce))
Eadt[t]=min(Eadt[t],Su[t])
Su[t]=Su[t]-Eadt[t]

#Capillary rise
Qrdt= (1 - Su[t]/Sumax) * Cmax * dt

#check if the groundwater has enough water (note: you need to use the Landscape percentage!!!)
Qrdt = min(Qrdt, landscape_per * Ss[t])

# su cannot be more than sumax
if( (Su[t] + Qrdt) > Sumax):
    Qrdt = Sumax - Su[t]

Su[t] = Su[t] + Qrdt * landscape_per
Ss[t] = Ss[t] - Qrdt * landscape_per # * Landscape_per

```

```

if t<tmax-1:
    Su[t+1]=Su[t]

Psnow[i] = Ps

# Fast Reservoir
Sf[t]=Sf[t]+Qufdt
Qfdt[t]= dt*Kf*Sf[t]
Sf[t]=Sf[t]-min(Qfdt[t],Sf[t])
if t<tmax-1:
    Sf[t+1]=Sf[t]

#save output
States[:,0] = Si
States[:,1] = Su
States[:,2] = Sf
States[:,3] = Ssnow

Fluxes[:,0]=Eidt
Fluxes[:,1]=Eadt
Fluxes[:,2]=Qfdt

return(Fluxes, States, Ss)

```

```
In [22]: df_data_comb_before = combined_forcing.loc[:'2000']
        df_data_comb_after = combined_forcing.loc['2000':]
```

```
In [26]: # GLUE
nmax = 1000
A = np.zeros((nmax,21))
n_feasible = 0

ParMinn = np.array([ 0.10,    0.1,   10,      .2,     .1,  0.0001,
                    1.10,    0.1,  10.0,     .2,  0.01,  0.01,
                   0.01,     .1,   10,     .2,  0.01,  0.0001,
                  0.0001,   .001])
ParMaxn = np.array([5,    1.0,   600,    10.0,   4.0,  .50,
                    8.00,   1.0, 100.0,   10.0,   4.0,   1.00,
```

```

    1.5,   1.0,   40, 10.0,  5.00, 0.40,
    1.000, 10])

for n in range(1,nmax):
    Rnum = np.random.random(20) #generate a vector of random number
    Par = Rnum * (ParMaxn - ParMinn) + ParMinn # calculate the random parameter set

    Qm = FLEXtopo(Par[0:6], Par[6:12], Par[12:18], Par[18:20], df_data_comb_before, landscape_per, snow=True)
    Qo = df_data_comb_before['Q'].values

    ind = np.where(Qo>=0)
    QoAv = np.mean(Qo[ind])
    ErrUp = np.sum((Qo - Qm) ** 2)
    ErrDo = np.sum((Qo - QoAv) ** 2)
    Obj = 1 - (ErrUp / ErrDo)

    if Obj>0:
        A[n_feasible,0:20]= Par
        A[n_feasible,20] = Obj
        n_feasible = n_feasible + 1

np.savetxt(f'{data_folder}\MC2_distributed.txt',A[0:n_feasible,:], delimiter = ',')

#find the optimum

Opt_obj = A.argmax(axis=0)[20]

#find the optimal parameter set
OptPar = A[Opt_obj, 0:20]

```

In [27]:

```

Qm = FLEXtopo(OptPar[0:6], OptPar[6:12], OptPar[12:18], OptPar[18:20], df_data_comb_before, landscape_per, snow=True)
Qo = df_data_comb_before['Q'].values

ind = np.where(Qm>=0)

```

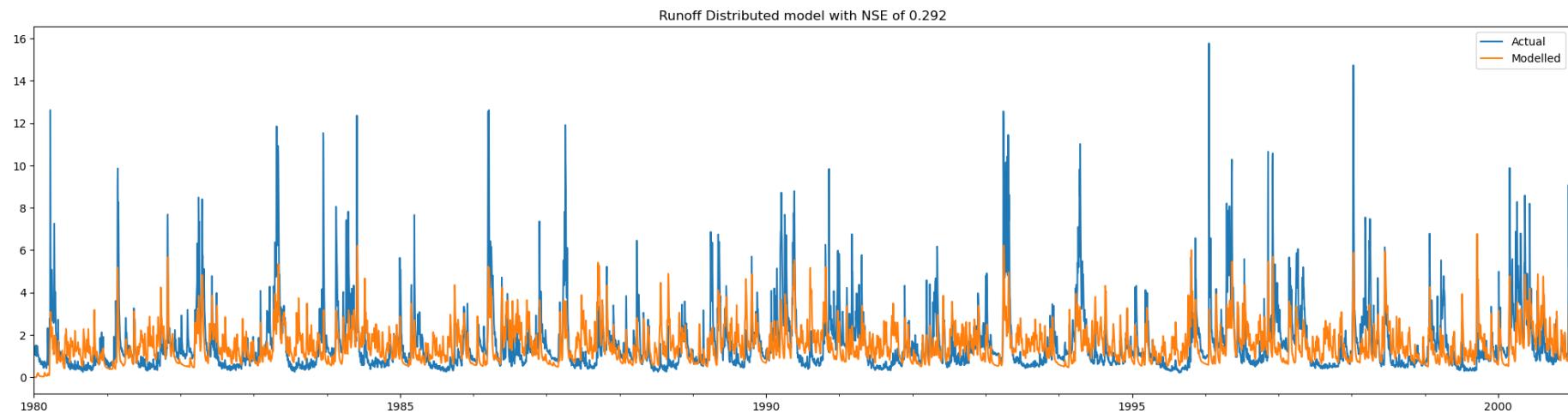
```
QoAv = np.mean(Qo[ind])
ErrUp = np.sum((Qo - Qm) ** 2)
ErrDo = np.sum((Qo - QoAv) ** 2)
Obj = 1 - (ErrUp / ErrDo)

Obj_check = A[Opt_obj, 20]

Qo = df_data_comb_before['Q']
df_data_comb_before.loc[:, 'Qm'] = Qm.tolist()

fig, ax = plt.subplots(figsize=(25,6))
Qo.plot(ax=ax, label='Actual')
df_data_comb_before.Qm.plot(ax=ax, label='Modelled')
ax.set_title(f'Runoff Distributed model with NSE of {Obj:.3f}')
ax.legend()
```

Out[27]: <matplotlib.legend.Legend at 0x23f2a8d4a10>



The data length and dates can be adjusted, so different times can be modelled.

In []: