User Documentation for IDA v2.4.0

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Chapter 1

Introduction

IDA is part of a software family called SUNDIALS: SUite of Nonlinear and DIfferential/ALgebraic equation Solvers [12]. This suite consists of CVODE, KINSOL, and IDA, and variants of these with sensitivity analysis capabilities.

IDA is a general purpose solver for the initial value problem for systems of differential-algebraic equations (DAEs). The name IDA stands for Implicit Differential-Algebraic solver. IDA is based on DASPK [3, 4], but is written in ANSI-standard C rather than FORTRAN77. Its most notable feature is that, in the solution of the underlying nonlinear system at each time step, it offers a choice of Newton/direct methods and a choice of Inexact Newton/Krylov (iterative) methods. Thus IDA shares significant modules previously written within CASC at LLNL to support the ordinary differential equation (ODE) solvers CVODE [14, 8] and PVODE [6, 7], and also the nonlinear system solver KINSOL [9].

The Newton/Krylov methods in IDA are: the GMRES (Generalized Minimal RESidual) [16], Bi-CGStab (Bi-Conjugate Gradient Stabilized) [17], and TFQMR (Transpose-Free Quasi-Minimal Residual) linear iterative methods [10]. As Krylov methods, these require almost no matrix storage for solving the Newton equations as compared to direct methods. However, the algorithms allow for a user-supplied preconditioner matrix, and for most problems preconditioning is essential for an efficient solution.

For very large DAE systems, the Krylov methods are preferable over direct linear solver methods, and are often the only feasible choice. Among the three Krylov methods in IDA, we recommend GMRES as the best overall choice. However, users are encouraged to compare all three, especially if encountering convergence failures with GMRES. Bi-CGFStab and TFQMR have an advantage in storage requirements, in that the number of workspace vectors they require is fixed, while that number for GMRES depends on the desired Krylov subspace size.

There are several motivations for choosing the C language for IDA. First, a general movement away from FORTRAN and toward C in scientific computing is apparent. Second, the pointer, structure, and dynamic memory allocation features in C are extremely useful in software of this complexity, with the great variety of method options offered. Finally, we prefer C over C++ for IDA because of the wider availability of C compilers, the potentially greater efficiency of C, and the greater ease of interfacing the solver to applications written in extended FORTRAN.

1.1 Changes from previous versions

Changes in v2.4.0

FIDA, a FORTRAN-C interface module, was added (for details see Chapter 6).

IDASPBCG and IDASPTFQMR modules have been added to interface with the Scaled Preconditioned Bi-CGstab (SPBCG) and Scaled Preconditioned Transpose-Free Quasi-Minimal Residual (SPTFQMR) linear solver modules, respectively (for details see Chapter 5). At the same time, function type names

2 Introduction

for Scaled Preconditioned Iterative Linear Solvers were added for the user-supplied Jacobian-timesvector and preconditioner setup and solve functions.

The rootfinding feature was added, whereby the roots of a set of given functions may be computed during the integration of the DAE system.

A user-callable routine was added to access the estimated local error vector.

The deallocation functions now take as arguments the address of the respective memory block pointer.

To reduce the possibility of conflicts, the names of all header files have been changed by adding unique prefixes (ida_ and sundials_). When using the default installation procedure, the header files are exported under various subdirectories of the target include directory. For more details see §2.

Changes in v2.3.0

The user interface has been further refined. Several functions used for setting optional inputs were combined into a single one. An optional user-supplied routine for setting the error weight vector was added. Additionally, to resolve potential variable scope issues, all SUNDIALS solvers release user data right after its use. The build systems has been further improved to make it more robust.

Changes in v2.2.2

Minor corrections and improvements were made to the build system. A new chapter in the User Guide was added — with constants that appear in the user interface.

Changes in v2.2.1

The changes in this minor SUNDIALS release affect only the build system.

Changes in v2.2.0

The major changes from the previous version involve a redesign of the user interface across the entire SUNDIALS suite. We have eliminated the mechanism of providing optional inputs and extracting optional statistics from the solver through the iopt and ropt arrays. Instead, IDA now provides a set of routines (with prefix IDASet) to change the default values for various quantities controlling the solver and a set of extraction routines (with prefix IDAGet) to extract statistics after return from the main solver routine. Similarly, each linear solver module provides its own set of Set- and Get-type routines. For more details see §5.5.6 and §5.5.8.

Additionally, the interfaces to several user-supplied routines (such as those providing Jacobians and preconditioner information) were simplified by reducing the number of arguments. The same information that was previously accessible through such arguments can now be obtained through Get-type functions.

Installation of IDA (and all of SUNDIALS) has been completely redesigned and is now based on configure scripts.

1.2 Reading this User Guide

The structure of this document is as follows:

- In Chapter 2 we begin with instructions for the installation of IDA, within the structure of SUNDIALS.
- In Chapter 3, we give short descriptions of the numerical methods implemented by IDA for the solution of initial value problems for systems of DAEs.
- The following chapter describes the structure of the SUNDIALS suite of solvers (§4.1) and the software organization of the IDA solver (§4.2).

- Chapter 5 is the main usage document for IDA for C applications. It includes a complete description of the user interface for the integration of DAE initial value problems.
- In Chapter 6, we describe FIDA, an interface module for the use of IDA with FORTRAN applications.
- Chapter 7 gives a brief overview of the generic NVECTOR module shared among the various components of SUNDIALS, as well as details on the two NVECTOR implementations provided with SUNDIALS: a serial implementation (§7.1) and a parallel MPI implementation (§7.2).
- Chapter 8 describes the interfaces to the linear solver modules, so that a user can provide his/her own such module.
- Chapter 9 describes in detail the generic linear solvers shared by all SUNDIALS solvers.
- Finally, Chapter 10 lists the constants used for input to and output from IDA.

Finally, the reader should be aware of the following notational conventions in this user guide: program listings and identifiers (such as IDAMalloc) within textual explanations appear in typewriter type style; fields in C structures (such as *content*) appear in italics; and packages or modules, such as IDADENSE, are written in all capitals. In the Index, page numbers that appear in bold indicate the main reference for that entry.

Acknowledgments. We wish to acknowledge the contributions to previous versions of the IDA code and user guide of Allan G. Taylor.

Chapter 2

IDA Installation Procedure

The installation of IDA is accomplished by installing the SUNDIALS suite as a whole, according to the instructions that follow. The same procedure applies whether or not the downloaded file contains solvers other than IDA.¹

Generally speaking, the installation procedure outlined in §2.1 below will work on commodity LINUX/UNIX systems without modification. Users are still encouraged, however, to carefully read the entire chapter before attempting to install the SUNDIALS suite, in case non-default choices are desired for compilers, compilation options, or the like. In lieu of reading the option list below, the user may invoke the configuration script with the help flag to view a complete listing of available options, which may be done by issuing

% ./configure --help

from within the sundials directory.

In the descriptions below, build_tree refers to the directory under which the user wants to build and/or install the SUNDIALS package. By default, the SUNDIALS libraries and header files are installed under the subdirectories build_tree/lib and build_tree/include, respectively. Also, source_tree refers to the directory where the SUNDIALS source code is located. The chosen build_tree may be different from the source_tree, thus allowing for multiple installations of the SUNDIALS suite with different configuration options.

Concerning the installation procedure outlined below, after invoking the tar command with the appropriate options, the contents of the SUNDIALS archive (or the *source_tree*) will be extracted to a directory named sundials. Since the name of the extracted directory is not version-specific it is recommended that the user refrain from extracting the archive to a directory containing a previous version/release of the SUNDIALS suite. If the user is only upgrading and the previous installation of SUNDIALS is not needed, then the user may remove the previous installation by issuing

% rm -rf sundials

from a shell command prompt.

Even though the installation procedure given below presupposes that the user will use the default vector modules supplied with the distribution, using the SUNDIALS suite with a user-supplied vector module normally will not require any changes to the build procedure.

2.1 Installation steps

To install the SUNDIALS suite, given a downloaded file named *sundials_file.tar.gz*, issue the following commands from a shell command prompt, while within the directory where *source_tree* is to be located.

¹Files for both the serial and parallel versions of IDA are included in the distribution. For users in a serial computing environment, the files specific to parallel environments (which may be deleted) are as follows: all files in nvec.par/; ida_bbdpre.c, ida_bbdpre.impl.h (in ida/source/); ida/include/ida_bbdpre.h; fidabbd.c, fidabbd.h (in ida/fcmix/); all files in ida/examples_par/; all files in ida/fcmix/examples_par/. (By "serial version" of IDA we mean the IDA solver with the serial NVECTOR module attached, and similarly for "parallel version".)

```
    gunzip sundials_file.tar.gz
    tar -xf sundials_file.tar [creates sundials directory]
    cd build_tree
    path_to_source_tree/configure options [options can be absent]
    make
    make install
    make examples
    If system storage space conservation is a priority, then issue make clean and/or make examples_clean
```

from a shell command prompt to remove unneeded object files.

2.2 Configuration options

The installation procedure given above will generally work without modification; however, if the system includes multiple MPI implementations, then certain configure script-related options may be used to indicate which MPI implementation should be used. Also, if the user wants to use non-default language compilers, then, again, the necessary shell environment variables must be appropriately redefined. The remainder of this section provides explanations of available configure script options.

General options

--prefix=PREFIX

Location for architecture-independent files.

Default: PREFIX=build_tree

--includedir=DIR

Alternate location for installation of header files.

Default: DIR=PREFIX/include

--libdir=DIR

Alternate location for installation of libraries.

Default: DIR=PREFIX/lib

--disable-examples

All available example programs are automatically built unless this option is given. The example executables are stored under the following subdirectories of the associated solver:

```
build_tree/solver/examples_ser : serial C examples
build_tree/solver/examples_par : parallel C examples (MPI-enabled)
build_tree/solver/fcmix/examples_ser: serial FORTRAN examples
build_tree/solver/fcmix/examples_par: parallel FORTRAN examples (MPI-enabled)
```

Note: Some of these subdirectories may not exist depending upon the solver and/or the configuration options given.

--disable-solver

Although each existing solver module is built by default, support for a given solver can be explicitly disabled using this option. The valid values for *solver* are: cvode, cvodes, ida, and kinsol.

--with-cppflags=ARG

Specify additional C preprocessor flags (e.g., ARG=-I<include_dir> if necessary header files are located in nonstandard locations).

--with-cflags=ARG

Specify additional C compilation flags.

--with-ldflags=ARG

Specify additional linker flags (e.g., ARG=-L<lib_dir> if required libraries are located in nonstandard locations).

--with-libs=ARG

Specify additional libraries to be used (e.g., ARG=-1<foo> to link with the library named libfoo.a or libfoo.so).

--with-precision=ARG

By default, SUNDIALS will define a real number (internally referred to as realtype) to be a double-precision floating-point numeric data type (double C-type); however, this option may be used to build SUNDIALS with realtype alternatively defined as a single-precision floating-point numeric data type (float C-type) if ARG=single, or as a long double C-type if ARG=extended.

Default: ARG=double

Users should *not* build SUNDIALS with support for single-precision floating-point arithmetic on 32- or 64-bit systems. This will almost certainly result in unreliable numerical solutions. The configuration option --with-precision=single is intended for systems on which single-precision arithmetic involves at least 14 decimal digits.

Options for Fortran support

--disable-f77

Using this option will disable all FORTRAN support. The FCVODE, FKINSOL, FIDA, and FNVECTOR modules will not be built, regardless of availability.

--with-fflags=ARG

Specify additional FORTRAN compilation flags.

The configuration script will attempt to automatically determine the function name mangling scheme required by the specified FORTRAN compiler, but the following two options may be used to override the default behavior.

--with-f77underscore=ARG

This option pertains to the FCVODE, FKINSOL, FIDA, and FNVECTOR FORTRAN-C interface modules and is used to specify the number of underscores to append to function names so FORTRAN routines can properly link with the associated SUNDIALS libraries. Valid values for ARG are: none, one and two.

Default: ARG=one



--with-f77case=ARG

Use this option to specify whether the external names of the FCVODE, FKINSOL, FIDA, and FNVECTOR FORTRAN-C interface functions should be lowercase or uppercase so FORTRAN routines can properly link with the associated SUNDIALS libraries. Valid values for ARG are: lower and upper.

Default: ARG=lower

Options for MPI support

The following configuration options are only applicable to the parallel SUNDIALS packages:

--disable-mpi

Using this option will completely disable MPI support.

--with-mpicc=ARG

--with-mpif77=ARG

By default, the configuration utility script will use the MPI compiler scripts named mpicc and mpif77 to compile the parallelized SUNDIALS subroutines; however, for reasons of compatibility, different executable names may be specified via the above options. Also, ARG=no can be used to disable the use of MPI compiler scripts, thus causing the serial C and FORTRAN compilers to be used to compile the parallelized SUNDIALS functions and examples.

--with-mpi-root=MPIDIR

This option may be used to specify which MPI implementation should be used. The SUNDIALS configuration script will automatically check under the subdirectories MPIDIR/include and MPIDIR/lib for the necessary header files and libraries. The subdirectory MPIDIR/bin will also be searched for the C and FORTRAN MPI compiler scripts, unless the user uses --with-mpicc=no or --with-mpif77=no.

- --with-mpi-incdir=INCDIR
- --with-mpi-libdir=LIBDIR
- --with-mpi-libs=LIBS

These options may be used if the user would prefer not to use a preexisting MPI compiler script, but instead would rather use a serial complier and provide the flags necessary to compile the MPI-aware subroutines in SUNDIALS.

Often an MPI implementation will have unique library names and so it may be necessary to specify the appropriate libraries to use (e.g., LIBS=-lmpich).

Default: INCDIR=MPIDIR/include and LIBDIR=MPIDIR/lib

--with-mpi-flags=ARG

Specify additional MPI-specific flags.

Options for library support

By default, only static libraries are built, but the following option may be used to build shared libraries on supported platforms.

--enable-shared

Using this particular option will result in both static and shared versions of the available SUNDIALS libraries being built if the system supports shared libraries. To build only shared libraries also specify --disable-static.

Note: The FCVODE, FKINSOL, and FIDA libraries can only be built as static libraries because they contain references to externally defined symbols, namely user-supplied FORTRAN subroutines. Although the FORTRAN interfaces to the serial and parallel implementations of the supplied NVECTOR module do not contain any unresolvable external symbols, the libraries are still built as static libraries for the purpose of consistency.

Environment variables

The following environment variables can be locally (re)defined for use during the configuration of SUNDIALS. See the next section for illustrations of these.

CC

F77

Since the configuration script uses the first C and FORTRAN compilers found in the current executable search path, then each relevant shell variable (CC and F77) must be locally (re)defined in order to use a different compiler. For example, to use xcc (executable name of chosen compiler) as the C language compiler, use CC=xcc in the configure step.

CFLAGS

FFLAGS

Use these environment variables to override the default C and FORTRAN compilation flags.

2.3 Configuration examples

The following examples are meant to help demonstrate proper usage of the configure options:

The above example builds SUNDIALS using gcc as the serial C compiler, g77 as the serial FORTRAN compiler, mpicc as the parallel C compiler, mpif77 as the parallel FORTRAN compiler, and appends the -g3 compilaton flag to the list of default flags.

This example again builds SUNDIALS using gcc as the serial C compiler, but the --with-mpicc=no option explicitly disables the use of the corresponding MPI compiler script. In addition, since the --with-mpi-root option is given, the compilation flags -I/usr/apps/mpich/1.2.4/include and -L/usr/apps/mpich/1.2.4/lib are passed to gcc when compiling the MPI-enabled functions. The --disable-examples option disables the examples (which means a FORTRAN compiler is not required). The --with-mpi-libs option is required so that the configure script can check if gcc can link with the appropriate MPI library.

2.4 Installed libraries and exported header files

Using the standard SUNDIALS build system, the command

```
% make install
```

will install the libraries under *libdir* and the public header files under *incdir*. The default values for these directories are *build_tree/lib* and *build_tree/include*, respectively, but can be changed using the configure script options --prefix, --includedir and --libdir (see §2.2). For example, a global installation of SUNDIALS on a *NIX system could be accomplished using

% configure --prefix=/usr/local

Although all installed libraries reside under *libdir*, the public header files are further organized into subdirectories under *incdir*.

The installed libraries and exported header files are listed for reference in Table 2.1. The file extension .lib is typically .so for shared libraries and .a for static libraries (see *Options for library support* for additional details).

A typical user program need not explicitly include any of the shared SUNDIALS header files from under the *incdir*/sundials directory since they are explicitly included by the appropriate solver header files (e.g., cvode_dense.h includes sundials_dense.h). However, it is both legal and safe to do so (e.g., the functions declared in sundials_smalldense.h could be used in building a preconditioner).

2.5 Building SUNDIALS without the configure script

If the configure script cannot be used (e.g., when building SUNDIALS under Microsoft Windows without using Cygwin), or if the user prefers to own the build process (e.g., when SUNDIALS is incorporated into a larger project with its own build system), then the header and source files for a given module can be copied from the source_tree to some other location and compiled separately.

The following files are required to compile a SUNDIALS solver module:

- public header files located under source_tree/solver/include
- implementation header files and source files located under source_tree/solver/source
- (optional) Fortran/C interface files located under source_tree/solver/fcmix
- shared public header files located under *source_tree*/shared/include
- shared source files located under *source_tree*/shared/source
- (optional) NVECTOR_SERIAL header and source files located under source_tree/nvec_ser
- (optional) NVECTOR_PARALLEL header and source files located under source_tree/nvec_par
- configuration header file sundials_config.h (see below)

A sample header file that, appropriately modified, can be used as sundials_config.h (otherwise created automatically by the configure script) is provided below. The various preprocessor macros defined within sundials_config.h have the following uses:

• Precision of the SUNDIALS realtype type

Only one of the macros SUNDIALS_SINGLE_PRECISION, SUNDIALS_DOUBLE_PRECISION and SUNDIALS_EXTENDED_PRECISION should be defined to indicate if the SUNDIALS realtype type is an alias for float, double, or long double, respectively.

• Use of generic math functions

If SUNDIALS_USE_GENERIC_MATH is defined, then the functions in sundials_math.(h,c) will use the pow, sqrt, fabs, and exp functions from the standard math library (see math.h), regardless of the definition of realtype. Otherwise, if realtype is defined to be an alias for the float C-type, then SUNDIALS will use powf, sqrtf, fabsf, and expf. If realtype is instead defined to be a synonym for the long double C-type, then powl, sqrtl, fabsl, and expl will be used.

Table 2.1: SUNDIALS libraries and header files (names are relative to libdir for libraries and to incdir for header files)

SHARED	Libraries	n/a	
	Header files	sundials/sundials_types.h	sundials/sundials_math.h
		sundials/sundials_config.h	sundias/sundials_nvector.h
		sundials/sunials_smalldense.h	sundials/sundials_dense.h
		sundials/sundials_iterative.h	sundials/sundials_band.h
		sundials/sundials_spbcgs.h	sundials/sundials_sptfqmr.h
		sundials/sundials_spgmr.h	, 1
NVECTOR_SERIAL	Libraries	libsundials_nvecserial.lib	libsundials_fnvecserial.a
	Header files	nvector_serial.h	
NVECTOR_PARALLEL	Libraries	libsundials_nvecparallel.lib	libsundials_fnvecparallel.a
	Header files	nvector_parallel.h	
CVODE	Libraries	$libsundials_cvode.lib$	libsundials_fcvode.a
	Header files	cvode.h	
		$cvode/cvode_dense.h$	$cvode/cvode_band.h$
		cvode/cvode_diag.h	$cvode/cvode_spils.h$
		cvode/cvode_bandpre.h	$cvode/cvode_bbdpre.h$
		cvode/cvode_spgmr.h	$cvode/cvode_spbcgs.h$
		cvode/cvode_sptfqmr.h	$cvode/cvode_impl.h$
CVODES	Libraries	$libsundials_cvodes.lib$	
	Header files	cvodes.h	cvodea.h
		cvodes/cvodes_dense.h	$cvodes/cvodes_band.h$
		cvodes/cvodes_diag.h	$cvodes/cvodes_spils.h$
		cvodes/cvodes_bandpre.h	$cvodes/cvodes_bbdpre.h$
		cvodes/cvodes_spgmr.h	$cvodes/cvodes_spbcgs.h$
		cvodes/cvodes_sptfqmr.h	$cvodes/cvodes_impl.h$
		cvodes/cvodea_impl.h	•
IDA	Libraries	libsundials_ida.lib	libsundials_fida.a
	Header files	ida.h	
		ida/ida_dense.h	ida/ida_band.h
		ida/ida_spils.h	$ida/ida_spgmr.h$
		ida/ida_spbcgs.h	$ida/ida_sptfqmr.h$
		ida/ida_bbdpre.h	$ida/ida_impl.h$
KINSOL	Libraries	libsundials_kinsol.lib	libsundials_fkinsol.a
	Header files	kinsol.h	
		kinsol/kinsol_dense.h	kinsol/kinsol_band.h
		kinsol/kinsol_spils.h	kinsol/kinsol_spgmr.h
		kinsol/kinsol_spbcgs.h	$kinsol/kinsol_sptfqmr.h$
		kinsol/kinsol_bbdpre.h	kinsol/kinsol_impl.h

Note: Although the powf/powl, sqrtf/sqrtl, fabsf/fabsl, and expf/expl routines are not specified in the ANSI C standard, they are ISO C99 requirements. Consequently, these routines will only be used if available.

• FORTRAN name-mangling scheme

The macros given below are used to transform the C-language function names defined in the FORTRAN-C inteface modules in a manner consistent with the preferred FORTRAN compiler, thus allowing native C functions to be called from within a FORTRAN subroutine. The name-mangling scheme can be specified either by appropriately defining the parameterized macros (using the stringization operator, ##, if necessary)

```
- F77_FUNC(name,NAME)
```

- F77_FUNC_(name,NAME)

or by defining one macro from each of the following lists:

- SUNDIALS_CASE_LOWER or SUNDIALS_CASE_UPPER
- SUNDIALS_UNDERSCORE_NONE, SUNDIALS_UNDERSCORE_ONE, or SUNDIALS_UNDERSCORE_TWO

For example, to specify that mangled C-language function names should be lowercase with one underscore appended include either

```
#define F77_FUNC(name,NAME) name ## _
#define F77_FUNC_(name,NAME) name ## _

or

#define SUNDIALS_CASE_LOWER 1
#define SUNDIALS_UNDERSCORE_ONE 1
```

in the sundials_config.h header file.

• Use of an MPI communicator other than MPI_COMM_WORLD in FORTRAN

If the macro SUNDIALS_MPI_COMM_F2C is defined, then the MPI implementation used to build SUNDIALS defines the type MPI_Fint and the function MPI_Comm_f2c, and it is possible to use MPI communicators other than MPI_COMM_WORLD with the FORTRAN-C interface modules.

```
/*
1
    * Copyright (c) 2005, The Regents of the University of California.
    * Produced at the Lawrence Livermore National Laboratory.
4
    * All rights reserved.
    * For details, see sundials/shared/LICENSE.
    * SUNDIALS configuration header file
9
10
11
   /* Define SUNDIALS version number
13
      * ----- */
14
15
    #define SUNDIALS_PACKAGE_VERSION "2.2.0"
16
   /* Define precision of SUNDIALS data type 'realtype'
18
     * ------*
19
20
   /* Define SUNDIALS data type 'realtype' as 'double' */
21
   #define SUNDIALS_DOUBLE_PRECISION 1
23
   /* Define SUNDIALS data type 'realtype' as 'float' */
   /* #define SUNDIALS_SINGLE_PRECISION 1 */
25
   /* Define SUNDIALS data type 'realtype' as 'long double' */
27
   /* #define SUNDIALS_EXTENDED_PRECISION 1 */
28
   /* Use generic math functions
30
    * ----- */
32
    #define SUNDIALS_USE_GENERIC_MATH 1
33
34
   /* FCMIX: Define Fortran name-mangling macro
35
37
38
    #define F77_FUNC(name,NAME) name ## _
   #define F77_FUNC_(name, NAME) name ## _
39
40
   /* FCMIX: Define case of function names
41
42
43
   /* FCMIX: Make function names lowercase */
44
   /* #define SUNDIALS_CASE_LOWER 1 */
45
   /* FCMIX: Make function names uppercase */
47
   /* #define SUNDIALS_CASE_UPPER 1 */
   /* FCMIX: Define number of underscores to append to function names
50
51
    * ----- */
52
   /* FCMIX: Do NOT append any underscores to functions names */
   /* #define SUNDIALS_UNDERSCORE_NONE 1 */
54
   /* FCMIX: Append ONE underscore to function names */
   /* #define SUNDIALS_UNDERSCORE_ONE 1 */
   /* FCMIX: Append TWO underscores to function names */
59
   /* #define SUNDIALS_UNDERSCORE_TWO 1 */
61
   /* FNVECTOR: Allow user to specify different MPI communicator
62
    * ----- */
63
64
   #define SUNDIALS_MPI_COMM_F2C 1
```

Chapter 3

Mathematical Considerations

IDA solves the initial-value problem (IVP) for a DAE system of the general form

$$F(t, y, y') = 0, \quad y(t_0) = y_0, \ y'(t_0) = y'_0,$$
 (3.1)

where y, y', and F are vectors in \mathbf{R}^N , t is the independent variable, y' = dy/dt, and initial values y_0 , y'_0 are given. (Often t is time, but it certainly need not be.)

3.1 IVP solution

Prior to integrating a DAE initial-value problem, an important requirement is that the pair of vectors y_0 and y_0' are both initialized to satisfy the DAE residual $F(t_0, y_0, y_0') = 0$. For a class of problems that includes so-called semi-explicit index-one systems, IDA provides a routine that computes consistent initial conditions from a user's initial guess [4]. For this, the user must identify sub-vectors of y (not necessarily contiguous), denoted y_d and y_a , which are its differential and algebraic parts, respectively, such that F depends on y_d' but not on any components of y_a' . The assumption that the system is "index one" means that for a given t and y_d , the system F(t, y, y') = 0 defines y_a uniquely. In this case, a solver within IDA computes y_a and y_d' at $t = t_0$, given y_d and an initial guess for y_a . A second available option with this solver also computes all of $y(t_0)$ given $y'(t_0)$; this is intended mainly for quasi-steady-state problems, where $y'(t_0) = 0$ is given. In both cases, IDA solves the system $F(t_0, y_0, y_0') = 0$ for the unknown components of y_0 and y_0' , using Newton iteration augmented with a line search global strategy. In doing this, it makes use of the existing machinery that is to be used for solving the linear systems during the integration, in combination with certain tricks involving the step size (which is set artificially for this calculation). For problems that do not fall into either of these categories, the user is responsible for passing consistent values or risk failure in the numerical integration.

The integration method used in IDA is the variable-order, variable-coefficient BDF (Backward Differentiation Formula), in fixed-leading-coefficient form [1]. The method order ranges from 1 to 5, with the BDF of order q given by the multistep formula

$$\sum_{i=0}^{q} \alpha_{n,i} y_{n-i} = h_n y_n' \,, \tag{3.2}$$

where y_n and y'_n are the computed approximations to $y(t_n)$ and $y'(t_n)$, respectively, and the step size is $h_n = t_n - t_{n-1}$. The coefficients $\alpha_{n,i}$ are uniquely determined by the order q, and the history of the step sizes. The application of the BDF (3.2) to the DAE system (3.1) results in a nonlinear algebraic system to be solved at each step:

$$G(y_n) \equiv F\left(t_n, y_n, h_n^{-1} \sum_{i=0}^{q} \alpha_{n,i} y_{n-i}\right) = 0.$$
(3.3)

Regardless of the method options, the solution of the nonlinear system (3.3) is accomplished with some form of Newton iteration. This leads to a linear system for each Newton correction, of the form

$$J[y_{n(m+1)} - y_{n(m)}] = -G(y_{n(m)}), (3.4)$$

where $y_{n(m)}$ is the m-th approximation to y_n . Here J is some approximation to the system Jacobian

$$J = \frac{\partial G}{\partial y} = \frac{\partial F}{\partial y} + \alpha \frac{\partial F}{\partial y'}, \qquad (3.5)$$

where $\alpha = \alpha_{n,0}/h_n$. The scalar α changes whenever the step size or method order changes. The linear systems are solved by one of five methods:

- dense direct solver (serial version only),
- band direct solver (serial version only),
- diagonal approximate Jacobian solver,
- SPGMR = scaled preconditioned GMRES (Generalized Minimal Residual method) with restarts allowed.
- SPBCG = scaled preconditioned Bi-CGStab (Bi-Conjugate Gradient Stable method), or
- SPTFQMR = scaled preconditioned TFQMR (Transpose-Free Quasi-Minimal Residual method).

For the SPGMR, SPBCG, and SPTFQMR cases, preconditioning is allowed only on the left, so that the iterative method is applied to systems $(P^{-1}J)\Delta y = -P^{-1}G$. Note that the direct linear solvers (dense and band) can only be used with serial vector representations.

In the process of controlling errors at various levels, IDA uses a weighted root-mean-square norm, denoted $\|\cdot\|_{WRMS}$, for all error-like quantities. The multiplicative weights used are based on the current solution and on the relative and absolute tolerances input by the user, namely

$$W_i = 1/[\text{RTOL} \cdot |y_i| + \text{ATOL}_i]. \tag{3.6}$$

Because $1/W_i$ represents a tolerance in the component y_i , a vector whose norm is 1 is regarded as "small." For brevity, we will usually drop the subscript WRMS on norms in what follows.

In the case of a direct linear solver (dense or banded), the nonlinear iteration (3.4) is a Modified Newton iteration, in that the Jacobian J is fixed (and usually out of date), with a coefficient $\bar{\alpha}$ in place of α in J. When using one of the Krylov methods SPGMR, SPBCG, or SPTFQMR as the linear solver, the iteration is an Inexact Newton iteration, using the current Jacobian (through matrix-free products Jv), in which the linear residual $J\Delta y + G$ is nonzero but controlled. The Jacobian matrix J (direct cases) or preconditioner matrix P (SPGMR/SPBCG/SPTFQMR case) is updated when:

- starting the problem,
- the value $\bar{\alpha}$ at the last update is such that $\alpha/\bar{\alpha} < 3/5$ or $\alpha/\bar{\alpha} > 5/3$, or
- \bullet a non-fatal convergence failure occurred with an out-of-date J or P.

The above strategy balances the high cost of frequent matrix evaluations and preprocessing with the slow convergence due to infrequent updates. To reduce storage costs on an update, Jacobian information is always reevaluated from scratch.

The stopping test for the Newton iteration in IDA ensures that the iteration error $y_n - y_{n(m)}$ is small relative to y itself. For this, we estimate the linear convergence rate at all iterations m > 1 as

$$R = \left(\frac{\delta_m}{\delta_1}\right)^{\frac{1}{m-1}},\,$$

¹Left preconditioning is required to make the norm of the linear residual in the Newton iteration meaningful; in general, $||J\Delta y + G||$ is meaningless, since the weights used in the WRMS-norm correspond to y.

3.1 IVP solution 17

where the $\delta_m = y_{n(m)} - y_{n(m-1)}$ is the correction at iteration $m = 1, 2, \ldots$ The Newton iteration is halted if R > 0.9. The convergence test at the m-th iteration is then

$$S\|\delta_m\| < 0.33\,,\tag{3.7}$$

where S = R/(R-1) whenever m > 1 and $R \le 0.9$. The user has the option of changing the constant in the convergence test from its default value of 0.33. The quantity S is set to S = 20 initially and whenever J or P is updated, and it is reset to S = 100 on a step with $\alpha \ne \bar{\alpha}$. Note that at m = 1, the convergence test (3.7) uses an old value for S. Therefore, at the first Newton iteration, we make an additional test and stop the iteration if $\|\delta_1\| < 0.33 \cdot 10^{-4}$ (since such a δ_1 is probably just noise and therefore not appropriate for use in evaluating R). We allow only a small number (default value 4) of Newton iterations. If convergence fails with J or P current, we are forced to reduce the step size h_n , and we replace h_n by $h_n/4$. The integration is halted after a preset number (default value 10) of convergence failures. Both the maximum allowable Newton iterations and the maximum nonlinear convergence failures can be changed by the user from their default values.

When SPGMR, SPBCG, or SPTFQMR is used to solve the linear system, to minimize the effect of linear iteration errors on the nonlinear and local integration error controls, we require the preconditioned linear residual to be small relative to the allowed error in the Newton iteration, i.e., $||P^{-1}(Jx+G)|| < 0.05 \cdot 0.33$. The safety factor 0.05 can be changed by the user.

In the direct linear solver cases, the Jacobian J defined in (3.5) can be either supplied by the user or have IDA compute one internally by difference quotients. In the latter case, we use the approximation

$$J_{ij} = [F_i(t, y + \sigma_j e_j, y' + \alpha \sigma_j e_j) - F_i(t, y, y')]/\sigma_j, \text{ with}$$

$$\sigma_j = \sqrt{U} \max\{|y_j|, |hy_j'|, 1/W_j\} \operatorname{sign}(hy_j'),$$

where U is the unit roundoff, h is the current step size, and W_j is the error weight for the component y_j defined by (3.6). In the SPGMR/SPBCG/SPTFQMR case, if a routine for Jv is not supplied, such products are approximated by

$$Jv = [F(t, y + \sigma v, y' + \alpha \sigma v) - F(t, y, y')]/\sigma,$$

where the increment σ is $1/\|v\|$. As an option, the user can specify a constant factor that is inserted into this expression for σ .

During the course of integrating the system, IDA computes an estimate of the local truncation error, LTE, at the n-th time step, and requires this to satisfy the inequality

$$\|\text{LTE}\|_{\text{WRMS}} \leq 1$$
.

Asymptotically, LTE varies as h^{q+1} at step size h and order q, as does the predictor-corrector difference $\Delta_n \equiv y_n - y_{n(0)}$. Thus there is a constant C such that

$$LTE = C\Delta_n + O(h^{q+2}),$$

and so the norm of LTE is estimated as $|C| \cdot ||\Delta_n||$. In addition, IDA requires that the error in the associated polynomial interpolant over the current step be bounded by 1 in norm. The leading term of the norm of this error is bounded by $\bar{C}||\Delta_n||$ for another constant \bar{C} . Thus the local error test in IDA is

$$\max\{|C|, \bar{C}\}\|\Delta_n\| \le 1. \tag{3.8}$$

A user option is available by which the algebraic components of the error vector are omitted from the test (3.8), if these have been so identified.

In IDA, the local error test is tightly coupled with the logic for selecting the step size and order. First, there is an initial phase that is treated specially; for the first few steps, the step size is doubled and the order raised (from its initial value of 1) on every step, until (a) the local error test (3.8) fails, (b) the order is reduced (by the rules given below), or (c) the order reaches 5 (the maximum). For step and order selection on the general step, IDA uses a different set of local error estimates, based

on the asymptotic behavior of the local error in the case of fixed step sizes. At each of the orders q' equal to q, q-1 (if q>1), q-2 (if q>2), or q+1 (if q<5), there are constants C(q') such that the norm of the local truncation error at order q' satisfies

$$LTE(q') = C(q') \|\phi(q'+1)\| + O(h^{q'+2}),$$

where $\phi(k)$ is a modified divided difference of order k that is retained by IDA (and behaves asymptotically as h^k). Thus the local truncation errors are estimated as $\mathrm{ELTE}(q') = C(q') \|\phi(q'+1)\|$ to select step sizes. But the choice of order in IDA is based on the requirement that the scaled derivative norms, $\|h^k y^{(k)}\|$, are monotonically decreasing with k, for k near q. These norms are again estimated using the $\phi(k)$, and in fact

$$||h^{q'+1}y^{(q'+1)}|| \approx T(q') \equiv (q'+1)\text{ELTE}(q').$$

The step/order selection begins with a test for monotonicity that is made even before the local error test is performed. Namely, the order is reset to q' = q - 1 if (a) q = 2 and $T(1) \le T(2)/2$, or (b) q > 2 and $\max\{T(q-1), T(q-2)\} \le T(q)$; otherwise q' = q. Next the local error test (3.8) is performed, and if it fails, the step is redone at order $q \leftarrow q'$ and a new step size h'. The latter is based on the h^{q+1} asymptotic behavior of ELTE(q), and, with safety factors, is given by

$$\eta = h'/h = 0.9/[2 \text{ELTE}(q)]^{1/(q+1)}$$
.

The value of η is adjusted so that $0.25 \le \eta \le 0.9$ before setting $h \leftarrow h' = \eta h$. If the local error test fails a second time, IDA uses $\eta = 0.25$, and on the third and subsequent failures it uses q = 1 and $\eta = 0.25$. After 10 failures, IDA returns with a give-up message.

As soon as the local error test has passed, the step and order for the next step may be adjusted. No such change is made if q' = q - 1 from the prior test, if q = 5, or if q was increased on the previous step. Otherwise, if the last q + 1 steps were taken at a constant order q < 5 and a constant step size, IDA considers raising the order to q + 1. The logic is as follows: (a) If q = 1, then reset q = 2 if T(2) < T(1)/2. (b) If q > 1 then

- reset $q \leftarrow q 1$ if $T(q 1) \le \min\{T(q), T(q + 1)\};$
- else reset $q \leftarrow q+1$ if T(q+1) < T(q);
- leave q unchanged otherwise [then T(q-1) > T(q) < T(q+1)].

In any case, the new step size h' is set much as before:

$$\eta = h'/h = 1/[2 \text{ELTE}(q)]^{1/(q+1)}$$
.

The value of η is adjusted such that (a) if $\eta > 2$, η is reset to 2; (b) if $\eta \le 1$, η is restricted to $0.5 \le \eta \le 0.9$; and (c) if $1 < \eta < 2$ we use $\eta = 1$. Finally h is reset to $h' = \eta h$. Thus we do not increase the step size unless it can be doubled. See [1] for details.

IDA permits the user to impose optional inequality constraints on individual components of the solution vector y. Any of the following four constraints can be imposed: $y_i > 0$, $y_i < 0$, $y_i \geq 0$, or $y_i \leq 0$. The constraint satisfaction is tested after a successful nonlinear system solution. If any constraint fails, we declare a convergence failure of the Newton iteration and reduce the step size. Rather than cutting the step size by some arbitrary factor, IDA estimates a new step size h' using a linear approximation of the components in y that failed the constraint test (including a safety factor of 0.9 to cover the strict inequality case). These additional constraints are also imposed during the calculation of consistent initial conditions.

Normally, IDA takes steps until a user-defined output value $t = t_{\text{out}}$ is overtaken, and then computes $y(t_{\text{out}})$ by interpolation. However, a "one step" mode option is available, where control returns to the calling program after each step. There are also options to force IDA not to integrate past a given stopping point $t = t_{\text{stop}}$.

3.2 Rootfinding

3.2 Rootfinding

The IDA solver has been augmented to include a rootfinding feature. This means that, while integrating the Initial Value Problem (3.1), IDA can also find the roots of a set of user-defined functions $g_i(t, y, y')$ that depend on t, the solution vector y = y(t), and its t-derivative y'(t). The number of these root functions is arbitrary, and if more than one g_i is found to have a root in any given interval, the various root locations are found and reported in the order that they occur on the t axis, in the direction of integration.

Generally, this rootfinding feature finds only roots of odd multiplicity, corresponding to changes in sign of $g_i(t, y(t), y'(t))$, denoted $g_i(t)$ for short. If a user root function has a root of even multiplicity (no sign change), it will probably be missed by IDA. If such a root is desired, the user should reformulate the root function so that it changes sign at the desired root.

The basic scheme used is to check for sign changes of any $g_i(t)$ over each time step taken, and then (when a sign change is found) to home in on the root (or roots) with a modified secant method [11]. In addition, each time g is computed, IDA checks to see if $g_i(t) = 0$ exactly, and if so it reports this as a root. However, if an exact zero of any g_i is found at a point t, IDA computes g at $t + \delta$ for a small increment δ , slightly further in the direction of integration, and if any $g_i(t + \delta) = 0$ also, IDA stops and reports an error. This way, each time IDA takes a time step, it is guaranteed that the values of all g_i are nonzero at some past value of t, beyond which a search for roots is to be done.

At any given time in the course of the time-stepping, after suitable checking and adjusting has been done, IDA has an interval $(t_{lo}, t_{hi}]$ in which roots of the $g_i(t)$ are to be sought, such that t_{hi} is further ahead in the direction of integration, and all $g_i(t_{lo}) \neq 0$. The endpoint t_{hi} is either t_n , the end of the time step last taken, or the next requested output time t_{out} if this comes sooner. The endpoint t_{lo} is either t_{n-1} , or the last output time t_{out} (if this occurred within the last step), or the last root location (if a root was just located within this step), possibly adjusted slightly toward t_n if an exact zero was found. The algorithm checks g at t_{hi} for zeros and for sign changes in (t_{lo}, t_{hi}) . If no sign changes are found, then either a root is reported (if some $g_i(t_{hi}) = 0$) or we proceed to the next time interval (starting at t_{hi}). If one or more sign changes were found, then a loop is entered to locate the root to within a rather tight tolerance, given by

$$\tau = 100 * U * (|t_n| + |h|)$$
 (U = unit roundoff).

Whenever sign changes are seen in two or more root functions, the one deemed most likely to have its root occur first is the one with the largest value of $|g_i(t_{hi})|/|g_i(t_{hi}) - g_i(t_{lo})|$, corresponding to the closest to t_{lo} of the secant method values. At each pass through the loop, a new value t_{mid} is set, strictly within the search interval, and the values of $g_i(t_{mid})$ are checked. Then either t_{lo} or t_{hi} is reset to t_{mid} according to which subinterval is found to have the sign change. If there is none in (t_{lo}, t_{mid}) but some $g_i(t_{mid}) = 0$, then that root is reported. The loop continues until $|t_{hi} - t_{lo}| < \tau$, and then the reported root location is t_{hi} .

In the loop to locate the root of $g_i(t)$, the formula for t_{mid} is

$$t_{mid} = t_{hi} - (t_{hi} - t_{lo})g_i(t_{hi})/[g_i(t_{hi}) - \alpha g_i(t_{lo})]$$
,

where α a weight parameter. On the first two passes through the loop, α is set to 1, making t_{mid} the secant method value. Thereafter, α is reset according to the side of the subinterval (low vs high, i.e. toward t_{lo} vs toward t_{hi}) in which the sign change was found in the previous two passes. If the two sides were opposite, α is set to 1. If the two sides were the same, α is halved (if on the low side) or doubled (if on the high side). The value of t_{mid} is closer to t_{lo} when $\alpha < 1$ and closer to t_{hi} when $\alpha > 1$. If the above value of t_{mid} is within $\tau/2$ of t_{lo} or t_{hi} , it is adjusted inward, such that its fractional distance from the endpoint (relative to the interval size) is between .1 and .5 (.5 being the midpoint), and the actual distance from the endpoint is at least $\tau/2$.

Chapter 4

Code Organization

4.1 SUNDIALS organization

The family of solvers referred to as SUNDIALS consists of the solvers CVODE (for ODE systems), KINSOL (for nonlinear algebraic systems), and IDA (for differential-algebraic systems). In addition, variants of these which also do sensitivity analysis calculations are available or in development. CVODES, an extension of CVODE that provides both forward and adjoint sensitivity capabilities is available, while IDAS is currently in development.

The various solvers of this family share many subordinate modules. For this reason, it is organized as a family, with a directory structure that exploits that sharing (see Fig. 4.1). The following is a list of the solver packages presently available:

- CVODE, a solver for stiff and nonstiff ODEs dy/dt = f(t, y);
- CVODES, a solver for stiff and nonstiff ODEs dy/dt = f(t, y, p) with sensitivity analysis capabilities;
- KINSOL, a solver for nonlinear algebraic systems F(u) = 0;
- IDA, a solver for differential-algebraic systems F(t, y, y') = 0.

4.2 IDA organization

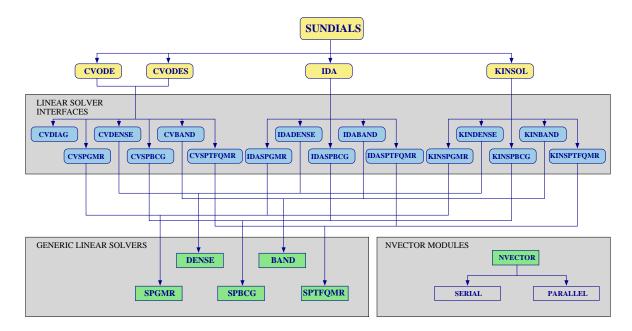
The IDA package is written in the ANSI C language. The following summarizes the basic structure of the package, although knowledge of this structure is not necessary for its use.

The overall organization of the IDA package is shown in Figure 4.2. The central integration module, implemented in the files ida.h, ida_impl.h, and ida.c, deals with the evaluation of integration coefficients, the Newton iteration process, estimation of local error, selection of stepsize and order, and interpolation to user output points, among other issues. Although this module contains logic for the basic Newton iteration algorithm, it has no knowledge of the method being used to solve the linear systems that arise. For any given user problem, one of the linear system modules is specified, and is then invoked as needed during the integration.

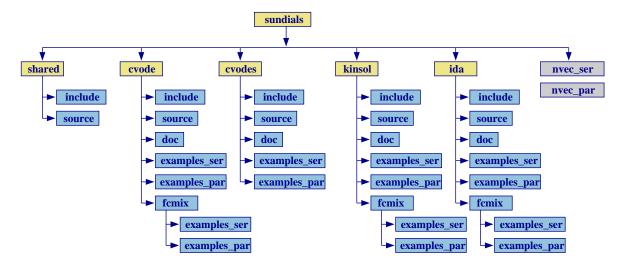
At present, the package includes the following five IDA linear system modules:

- IDADENSE: LU factorization and backsolving with dense matrices;
- IDABAND: LU factorization and backsolving with banded matrices;
- IDASPGMR: scaled preconditioned GMRES method;
- IDASPBCG: scaled preconditioned Bi-CGStab method;
- IDASPTFQMR: scaled preconditioned TFQMR method.

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(a) High-level diagram



(b) Directory structure of the source tree

Figure 4.1: Organization of the SUNDIALS suite

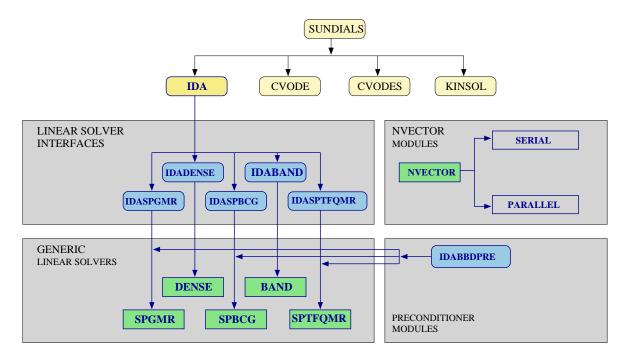


Figure 4.2: Overall structure diagram of the IDA package. Modules specific to IDA are distinguished by rounded boxes, while generic solver and auxiliary modules are in square boxes.

This set of linear solver modules is intended to be expanded in the future as new algorithms are developed.

In the case of the direct methods IDADENSE and IDABAND, the package includes an algorithm for the approximation of the Jacobian by difference quotients, but the user also has the option of supplying the Jacobian (or an approximation to it) directly. In the case of the Krylov iterative methods IDASPGMR, IDASPEGG, and IDASPTFQMR, the package includes an algorithm for the approximation by difference quotients of the product between the Jacobian matrix and a vector of appropriate length. Again, the user has the option of providing a routine for this operation. When using any of the Krylov methods, the user must supply the preconditioning in two phases: a setup phase (preprocessing of Jacobian data) and a solve phase. While there is no default choice of preconditioner analogous to the difference quotient approximation in the direct case, the references [2]-[5], together with the example and demonstration programs included with IDA, offer considerable assistance in building preconditioners.

Each IDA linear solver module consists of five routines, devoted to (1) memory allocation and initialization, (2) setup of the matrix data involved, (3) solution of the system, (4) monitoring performance, and (5) freeing of memory. The setup and solution phases are separate because the evaluation of Jacobians and preconditioners is done only periodically during the integration, as required to achieve convergence. The call list within the central IDA module to each of the five associated functions is fixed, thus allowing the central module to be completely independent of the linear system method.

These modules are also decomposed in another way. Each of the modules IDADENSE, IDABAND, IDASPGMR, IDASPGMR, and IDASPTFQMR is a set of interface routines built on top of a generic solver module, named DENSE, BAND, SPGMR, SPBCG, and SPTFQMR, respectively. The interfaces deal with the use of these methods in the IDA context, whereas the generic solver is independent of the context. While the generic solvers here were generated with SUNDIALS in mind, our intention is that they be usable in other applications as general-purpose solvers. This separation also allows for any generic solver to be replaced by an improved version, with no necessity to revise the IDA package elsewhere.

IDA also provides a preconditioner module, IDABBDPRE, that works in conjunction with NVECTOR_PARALLEL and generates a preconditioner that is a block-diagonal matrix with each block being a band matrix.

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All state information used by IDA to solve a given problem is saved in a structure, and a pointer to that structure is returned to the user. There is no global data in the IDA package, and so in this respect it is reentrant. State information specific to the linear solver is saved in a separate structure, a pointer to which resides in the IDA memory structure. The reentrancy of IDA was motivated by the situation where two or more problems are solved by intermixed calls to the package from one user program.

Chapter 5

Using IDA for C Applications

This chapter is concerned with the use of IDA for the integration of DAEs. The following sections treat the header files, the layout of the user's main program, description of the IDA user-callable functions, and description of user-supplied functions. The listings of the sample programs in the companion document [13] may also be helpful. Those codes may be used as templates (with the removal of some lines involved in testing), and are included in the IDA package.

The user should be aware that not all linear solver modules are compatible with all NVECTOR implementations. For example, NVECTOR_PARALLEL is not compatible with the direct dense or direct band linear solvers, since these linear solver modules need to form the complete system Jacobian. The IDADENSE and IDABAND modules can only be used with NVECTOR_SERIAL. The preconditioner module IDABBDPRE can only be used with NVECTOR_PARALLEL.

IDA uses various constants for both input and output. These are defined as needed in this chapter, but for convenience are also listed separately in Chapter 10.

5.1 Access to library and header files

At this point, it is assumed that the installation of IDA, following the procedure described in Chapter 2, has been completed successfully.

Regardless of where the user's application program resides, its associated compilation and load commands must make reference to the appropriate locations for the library and header files required by IDA. The relevant library files are

- *libdir*/libsundials_ida. *lib*,
- libdir/libsundials_nvec*. lib (one or two files),

where the file extension .lib is typically .so for shared libraries and .a for static libraries. The relevant header files are located in the subdirectories

- incdir/include
- *incdir*/include/ida
- incdir/include/sundials

The directories *libdir* and *incdir* are the install libray and include directories. For a default installation, these are *build_tree*/lib and *build_tree*/include, respectively, where *build_tree* was defined in Chapter 2.

5.2 Data types

The sundials_types.h file contains the definition of the type realtype, which is used by the SUNDIALS solvers for all floating-point data. The type realtype can be float, double, or long double, with the default being double. The user can change the precision of the SUNDIALS solvers arithmetic at the configuration stage (see §2.2).

Additionally, based on the current precision, sundials_types.h defines BIG_REAL to be the largest value representable as a realtype, SMALL_REAL to be the smallest value representable as a realtype, and UNIT_ROUNDOFF to be the difference between 1.0 and the minimum realtype greater than 1.0.

Within SUNDIALS, real constants are set by way of a macro called RCONST. It is this macro that needs the ability to branch on the definition realtype. In ANSI C, a floating-point constant with no suffix is stored as a double. Placing the suffix "F" at the end of a floating point constant makes it a float, whereas using the suffix "L" makes it a long double. For example,

```
#define A 1.0
#define B 1.0F
#define C 1.0L
```

defines A to be a double constant equal to 1.0, B to be a float constant equal to 1.0, and C to be a long double constant equal to 1.0. The macro call RCONST(1.0) automatically expands to 1.0 if realtype is double, to 1.0F if realtype is float, or to 1.0L if realtype is long double. SUNDIALS uses the RCONST macro internally to declare all of its floating-point constants.

A user program which uses the type realtype and the RCONST macro to handle floating-point constants is precision-independent except for any calls to precision-specific standard math library functions. (Our example programs use both realtype and RCONST.) Users can, however, use the type double, float, or long double in their code (assuming the typedef for realtype matches this choice). Thus, a previously existing piece of ANSI C code can use SUNDIALS without modifying the code to use realtype, so long as the SUNDIALS libraries use the correct precision (for details see §2.2).

5.3 Header files

The calling program must include several header files so that various macros and data types can be used. The header file that is always required is:

• ida.h, the header file for IDA, which defines the several types and various constants, and includes function prototypes.

Note that ida.h includes sundials_types.h, which defines the types realtype and booleantype and the constants FALSE and TRUE.

The calling program must also include an NVECTOR implementation header file (see Chapter 7 for details). For the two NVECTOR implementations that are included in the IDA package, the corresponding header files are:

- nvector_serial.h, which defines the serial implementation NVECTOR_SERIAL;
- nvector_parallel.h, which defines the parallel MPI implementation, NVECTOR_PARALLEL.

Note that both these files include in turn the header file sundials_nvector.h which defines the abstract N_Vector type.

Finally, a linear solver module header file is required. The header files corresponding to the various linear solver options in IDA are as follows:

• ida_dense.h, which is used with the dense direct linear solver in the context of IDA. This in turn includes a header file (sundials_dense.h) which defines the DenseMat type and corresponding accessor macros;

- ida_band.h, which is used with the band direct linear solver in the context of IDA. This in turn includes a header file (sundials_band.h) which defines the BandMat type and corresponding accessor macros;
- ida_spgmr.h, which is used with the Krylov solver SPGMR in the context of IDA;
- ida_spbcgs.h, which is used with the Krylov solver SPBCG in the context of IDA;
- ida_sptfqmr.h, which is used with the Krylov solver SPTFQMR in the context of IDA;

The header files for the Krylov iterative solvers include ida_spils.h which defined common fuunctions and which in turn includes a header file (sundials_iterative.h) which enumerates the kind of preconditioning and for the choices for the Gram-Schmidt process for SPGMR.

5.4 A skeleton of the user's main program

The following is a skeleton of the user's main program (or calling program) for the integration of a DAE IVP. Some steps are independent of the NVECTOR implementation used; where this is not the case, usage specifications are given for the two implementations provided with IDA: steps marked with [P] correspond to NVECTOR_PARALLEL, while steps marked with [S] correspond to NVECTOR_SERIAL.

1. [P] Initialize MPI

Call MPI_Init(&argc, &argv); to initialize MPI if used by the user's program, aside from the internal use in NVECTOR_PARALLEL. Here argc and argv are the command line argument counter and array received by main.

2. Set problem dimensions

[S] Set N, the problem size N.

[P] Set Nlocal, the local vector length (the sub-vector length for this processor); N, the global vector length (the problem size N, and the sum of all the values of Nlocal); and the active set of processors.

3. Set vector of initial values

To set the vectors y0 and yp0 to initial values for y and y', use functions defined by a particular NVECTOR implementation. For the two NVECTOR implementations provided, if a realtype array ydata already exists, containing the initial values of y, make the call:

```
[S] y0 = N_VMake_Serial(N, ydata);
[P] y0 = N_VMake_Parallel(comm, Nlocal, N, ydata);
Otherwise, make the call:
[S] y0 = N_VNew_Serial(N);
[P] y0 = N_VNew_Parallel(comm, Nlocal, N);
and load initial values into the structure defined by:
[S] NV_DATA_S(y0)
[P] NV_DATA_P(y0)
```

Here comm is the MPI communicator, set in one of two ways: If a proper subset of active processors is to be used, comm must be set by suitable MPI calls. Otherwise, to specify that all processors are to be used, comm must be MPI_COMM_WORLD.

The initial conditions for y' are set similarly.

4. Create IDA object

Call ida_mem = IDACreate(); to create the IDA memory block. IDACreate returns a pointer to the IDA memory structure. See §5.5.1 for details.

5. Allocate internal memory

Call IDAMalloc(...); to provide required problem specifications, allocate internal memory for IDA, and initialize IDA. IDAMalloc returns an error flag to indicate success or an illegal argument value. See §5.5.1 for details.

6. Set optional inputs

Call IDASet* functions to change from their default values any optional inputs that control the behavior of IDA. See §5.5.6.1 for details.

7. Attach linear solver module

Initialize the linear solver module with one of the following calls (for details see §5.5.3):

```
[S] flag = IDADense(...);
[S] flag = IDABand(...);
flag = IDASpgmr(...);
flag = IDASpbcg(...);
flag = IDASptfqmr(...);
```

8. Set linear solver optional inputs

Call IDA*Set* functions from the selected linear solver module to change optional inputs specific to that linear solver. See §5.5.6.3 for details.

9. Correct initial values

Optionally, call IDACalcIC to correct the initial values y0 and yp0. See §5.5.4. Also see §5.5.6.2 for relevant optional input calls.

10. Specify rootfinding problem

Optionally, call IDARootInit to initialize a rootfinding problem to be solved during the integration of the DAE system. See §5.7.1 for details.

11. Advance solution in time

For each point at which output is desired, call flag = IDASolve(ida_mem, tout, &tret, yret, ypret, itask); Set itask to specify the return mode. The vector yret (which can be the same as the vector y0 above) will contain y(t), while the vector ypret will contain y'(t). See §5.5.5 for details.

12. Get optional outputs

Call IDA*Get* functions to obtain optional output. See §5.5.8 and §5.7.1 for details.

13. Deallocate memory for solution vector

Upon completion of the integration, deallocate memory for the vectors yret and ypret by calling the destructor function defined by the NVECTOR implementation:

```
[S] N_VDestroy_Serial(yret);[P] N_VDestroy_Parallel(yret);and similarly for ypret.
```

14. Free solver memory

IDAFree(&ida_mem); to free the memory allocated for IDA.

15. [P] Finalize MPI

Call MPI_Finalize(); to terminate MPI.

5.5 User-callable functions

This section describes the IDA functions that are called by the user to set up and solve a DAE. Some of these are required. However, starting with §5.5.6, the functions listed involve optional inputs/outputs or restarting, and those paragraphs can be skipped for a casual use of IDA. In any case, refer to §5.4 for the correct order of these calls. Calls related to rootfinding are described in §5.7.

5.5.1 IDA initialization and deallocation functions

The following three functions must be called in the order listed. The last one is to be called only after the DAE solution is complete, as it frees the IDA memory block created and allocated by the first two calls.

IDACreate

Call ida_mem = IDACreate();

Description The function IDACreate instantiates an IDA solver object.

Arguments IDACreate has no arguments.

Return value If successful, IDACreate returns a pointer to the newly created IDA memory block (of

type void *). If an error occurred, IDACreate prints an error message to stderr and

returns NULL.

IDAMalloc

Call flag = IDAMalloc(ida_mem, res, t0, y0, yp0, itol, reltol, abstol);

Description The function IDAMalloc provides required problem and solution specifications, allocates

internal memory, and initializes IDA.

Arguments ida_mem (void *) pointer to the IDA memory block returned by IDACreate.

res (IDAResFn) is the C function which computes F in the DAE. This function has the form res(t, yy, yp, resval, res_data) (for full details see $\S 5.6$).

to (realtype) is the initial value of t.

y0 (N_Vector) is the initial value of y.

yp0 (N_Vector) is the initial value of y'.

(int) is one of IDA_SS, IDA_SV, or IDA_WF. Here itol = IDA_SS indicates scalar relative error tolerance and scalar absolute error tolerance, while itol = IDA_SV indicates scalar relative error tolerance and vector absolute error tolerance. The latter choice is important when the absolute error tolerance needs to be different for each component of the DAE. If itol = IDA_WF, the arguments reltol and abstol are ignored and the user is expected to provide a function to evaluate the error weight vector W, replacing (3.6). See

IDASetEwtFn in $\S5.5.6.1$.

reltol (realtype) is the relative error tolerance.

abstol (void *) is a pointer to the absolute error tolerance. If itol = IDA_SS, abstol must be a pointer to a realtype variable. If itol = IDA_SV, abstol must be an N_Vector variable.

Return value The return flag flag (of type int) will be one of the following:

IDA_SUCCESS The call to IDAMalloc was successful.

IDA_MEM_NULL The IDA memory block was not initialized through a previous call to

IDACreate.

IDA_MEM_FAIL A memory allocation request has failed.

IDA_ILL_INPUT An input argument to IDAMalloc has an illegal value.

Notes See also §5.5.2 for advice on tolerances.

The tolerance values in reltol and abstol may be changed between calls to IDASolve (see IDASetTolerances in §5.5.6.1).

It is the user's responsibility to provide compatible itol and abstol arguments.

If an error occurred, IDAMalloc also sends an error message to the error handler function.

IDAFree

Call IDAFree(&ida_mem);

Description The function IDAFree frees the pointer allocated by a previous call to IDAMalloc.

Arguments The argument is the pointer to the IDA memory block (of type void *).

Return value The function IDAFree has no return value.

5.5.2 Advice on choice and use of tolerances

General advice on choice of tolerances. For many users, the appropriate choices for tolerance values in reltol and abstol are a concern. The following pieces of advice are relevant.

- (1) The scalar relative tolerance reltol is to be set to control relative errors. So reltol = 1.0E-4 means that errors are controlled to .01%. We do not recommend using reltol larger than 1.0E-3. On the other hand, reltol should not be so small that it is comparable to the unit roundoff of the machine arithmetic (generally around 1.0E-15).
- (2) The absolute tolerances abstol (whether scalar or vector) need to be set to control absolute errors when any components of the solution vector y may be so small that pure relative error control is meaningless. For example, if y[i] starts at some nonzero value, but in time decays to zero, then pure relative error control on y[i] makes no sense (and is overly costly) after y[i] is below some noise level. Then abstol (if scalar) or abstol[i] (if a vector) needs to be set to that noise level. If the different components have different noise levels, then abstol should be a vector. See the example idadenx in the IDA package, and the discussion of it in the IDA Examples document [13]. In that problem, the three components vary betwen 0 and 1, and have different noise levels; hence the abstol vector. It is impossible to give any general advice on abstol values, because the appropriate noise levels are completely problem-dependent. The user or modeler hopefully has some idea as to what those noise levels are.
- (3) Finally, it is important to pick all the tolerance values conservately, because they control the error committed on each individual time step. The final (global) errors are some sort of accumulation of those per-step errors. A good rule of thumb is to reduce the tolerances by a factor of .01 from the actual desired limits on errors. So if you want .01% accuracy (globally), a good choice is reltol = 1.0E-6. But in any case, it is a good idea to do a few experiments with the tolerances to see how the computed solution values vary as tolerances are reduced.

Advice on controlling unphysical negative values. In many applications, some components in the true solution are always positive or non-negative, though at times very small. In the numerical solution, however, small negative (hence unphysical) values can then occur. In most cases, these values are harmless, and simply need to be controlled, not eliminated. The following pieces of advice are relevant.



- (1) The way to control the size of unwanted negative computed values is with tighter absolute tolerances. Again this requires some knowledge of the noise level of these components, which may or may not be different for different components. Some experimentation may be needed.
- (2) If output plots or tables are being generated, and it is important to avoid having negative numbers appear there (for the sake of avoiding a long explanation of them, if nothing else), then eliminate them, but only in the context of the output medium. Then the internal values carried by the solver are unaffected. Remember that a small negative value in yret returned by IDA, with magnitude comparable to abstol or less, is equivalent to zero as far as the computation is concerned.
- (3) The user's residual routine **res** should never change a negative value in the solution vector **yy** to a non-negative value, as a "solution" to this problem. This can cause instability. If the **res** routine cannot tolerate a zero or negative value (e.g. because there is a square root or log of it), then the offending value should be changed to zero or a tiny positive number in a temporary variable (not in the input yy vector) for the purposes of computing F(t, y).
- (4) IDA provides the option of enforcing positivity or non-negativity on components. But these constraint options should only be exercised if the use of absolute tolerances to control the computed values is unsuccessful, because they involve some extra overhead cost.

5.5.3 Linear solver specification functions

As previously explained, Newton iteration requires the solution of linear systems of the form (3.4). There are five IDA linear solvers currently available for this task: IDADENSE, IDABAND, IDASPGMR, IDASPBCG, and IDASPTFQMR. The first two are direct solvers and derive their name from the type of approximation used for the Jacobian $J = \partial F/\partial y + c_j \partial F/\partial y'$. IDADENSE and IDABAND work with dense and banded approximations to J, respectively. The remaining three IDA linear solvers, IDASPGMR, IDASPBCG, and IDASPTFQMR, are Krylov iterative solvers. The SPGMR, SPBCG, and SPTFQMR in the names indicate the scaled preconditioned GMRES, scaled preconditioned Bi-CGStab, and scaled preconditioned TFQMR methods, respectively. Together, they are referred to as IDASPILS (from scaled preconditioned iterative linear solvers).

When using any of the Krylov linear solvers, preconditioning (on the left) is permitted, and in fact encouraged, for the sake of efficiency. A preconditioner matrix P must approximate the Jacobian J, at least crudely. For the specification of a preconditioner, see §5.5.6.3 and §5.6.

To specify an IDA linear solver, after the call to IDACreate but before any calls to IDASolve, the user's program must call one of the functions IDADense, IDABand, IDASpgmr, IDASpbcg, or IDASptfqmr, as documented below. The first argument passed to these functions is the IDA memory pointer returned by IDACreate. A call to one of these functions links the main IDA integrator to a linear solver and allows the user to specify parameters which are specific to a particular solver, such as the bandwidths in the IDABAND case. The use of each of the linear solvers involves certain constants and possibly some macros, that are likely to be needed in the user code. These are available in the corresponding header file associated with the linear solver, as specified below.

In each case the linear solver module used by IDA is actually built on top of a generic linear system solver, which may be of interest in itself. These generic solvers, denoted DENSE, BAND, SPGMR, SPBCG, and SPTFQMR, are described separately in Chapter 9.

```
Call flag = IDADense(ida_mem, N);

Description The function IDADense selects the IDADENSE linear solver.

The user's main function must include the ida_dense.h header file.

Arguments ida_mem (void *) pointer to the IDA memory block.

N (long int) problem dimension.

Return value The return value flag (of type int) is one of
```

IDADENSE_SUCCESS The IDADENSE initialization was successful.

IDADENSE_MEM_NULL The ida_mem pointer is NULL.

IDADENSE_ILL_INPUT The IDADENSE solver is not compatible with the current NVECTOR module.

IDADENSE_MEM_FAIL A memory allocation request failed.

Notes

The IDADENSE linear solver may not be compatible with a particular implementation of the NVECTOR module. Of the two NVECTOR modules provided by SUNDIALS, only NVECTOR_SERIAL is compatible, while NVECTOR_PARALLEL is not.

IDABand

Call flag = IDABand(ida_mem, N, mupper, mlower);

Description The function IDABand selects the IDABAND linear solver.

The user's main function must include the ida_band.h header file.

Arguments ida_mem (void *) pointer to the IDA memory block.

N (long int) problem dimension.

mupper (long int) upper half-bandwidth of the problem Jacobian (or of the approx-

imation of it).

mlower (long int) lower half-bandwidth of the problem Jacobian (or of the approxi-

mation of it).

Return value The return value flag (of type int) is one of

IDABAND_SUCCESS The IDABAND initialization was successful.

IDABAND_MEM_NULL The ida_mem pointer is NULL.

IDABAND_ILL_INPUT The IDABAND solver is not compatible with the current NVECTOR

module, or one of the Jacobian half-bandwidths is outside its valid

range $(0 \dots N-1)$.

IDABAND_MEM_FAIL A memory allocation request failed.

Notes

The IDABAND linear solver may not be compatible with a particular implementation of the NVECTOR module. Of the two NVECTOR modules provided by SUNDIALS, only NVECTOR_SERIAL is compatible, while NVECTOR_PARALLEL is not. The half-bandwidths are to be set so that the nonzero locations (i,j) in the banded (approximate) Jacobian satisfy $-\mathtt{mlower} \leq j-i \leq \mathtt{mupper}$.

IDASpgmr

Call flag = IDASpgmr(ida_mem, maxl);

Description The function IDASpgmr selects the IDASPGMR linear solver.

The user's main function must include the ida_spgmr.h header file.

Arguments ida_mem (void *) pointer to the IDA memory block.

maxl (int) maximum dimension of the Krylov subspace to be used. Pass 0 to use the default value IDA_SPGMR_MAXL= 5.

Return value The return value flag (of type int) is one of

IDASPILS_SUCCESS The IDASPGMR initialization was successful.

IDASPILS_MEM_NULL The ida_mem pointer is NULL.

IDASPILS_MEM_FAIL A memory allocation request failed.

IDASpbcg

Call flag = IDASpbcg(ida_mem, maxl);

Description The function IDASpbcg selects the IDASPBCG linear solver.

The user's main function must include the ida_spbcgs.h header file.

Arguments ida_mem (void *) pointer to the IDA memory block.

maxl (int) maximum dimension of the Krylov subspace to be used. Pass 0 to use

the default value $\mathtt{IDA_SPBCG_MAXL} = 5$.

Return value The return value flag (of type int) is one of

IDASPILS_SUCCESS The IDASPBCG initialization was successful.

IDASPILS_MEM_NULL The ida_mem pointer is NULL.

IDASPILS_MEM_FAIL A memory allocation request failed.

IDASptfqmr

Call flag = IDASptfqmr(ida_mem, maxl);

Description The function IDASptfqmr selects the IDASPTFQMR linear solver.

The user's main function must include the ida_sptfqmr.h header file.

Arguments ida_mem (void *) pointer to the IDA memory block.

maxl (int) maximum dimension of the Krylov subspace to be used. Pass 0 to use

the default value IDA_SPTFQMR_MAXL= 5.

Return value The return value flag (of type int) is one of

IDASPILS_SUCCESS The IDASPTFQMR initialization was successful.

IDASPILS_MEM_NULL The ida_mem pointer is NULL.

IDASPILS_MEM_FAIL A memory allocation request failed.

5.5.4 Initial condition calculation function

IDACalcIC calculates corrected initial conditions for the DAE system for a class of index-one problems of semi-implicit form. (See §3.1 and Ref. [4].) It uses Newton iteration combined with a linesearch algorithm. Calling IDACalcIC is optional. It is only necessary when the initial conditions do not solve the given system. Thus if y0 and yp0 are known to satisfy $F(t_0, y_0, y_0') = 0$, then a call to IDACalcIC is generally not necessary.

A call to IDACalcIC must be preceded by successful calls to IDACreate and IDAMalloc, and by a successful call to the linear system solver specification function. The call to IDACalcIC should precede the call(s) to IDASolve for the given problem.

IDACalcIC

Call flag = IDACalcIC(ida_mem, t0, y0, yp0, icopt, tout1);

Description The function IDACalcIC corrects the initial values y0 and yp0 at time t0.

Arguments ida_mem (void *) pointer to the IDA memory block.

t0 (realtype) is the initial value of t. y0 (N_Vector) is the initial value of y. yp0 (N_Vector) is the initial value of y'.

icopt (int) is one of the following two options for the initial condition calculation.

icopt=IDA_YA_YDP_INIT directs IDACalcIC to compute the algebraic components of y and differential components of y', given the differential components of y. This option requires that the N_Vector id was set through IDASetId, specifying the differential and algebraic components.

 $icopt=IDA_Y_INIT$ directs IDACalcIC to compute all components of y, given y'. In this case, id is not required.

(realtype) is the first value of t at which a solution will be requested (from tout1 IDASolve). This value is needed here to determine the direction of integration and rough scale in the independent variable t.

Return value The return value flag (of type int) will be one of the following:

IDA_SUCCESS IDASolve succeeded. IDA_MEM_NULL The argument ida_mem was NULL. IDA_NO_MALLOC The allocation function IDAMalloc has not been called. IDA_ILL_INPUT One of the input arguments was illegal. IDA_LSETUP_FAIL The linear solver's setup function failed in an unrecoverable manner. IDA_LINIT_FAIL The linear solver's initialization function failed. The linear solver's solve function failed in an unrecoverable man-IDA_LSOLVE_FAIL IDA_BAD_EWT Some component of the error weight vector is zero (illegal), either for the input value of y0 or a corrected value. IDA_FIRST_RES_FAIL The user's residual function returned a recoverable error flag on the first call, but IDACalcIC was unable to recover. IDA_RES_FAIL The user's residual function returned a nonrecoverable error flag. IDA_NO_RECOVERY The user's residual function, or the linear solver's setup or solve function had a recoverable error, but IDACalcIC was unable to recover. IDA_CONSTR_FAIL IDACalcIC was unable to find a solution satisfying the inequality constraints. IDA_LINESEARCH_FAIL The linesearch algorithm failed to find a solution with a step

larger than steptol in weighted RMS norm. IDA_CONV_FAIL IDACalcIC failed to get convergence of the Newton iterations.

Notes All failure return values are negative and therefore a test flag < 0 will trap all IDACalcIC failures.

> Note that IDACalcIC is typically called after IDAMalloc and before the first call to IDASolve, to compute consistent initial conditions for the DAE problem. However, it can be also called at any other time to correct a pair (y, y').

5.5.5 IDA solver function

This is the central step in the solution process — the call to perform the integration of the DAE.

IDASolve

Call flag = IDASolve(ida_mem, tout, tret, yret, ypret, itask);

Description The function IDASolve integrates the DAE over an interval in t.

ida_mem (void *) pointer to the IDA memory block. Arguments

> (realtype) the next time at which a computed solution is desired. tout

(realtype *) the time reached by the solver. tret (N_Vector) the computed solution vector y. yret (N_Vector) the computed solution vector y'. ypret

itask (int) a flag indicating the job of the solver for the next user step. The IDA_NORMAL task is to have the solver take internal steps until it has reached or just passed the user specified tout parameter. The solver then interpolates in order to return approximate values of y(tout) and y'(tout). The IDA_ONE_STEP option tells the solver to just take one internal step and return the solution at the point reached by that step. The IDA_NORMAL_TSTOP and IDA_ONE_STEP_TSTOP modes are similar to IDA_NORMAL and IDA_ONE_STEP, respectively, except that the integration never proceeds past the value tstop, specified through the function IDASetStopTime (see §5.5.6.1).

Return value On return, IDASolve returns vectors yeet and ypret and a corresponding independent variable value t = *tret, such that (yret, ypret) are the computed values of (y(t), y'(t)).

In IDA_NORMAL mode with no errors, *tret will be equal to tout and yret = y(tout), ypret = y'(tout).

The return value flag (of type int) will be one of the following:

IDA_SUCCESS IDASolve succeeded.

IDA_TSTOP_RETURN IDASolve succeeded by reaching the stop point specified through

the optional input function IDASetStopTime.

IDA_ROOT_RETURN IDASolve succeeded and found one or more roots. If nrtfn > 1,

call IDAGetRootInfo to see which g_i were found to have a root.

See §5.7 for more information.

IDA_MEM_NULL The ida_mem argument was NULL.

IDA_ILL_INPUT One of the inputs to IDASolve is illegal. This includes the situation

where a root of one of the root functions was found both at a point t and also very near t. It also includes the situation when a component of the error weight vectors becomes negative during internal time-stepping. The <code>IDA_ILL_INPUT</code> flag will also be returned if the linear solver function initialization (called by the user after calling <code>IDACreate</code>) failed to set the linear solver-specific <code>lsolve</code> field in <code>ida_mem</code>. In any case, the user should see the printed error message

for more details.

 ${\tt IDA_TOO_MUCH_WORK~The~solver~took~mxstep~internal~steps~but~could~not~reach~tout.}$

The default value for mxstep is MXSTEP_DEFAULT = 500.

IDA_TOO_MUCH_ACC The solver could not satisfy the accuracy demanded by the user for

some internal step.

IDA_ERR_FAIL Error test failures occurred too many times (MXNEF = 10) during one internal time step or occurred with $|h| = h_{min}$.

IDA_CONV_FAIL Convergence test failures occurred too many times (MXNCF = 10)

during one internal time step or occurred with $|h| = h_{min}$.

IDA_LINIT_FAIL The linear solver's initialization function failed.

 ${\tt IDA_LSETUP_FAIL} \quad \text{The linear solver's setup function failed in an unrecoverable man-}$

ner.

IDA_LSOLVE_FAIL The linear solver's solve function failed in an unrecoverable manner.

 ${\tt IDA_CONSTR_FAIL} \quad \text{ The inequality constraints were violated and the solver was unable}$

to recover.

IDA_REP_RES_ERR The user's residual function repeatedly returned a recoverable error

flag, but the solver was unable to recover.

IDA_RES_FAIL The user's residual function returned a nonrecoverable error flag.

IDA_RTFUNC_FAIL The rootfinding function failed.

Notes

The vector yret can occupy the same space as the y0 vector of initial conditions that was passed to IDAMalloc, while the vector ypret can occupy the same space as the ур0.

In the IDA_ONE_STEP mode, tout is used on the first call only, to get the direction and rough scale of the independent variable.

All failure return values are negative and therefore a test flag < 0 will trap all IDASolve failures.

On any error return in which one or more internal steps were taken by IDASolve, the returned values of tret, yret, and ypret correspond to the farthest point reached in the integration. On all other error returns, these values are left unchanged from the previous IDASolve return.

5.5.6Optional input functions

IDA provides an extensive list of functions that can be used to change various optional input parameters that control the behavior of the IDA solver from their default values. Table 5.1 lists all optional input functions in IDA which are then described in detail in the remainder of this section. For the most casual use of IDA, the reader can skip to §5.6.

We note that, on error return, all these functions also send an error message to the error handler function. We also note that all error return values are negative, so a test flag < 0 will catch any error.

5.5.6.1 Main solver optional input functions

The calls listed here can be executed in any order.

However, if IDASetErrHandlerFn or IDASetErrFile are to be called, that call should be first, in order to take effect for any later error message.

IDASetErrHandlerFn

Call flag = IDASetErrHandlerFn(ida_mem, ehfun, eh_data);

Description The function IDASetErrHandlerFn specifies the optional user-defined function to be

used in handling error messages.

Arguments ida_mem (void *) pointer to the IDA memory block.

(IDAErrHandlerFn) is the C error handler function (see §5.6.2).

eh_data (void *) pointer to user data passed to ehfun every time it is called.

Return value The return value flag (of type int) is one of

IDA_SUCCESS The function enfun and data pointer eh_data have been successfully set.

IDA_MEM_NULL The ida_mem pointer is NULL.

Notes The default internal error handler function directs error messages to the file specified

by the file pointer errfp (see IDASetErrFile below).

Error messages indicating that the IDA solver memory is NULL will always be directed to stderr.

IDASetErrFile

Call flag = IDASetErrFile(ida_mem, errfp);

The function IDASetErrFile specifies the pointer to the file where all IDA messages Description should be directed in case the default IDA error handler function is used.

Arguments ida_mem (void *) pointer to the IDA memory block.

> (FILE *) pointer to output file. errfp

Table 5.1: Optional inputs for IDA, IDADENSE, IDABAND, and IDASPILS

Optional input	Function name	Default	
IDA main solver			
Error handler function	IDASetErrHandlerFn	internal fn.	
Pointer to an error file	IDASetErrFile	stderr	
Data for residual function	IDASetRdata	NULL	
Maximum order for BDF method	IDASetMaxOrd	5	
Maximum no. of internal steps before t_{out}	IDASetMaxNumSteps	500	
Initial step size	IDASetInitStep	estimated	
Maximum absolute step size	IDASetMaxStep	∞	
Value of t_{stop}	IDASetStopTime	∞	
Maximum no. of error test failures	IDASetMaxErrTestFails	10	
Maximum no. of nonlinear iterations	IDASetMaxNonlinIters	4	
Maximum no. of convergence failures	IDASetMaxConvFails	10	
Maximum no. of error test failures	IDASetMaxErrTestFails	7	
Coeff. in the nonlinear convergence test	IDASetNonlinConvCoef	0.33	
Suppress alg. vars. from error test	IDASetSuppressAlg	FALSE	
Variable types (differential/algebraic)	IDASetId	NULL	
Inequality constraints on solution	IDASetConstraints	NULL	
Integration tolerances	IDASetTolerances	none	
IDA initial conditions calculation			
Coeff. in the nonlinear convergence test	IDASetNonlinConvCoefIC	0.0033	
Maximum no. of steps	IDASetMaxNumStepsIC	5	
Maximum no. of Jacobian/precond. evals.	IDASetMaxNumJacsIC	4	
Maximum no. of Newton iterations	IDASetMaxNumItersIC	10	
Turn off linesearch	IDASetLineSearchOffIC	FALSE	
Lower bound on Newton step	IDASetStepToleranceIC	$uround^{2/3}$	
IDADENSE linear solver			
Dense Jacobian function and data	IDADenseSetJacFn	DQ, NULL	
IDABAND linear solver			
Band Jacobian function and data	IDABandSetJacFn	DQ, NULL	
IDASPILS linear solvers			
Preconditioner functions and data	IDASpilsSetPreconditioner	all NULL	
Jacobian-times-vector function and data	IDASpilsSetJacTimesVecFn	DQ, NULL	
Factor in linear convergence test	IDASpilsSetEpsLin	0.05	
Factor in DQ increment calculation	IDASpilsSetIncrementFactor	1.0	
Maximum no. of restarts (IDASPGMR)	IDASpilsSetMaxRestarts	5	
Type of Gram-Schmidt orthogonalization (a)	IDASpilsSetGSType	classical GS	
Maximum Krylov subspace $size^{(b)}$	IDASpilsSetMaxl	5	

 $^{^{(}a)}$ Only for <code>IDASPGMR</code> $^{(b)}$ Only for <code>IDASPBCG</code> and <code>IDASPTFQMR</code>

Return value The return value flag (of type int) is one of

IDA_SUCCESS The optional value has been successfully set.

IDA_MEM_NULL The ida_mem pointer is NULL.

Notes The default value for errfp is stderr.

Passing a value NULL disables all future error message output (except for the case in

which the IDA memory pointer is NULL).

If IDASetErrFile is to be called, it should be called before any other optional input

functions, in order to take effect for any later error message.

IDASetRdata

Call flag = IDASetRdata(ida_mem, res_data);

Description The function IDASetRdata specifies the user data block res_data and attaches it to the

main IDA memory block.

Arguments ida_mem (void *) pointer to the IDA memory block.

res_data (void *) pointer to the user data.

Return value The return value flag (of type int) is one of

IDA_SUCCESS The optional value has been successfully set.

IDA_MEM_NULL The ida_mem pointer is NULL.

Notes If res_data is not specified, a NULL pointer is passed to all user functions that have it

as an argument.

IDASetMaxOrd

Call flag = IDASetMaxOrd(ida_mem, maxord);

Description The function IDASetMaxOrd specifies the maximum order of the linear multistep method.

Arguments ida_mem (void *) pointer to the IDA memory block.

maxord (int) value of the maximum method order.

Return value The return value flag (of type int) is one of

IDA_SUCCESS The optional value has been successfully set.

IDA_MEM_NULL The ida_mem pointer is NULL.

IDA_ILL_INPUT The specified value maxord is negative, or larger than its previous value.

Notes The default value is 5. Since maxord affects the memory requirements for the internal

IDA memory block, its value can not be increased past its previous value.

IDASetMaxNumSteps

Call flag = IDASetMaxNumSteps(ida_mem, mxsteps);

Description The function IDASetMaxNumSteps specifies the maximum number of steps to be taken

by the solver in its attempt to reach the next output time.

Arguments ida_mem (void *) pointer to the IDA memory block.

mxsteps (long int) maximum allowed number of steps.

Return value The return value flag (of type int) is one of

IDA_SUCCESS The optional value has been successfully set.

IDA_MEM_NULL The ida_mem pointer is NULL.

IDA_ILL_INPUT mxsteps is non-positive.

Notes Passing mxsteps= 0 results in IDA using the default value (500).



IDASetInitStep

Call flag = IDASetInitStep(ida_mem, hin);

Description The function IDASetInitStep specifies the initial step size.

Arguments ida_mem (void *) pointer to the IDA memory block.

(realtype) value of the initial step size.

Return value The return value flag (of type int) is one of

IDA_SUCCESS The optional value has been successfully set.

IDA_MEM_NULL The ida_mem pointer is NULL.

Notes By default, IDA estimates the initial step as the solution of $||hy'||_{WRMS} = 1/2$, with an

added restriction that $|h| \leq .001 |$ tout - t0|.

IDASetMaxStep

flag = IDASetMaxStep(ida_mem, hmax); Call

Description The function IDASetMaxStep specifies the maximum absolute value of the step size.

Arguments ida_mem (void *) pointer to the IDA memory block.

(realtype) maximum absolute value of the step size.

Return value The return value flag (of type int) is one of

IDA SUCCESS The optional value has been successfully set.

IDA_MEM_NULL The ida_mem pointer is NULL.

IDA_ILL_INPUT Either hmax is not positive or it is smaller than the minimum allowable

Notes Pass hmax = 0 to obtain the default value ∞ .

IDASetStopTime

flag = IDASetStopTime(ida_mem, tstop); Call

The function IDASetStopTime specifies the value of the independent variable t past Description which the solution is not to proceed.

ida_mem (void *) pointer to the IDA memory block.

Arguments (realtype) value of the independent variable past which the solution should tstop not proceed.

Return value The return value flag (of type int) is one of

IDA_SUCCESS The optional value has been successfully set.

IDA_MEM_NULL The ida_mem pointer is NULL.

Notes The default, if this routine is not called, is that no stop time is imposed.

IDASetMaxErrTestFails

Call flag = IDASetMaxErrTestFails(ida_mem, maxnef);

Description The function IDASetMaxErrTestFails specifies the maximum number of error test

failures in attempting one step.

ida_mem (void *) pointer to the IDA memory block. Arguments

maxnef (int) maximum number of error test failures allowed on one step.

Return value The return value flag (of type int) is one of

IDA_SUCCESS The optional value has been successfully set.

IDA_MEM_NULL The ida_mem pointer is NULL.

Notes The default value is 7.

IDASetMaxNonlinIters

Call flag = IDASetMaxNonlinIters(ida_mem, maxcor);

Description The function IDASetMaxNonlinIters specifies the maximum number of nonlinear solver

iterations at one step.

Arguments ida_mem (void *) pointer to the IDA memory block.

maxcor (int) maximum number of nonlinear solver iterations allowed on one step.

Return value The return value flag (of type int) is one of

IDA_SUCCESS The optional value has been successfully set.

IDA_MEM_NULL The ida_mem pointer is NULL.

Notes The default value is 3.

IDASetMaxConvFails

Call flag = IDASetMaxConvFails(ida_mem, maxncf);

Description The function IDASetMaxConvFails specifies the maximum number of nonlinear solver

convergence failures at one step.

Arguments ida_mem (void *) pointer to the IDA memory block.

maxncf (int) maximum number of allowable nonlinear solver convergence failures on

one step.

Return value The return value flag (of type int) is one of

IDA_SUCCESS The optional value has been successfully set.

IDA_MEM_NULL The ida_mem pointer is NULL.

Notes The default value is 10.

IDASetNonlinConvCoef

Call flag = IDASetNonlinConvCoef(ida_mem, nlscoef);

Description The function IDASetNonlinConvCoef specifies the safety factor in the nonlinear con-

vergence test; see Chapter 3, Eq. (3.7).

Arguments ida_mem (void *) pointer to the IDA memory block.

nlscoef (realtype) coefficient in nonlinear convergence test.

Return value The return value flag (of type int) is one of

IDA_SUCCESS The optional value has been successfully set.

IDA_MEM_NULL The ida_mem pointer is NULL.

Notes The default value is 0.33.

IDASetSuppressAlg

Call flag = IDASetSuppressAlg(ida_mem, suppressalg);

Description The function IDASetSuppressAlg indicates whether or not to suppress algebraic vari-

ables in the local error test.

Arguments ida_mem (void *) pointer to the IDA memory block.

suppresslag (booleantype) indicates whether to suppress (TRUE) or not (FALSE) the

algebraic variables in the local error test.

Return value The return value flag (of type int) is one of

IDA_SUCCESS The optional value has been successfully set.

IDA_MEM_NULL The ida_mem pointer is NULL.

Notes The default value is FALSE.

If suppresslag=TRUE is selected, then the id vector must be set (through IDASetId) to specify the algebraic components.

IDASetId

Call flag = IDASetId(ida_mem, id);

Description The function IDASetId specifies algebraic/differential components in the y vector.

Arguments ida_mem (void *) pointer to the IDA memory block.

id (N_Vector) state vector. A value of 1.0 indicates a differential variable, while 0.0 indicates an algebraic variable.

Return value The return value flag (of type int) is one of

IDA_SUCCESS The optional value has been successfully set.

IDA_MEM_NULL The ida_mem pointer is NULL.

Notes The vector id is required if the algebraic variables are to be suppressed from the lo-

cal error test (see IDASetSuppressAlg) or if IDACalcIC is to be called with icopt = IDA_YA_YDP_INIT (see §5.5.4).

IDASetConstraints

Call flag = IDASetConstraints(ida_mem, constraints);

 $\label{lem:description} \textbf{Description} \quad \textbf{The function $\tt IDASetConstraints} \ \ \text{specifies a vector defining inequality constraints for the state of the property of the state of the$

each component of the solution vector y.

Arguments ida_mem (void *) pointer to the IDA memory block.

constraints (N_Vector) vector of constraint flags. If constraints[i] is

0.0 then no constraint is imposed on y_i .

1.0 then y_i will be constrained to be $y_i \ge 0.0$.

-1.0 then y_i will be constrained to be $y_i \leq 0.0$.

2.0 then y_i will be constrained to be $y_i > 0.0$.

-2.0 then y_i will be constrained to be $y_i < 0.0$.

Return value The return value flag (of type int) is one of

IDA_SUCCESS The optional value has been successfuly set.

IDA_MEM_NULL The ida_mem pointer is NULL.

IDA_ILL_INPUT The constraints vector contains illegal values.

Notes The presence of a non-NULL constraints vector that is not 0.0 in all components will cause constraint checking to be performed.

IDASetTolerances

Call flag = IDASetTolerances(ida_mem, itol, reltol, abstol);

Description The function IDASetTolerances resets the integration tolerances.

Arguments ida_mem (void *) pointer to the IDA memory block.

itol (int) is either IDA_SS or IDA_SV, where itol=IDA_SS indicates scalar relative error tolerance and scalar absolute error tolerance, while itol=IDA_SV indicates scalar relative error tolerance and vector absolute error tolerance. The latter choice is important when the absolute error tolerance needs to be

different for each component of the DAE.

reltol (realtype) is the relative error tolerance.

abstol (void *) is a pointer to the absolute error tolerance. If itol=IDA_SS, abstol must be a pointer to a realtype variable. If itol = IDA_SV, abstol must be an N_Vector variable.

Return value The return value flag (of type int) is one of

IDA_SUCCESS The tolerances have been successfully set.

IDA_MEM_NULL The ida_mem pointer is NULL.

IDA_ILL_INPUT An input argument has an illegal value.

Notes The integration tolerances are initially specified in the call to IDAMalloc (see §5.5.1).

This function call to ${\tt IDASetTolerances}$ is needed only if the tolerances are being

changed from their values between successive calls to ${\tt IDASolve}.$

It is the user's responsibility to provide compatible itol and abstol arguments.

It is illegal to call IDASetTolerances before a call to IDAMalloc.

IDASetEwtFn

Call flag = IDASetEwtFn(ida_mem, efun, edata);

Description The function IDASetEwtFn specifies the user-defined function that sets the multiplicative

error weights W_i for use in the weighted RMS norm, which are normally defined by Eq.

(3.6).

Arguments ida_mem (void *) pointer to the IDA memory block.

efun (IDAEwtFn) is the C function which defines the ewt vector (see $\S 5.6.3$).

edata (void *) pointer to user data passed to efun every time it is called.

Return value The return value flag (of type int) is one of

IDA_SUCCESS The function efun and data pointer edata have been successfully set.

IDA_MEM_NULL The ida_mem pointer is NULL.

Notes This function can be called between successive calls to IDASolve.

If not needed, pass NULL for edata.

It is illegal to call IDASetEwtFn before a call to IDAMalloc.

5.5.6.2 Initial condition calculation optional input functions

The following functions can be called to set optional inputs to control the initial condition calculations.

IDASetNonlinConvCoefIC

Call flag = IDASetNonlinConvCoefIC(ida_mem, epiccon);

Description The function IDASetNonlinConvCoefIC specifies the positive constant in the Newton

iteration convergence test within the initial condition calculation.

Arguments ida_mem (void *) pointer to the IDA memory block.

epiccon (realtype) coefficient in the Newton convergence test.

Return value The return value flag (of type int) is one of

IDA_SUCCESS The optional value has been successfuly set.

IDA_MEM_NULL The ida_mem pointer is NULL.

IDA_ILL_INPUT The epiccon factor is negative (illegal).

Notes The default value is $0.01 \cdot 0.33$.

This test uses a weighted RMS norm (with weights defined by the tolerances). For new initial value vectors y and y' to be accepted, the norm of $J^{-1}F(t_0, y, y')$ must be \leq epiccon, where J is the system Jacobian.



IDASetMaxNumStepsIC

Call flag = IDASetMaxNumStepsIC(ida_mem, maxnh);

Description The function IDASetMaxNumStepsIC specifies the maximum number of steps allowed

when $icopt=IDA_YA_YDP_INIT$ in IDACalcIC, where h appears in the system Jacobian,

 $J = \partial F/\partial y + (1/h)\partial F/\partial y'.$

Arguments ida_mem (void *) pointer to the IDA memory block.

maxnh (int) maximum allowed number of values for h.

Return value The return value flag (of type int) is one of

IDA_SUCCESS The optional value has been successfuly set.

IDA_MEM_NULL The ida_mem pointer is NULL.

IDA_ILL_INPUT maxnh is non-positive.

Notes The default value is 5.

IDASetMaxNumJacsIC

Call flag = IDASetMaxNumJacsIC(ida_mem, maxnj);

Description The function IDASetMaxNumJacsIC specifies the maximum number of the approximate

Jacobian or preconditioner evaluations allowed when the Newton iteration appears to

be slowly converging.

Arguments ida_mem (void *) pointer to the IDA memory block.

maxnj (int) maximum allowed number of Jacobian or preconditioner evaluations.

Return value The return value flag (of type int) is one of

IDA_SUCCESS The optional value has been successfuly set.

IDA_MEM_NULL The ida_mem pointer is NULL.

IDA_ILL_INPUT maxnj is non-positive.

Notes The default value is 4.

IDASetMaxNumItersIC

Call flag = IDASetMaxNumItersIC(ida_mem, maxnit);

Description The function IDASetMaxNumItersIC specifies the maximum number of Newton itera-

tions allowed in any one attempt to solve the initial conditions calculation problem.

Arguments ida_mem (void *) pointer to the IDA memory block.

maxnit (int) maximum number of Newton iterations.

Return value The return value flag (of type int) is one of

IDA_SUCCESS The optional value has been successfuly set.

IDA_MEM_NULL The ida_mem pointer is NULL.

IDA_ILL_INPUT maxnit is non-positive.

Notes The default value is 10.

IDASetLineSearchOffIC

Call flag = IDASetLineSearchOffIC(ida_mem, lsoff);

Description The function IDASetLineSearchOffIC specifies whether to turn on or off the linesearch

algorithm.

Arguments ida_mem (void *) pointer to the IDA memory block.

lsoff (booleantype) a flag to turn off (TRUE) or keep (FALSE) the linesearch algo-

rithm.

Return value The return value flag (of type int) is one of

IDA_SUCCESS The optional value has been successfuly set.

IDA_MEM_NULL The ida_mem pointer is NULL.

Notes The default value is FALSE.

IDASetStepToleranceIC

Call flag = IDASetStepToleranceIC(ida_mem, steptol);

Description The function IDASetStepToleranceIC specifies a positive lower bound on the Newton

step.

Arguments ida_mem (void *) pointer to the IDA memory block.

steptol (int) Newton step tolerance.

Return value The return value flag (of type int) is one of

IDA_SUCCESS The optional value has been successfuly set.

IDA_MEM_NULL The ida_mem pointer is NULL.

IDA_ILL_INPUT The steptol tolerance is negative (illegal).

Notes The default value is (unit roundoff) $^{2/3}$.

5.5.6.3 Linear solver optional input functions

The linear solver modules allow for various optional inputs, which are described here.

5.5.6.4 Dense linear solver

The IDADENSE solver needs a function to compute a dense approximation to the Jacobian matrix J(t,y,y'). This function must be of type IDADenseJacFn. The user can supply his/her own dense Jacobian function, or use the default difference quotient function IDADenseDQJac that comes with the IDADENSE solver. To specify a user-supplied Jacobian function djac and associated user data jac_data, IDADENSE provides the function IDADenseSetJacFn. The IDADENSE solver passes the pointer jac_data to its dense Jacobian function. This allows the user to create an arbitrary structure with relevant problem data and access it during the execution of the user-supplied Jacobian function, without using global data in the program. The pointer jac_data may be identical to res_data, if the latter was specified through IDASetFdata.

IDADenseSetJacFn

Call flag = IDADenseSetJacFn(ida_mem, djac, jac_data);

Description The function IDADenseSetJacFn specifies the dense Jacobian approximation function

to be used and the pointer to user data.

Arguments ida_mem (void *) pointer to the IDA memory block.

djac (IDADenseJacFn) user-defined dense Jacobian approximation function.

 ${\tt jac_data}$ (void *) pointer to the user-defined data structure.

Return value The return value flag (of type int) is one of

IDADENSE_SUCCESS The optional value has been successfully set.

IDADENSE_MEM_NULL The ida_mem pointer is NULL.

IDADENSE_LMEM_NULL The IDADENSE linear solver has not been initialized.

Notes By default, IDADENSE uses the difference quotient function IDADenseDQJac. If NULL is

passed to djac, this default function is used.

The function type IDADenseJacFn is described in §5.6.4.

5.5.6.5 Band linear solver

The IDABAND solver needs a function to compute a banded approximation to the Jacobian matrix J(t,y,y'). This function must be of type IDABandJacFn. The user can supply his/her own banded Jacobian approximation function, or use the default difference quotient function IDABandDQJac that comes with the IDABAND solver. To specify a user-supplied Jacobian function bjac and associated user data jac_data, IDABAND provides the function IDABandSetJacFn. The IDABAND solver passes the pointer jac_data to its banded Jacobian approximation function. This allows the user to create an arbitrary structure with relevant problem data and access it during the execution of the user-supplied Jacobian function, without using global data in the program. The pointer jac_data may be identical to res_data, if the latter was specified through IDAodeSetFdata.

IDABandSetJacFn

Call flag = IDABandSetJacFn(ida_mem, bjac, jac_data);

Description The function IDABandSetJacFn specifies the banded Jacobian approximation function

to be used and the pointer to user data.

Arguments ida_mem (void *) pointer to the IDA memory block.

bjac (IDABandJacFn) user-defined banded Jacobian approximation function.

jac_data (void *) pointer to the user-defined data structure.

Return value The return value flag (of type int) is one of

IDABAND_SUCCESS The optional value has been successfully set.

IDABAND_MEM_NULL The ida_mem pointer is NULL.

IDABAND_LMEM_NULL The IDABAND linear solver has not been initialized.

Notes By default, IDABAND uses the difference quotient function IDABandDQJac. If NULL is

passed to bjac, this default function is used.

The function type IDABandJacFn is described in §5.6.5.

5.5.6.6 SPGMR Linear solver

If preconditioning is to be done with one of the IDASPILS linear solvers, then the user must supply a preconditioner solve function and specify its name through a call to IDASpilsSetPreconditioner. The evaluation and preprocessing of any Jacobian-related data needed by the user's preconditioner solve function is done in the optional user-supplied function psetup. Both of these functions are fully specified in §5.6. If used, the name of the psetup function should be specified in the call to IDASpilsSetPreconditioner.

Optionally, the pointer p_data received through IDASpilsSetPreconditioner is passed to the preconditioner psetup and psolve functions. This allows the user to create an arbitrary structure with relevant problem data and access it during the execution of the user-supplied preconditioner functions without using global data in the program. The pointer p_data may be identical to res_data, if the latter was specified through IDASetRdata.

The IDASPILS solvers require a function to compute an approximation to the product between the Jacobian matrix J(t,y) and a vector v. The user can supply his/her own Jacobian-times-vector approximation function, or use the difference quotient function IDASpilsDQJtimes that comes with the IDASPILS solvers. A user-defined Jacobian-vector function must be of type IDASpilsJacTimesVecFn and can be specified through a call to IDASpilsSetJacTimesVecFn (see §5.6.6 for specification details). As with the preconditioner user data structure p_data, the user can also specify in the call to IDASpilsSetJacTimesVecFn, a pointer to a user-defined data structure, jac_data, which the IDASPILS solver passes to the Jacobian-times-vector function jtimes each time it is called. The pointer jac_data may be identical to p_data and/or res_data.

${\tt IDASpilsSetPreconditioner}$

Call flag = IDASpilsSetPreconditioner(ida_mem, psetup, psolve, p_data);

Description The function IDASpilsSetPreconditioner specifies the preconditioner setup and solve

functions and the pointer to user data.

Arguments ida_mem (void *) pointer to the IDA memory block.

psetup (IDASpilsPrecSetupFn) user-defined preconditioner setup function.
psolve (IDASpilsPrecSolveFn) user-defined preconditioner solve function.

p_data (void *) pointer to the user-defined data structure.

Return value The return value flag (of type int) is one of

IDASPILS_SUCCESS The optional value has been successfully set.

IDASPILS_MEM_NULL The ida_mem pointer is NULL.

IDASPILS_LMEM_NULL The IDASPILS linear solver has not been initialized.

Notes The function type IDASpilsPrecSolveFn is described in §5.6.7. The function type

IDASpilsPrecSetupFn is described in §5.6.8.

IDASpilsSetJacTimesVecFn

Call flag = IDASpilsSetJacTimesVecFn(ida_mem, jtimes, jac_data);

Description The function IDASpilsSetJacTimesFn specifies the Jacobian-vector function to be used

and the pointer to user data.

Arguments ida_mem (void *) pointer to the IDA memory block.

jtimes (IDASpilsJacTimesVecFn) user-defined Jacobian-vector product function.

jac_data (void *) pointer to the user-defined data structure.

Return value The return value flag (of type int) is one of

IDASPILS_SUCCESS The optional value has been successfully set.

IDASPILS_MEM_NULL The ida_mem pointer is NULL.

IDASPILS_LMEM_NULL The IDASPILS linear solver has not been initialized.

Notes By default, the IDASPILS solvers use the difference quotient function IDASpilsDQJtimes.

If NULL is passed to jtimes, this default function is used.

The function type IDASpilsJacTimesVecFn is described in §5.6.6.

IDASpilsSetGSType

Call flag = IDASpilsSetGSType(ida_mem, gstype);

Description The function IDASpilsSetGSType specifies the Gram-Schmidt orthogonalization to be

used. This must be one of the enumeration constants MODIFIED_GS or CLASSICAL_GS. These correspond to using modified Gram-Schmidt and classical Gram-Schmidt, respec-

tively.

Arguments ida_mem (void *) pointer to the IDA memory block.

gstype (int) type of Gram-Schmidt orthogonalization.

Return value The return value flag (of type int) is one of

IDASPILS_SUCCESS The optional value has been successfuly set.

IDASPILS_MEM_NULL The ida_mem pointer is NULL.

IDASPILS_LMEM_NULL The IDASPILS linear solver has not been initialized.

IDASPILS_ILL_INPUT The Gram-Schmidt orthogonalization type gstype is not valid.

Notes The default value is MODIFIED_GS.

This option is available only for the IDASPGMR linear solver.



IDASpilsSetMaxRestarts

Call flag = IDASpilsSetMaxRestarts(ida_mem, maxrs);

Description The function IDASpilsSetMaxRestarts specifies the maximum number of restarts to

be used in the GMRES algorithm.

Arguments ida_mem (void *) pointer to the IDA memory block.

maxrs (int) maximum number of restarts.

Return value The return value flag (of type int) is one of

IDASPILS_SUCCESS The optional value has been successfuly set.

IDASPILS_MEM_NULL The ida_mem pointer is NULL.

IDASPILS_LMEM_NULL The IDASPILS linear solver has not been initialized.

IDASPILS_ILL_INPUT The maxrs argument is negative.

Notes The default value is 5. Pass maxrs = 0 to specify no restarts.

This option is available only for the IDASPGMR linear solver.



IDASpilsSetEpsLin

Call flag = IDASpilsSetEpsLin(ida_mem, eplifac);

Description The function IDASpilsSetEpsLin specifies the factor by which the GMRES convergence

test constant is reduced from the Newton iteration test constant. (See §3).

Arguments ida_mem (void *) pointer to the IDA memory block.

eplifac (realtype)

Return value The return value flag (of type int) is one of

IDASPILS_SUCCESS The optional value has been successfuly set.

IDASPILS_MEM_NULL The ida_mem pointer is NULL.

IDASPILS_LMEM_NULL The IDASPILS linear solver has not been initialized.

IDASPILS_ILL_INPUT The factor eplifac is negative.

Notes The default value is 0.05.

Passing a value eplifac= 0.0 also indicates using the default value.

${\tt IDASpilsSetIncrementFactor}$

Call flag = IDASpilsSetIncrementFactor(ida_mem, dqincfac);

Description The function IDASpilsSetIncrementFactor specifies a factor in the increments to y

used in the difference quotient approximations to the Jacobian-vector products. (See

§3).

Arguments ida_mem (void *) pointer to the IDA memory block.

dqincfac (realtype) difference quotient increment factor.

Return value The return value flag (of type int) is one of

IDASPILS_SUCCESS The optional value has been successfuly set.

IDASPILS_MEM_NULL The ida_mem pointer is NULL.

IDASPILS_LMEM_NULL The IDASPILS linear solver has not been initialized.

 ${\tt IDASPILS_ILL_INPUT}$ The increment factor was non-positive.

Notes The default value is dqincfac = 1.0.

IDASpbcgSetMaxl

Call flag = IDASpbcgSetMaxl(ida_mem, maxl);

Description The function IDASpbcgSetMaxl specifies maximum of the Krylov subspace dimension

for the Bi-CGStab method.

Arguments ida_mem (void *) pointer to the IDA memory block.

maxl (int) maximum dimension of the Krylov subspace.

Return value The return value flag (of type int) is one of

IDASPILS_SUCCESS The optional value has been successfuly set.

IDASPILS_MEM_NULL The ida_mem pointer is NULL.

IDASPILS_LMEM_NULL The IDASPILS linear solver has not been initialized.

Notes The default value is 5. Passing maxl = 0 also results in the default value.

This option is available only for the IDASPBCG and IDASPTFQMR linear solvers.



5.5.7 Interpolated output function

An optional function IDAGetSolution is available to obtain additional output values. This function must be called after a successful return from IDASolve and provides interpolated values of y and y' for any value of t in the last internal step taken by IDA.

The call to the IDAGetSolution function has the following form:

IDAGetSolution

Call flag = IDAGetSolution(ida_mem, t, yret, ypret);

Description The function IDAGetSolution computes the interpolated values of y and y' for any value

of t in the last internal step taken by IDA. The value of t must satisfy $t_n - h_u \le t \le t_n$, where t_n denotes the current internal time reached, and h_u is the last internal step size

used successfully.

Arguments ida_mem (void *) pointer to the IDA memory block.

t (realtype)

yret (N_Vector) vector containing the interpolated y(t).

ypret (N_Vector) vector containing the interpolated y'(t).

Return value The return value flag (of type int) is one of

IDA_SUCCESS IDAGetSolution succeeded.

IDA_MEM_NULL The ida_mem argument was NULL.

IDA_BAD_T t is not in the interval $[t_n - h_u, t_n]$.

Notes It is only legal to call the function IDAGetSolution after a successful return from

IDASolve. See IDAGetCurrentTime and IDAGetLastStep for access to t_n and h_u .

5.5.8 Optional output functions

IDA provides an extensive list of functions that can be used to obtain solver performance information. Table 5.2 lists all optional output functions in IDA, which are then described in detail in the remainder of this section.

Table 5.2: Optional outputs from IDA, IDADENSE, IDABAND, and IDASPILS

Optional output	Function name	
IDA main solver		
Size of IDA real and integer workspace	IDAGetWorkSpace	
Cumulative number of internal steps	IDAGetNumSteps	
No. of calls to residual function	IDAGetNumResEvals	
No. of calls to linear solver setup function	IDAGetNumLinSolvSetups	
No. of local error test failures that have occurred	IDAGetNumErrTestFails	
Order used during the last step	IDAGetLastOrder	
Order to be attempted on the next step	IDAGetCurrentOrder	
Order reductions due to stability limit detection	IDAGetNumStabLimOrderReds	
Actual initial step size used	IDAGetActualInitStep	
Step size used for the last step	IDAGetLastStep	
Step size to be attempted on the next step	IDAGetCurrentStep	
Current internal time reached by the solver	IDAGetCurrentTime	
Suggested factor for tolerance scaling	IDAGetTolScaleFactor	
Error weight vector for state variables	IDAGetErrWeights	
Estimated local errors	IDAGetEstLocalErrors	
No. of nonlinear solver iterations	IDAGetNumNonlinSolvIters	
No. of nonlinear convergence failures	IDAGetNumNonlinSolvConvFails	
Array showing roots found	IDAGetRootInfo	
No. of calls to user root function	IDAGetNumGEvals	
Name of constant associated with a return flag	IDAGetReturnFlagName	
IDADENSE linear solver		
Size of IDADENSE real and integer workspace	IDADenseGetWorkSpace	
No. of Jacobian evaluations	IDADenseGetNumJacEvals	
No. of residual calls for finite diff. Jacobian evals.	IDADenseGetNumResEvals	
Last return from a idadense function	IDADenseGetLastFlag	
Name of constant associated with a return flag	IDADenseGetReturnFlagName	
IDABAND linear solver		
Size of IDABAND real and integer workspace	IDABandGetWorkSpace	
No. of Jacobian evaluations	IDABandGetNumJacEvals	
No. of residual calls for finite diff. Jacobian evals.	IDABandGetNumResEvals	
Last return from a IDABAND function	IDABandGetLastFlag	
Name of constant associated with a return flag	${\tt IDABandGetReturnFlagName}$	
IDASPILS linear solvers		
Size of real and integer workspace	IDASpilsGetWorkSpace	
No. of linear iterations	IDASpilsGetNumLinIters	
No. of linear convergence failures	IDASpilsGetNumConvFails	
No. of preconditioner evaluations	IDASpilsGetNumPrecEvals	
No. of preconditioner solves	IDASpilsGetNumPrecSolves	
No. of Jacobian-vector product evaluations	IDASpilsGetNumJtimesEvals	
No. of residual calls for finite diff. Jacobian-vector evals.	IDASpilsGetNumResEvals	
Last return from a linear solver function	IDASpilsGetLastFlag	
Name of constant associated with a return flag	${\tt IDASpilsGetReturnFlagName}$	

5.5.8.1 Main solver optional output functions

IDA provides several user-callable functions that can be used to obtain different quantities that may be of interest to the user, such as solver workspace requirements, solver performance statistics, as well as additional data from the IDA memory block (a suggested tolerance scaling factor, the error weight vector, and the vector of estimated local errors). Also provided are functions to extract statistics related to the performance of the IDA nonlinear solver being used. As a convenience, additional extraction functions provide the optional outputs in groups. These optional output functions are described next.

IDAGetWorkSpace

Call flag = IDAGetWorkSpace(ida_mem, &lenrw, &leniw);

Description The function IDAGetWorkSpace returns the IDA real and integer workspace sizes.

Arguments ida_mem (void *) pointer to the IDA memory block.

lenrw (long int) number of real values in the IDA workspace.

leniw (long int) number of integer values in the IDA workspace.

Return value The return value flag (of type int) is one of

IDA_SUCCESS The optional output value has been successfuly set.

IDA_MEM_NULL The ida_mem pointer is NULL.

Notes

In terms of the problem size N, the maximum method order maxord, and the number nrtfn of root functions (see $\S5.7$), the actual size of the real workspace, in realtype words, is given by the following:

- base value: lenrw = $55 + (m+6) * N_r + 3*nrtfn$;
- with itol = IDA_SV: lenrw = lenrw $+N_r$;
- with constraint checking (see IDASetConstraints): lenrw = lenrw $+N_r$;
- with id specified (see IDASetId): lenrw = lenrw $+N_r$;

where $m = \max(\max, 3)$, and N_r is the number of real words in one N-Vector $(\approx N)$.

The size of the integer workspace (without distinction between int and long int words) is given by:

- base value: leniw = $38 + (m+6) * N_i + \text{nrtfn};$
- with itol = IDA_SV: leniw = leniw $+N_i$;
- with constraint checking: lenrw = lenrw + N_i ;
- with id specified: lenrw = lenrw $+N_i$;

where N_i is the number of integer words in one N_Vector (= 1 for NVECTOR_SERIAL and 2*npes for NVECTOR_PARALLEL on npes processors).

For the default value of maxord, with no rootfinding, no id, no constraints, and with itol \neq IDA_SV, these lengths are given roughly by: lenrw = 55 + 11N, leniw = 38.

IDAGetNumSteps

Call flag = IDAGetNumSteps(ida_mem, &nsteps);

Description The function IDAGetNumSteps returns the cumulative number of internal steps taken by the solver (total so far).

Arguments ida_mem (void *) pointer to the IDA memory block.

nsteps (long int) number of steps taken by IDA.

Return value The return value flag (of type int) is one of

IDA_SUCCESS The optional output value has been successfuly set.

IDA_MEM_NULL The ida_mem pointer is NULL.

IDAGetNumResEvals

Call flag = IDAGetNumResEvals(ida_mem, &nrevals);

Description The function IDAGetNumResEvals returns the number of calls to the user's residual

evaluation function.

Arguments ida_mem (void *) pointer to the IDA memory block.

nrevals (long int) number of calls to the user's res function.

Return value The return value flag (of type int) is one of

IDA_SUCCESS The optional output value has been successfuly set.

IDA_MEM_NULL The ida_mem pointer is NULL.

Notes The nrevals value returned by IDAGetNumResEvals does not account for calls made to

res from a linear solver or preconditioner module.

IDAGetNumLinSolvSetups

Call flag = IDAGetNumLinSolvSetups(ida_mem, &nlinsetups);

Description The function IDAGetNumLinSolvSetups returns the cumulative number of calls made

to the linear solver's setup function (total so far).

Arguments ida_mem (void *) pointer to the IDA memory block.

nlinsetups (long int) number of calls made to the linear solver setup function.

Return value The return value flag (of type int) is one of

IDA_SUCCESS The optional output value has been successfuly set.

IDA_MEM_NULL The ida_mem pointer is NULL.

IDAGetNumErrTestFails

Call flag = IDAGetNumErrTestFails(ida_mem, &netfails);

Description The function IDAGetNumErrTestFails returns the cumulative number of local error

test failures that have occurred (total so far).

Arguments ida_mem (void *) pointer to the IDA memory block.

netfails (long int) number of error test failures.

Return value The return value flag (of type int) is one of

IDA_SUCCESS The optional output value has been successfuly set.

IDA_MEM_NULL The ida_mem pointer is NULL.

IDAGetLastOrder

Call flag = IDAGetLastOrder(ida_mem, &qlast);

Description The function IDAGetLastOrder returns the integration method order used during the

last internal step.

Arguments ida_mem (void *) pointer to the IDA memory block.

qlast (int) method order used on the last internal step.

Return value The return value flag (of type int) is one of

IDA_SUCCESS The optional output value has been successfuly set.

IDA_MEM_NULL The ida_mem pointer is NULL.

IDAGetCurrentOrder

Call flag = IDAGetCurrentOrder(ida_mem, &qcur);

Description The function IDAGetCurrentOrder returns the integration method order to be used on

the next internal step.

Arguments ida_mem (void *) pointer to the IDA memory block.

qcur (int) method order to be used on the next internal step.

Return value The return value flag (of type int) is one of

IDA_SUCCESS The optional output value has been successfuly set.

IDA_MEM_NULL The ida_mem pointer is NULL.

IDAGetLastStep

Call flag = IDAGetLastStep(ida_mem, &hlast);

Description The function IDAGetLastStep returns the integration step size taken on the last internal

step.

Arguments ida_mem (void *) pointer to the IDA memory block.

hlast (realtype) step size taken on the last internal step.

Return value The return value flag (of type int) is one of

IDA_SUCCESS The optional output value has been successfuly set.

IDA_MEM_NULL The ida_mem pointer is NULL.

IDAGetCurrentStep

Call flag = IDAGetCurrentStep(ida_mem, &hcur);

Description The function IDAGetCurrentStep returns the integration step size to be attempted on

the next internal step.

Arguments ida_mem (void *) pointer to the IDA memory block.

hcur (realtype) step size to be attempted on the next internal step.

Return value The return value flag (of type int) is one of

IDA_SUCCESS The optional output value has been successfuly set.

IDA_MEM_NULL The ida_mem pointer is NULL.

IDAGetActualInitStep

Call flag = IDAGetActualInitStep(ida_mem, &hinused);

Description The function IDAGetActualInitStep returns the value of the integration step size used

on the first step.

Arguments ida_mem (void *) pointer to the IDA memory block.

hinused (realtype) actual value of initial step size.

Return value The return value flag (of type int) is one of

IDA_SUCCESS The optional output value has been successfuly set.

IDA_MEM_NULL The ida_mem pointer is NULL.

Notes Even if the value of the initial integration step size was specified by the user through a

call to IDASetInitStep, this value might have been changed by IDA to ensure that the step size is within the prescribed bounds $(h_{\min} \leq h_0 \leq h_{\max})$, or to meet the local error

test.

IDAGetCurrentTime

Call flag = IDAGetCurrentTime(ida_mem, &tcur);

Description The function IDAGetCurrentTime returns the current internal time reached by the

solver.

Arguments ida_mem (void *) pointer to the IDA memory block.

tcur (realtype) current internal time reached.

Return value The return value flag (of type int) is one of

IDA_SUCCESS The optional output value has been successfuly set.

IDA_MEM_NULL The ida_mem pointer is NULL.

IDAGetTolScaleFactor

Call flag = IDAGetTolScaleFactor(ida_mem, &tolsfac);

Description The function IDAGetTolScaleFactor returns a suggested factor by which the user's

tolerances should be scaled when too much accuracy has been requested for some internal

step.

Arguments ida_mem (void *) pointer to the IDA memory block.

tolsfac (realtype) suggested scaling factor for user tolerances.

Return value The return value flag (of type int) is one of

IDA_SUCCESS The optional output value has been successfuly set.

IDA_MEM_NULL The ida_mem pointer is NULL.

IDAGetErrWeights

Call flag = IDAGetErrWeights(ida_mem, eweight);

Description The function IDAGetErrWeights returns the solution error weights at the current time.

These are the W_i given by Eq. (3.6) (or by the user's IDAEwtFn).

Arguments ida_mem (void *) pointer to the IDA memory block.

eweight (N_Vector) solution error weights at the current time.

Return value The return value flag (of type int) is one of

IDA_SUCCESS The optional output value has been successfuly set.

IDA_MEM_NULL The ida_mem pointer is NULL.

Notes The user must allocate space for eweight.

IDAGetEstLocalErrors

Call flag = IDAGetEstLocalErrors(ida_mem, ele);

Description The function IDAGetEstLocalErrors returns the estimated local errors.

Arguments ida_mem (void *) pointer to the IDA memory block.

eweight (N_Vector) estimated local errors at the current time.

Return value The return value flag (of type int) is one of

IDA_SUCCESS The optional output value has been successfuly set.

IDA_MEM_NULL The ida_mem pointer is NULL.

Notes The user must allocate space for ele.

The values returned in ele are only valid if IDASolve returned a positive value.

The ele vector, together with the eweight vector from IDAGetErrWeights, can be used to determine how the various components of the system contributed to the estimated





local error test. Specifically, that error test uses the RMS norm of a vector whose components are the products of the components of the two vectors. Thus, for example, if there were recent error test failures, the components causing the failures are those with largest values for the products, denoted loosely as eweight[i]*ele[i].

IDAGetIntegratorStats

Call flag = IDAGetIntegratorStats(ida_mem, &nsteps, &nrevals, &nlinsetups, &netfails, &qlast, &qcur, &hinused, &hlast, &hcur, &tcur);

Description The function IDAGetIntegratorStats returns the IDA integrator statistics as a group.

Arguments ida_mem (void *) pointer to the IDA memory block.

nsteps (long int) cumulative number of steps taken by IDA.

nrevals (long int) cumulative number of calls to the user's res function.

nlinsetups (long int) cumulative number of calls made to the linear solver setup

function.

netfails (long int) cumulative number of error test failures.
qlast (int) method order used on the last internal step.

qcur (int) method order to be used on the next internal step.

hinused (realtype) actual value of initial step size.

hlast (realtype) step size taken on the last internal step.

hcur (realtype) step size to be attempted on the next internal step.

tcur (realtype) current internal time reached.

Return value The return value flag (of type int) is one of

IDA_SUCCESS the optional output values have been successfuly set.

IDA_MEM_NULL the ida_mem pointer is NULL.

IDAGetNumNonlinSolvIters

Call flag = IDAGetNumNonlinSolvIters(ida_mem, &nniters);

Description The function IDAGetNumNonlinSolvIters returns the cumulative number of nonlinear

(functional or Newton) iterations performed.

Arguments ida_mem (void *) pointer to the IDA memory block.

nniters (long int) number of nonlinear iterations performed.

Return value The return value flag (of type int) is one of

IDA_SUCCESS The optional output value has been successfuly set.

IDA_MEM_NULL The ida_mem pointer is NULL.

IDAGetNumNonlinSolvConvFails

Call flag = IDAGetNumNonlinSolvConvFails(ida_mem, &nncfails);

Description The function IDAGetNumNonlinSolvConvFails returns the cumulative number of non-

linear convergence failures that have occurred.

Arguments ida_mem (void *) pointer to the IDA memory block.

nncfails (long int) number of nonlinear convergence failures.

Return value The return value flag (of type int) is one of

IDA_SUCCESS The optional output value has been successfuly set.

IDA_MEM_NULL The ida_mem pointer is NULL.

IDAGetNonlinSolvStats

Call flag = IDAGetNonlinSolvStats(ida_mem, &nniters, &nncfails);

Description The function IDAGetNonlinSolvStats returns the IDA nonlinear solver statistics as a

group.

Arguments ida_mem (void *) pointer to the IDA memory block.

nniters (long int) cumulative number of nonlinear iterations performed. nncfails (long int) cumulative number of nonlinear convergence failures.

Return value The return value flag (of type int) is one of

IDA_SUCCESS The optional output value has been successfuly set.

IDA_MEM_NULL The ida_mem pointer is NULL.

IDAGetReturnFlagName

Description The function IDAGetReturnFlagName returns the name of the IDA constant correspond-

ing to flag.

Arguments The only argument, of type int is a return flag from a IDA function.

Return value The return value is a string containing the name of the corresponding constant.

5.5.8.2 Linear solver optional output functions

For each of the linear system solver modules, there are various optional outputs that describe the performance of the module. The functions available to access these are described below. Where the name of an output would otherwise conflict with the name of an optional output from the main solver, a suffix LS (for Linear Solver) has been added here (e.g. lenrwLS).

5.5.8.3 Dense linear solver

The following optional outputs are available from the IDADENSE module: workspace requirements, number of calls to the Jacobian routine, number of calls to the residual routine for finite-difference Jacobian approximation, and last return value from a IDADENSE function.

IDADenseGetWorkSpace

Call flag = IDADenseGetWorkSpace(ida_mem, &lenrwLS, &leniwLS);

Description The function IDADenseGetWorkSpace returns the sizes of the IDADENSE real and integer

workspaces.

Arguments ida_mem (void *) pointer to the IDA memory block.

lenrwLS (long int) the number of real values in the IDADENSE workspace.

leniwLS (long int) the number of integer values in the IDADENSE workspace.

Return value The return value flag (of type int) is one of

IDA_SUCCESS The optional output value has been successfuly set.

IDA_MEM_NULL The ida_mem pointer is NULL.

IDA_MEM_NULL The IDADENSE linear solver has not been initialized.

Notes In terms of the problem size N, the actual size of the real workspace is $2N^2$ realtype

words. The actual size of the integer workspace is N integer words.

IDADenseGetNumJacEvals

Call flag = IDADenseGetNumJacEvals(ida_mem, &njevals);

Description The function IDADenseGetNumJacEvals returns the cumulative number of calls to the

dense Jacobian approximation function.

Arguments ida_mem (void *) pointer to the IDA memory block.

njevals (long int) the cumulative number of calls to the Jacobian function (total so

far).

Return value The return value flag (of type int) is one of

IDADENSE_SUCCESS The optional output value has been successfuly set.

IDADENSE_MEM_NULL The ida_mem pointer is NULL.

IDADENSE_LMEM_NULL The IDADENSE linear solver has not been initialized.

IDADenseGetNumResEvals

Call flag = IDADenseGetNumResEvals(ida_mem, &nrevalsLS);

Description The function IDADenseGetNumResEvals returns the cumulative number of calls to the

user residual function due to the finite difference dense Jacobian approximation.

Arguments ida_mem (void *) pointer to the IDA memory block.

nrevalsLS (long int) the cumulative number of calls to the user residual function.

Return value The return value flag (of type int) is one of

IDADENSE_SUCCESS The optional output value has been successfully set.

IDADENSE_MEM_NULL The ida_mem pointer is NULL.

IDADENSE_LMEM_NULL The IDADENSE linear solver has not been initialized.

Notes The value nrevalsLS is incremented only if the default IDADenseDQJac difference quo-

tient function is used.

IDADenseGetLastFlag

Call flag = IDADenseGetLastFlag(ida_mem, &flag);

Description The function IDADenseGetLastFlag returns the last return value from an IDADENSE

routine.

Arguments ida_mem (void *) pointer to the IDA memory block.

flag (int) the value of the last return flag from an IDADENSE function.

Return value The return value flag (of type int) is one of

IDADENSE_SUCCESS The optional output value has been successfully set.

IDADENSE_MEM_NULL The ida_mem pointer is NULL.

IDADENSE_LMEM_NULL The IDADENSE linear solver has not been initialized.

Notes If the IDADENSE setup function failed (IDASolve returned IDALSETUP_FAIL), the value

flag is equal to the column index (numbered from one) at which a zero diagonal element

was encountered during the LU factorization of the dense Jacobian matrix.

${\tt IDADenseGetReturnFlagName}$

Description The function IDADenseGetReturnFlagName returns the name of the CVDENSE constant

corresponding to flag.

Arguments The only argument, of type int is a return flag from a CVDENSE function.

Return value The return value is a string containing the name of the corresponding constant.

5.5.8.4 Band linear solver

The following optional outputs are available from the IDABAND module: workspace requirements, number of calls to the Jacobian routine, number of calls to the residual routine for finite-difference Jacobian approximation, and last return value from a IDABAND function.

IDABandGetWorkSpace

Call flag = IDABandGetWorkSpace(ida_mem, &lenrwLS, &leniwLS);

Description The function IDABandGetWorkSpace returns the sizes of the IDABAND real and integer

workspaces.

Arguments ida_mem (void *) pointer to the IDA memory block.

lenrwKS (long int) the number of real values in the IDABAND workspace.

leniwLS (long int) the number of integer values in the IDABAND workspace.

Return value The return value flag (of type int) is one of

IDABAND_SUCCESS The optional output value has been successfuly set.

IDABAND_MEM_NULL The ida_mem pointer is NULL.

IDABAND_LMEM_NULL The IDABAND linear solver has not been initialized.

Notes In terms of the problem size N and Jacobian half-bandwidths, the actual size of the

real workspace is N(2 mupper + 3 mlower + 2) realtype words. The actual size of the

integer workspace is N integer words.

IDABandGetNumJacEvals

Call flag = IDABandGetNumJacEvals(ida_mem, &njevals);

Description The function IDABandGetNumJacEvals returns the cumulative number of calls to the

banded Jacobian approximation function.

Arguments ida_mem (void *) pointer to the IDA memory block.

njevals (long int) the cumulative number of calls to the Jacobian function.

Return value The return value flag (of type int) is one of

IDABAND_SUCCESS The optional output value has been successfuly set.

IDABAND_MEM_NULL The ida_mem pointer is NULL.

IDABAND_LMEM_NULL The IDABAND linear solver has not been initialized.

IDABandGetNumResEvals

Call flag = IDABandGetNumResEvals(ida_mem, &nrevalsLS);

Description The function IDABandGetNumResEvals returns the cumulative number of calls to the

user residual function due to the finite difference banded Jacobian approximation.

Arguments ida_mem (void *) pointer to the IDA memory block.

nrevalsLS (long int) the cumulative number of calls to the user residual function.

Return value The return value flag (of type int) is one of

IDA_SUCCESS The optional output value has been successfuly set.

IDABAND_MEM_NULL The ida_mem pointer is NULL.

IDABAND_LMEM_NULL The IDABAND linear solver has not been initialized.

Notes The value nrevalsLS is incremented only if the default IDABandDQJac difference quo-

tient function is used.

IDABandGetLastFlag

Call flag = IDABandGetLastFlag(ida_mem, &flag);

Description The function IDABandGetLastFlag returns the last return value from an IDABAND rou-

tine.

Arguments ida_mem (void *) pointer to the IDA memory block.

flag (int) the value of the last return flag from an IDABAND function.

Return value The return value flag (of type int) is one of

IDABAND_SUCCESS The optional output value has been successfully set.

IDABAND_MEM_NULL The ida_mem pointer is NULL.

IDABAND_LMEM_NULL The IDABAND linear solver has not been initialized.

Notes If the IDABAND setup function failed (IDASolve returned IDALSETUP_FAIL), the value

flag is equal to the column index (numbered from one) at which a zero diagonal element

was encountered during the LU factorization of the banded Jacobian matrix.

IDABandGetReturnFlagName

Description The function IDABandGetReturnFlagName returns the name of the CVBAND constant

corresponding to flag.

Arguments The only argument, of type int is a return flag from a CVBAND function.

Return value The return value is a string containing the name of the corresponding constant.

5.5.8.5 SPILS linear solvers

The following optional outputs are available from the IDASPILS modules: workspace requirements, number of linear iterations, number of linear convergence failures, number of calls to the preconditioner setup and solve routines, number of calls to the Jacobian-vector product routine, number of calls to the residual routine for finite-difference Jacobian-vector product approximation, and last return value from a linear solver function.

IDASpilsGetWorkSpace

Call flag = IDASpilsGetWorkSpace(ida_mem, &lenrwLS, &leniwLS);

Description The function IDASpilsGetWorkSpace returns the global sizes of the IDASPGMR real and

integer workspaces.

Arguments ida_mem (void *) pointer to the IDA memory block.

 ${\tt lenrwLS}$ (long int) global number of real values in the <code>IDASPILS</code> workspace.

leniwLS (long int) global number of integer values in the idaspils workspace.

Return value The return value flag (of type int) is one of

IDASPILS_SUCCESS The optional output value has been successfuly set.

IDASPILS_MEM_NULL The ida_mem pointer is NULL.

IDASPILS_LMEM_NULL The IDASPILS linear solver has not been initialized.

Notes In terms of the problem size N and maximum subspace size max1, the actual size of the

real workspace is roughly:

 $N*(\max 1+5)+\max 1*(\max 1+4)+1$ realtype words for IDASPGMR,

10 * N realtype words for IDASPBCG,

and 13*N realtype words for IDASPTFQMR.

In a parallel setting, the above values are global — summed over all processors.

IDASpilsGetNumLinIters

Call flag = IDASpilsGetNumLinIters(ida_mem, &nliters);

Description The function IDASpilsGetNumLinIters returns the cumulative number of linear itera-

tions.

Arguments ida_mem (void *) pointer to the IDA memory block.

nliters (long int) the current number of linear iterations.

Return value The return value flag (of type int) is one of

IDASPILS_SUCCESS The optional output value has been successfuly set.

IDASPILS_MEM_NULL The ida_mem pointer is NULL.

IDASPILS_LMEM_NULL The IDASPILS linear solver has not been initialized.

IDASpilsGetNumConvFails

Call flag = IDASpilsGetNumConvFails(ida_mem, &nlcfails);

Description The function IDASpilsGetNumConvFails returns the cumulative number of linear con-

vergence failures.

Arguments ida_mem (void *) pointer to the IDA memory block.

nlcfails (long int) the current number of linear convergence failures.

Return value The return value flag (of type int) is one of

IDASPILS_SUCCESS The optional output value has been successfuly set.

IDASPILS_MEM_NULL The ida_mem pointer is NULL.

IDASPILS_LMEM_NULL The IDASPILS linear solver has not been initialized.

IDASpilsGetNumPrecEvals

Call flag = IDASpilsGetNumPrecEvals(ida_mem, &npevals);

Description The function IDASpilsGetNumPrecEvals returns the cumulative number of precondi-

tioner evaluations, i.e., the number of calls made to psetup.

Arguments ida_mem (void *) pointer to the IDA memory block.

npevals (long int) the cumulative number of calls to psetup.

Return value The return value flag (of type int) is one of

IDASPILS_SUCCESS The optional output value has been successfuly set.

IDASPILS_MEM_NULL The ida_mem pointer is NULL.

IDASPILS_LMEM_NULL The IDASPILS linear solver has not been initialized.

IDASpilsGetNumPrecSolves

Call flag = IDASpilsGetNumPrecSolves(ida_mem, &npsolves);

Description The function IDASpilsGetNumPrecSolves returns the cumulative number of calls made

to the preconditioner solve function, psolve.

Arguments ida_mem (void *) pointer to the IDA memory block.

npsolves (long int) the cumulative number of calls to psolve.

Return value The return value flag (of type int) is one of

IDASPILS_SUCCESS The optional output value has been successfuly set.

IDASPILS_MEM_NULL The ida_mem pointer is NULL.

IDASPILS_LMEM_NULL The IDASPILS linear solver has not been initialized.

IDASpilsGetNumJtimesEvals

Call flag = IDASpilsGetNumJtimesEvals(ida_mem, &njvevals);

Description The function IDASpilsGetNumJtimesEvals returns the cumulative number of calls

made to the Jacobian-vector function, jtimes.

Arguments ida_mem (void *) pointer to the IDA memory block.

njvevals (long int) the cumulative number of calls to jtimes.

Return value The return value flag (of type int) is one of

IDASPILS_SUCCESS The optional output value has been successfuly set.

IDASPILS_MEM_NULL The ida_mem pointer is NULL.

IDASPILS_LMEM_NULL The IDASPILS linear solver has not been initialized.

IDASpilsGetNumResEvals

Call flag = IDASpilsGetNumResEvals(ida_mem, &nrevalsLS);

Description The function IDASpilsGetNumResEvals returns the cumulative number of calls to the

user residual function for finite difference Jacobian-vector product approximation.

Arguments ida_mem (void *) pointer to the IDA memory block.

nrevalsLS (long int) the cumulative number of calls to the user residual function.

Return value The return value flag (of type int) is one of

IDASPILS_SUCCESS The optional output value has been successfuly set.

IDASPILS_MEM_NULL The ida_mem pointer is NULL.

IDASPILS_LMEM_NULL The IDASPILS linear solver has not been initialized.

Notes The value nrevalsLS is incremented only if the default IDASpilsDQJtimes difference

quotient function is used.

IDASpilsGetLastFlag

Call flag = IDASpilsGetLastFlag(ida_mem, &flag);

Description The function IDASpilsGetLastFlag returns the last return value from an IDASPILS

routine.

Arguments ida_mem (void *) pointer to the IDA memory block.

flag (int) the value of the last return flag from an IDASPILS function.

Return value The return value flag (of type int) is one of

IDASPILS_SUCCESS The optional output value has been successfully set.

IDASPILS_MEM_NULL The ida_mem pointer is NULL.

IDASPILS_LMEM_NULL The IDASPILS linear solver has not been initialized.

Notes If the IDASPILS setup function failed (IDASolve returned IDALSETUP_FAIL), flag will be SPGMR_PSET_FAIL_UNREC, SPBCG_PSET_FAIL_UNREC, or SPTFQMR_PSET_FAIL_UNREC.

If the IDASPGMR solve function failed (IDASolve returned IDA_LSOLVE_FAIL), flag contains the error return flag from SpgmrSolve and will be one of: SPGMR_MEM_NULL, indicating that the SPGMR memory is NULL; SPGMR_ATIMES_FAIL_UNREC, indicating an unrecoverable failure in the J*v function; SPGMR_PSOLVE_FAIL_UNREC, indicating that the preconditioner solve function psolve failed unrecoverably; SPGMR_GS_FAIL, indicating a failure in the Gram-Schmidt procedure; or SPGMR_QRSOL_FAIL, indicating that the matrix R was found to be singular during the QR solve phase.

If the IDASPBCG solve function failed (IDASolve returned IDA_LSOLVE_FAIL), flag contains the error return flag from SpbcgSolve and will be one of: SPBCG_MEM_NULL, indicating that the SPBCG memory is NULL; SPBCG_ATIMES_FAIL_UNREC, indicating an unrecoverable failure in the J*v function; or SPBCG_PSOLVE_FAIL_UNREC, indicating that the preconditioner solve function psolve failed unrecoverably.

If the IDASPTFQMR solve function failed (IDASolve returned IDA_LSOLVE_FAIL), flag contains the error flag from SptfqmrSolve and will be one of: SPTFQMR_MEM_NULL, indicating that the SPTFQMR memory is NULL; SPTFQMR_ATIMES_FAIL_UNREC, indicating an unrecoverable failure in the J*v function; or SPTFQMR_PSOLVE_FAIL_UNREC, indicating that the preconditioner solve function psolve failed unrecoverably.

IDASpilsGetReturnFlagName

Call name = IDASpilsGetReturnFlagName(flag);

 $\label{thm:local_decomposition} \textbf{Description} \quad \textbf{The function $\tt IDASpilsGetReturnFlagName$ returns the name of the CVSPILS constant}$

corresponding to flag.

Arguments The only argument, of type int is a return flag from a CVSPILS function.

Return value The return value is a string containing the name of the corresponding constant.

5.5.9 IDA reinitialization function

The function IDAReInit reinitializes the main IDA solver for the solution of a problem, where a prior call to IDAMalloc has been made. The new problem must have the same size as the previous one. IDAReInit performs the same input checking and initializations that IDAMalloc does, but does no memory allocation, assuming that the existing internal memory is sufficient for the new problem.

The use of IDAReInit requires that the maximum method order, maxord, is no larger for the new problem than for the problem specified in the last call to IDAMalloc. In addition, the same NVECTOR module set for the previous problem will be reused for the new problem.

If there are changes to the linear solver specifications, make the appropriate Set calls, as described in §5.5.3.

IDAReInit

Call flag = IDAReInit(ida_mem, res, t0, y0, yp0, itol, reltol, abstol);

Description The function IDAReInit provides required problem specifications and reinitializes IDA.

Arguments ida_mem (void *) pointer to the IDA memory block.

res (IDAResFn) is the C function which computes F. This function has the form $f(t, y, yp, r, res_data)$ (for full details see §5.6).

to (realtype) is the initial value of t.

y0 (N_Vector) is the initial value of y.

yp0 (N_Vector) is the initial value of y'.

(int) is one of IDA_SS, IDA_SV, or IDA_WF, where IDA_SS indicates scalar relative error tolerance and scalar absolute error tolerance, while IDA_SV indicates scalar relative error tolerance and vector absolute error tolerance. The latter choice is important when the absolute error tolerance needs to be different for each component of the DAE. If itol=IDA_WF, the arguments reltol and abstol are ignored and the user is expected to provide a function to evaluate the error weight vector W as an alternative to Eq. (3.6). See IDASetEwtFn in §5.5.6.1.

reltol (realtype) is the relative error tolerance.

Notes

abstol (void *) is a pointer to the absolute error tolerance. If itol=IDA_SS, abstol must be a pointer to a realtype variable. If itol=IDA_SV, abstol must be an N_Vector variable.

Return value The return flag flag (of type int) will be one of the following:

IDA_SUCCESS The call to IDAReInit was successful.

IDA_MEM_NULL The IDA memory block was not initialized through a previous call to

IDACreate.

IDA_NO_MALLOC Memory space for the IDA memory block was not allocated through a

previous call to IDAMalloc.

IDA_ILL_INPUT An input argument to IDAReInit has an illegal value.

If an error occurred, IDAReInit also sends an error message to the error handler func-

tion.

It is the user's responsibility to provide compatible itol and abstol arguments.



5.6 User-supplied functions

The user-supplied functions consist of one function defining the DAE residual, (optionally) a function that provides the error weight vector, (optionally) a function that provides Jacobian-related information for the linear solver (if Newton iteration is chosen), and (optionally) one or two functions that define the preconditioner for use in any of the Krylov iteration algorithms.

5.6.1 Residual function

The user must provide a function of type IDAResFn defined as follows:

IDAResFn

Definition typedef int (*IDAResFn)(realtype tt, N_Vector yy, N_Vector yp, N_Vector rr, void *res_data);

Purpose This function computes the problem residual for given values of the independent variable t, state vector y, and derivative y'.

Arguments tt is the current value of the independent variable.

yy is the current value of the dependent variable vector, y(t).

yp is the current value of y'(t).

rr is the output residual vector F(t, y, y').

res_data is a pointer to user data — the same as the res_data parameter passed to IDASetRdata.

Return value An IDAResFn function type should return a value of 0 if successful, a positive value if a recoverable error occured (e.g. yy has an illegal value), or a negative value if a nonrecoverable error occured.

In the latter case, the integrator halts. If a recoverable error occured, the integrator will attempt to correct and retry.

Notes Allocation of memory for yp is handled within IDA.

5.6.2 Error message handler function

As an alternative to the default behavior of directing error and warning messages to the file pointed to by errfp (see IDASetErrFile), the user may provide a function of type IDAErrHandlerFn to process any such messages. The function type IDAErrHandlerFn is defined as follows:

IDAErrHandlerFn

Definition typedef void (*IDAErrHandlerFn)(int error_code,

const char *module, const char *function,
char *msg, void *eh_data);

Purpose This function processes error and warning messages from IDA and its sub-modules.

Arguments error_code is the error code.

module is the name of the IDA module reporting the error.

function is the name of the function in which the error occurred.

msg is the error message.

eh_data is a pointer to user data, the same as the eh_data parameter passed to

IDASetErrHandlerFn.

Return value A IDAErrHandlerFn function has no return value.

Notes error_code is negative for errors and positive (IDA_WARNING) for warnings. If a function

returning a pointer to memory (e.g. IDABBDPrecAlloc) encounters an error, it sets

error_code to 0 before returning NULL.

5.6.3 Error weight function

As an alternative to providing the relative and absolute tolerances, the user may provide a function of type IDAEwtFn to compute a vector ewt containing the multiplicative weights W_i used in the WRMS norm $||v||_{\text{WRMS}} = \sqrt{(1/N)\sum_1^N (W_i \cdot v_i)^2}$. These weights will used in place of those defined by Eq. (3.6). The function type IDAEwtFn is defined as follows:

IDAEwtFn

Definition typedef int (*IDAEwtFn)(N_Vector y, N_Vector ewt, void *e_data);

Purpose This function computes the WRMS error weights for the vector y.

Arguments y is the value of the vector for which the WRMS norm must be computed.

ewt is the output vector containing the error weights.

e_data is a pointer to user data — the same as the e_data parameter passed to

 ${\tt IDASetEwtFn}.$

Return value An IDAEwtFn function type must return 0 if it successfully set the error weights and -1

otherwise. In case of failure, a message is printed and the integration stops.

Notes Allocation of memory for ewt is handled within IDA.

The error weight vector must have all components positive. It is the user's responsibility

to perform this test and return -1 if it is not satisfied.

5.6.4 Jacobian information (direct method with dense Jacobian)

If the direct linear solver with dense treatment of the Jacobian is used (i.e. IDADense is called in Step 7 of §5.4), the user may provide a function of type IDADenseJacFn defined by

IDADenseJacFn

Purpose This function computes the dense Jacobian J of the DAE system (or an approximation

to it), defined by Eq. (3.5).



Arguments Neq is the problem size (number of equations).

tt is the current value of the independent variable t.

yy is the current value of the dependent variable vector, y(t).

yp is the current value of y'(t).

rr is the current value of the residual vector F(t, y, y').

c_j is the scalar in the system Jacobian, proportional to the inverse of the step size (α in Eq. (3.5)).

jac_data is a pointer to user data — the same as the jac_data parameter passed to IDADenseSetJacFn.

Jac is the output Jacobian matrix.

tmp1

tmp2

tmp3 are pointers to memory allocated for variables of type N_Vector which can be used by IDADenseJacFn as temporary storage or work space.

Return value An IDADenseJacFn function type should return 0 if successful, a positive value if a recoverable error occured, or a negative value if a nonrecoverable error occured.

In the case of a recoverable error return, the integrator will attempt to recover by reducing the stepsize, and hence changing α in (3.5).

Notes

A user-supplied dense Jacobian function must load the Neq \times Neq dense matrix Jac with an approximation to the Jacobian matrix J at the point (tt, yy, yp). Only nonzero elements need to be loaded into Jac because Jac is set to the zero matrix before the call to the Jacobian function. The type of Jac is DenseMat (described below and in $\S 9.1$).

The accessor macros DENSE_ELEM and DENSE_COL allow the user to read and write dense matrix elements without making explicit references to the underlying representation of the DenseMat type. DENSE_ELEM(Jac, i, j) references the (i, j)-th element of the dense matrix Jac (i, j= 0... Neq-1). This macro is for use in small problems in which efficiency of access is not a major concern. Thus, in terms of indices m and n running from 1 to Neq, the Jacobian element $J_{m,n}$ can be loaded with the statement DENSE_ELEM(Jac, m-1, n-1) = $J_{m,n}$. Alternatively, DENSE_COL(Jac, j) returns a pointer to the storage for the jth column of Jac (j= 0... Neq-1), and the elements of the j-th column are then accessed via ordinary array indexing. Thus $J_{m,n}$ can be loaded with the statements col_n = DENSE_COL(Jac, n-1); col_n[m-1] = $J_{m,n}$. For large problems, it is more efficient to use DENSE_COL than to use DENSE_ELEM. Note that both of these macros number rows and columns starting from 0, not 1.

The DenseMat type and the accessor macros DENSE_ELEM and DENSE_COL are documented in §9.1.

If the user's IDADenseJacFn function uses difference quotient approximations, it may need to access quantities not in the call list. These include the current stepsize, the error weights, etc. To obtain these, use the IDAGet* functions described in §5.5.8.1. The unit roundoff can be accessed as UNIT_ROUNDOFF defined in sundials_types.h.

5.6.5 Jacobian information (direct method with banded Jacobian)

If the direct linear solver with banded treatment of the Jacobian is used (i.e. IDABand is called in Step 7 of §5.4), the user may provide a function of type IDABandJacFn defined as follows:

tmp3

Definition typedef int (*IDABandJacFn)(long int Neq, long int mupper, long int mlower, realtype tt, N_Vector yy, N_Vector yp, N_Vector rr, realtype c_j, void *jac_data, BandMat Jac, N_Vector tmp1, N_Vector tmp2, N_Vector tmp3); Purpose This function computes the banded Jacobian J of the DAE system (or a banded approximation to it), defined by Eq. (3.5). Arguments Neq is the problem size. mlower are the lower and upper half bandwidth of the Jacobian. mupper is the current value of the independent variable. tt is the current value of the dependent variable vector, y(t). уу is the current value of y'(t). ур is the current value of the residual vector F(t, y, y'). rr is the scalar in the system Jacobian, proportional to the inverse of the step c_j size (α in Eq. (3.5)). jac_data is a pointer to user data — the same as the jac_data parameter passed to IDABandSetJacFn. is the output Jacobian matrix. Jac tmp1 tmp2

Return value A IDABandJacFn function type should return 0 if successful, a positive value if a recoverable error occured, or a negative value if a nonrecoverable error occured.

In the case of a recoverable error return, the integrator will attempt to recover by reducing the stepsize, and hence changing α in (3.5).

be used by IDABandJacFn as temporary storage or work space.

are pointers to memory allocated for variables of type N_Vector which can

Notes

A user-supplied band Jacobian function must load the band matrix \mathtt{Jac} of type $\mathtt{BandMat}$ with the elements of the Jacobian J(t,y,y') at the point ($\mathtt{tt},\mathtt{yy},\mathtt{yp}$). Only nonzero elements need to be loaded into \mathtt{Jac} because \mathtt{Jac} is preset to zero before the call to the Jacobian function.

The accessor macros BAND_ELEM, BAND_COL, and BAND_COL_ELEM allow the user to read and write band matrix elements without making specific references to the underlying representation of the BandMat type. BAND_ELEM(Jac, i, j) references the (i, j)th element of the band matrix Jac, counting from 0. This macro is for use in small problems in which efficiency of access is not a major concern. Thus, in terms of indices m and n running from 1 to Neq with (m,n) within the band defined by mupper and mlower, the Jacobian element $J_{m,n}$ can be loaded with the statement BAND_ELEM(Jac, m-1, n-1) = $J_{m,n}$. The elements within the band are those with -mupper \leq m-n \leq mlower. Alternatively, BAND_COL(Jac, j) returns a pointer to the diagonal element of the jth column of Jac, and if we assign this address to realtype *col_j, then the ith element of the jth column is given by BAND_COL_ELEM(col_j, i, j), counting from 0. Thus for (m, n) within the band, $J_{m,n}$ can be loaded by setting col_n = BAND_COL(Jac, n-1); BAND_COL_ELEM(col_n, m-1, n-1) = $J_{m,n}$. The elements of the jth column can also be accessed via ordinary array indexing, but this approach requires knowledge of the underlying storage for a band matrix of type BandMat. The array col_n can be indexed from -mupper to mlower. For large problems, it is more efficient to use the combination of BAND_COL and BAND_COL_ELEM than to use the BAND_ELEM. As in the dense case, these macros all number rows and columns starting from 0, not 1.

The BandMat type and the accessor macros BAND_ELEM, BAND_COL, and BAND_COL_ELEM are documented in $\S 9.2$.

If the user's IDABandJacFn function uses difference quotient approximations, it may need to access quantities not in the call list. These include the current stepsize, the error weights, etc. To obtain these, use the IDAGet* functions described in §5.5.8.1. The unit roundoff can be accessed as UNIT_ROUNDOFF defined in sundials_types.h.

5.6.6 Jacobian information (matrix-vector product)

If one of the Krylov iterative linear solvers SPGMR, SPBCG, or SPTFQMR is selected (IDASp* is called in step 7 of §5.4), the user may provide a function of type IDASpilsJacTimesVecFn in the following form:

```
IDASpilsJacTimesVecFn
Definition
             typedef int (*IDASpilsJacTimesVecFn)(realtype tt, N_Vector yy,
                                                         N_Vector yp, N_Vector rr,
                                                         N_Vector v, N_Vector Jv,
                                                         realtype c_j, void *jac_data,
                                                         N_Vector tmp1, N_Vector tmp2);
             This function computes the product Jv of the DAE system Jacobian J (or an approxi-
Purpose
             mation to it) and a given vector \mathbf{v}, where J is defined by Eq. (3.5).
                        is the current value of the independent variable.
Arguments
             tt
                        is the current value of the dependent variable vector, y(t).
             уу
             ур
                        is the current value of y'(t).
                        is the current value of the residual vector F(t, y, y').
             rr
                        is the vector by which the Jacobian must be multiplied to the right.
             V
             .Tv
                        is the output vector computed.
                       is the scalar in the system Jacobian, proportional to the inverse of the step
             c_j
                        size (\alpha in Eq. (3.5)).
             jac_data is a pointer to user data — the same as the jac_data parameter passed to
                        IDASp*SetJacTimesVecFn.
             tmp1
                        are pointers to memory allocated for variables of type N_Vector which can
             tmp2
                        be used by IDASpilsJacTimesVecFn as temporary storage or work space.
Return value The value to be returned by the Jacobian-times-vector function should be 0 if successful.
             A nonzero value indicates that a nonrecoverable error occurred.
             If the user's IDASpilsJacTimesVecFn function uses difference quotient approximations,
             it may need to access quantities not in the call list. These include the current stepsize,
```

5.6.7 Preconditioning (linear system solution)

If preconditioning is used, then the user must provide a C function to solve the linear system Pz=r where P is a left preconditioner matrix which approximates (at least crudely) the Jacobian matrix $J=\partial F/\partial y+c_j\partial F/\partial y'$. This function must be of type IDASpilsPrecSolveFn, defined as follows:

the error weights, etc. To obtain these, use the IDAGet* functions described in §5.5.8.1. The unit roundoff can be accessed as UNIT_ROUNDOFF defined in sundials_types.h.

```
IDASpilsPrecSolveFn
```

```
Definition typedef int (*IDASpilsPrecSolveFn)(realtype tt, N_Vector yy, N_Vector yp, N_Vector rr, N_Vector rvec, N_Vector zvec, realtype c_j, realtype delta, void *p_data, N_Vector tmp);
```

Purpose This function solves the preconditioning system Pz = r.

Arguments

- tt is the current value of the independent variable.
- yy is the current value of the dependent variable vector, y(t).
- yp is the current value of y'(t).
- rr is the current value of the residual vector F(t, y, y').
- rvec is the right-hand side vector r of the linear system to be solved.
- zvec is the output vector computed.
- c_j is the scalar in the system Jacobian, proportional to the inverse of the step size $(\alpha \text{ in Eq. } (3.5))$.
- delta is an input tolerance to be used if an iterative method is employed in the solution. In that case, the residual vector Res = r Pz of the system should be made less than delta in weighted l_2 norm, i.e., $\sqrt{\sum_i (Res_i \cdot ewt_i)^2} < \text{delta}$. To obtain the N-Vector ewt, call IDAGetErrWeights (see §5.5.8.1).
- p_data is a pointer to user data the same as the p_data parameter passed to the function IDASp*SetPreconditioner.
- ${\tt tmp}$ is a pointer to memory allocated for a variable of type N_Vector which can be used for work space.

Return value The value to be returned by the preconditioner solve function is a flag indicating whether it was successful. This value should be 0 if successful, positive for a recoverable error (in which case the step will be retried), negative for an unrecoverable error (in which case the integration is halted).

5.6.8 Preconditioning (Jacobian data)

If the user's preconditioner requires that any Jacobian-related data be evaluated or preprocessed, then this needs to be done in a user-supplied C function of type IDASpilsPrecSetupFn, defined as follows:

IDASpilsPrecSetupFn

```
Definition typedef int (*IDASpilsPrecSetupFn)(realtype tt, N_Vector yy, N_Vector rr, realtype c_j, void *p_data, N_Vector tmp1, N_Vector tmp2, N_Vector tmp3);
```

Purpose This function evaluates and/or preprocesses Jacobian-related data needed by the preconditioner.

Arguments The arguments of an IDASpilsPrecSetupFn are as follows:

- tt is the current value of the independent variable.
- yy is the current value of the dependent variable vector, y(t).
- yp is the current value of y'(t).
- rr is the current value of the residual vector F(t, y, y').
- c_j is the scalar in the system Jacobian, proportional to the inverse of the step size $(\alpha \text{ in Eq. } (3.5))$.
- p_data is a pointer to user data the same as the p_data parameter passed to the function IDASp*SetPreconditioner.

tmp1

tmp2

tmp3 are pointers to memory allocated for variables of type N_Vector which can be used by IDASpilsPrecSetupFn as temporary storage or work space.

Return value The value to be returned by the preconditioner setup function is a flag indicating whether it was successful. This value should be 0 if successful, positive for a recoverable error (in which case the step will be retried), negative for an unrecoverable error (in which case the integration is halted).

Notes

The operations performed by this function might include forming a crude approximate Jacobian, and performing an LU factorization on the resulting approximation.

Each call to the preconditioner setup function is preceded by a call to the IDAResFn user function with the same (tt, yy, yp) arguments. Thus the preconditioner setup function can use any auxiliary data that is computed and saved during the evaluation of the DAE residual.

This function is not called in advance of every call to the preconditioner solve function, but rather is called only as often as needed to achieve convergence in the Newton iteration.

If the user's IDASpilsPrecSetupFn function uses difference quotient approximations, it may need to access quantities not in the call list. These include the current stepsize, the error weights, etc. To obtain these, use the IDAGet* functions described in §5.5.8.1. The unit roundoff can be accessed as UNIT_ROUNDOFF defined in sundials_types.h.

5.7 Rootfinding

While integrating the IVP, IDA has the capability of finding the roots of a set of user-defined functions. This section describes the user-callable functions used to initialize and define the rootfinding problem and obtain solution information, and it also describes the required additional user-supplied function.

5.7.1 User-callable functions for rootfinding

IDARootInit

Call flag = IDARootInit(ida_mem, nrtfn, g, g_data);

Description The function IDARootInit specifies that the roots of a set of functions $g_i(t, y, y')$ are to be found while the IVP is being solved.

Arguments ida_mem (void *) pointer to the IDA memory block returned by IDACreate.

nrtfn (int) is the number of root functions g_i .

g (IDARootFn) is the C function which defines the nrtfn functions $g_i(t, y, y')$ whose roots are sought. See §5.7.2 for details.

g_data (void *) pointer to the user data for use by the user's root function g.

Return value The return value flag (of type int) is one of

IDA_SUCCESS The call to IDARootInit was successful.

IDA_MEM_NULL The ida_mem argument was NULL.

IDA_MEM_FAIL A memory allocation failed.

IDA_ILL_INPUT The function g is NULL, but nrtfn> 0.

Notes If a new IVP is to be solved with a call to IDAReInit, where the new IVP has no rootfinding problem but the prior one did, then call IDARootInit with nrtfn= 0.

There are two optional output functions associated with rootfinding.

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IDAGetRootInfo

Call flag = IDAGetRootInfo(ida_mem, rootsfound);

Description The function IDAGetRootInfo returns an array showing which functions were found to

have a root.

Arguments ida_mem (void *) pointer to the IDA memory block.

rootsfound (int *) array of length nrtfn with the indices of the user functions g_i found to have a root. For i = 0, ..., nrtfn -1, rootsfound[i] = 1 if g_i has a

root, and = 0 if not.

Return value The return value flag (of type int) is one of

IDA_SUCCESS The optional output values have been successfully set.

IDA_MEM_NULL The ida_mem pointer is NULL.

Notes The user must allocate memory for the vector rootsfound.



IDAGetNumGEvals

Call flag = IDAGetNumGEvals(ida_mem, &ngevals);

Description The function IDAGetNumGEvals returns the cumulative number of calls to the user root

function q.

Arguments ida_mem (void *) pointer to the IDA memory block.

ngevals (long int) number of calls to the user's function g so far.

Return value The return value flag (of type int) is one of

IDA_SUCCESS The optional output value has been successfully set.

IDA_MEM_NULL The ida_mem pointer is NULL.

5.7.2 User-supplied function for rootfinding

If a rootfinding problem is to be solved during the integration of the ODE system, the user must supply a C function of type IDARootFn, defined as follows:

IDARootFn

Definition typedef int (*IDARootFn)(realtype t, N_Vector y, N_Vector yp, realtype *gout, void *g_data);

Purpose This function computes a vector-valued function g(t, y, y') such that the roots of the

nrtfn components $g_i(t, y, y')$ are to be found during the integration.

Arguments t is the current value of the independent variable.

y is the current value of the dependent variable vector, y(t).

yp is the current value of y'(t), the t-derivative of y.

gout is the output array, of length nrtfn, with components $g_i(t, y, y')$.

g_data is a pointer to user data — the same as the g_data parameter passed to IDARootInit.

Return value An IDARootFn should return 0 if successful or a non-zero value if an error occured (in which case the integration is halted and IDASolve returns IDA_RTFUNC_FAIL).

Notes Allocation of memory for gout is handled within IDA.

5.8 A parallel band-block-diagonal preconditioner module

A principal reason for using a parallel DAE solver such as IDA lies in the solution of partial differential equations (PDEs). Moreover, the use of a Krylov iterative method for the solution of many such problems is motivated by the nature of the underlying linear system of equations (3.4) that must be solved at each time step. The linear algebraic system is large, sparse, and structured. However, if a Krylov iterative method is to be effective in this setting, then a nontrivial preconditioner needs to be used. Otherwise, the rate of convergence of the Krylov iterative method is usually unacceptably slow. Unfortunately, an effective preconditioner tends to be problem-specific.

However, we have developed one type of preconditioner that treats a rather broad class of PDE-based problems. It has been successfully used for several realistic, large-scale problems [15] and is included in a software module within the IDA package. This module works with the parallel vector module NVECTOR_PARALLEL and generates a preconditioner that is a block-diagonal matrix with each block being a band matrix. The blocks need not have the same number of super- and sub-diagonals and these numbers may vary from block to block. This Band-Block-Diagonal Preconditioner module is called IDABBDPRE.

One way to envision these preconditioners is to think of the domain of the computational PDE problem as being subdivided into M non-overlapping sub-domains. Each of these sub-domains is then assigned to one of the M processors to be used to solve the DAE system. The basic idea is to isolate the preconditioning so that it is local to each processor, and also to use a (possibly cheaper) approximate residual function. This requires the definition of a new function G(t,y,y') which approximates the function F(t,y,y') in the definition of the DAE system (3.1). However, the user may set G=F. Corresponding to the domain decomposition, there is a decomposition of the solution vectors y and y' into M disjoint blocks y_m and y'_m , and a decomposition of G into blocks G_m . The block G_m depends on y_m and y'_m , and also on components of $y_{m'}$ and $y'_{m'}$ associated with neighboring sub-domains (so-called ghost-cell data). Let \bar{y}_m and \bar{y}'_m denote y_m and y'_m (respectively) augmented with those other components on which G_m depends. Then we have

$$G(t, y, y') = [G_1(t, \bar{y}_1, \bar{y}'_1), G_2(t, \bar{y}_2, \bar{y}'_2), \dots, G_M(t, \bar{y}_M, \bar{y}'_M)]^T,$$
(5.1)

and each of the blocks $G_m(t, \bar{y}_m, \bar{y}'_m)$ is uncoupled from the others.

The preconditioner associated with this decomposition has the form

$$P = diag[P_1, P_2, \dots, P_M] \tag{5.2}$$

where

$$P_m \approx \partial G_m / \partial y_m + \alpha \partial G_m / \partial y_m' \tag{5.3}$$

This matrix is taken to be banded, with upper and lower half-bandwidths mudq and mldq defined as the number of non-zero diagonals above and below the main diagonal, respectively. The difference quotient approximation is computed using mudq + mldq +2 evaluations of G_m , but only a matrix of bandwidth mukeep + mlkeep +1 is retained.

Neither pair of parameters need be the true half-bandwidths of the Jacobians of the local block of G, if smaller values provide a more efficient preconditioner. Such an efficiency gain may occur if the couplings in the DAE system outside a certain bandwidth are considerably weaker than those within the band. Reducing mukeep and mlkeep while keeping mudq and mldq at their true values, discards the elements outside the narrower band. Reducing both pairs has the additional effect of lumping the outer Jacobian elements into the computed elements within the band, and requires more caution and experimentation.

The solution of the complete linear system

$$Px = b (5.4)$$

reduces to solving each of the equations

$$P_m x_m = b_m (5.5)$$

and this is done by banded LU factorization of P_m followed by a banded backsolve.

Similar block-diagonal preconditioners could be considered with different treatment of the blocks P_m . For example, incomplete LU factorization or an iterative method could be used instead of banded LU factorization.

The IDABBDPRE module calls two user-provided functions to construct P: a required function Gres (of type IDABBDLocalFn) which approximates the residual function $G(t,y,y')\approx F(t,y,y')$ and which is computed locally, and an optional function Gcomm (of type IDABBDCommFn) which performs all inter-process communication necessary to evaluate the approximate residual G. These are in addition to the user-supplied residual function res . Both functions take as input the same pointer $\operatorname{res_data}$ as passed by the user to IDASetRdata and passed to the user's function res , and neither function has a return value. The user is responsible for providing space (presumably within $\operatorname{res_data}$) for components of yy and yp that are communicated by Gcomm from the other processors, and that are then used by Gres , which is not expected to do any communication.

IDABBDLocalFn

Purpose This function computes G(t, y, y'). It loads the vector gval as a function of tt, yy, and

ур.

Arguments Nlocal is the local vector length.

tt is the value of the independent variable.

yy is the dependent variable.

yp is the derivative of the dependent variable.

gval is the output vector.

res_data is a pointer to user data — the same as the res_data parameter passed to IDASetRdata.

Return value An IDABBDLocalFn function type should return 0 to indicate success, 1 for a recoverable error, or -1 for a non-recoverable error.

Notes This function assumes that all inter-processor communication of data needed to calculate

gval has already been done, and this data is accessible within res_data.

The case where G is mathematically identical to F is allowed.

IDABBDCommFn

Definition typedef int (*IDABBDCommFn)(long int Nlocal, realtype tt, N_Vector yy, N_Vector yp, void *res_data);

Purpose This function performs all inter-processor communications necessary for the execution of the Gres function above, using the input vectors yy and yp.

Arguments Nlocal is the local vector length.

tt is the value of the independent variable.

yy is the dependent variable.

yp is the derivative of the dependent variable.

res_data is a pointer to user data — the same as the res_data parameter passed to IDASetRdata.

Return value An IDABBDCommFn function type should return 0 to indicate success, 1 for a recoverable error, or -1 for a non-recoverable error.

Notes The Gcomm function is expected to save communicated data in space defined within the structure res_data.

Each call to the Gcomm function is preceded by a call to the residual function res with the same (tt, yy, yp) arguments. Thus Gcomm can omit any communications done by

res if relevant to the evaluation of Gres. If all necessary comunication was done in res, then Gcomm = NULL can be passed in the call to IDABBDPrecAlloc (see below).

Besides the header files required for the integration of the DAE problem (see §5.3), to use the IDABBDPRE module, the main program must include the header file ida_bbdpre.h which declares the needed function prototypes.

The following is a summary of the usage of this module and describes the sequence of calls in the user main program. Steps that are unchanged from the user main program presented in §5.4 are grayed-out.

- 1. Initialize MPI
- 2. Set problem dimensions
- 3. Set vector of initial values
- 4. Create IDA object
- 5. Allocate internal memory
- 6. Set optional inputs

7. Initialize the IDABBDPRE preconditioner module

Specify the upper and lower bandwidths mudg, mldg and mukeep, mlkeep and call

to allocate memory for and initialize a data structure bbd_data, of type void *, to be passed to any of the Krylov linear solvers. The last two arguments of IDABBDPrecAlloc are the two user-supplied functions described above.

8. Attach iterative linear solver, one of:

- (a) flag = IDABBDSpgmr(ida_mem, maxl, bbd_data);
- (b) flag = IDABBDSpbcg(ida_mem, maxl, bbd_data);
- (c) flag = IDABBDSptfqmr(ida_mem, maxl, bbd_data);

The function IDABBDSp* is a wrapper around the specification function IDASp* and performs the following actions:

- •Attaches the IDASPGMR, IDASPBCG, or IDASPTFQMR linear solver to the main IDA solver memory;
- •Sets the preconditioner data structure for IDABBDPRE;
- •Sets the preconditioner setup function for IDABBDPRE;
- •Sets the preconditioner solve function for IDABBDPRE;

9. Set linear solver optional inputs

Note that the user should not overwrite the preconditioner data, setup function, or solve function through calls to IDASPGMR, IDASPBCG, or IDASPTFQMR optional input functions.

- 10. Correct initial values
- 11. Specify rootfinding problem
- 12. Advance solution in time

13. Get optional outputs

Additional optional outputs associated with IDABBDPRE are available by way of two routines described below — IDABBDPreconGetWorkSpace and IDABBDPreconGetNumGfnEvals.

14. Deallocate memory for solution vector

15. Free the IDABBDPRE data structure

IDABBDPrecFree(&bbd_data);

16. Free solver memory

17. Finalize MPI

The user-callable functions that initialize, attach, and deallocate the IDABBDPRE preconditioner module (steps 7, 8, and 15 above) are described next.

IDABBDPrecAlloc

Notes

Description The function IDABBDPrecAlloc initializes and allocates memory for the IDABBDPRE preconditioner.

Arguments ida_mem (void *) pointer to the IDA memory block.

Nlocal (long int) local vector dimension.

mudq (long int) upper half-bandwidth to be used in the difference-quotient Jacobian approximation.

mldq (long int) lower half-bandwidth to be used in the difference-quotient Jacobian approximation.

mukeep (long int) upper half-bandwidth of the retained banded approximate Jacobian block.

mlkeep (long int) lower half-bandwidth of the retained banded approximate Jacobian block.

dq_rel_yy (realtype) the relative increment in components of y used in the difference quotient approximations. The default is dq_rel_yy= $\sqrt{\text{unit roundoff}}$, which can be specified by passing dq_rel_yy= 0.0.

Gres (IDABBDLocalFn) the C function which computes the local residual approximation G(t, y, y').

Gcomm (IDABBDCommFn) the optional C function which performs all inter-process communication required for the computation of G(t, y, y').

Return value If successful, IDABBDPrecAlloc returns a pointer to the newly created IDABBDPRE memory block (of type void *). If an error occurred, IDABBDPrecAlloc returns NULL.

If one of the half-bandwidths mudq or mldq to be used in the difference-quotient calculation of the approximate Jacobian is negative or exceeds the value Nlocal-1, it is replaced by 0 or Nlocal-1 accordingly.

The half-bandwidths mudq and mldq need not be the true half-bandwidths of the Jacobian of the local block of G, when smaller values may provide a greater efficiency.

Also, the half-bandwidths mukeep and mlkeep of the retained banded approximate Jacobian block may be even smaller, to reduce storage and computation costs further.

For all four half-bandwidths, the values need not be the same on every processor.

IDABBDSpgmr

Call flag = IDABBDSpgmr(ida_mem, maxl, bbd_data);

Description The function IDABBDSpgmr links the IDABBDPRE data to the IDASPGMR linear solver

and attaches the latter to the IDA memory block.

Arguments ida_mem (void *) pointer to the IDA memory block.

maxl (int) maximum dimension of the Krylov subspace to be used. Pass 0 to use

the default value IDA_SPGMR_MAXL= 5.

bbd_data (void *) pointer to the IDABBDPRE data structure.

Return value The return value flag (of type int) is one of

IDASPILS_SUCCESS The IDASPGMR initialization was successful.

IDASPILS_MEM_NULL The ida_mem pointer is NULL.

IDASPILS_MEM_FAIL A memory allocation request failed.

IDABBDPRE_PDATA_NULL The IDABBDPRE preconditioner has not been initialized.

IDABBDSpbcg

Call flag = IDABBDSpbcg(ida_mem, maxl, bbd_data);

Description The function IDABBDSpbcg links the IDABBDPRE data to the IDASPBCG linear solver and

attaches the latter to the IDA memory block.

Arguments ida_mem (void *) pointer to the IDA memory block.

maxl (int) maximum dimension of the Krylov subspace to be used. Pass 0 to use

the default value IDA_SPBCG_MAXL= 5.

bbd_data (void *) pointer to the IDABBDPRE data structure.

Return value The return value flag (of type int) is one of

IDASPILS_SUCCESS The IDASPBCG initialization was successful.

IDASPILS_MEM_NULL The ida_mem pointer is NULL.

IDASPILS_MEM_FAIL A memory allocation request failed.

IDABBDPRE_PDATA_NULL The IDABBDPRE preconditioner has not been initialized.

IDABBDSptfqmr

Call flag = IDABBDSptfqmr(ida_mem, maxl, bbd_data);

Description The function IDABBDSptfqmr links the IDABBDPRE data to the IDASPTFQMR linear solver

and attaches the latter to the IDA memory block.

Arguments ida_mem (void *) pointer to the IDA memory block.

maxl (int) maximum dimension of the Krylov subspace to be used. Pass 0 to use

the default value IDA_SPTFQMR_MAXL= 5.

bbd_data (void *) pointer to the IDABBDPRE data structure.

Return value The return value flag (of type int) is one of

IDASPILS_SUCCESS The IDASPTFQMR initialization was successful.

IDASPILS_MEM_NULL The ida_mem pointer is NULL.

IDASPILS_MEM_FAIL A memory allocation request failed.

IDABBDPRE_PDATA_NULL The IDABBDPRE preconditioner has not been initialized.

IDABBDPrecFree

Call IDABBDPrecFree(&bbd_data);

Description The function IDABBDPrecFree frees the pointer allocated by IDABBDPrecAlloc.

Arguments The only argument of IDABBDPrecFree is the pointer to the IDABBDPRE data structure

(of type void *).

Return value The function IDABBDPrecFree has no return value.

The IDABBDPRE module also provides a reinitialization function to allow for a sequence of problems of the same size with IDASPGMR/IDABBDPRE, IDASPBCG/IDABBDPRE, or IDASPTFQMR/IDABBDPRE, provided there is no change in local_N, mukeep, or mlkeep. After solving one problem, and after calling IDAReInit to re-initialize IDA for a subsequent problem, a call to IDABBDPrecReInit can be made to change any of the following: the half-bandwidths mudq and mldq used in the difference-quotient Jacobian approximations, the relative increment dq_rel_yy, or one of the user-supplied functions Gres and Gcomm.

IDABBDPrecReInit

Call flag = IDABBDPrecReInit(bbd_data, mudq, mldq, dq_rel_yy, Gres, Gcomm);

Description The function IDABBDPrecReInit reinitializes the IDABBDPRE preconditioner.

Arguments bbd_data (void *) pointer to the IDABBDPRE data structure.

mudq (long int) upper half-bandwidth to be used in the difference-quotient Ja-

cobian approximation.

mldq (long int) lower half-bandwidth to be used in the difference-quotient Jaco-

bian approximation.

dq_rel_yy (realtype) the relative increment in components of y used in the difference

quotient approximations. The default is $dq_rel_yy = \sqrt{unit\ roundoff}$, which

can be specified by passing $dq_rel_yy = 0.0$.

Gres (IDABBDLocalFn) the C function which computes the local residual approx-

imation G(t, y, y').

Gcomm (IDABBDCommFn) the optional C function which performs all inter-process

communication required for the computation of G(t, y, y').

 $Return\ value\ The\ return\ value\ of\ {\tt IDABBDPrecReInit}\ is\ {\tt IDABBDPRE_SUCCESS}\ indicating\ success,\ or\ {\tt IDABBDPRE_SUCCES$

IDABBDPRE_PDATA_NULL if bbd_data is NULL.

Notes If one of the half-bandwidths mudq or mldq is negative or exceeds the value Nlocal-1,

it is replaced by 0 or Nlocal-1, accordingly.

The following two optional output functions are available for use with the IDABBDPRE module:

IDABBDPrecGetWorkSpace

Call flag = IDABBDPrecGetWorkSpace(bbd_data, &lenrwBBDP, &leniwBBDP);

Description The function IDABBDPrecGetWorkSpace returns the local sizes of the IDABBDPRE real

and integer workspaces.

Arguments bbd_data (void *) pointer to the IDABBDPRE data structure.

lenrwBBDP (long int) local number of real values in the IDABBDPRE workspace.

leniwBBDP (long int) local number of integer values in the IDABBDPRE workspace.

Return value The return value flag (of type int) is one of

IDABBDPRE_SUCCESS The optional output value has been successfuly set.

IDABBDPRE_PDATA_NULL The IDABBDPRE preconditioner has not been initialized.

Notes In terms of the local vector dimension N_l , and $smu = min(N_l - 1, mukeep + mlkeep),$

the actual size of the real workspace is $N_l\left(2\,\,\mathrm{mlkeep}\,+\,\mathrm{mukeep}\,+\,\mathrm{smu}\,+2\right)$ realtype

words. The actual size of the integer workspace is N_l integer words.

IDABBDPrecGetNumGfnEvals

Call flag = IDABBDPrecGetNumGfnEvals(bbd_data, &ngevalsBBDP);

Description The function IDABBDPrecGetNumGfnEvals returns the cumulative number of calls to

the user Gres function due to the finite difference approximation of the Jacobian blocks

used within IDABBDPRE's preconditioner setup function.

Arguments bbd_data (void *) pointer to the IDABBDPRE data structure.

ngevalsBBDP (long int) the cumulative number of calls to the user Gres function.

Return value The return value flag (of type int) is one of

IDABBDPRE_SUCCESS The optional output value has been successfuly set.

IDABBDPRE_PDATA_NULL The IDABBDPRE preconditioner has not been initialized.

IDABandPrecGetReturnFlagName

Description The function IDABandPrecGetReturnFlagName returns the name of the CVBANDPRE

constant corresponding to flag.

Arguments The only argument, of type int is a return flag from a CVBANDPRE function.

Return value The return value is a string containing the name of the corresponding constant.

In addition to the ngevalsBBDP Gres evaluations, the costs associated with IDABBDPRE also include nlinsetups LU factorizations, nlinsetups calls to Gcomm, npsolves banded backsolve calls, and nrevalsLS residual function evaluations, where nlinsetups is an optional IDA output (see §5.5.8.1), and npsolves and nrevalsLS are linear solver optional outputs (see §5.5.8.2).

Chapter 6

FIDA, an Interface Module for FORTRAN Applications

The fidal interface module is a package of C functions which support the use of the IDA solver, for the solution of DAE systems, in a mixed FORTRAN/C setting. While IDA is written in C, it is assumed here that the user's calling program and user-supplied problem-defining routines are written in FORTRAN. This package provides the necessary interface to IDA for both the serial and the parallel NVECTOR implementations.

6.1 FIDA routines

The user-callable functions, with the corresponding IDA functions, are as follows:

- Interface to the NVECTOR modules
 - FNVINITS (defined by NVECTOR_SERIAL) interfaces to N_VNewEmpty_Serial.
 - FNVINITP (defined by NVECTOR_PARALLEL) interfaces to N_VNewEmpty_Parallel.
- Interface to the main IDA module
 - FIDAMALLOC interfaces to IDACreate and IDAMalloc.
 - FIDAREINIT interfaces to IDAReInit.
 - FIDASETIIN, FIDASETVIN, and FIDASETRIN interface to IDASet* functions.
 - FIDATOLREINIT interfaces to IDASetTolerances.
 - FIDACALCIC interfaces to IDACalcIC.
 - FIDAEWTSET interfaces to IDAEwtSetFn.
 - FIDASOLVE interfaces to IDASolve, IDAGet* functions, and to the optional output functions for the selected linear solver module.
 - FIDAGETSOL interfaces to IDAGetSolution.
 - FIDAGETERRWEIGHTS interfaces to IDAGetErrWeights.
 - FIDAGETESTLOCALERR interfaces to IDAGetEstLocalErrors.
 - FIDAFREE interfaces to IDAFree.
- Interface to the linear solver modules
 - FIDADENSE interfaces to IDADense.
 - FIDADENSESETJAC interfaces to IDADenseSetJacFn.

- FIDABAND interfaces to IDABand.
- FIDABANDSETJAC interfaces to IDABandSetJacFn.
- FIDASPGMR interfaces to IDASpgmr and SPGMR optional input functions.
- FIDASPGMRREINIT interfaces to SPGMR optional input functions.
- FIDASPBCG interfaces to IDASpbcg and SPBCG optional input functions.
- FIDASPBCGREINIT interfaces to SPBCG optional input functions.
- FIDASPTFQMR interfaces to IDASptfqmr and SPTFQMR optional input functions.
- FIDASPTFQMRREINIT interfaces to SPTFQMR optional input functions.
- FIDASPILSSETJAC interfaces to IDASpilsSetJacTimesVecFn.
- FIDASPILSSETPREC interfaces to IDASpilsSetPreconditioner.

The user-supplied functions, each listed with the corresponding interface function which calls it (and its type within IDA), are as follows:

FIDA routine (FORTRAN)	IDA function (C)	IDA function type
FIDARESFUN	FIDAresfn	IDAResFn
FIDAEWT	FIDAEwtSet	IDAEwtFn
FIDADJAC	FIDADenseJac	IDADenseJacFn
FIDABJAC	FIDABandJac	IDABandJacFn
FIDAPSOL	FIDAPSol	IDASpilsPrecSolveFn
FIDAPSET	FIDAPSet	IDASpilsPrecSetupFn
FIDAJTIMES	FIDAJtimes	IDASpilsJacTimesVecFn

In contrast to the case of direct use of IDA, and of most FORTRAN DAE solvers, the names of all user-supplied routines here are fixed, in order to maximize portability for the resulting mixed-language program.

6.1.1 Important note on portability

In this package, the names of the interface functions, and the names of the FORTRAN user routines called by them, appear as dummy names which are mapped to actual values by a series of definitions in the header files fida.h, fidaroot.h, and fidabbd.h. By default, those mapping definitions depend in turn on the C macros F77_FUNC and F77_FUNC_ defined in the header file sundials_config.h by configure. However, the set of flags

SUNDIALS_CASE_UPPER, SUNDIALS_CASE_LOWER,

SUNDIALS_UNDERSCORE_NONE, SUNDIALS_UNDERSCORE_ONE, and SUNDIALS_UNDERSCORE_TWO

can be explicitly defined in the header file sundials_config.h when configuring SUNDIALS via the --with-f77underscore and --with-f77case options to override the default behavior if necessary (see Chapter 2). Either way, the names into which the dummy names are mapped are in upper or lower case and have up to two underscores appended.

The user must also ensure that variables in the user FORTRAN code are declared in a manner consistent with their counterparts in IDA. All real variables must be declared as REAL, DOUBLE PRECISION, or perhaps as REAL*n, where n denotes the number of bytes, depending on whether IDA was built in single, double, or extended precision (see Chapter 2). Moreover, some of the FORTRAN integer variables must be declared as INTEGER*4 or INTEGER*8 according to the C type long int. These integer variables include: the array of integer optional outputs (IOUT), problem dimensions (NEQ, NLOCAL, NGLOBAL), Jacobian half-bandwidths (MU, ML, etc.), as well as the array of user integer data, IPAR. This is particularly important when using IDA and the FIDA package on 64-bit architectures.

6.2 Usage of the FIDA interface module

The usage of FIDA requires calls to five or more interface functions, depending on the method options selected, and one or more user-supplied routines which define the problem to be solved. These function

calls and user routines are summarized separately below. Some details are omitted, and the user is referred to the description of the corresponding IDA functions for information on the arguments of any given user-callable interface routine, or of a given user-supplied function called by an interface function. The usage of FIDA for rootfinding, and usage of FIDA with preconditioner modules, are each described in later sections.

Steps marked with [S] in the instructions below apply to the serial NVECTOR implementation (NVECTOR_SERIAL) only, while those marked with [P] apply to NVECTOR_PARALLEL.

1. Residual function specification

The user must in all cases supply the following FORTRAN routine

```
SUBROUTINE FIDARESFUN (T, Y, YP, R, IPAR, RPAR, IER) DIMENSION Y(*), YP(*), R(*), IPAR(*), RPAR(*)
```

It must set the R array to F(t, y, y'), the residual function of the DAE system, as a function of T = t and the arrays Y = y and YP = y'. The arrays IPAR (of integers) and RPAR (of reals) contain user data and are the same as those passed to FIDAMALLOC. It should return IER = 0 if it was successful, IER = 1 if it had a recoverable failure, or IER = -1 if it had a non-recoverable failure.

2. NVECTOR module initialization

[S] To initialize the serial NVECTOR module, the user must make the following call:

```
CALL FNVINITS (KEY, NEQ, IER)
```

where KEY is the solver id (KEY=1 for IDA), NEQ is the size of vectors, and IER is a return flag, which is set to 0 on success and -1 if a failure occurred.

[P] To initialize the parallel vector module, the user must make the following call:

```
CALL FNVINITP (COMM, KEY, NLOCAL, NGLOBAL, IER)
```

in which the arguments are: COMM = MPI communicator, KEY = 1, NLOCAL = the local size of all vectors on this processor, and NGLOBAL = the system size (and the global size of vectors, equal to the sum of all values of NLOCAL). The return flag IER is set to 0 on a successful return and to -1 otherwise.

If the header file sundials_config.h defines SUNDIALS_MPI_COMM_F2C to be 1 (meaning the MPI implementation used to build SUNDIALS includes the MPI_Comm_f2c function), then COMM can be any valid MPI communicator. Otherwise, MPI_COMM_WORLD will be used, so just pass an integer value as a placeholder.

3. Problem specification

To set various problem and solution parameters and allocate internal memory, make the following call:

FIDAMALLOC

Call CALL FIDAMALLOC(TO, YO, YPO, IATOL, RTOL, ATOL, & IOUT, ROUT, IPAR, RPAR, IER)

Description This function provides required problem and solution specifications, specifies optional inputs, allocates internal memory, and initializes IDA.

Arguments T0 is the initial value of t.

Y0 is an array of initial conditions for y. YP0 is an array of initial conditions for y'.



IATOL specifies the type for absolute tolerance ATOL: 1 for scalar or 2 for array. If IATOL= 3, the arguments RTOL and ATOL are ignored and the user is expected to subsequently call FIDAEWTSET and provide the function FIDAEWT.

RTOL is the relative tolerance (scalar).

ATOL is the absolute tolerance (scalar or array).

IOUT is an integer array of length at least 21 for integer optional outputs.

ROUT is a real array of length at least 6 for real optional outputs.

IPAR is an integer array of user data which will be passed unmodified to all userprovided routines.

RPAR is a real array of user data which will be passed unmodified to all user-provided routines.

Return value IER is a return completion flag. Values are 0 for successful return and -1 otherwise. See printed message for details in case of failure.

Notes The user intger data array IPAR must be declared as INTEGER*4 or INTEGER*8 according to the C type long int.

Modifications to the user data arrays IPAR and RPAR inside a user-provided routine will be propagated to all subsequent calls to such routines.

The optional outputs associated with the main IDA integrator are listed in Table 6.2.

As an alternative to providing tolerances in the call to FIDAMALLOC, the user may provide a routine to compute the error weights used in the WRMS norm evaluations. If supplied, it must have the following form:

```
SUBROUTINE FIDAEWT (Y, EWT, IPAR, RPAR, IER)
DIMENSION Y(*), EWT(*), IPAR(*), RPAR(*)
```

It must set the positive components of the error weight vector EWT for the calculation of the WRMS norm of Y. On return, set IER = 0 if FIDAEWT was successful, and nonzero otherwise. The arrays IPAR (of integers) and RPAR (of reals) contain user data and are the same as those passed to FIDAMALLOC.

If the FIDAEWT routine is provided, then, following the call to FIDAMALLOC, the user must make the call:

```
CALL FIDAEWTSET (FLAG, IER)
```

with FLAG $\neq 0$ to specify use of the user-supplied error weight routine. The argument IER is an error return flag, which is 0 for success or non-zero if an error occurred.

4. Linear solver specification

The variable-order, variable-coefficient BDF method used by IDA involves the solution of linear systems related to the system Jacobian $J = \partial F/\partial y + \alpha \partial F/\partial y'$. See Eq. (3.4). IDA presently includes five choices for the treatment of these systems, and the user of FIDA must call a routine with a specific name to make the desired choice.

[S] Dense treatment of the linear system

The user must make the call:

```
CALL FIDADENSE (NEQ, IER)
```

where NEQ is the size of the DAE system. The argument IER is an error return flag, which is 0 for success, -1 if a memory allocation failure occurred, or -2 for illegal input. As an option when using the DENSE linear solver, the user may supply a routine that computes a dense approximation of the system Jacobian. If supplied, it must have the following form:

```
SUBROUTINE FIDADJAC (NEQ, T, Y, YP, R, DJAC, CJ, EWT, H, & IPAR, RPAR, WK1, WK2, WK3, IER)
DIMENSION Y(*), YP(*), R(*), EWT(*), DJAC(NEQ,*),
& IPAR(*), RPAR(*), WK1(*), WK2(*), WK3(*)
```

This routine must compute the Jacobian and store it columnwise in DJAC. The vectors WK1, WK2, and WK3 of length NEQ are provided as work space for use in FIDADJAC. The input arguments T, Y, YP, R, and CJ are the current values of t, y, y', F(t, y, y'), and α , respectively. The arrays IPAR (of integers) and RPAR (of reals) contain user data and are the same as those passed to FIDAMALLOC.

If the user's FIDADJAC uses difference quotient approximations, it may need to use the error weight array EWT and current stepsize H in the calculation of suitable increments. It may also need the unit roundoff, which can be obtained as the optional output ROUT(6), passed from the calling program to this routine using COMMON.

If the FIDADJAC routine is provided, then, following the call to FIDADENSE, the user must make the call:

```
CALL FIDADENSESETJAC (FLAG, IER)
```

with FLAG $\neq 0$ to specify use of the user-supplied Jacobian approximation. The argument IER is an error return flag, which is 0 for success or non-zero if an error occurred.

Optional outputs specific to the DENSE case are listed in Table 6.2.

[S] Band treatment of the linear system

The user must make the call:

```
CALL FIDABAND (NEQ, MU, ML, IER)
```

The arguments are: MU, the upper half-bandwidth; ML, the lower half-bandwidth; and IER, an error return flag, which is 0 for success, -1 if a memory allocation failure occurred, or -2 in case an input has an illegal value.

As an option when using the BAND linear solver, the user may supply a routine that computes a band approximation of the system Jacobian. If supplied, it must have the following form:

```
SUBROUTINE FIDABJAC(NEQ, MU, ML, MDIM, T, Y, YP, R, CJ, BJAC, & EWT, H, IPAR, RPAR, WK1, WK2, WK3, IER)
DIMENSION Y(*), YP(*), R(*), EWT(*), BJAC(MDIM,*),
& IPAR(*), RPAR(*), WK1(*), WK2(*), WK3(*)
```

This routine must load the MDIM by NEQ array BJAC with the Jacobian matrix at the current (t, y, y') in band form. Store in BJAC(k, j) the Jacobian element $J_{i,j}$ with k = i - j + MU + 1 ($k = 1 \cdots \text{ML} + \text{MU} + 1$) and $j = 1 \cdots N$. The vectors WK1, WK2, and WK3 of length NEQ are provided as work space for use in FIDABJAC. The input arguments T, Y, YP, R, and CJ are the current values of t, y, y', F(t, y, y'), and α , respectively. The arrays IPAR (of integers) and RPAR (of reals) contain user data and are the same as those passed to FIDAMALLOC.

If the user's FIDABJAC uses difference quotient approximations, it may need to use the error weight array EWT and current stepsize H in the calculation of suitable increments. It may also need the unit roundoff, which can be obtained as the optional output ROUT(6), passed from the calling program to this routine using COMMON.

If the FIDABJAC routine is provided, then, following the call to FIDABAND, the user must make the call:

```
CALL FIDABANDSETJAC (FLAG, IER)
```

with FLAG $\neq 0$ to specify use of the user-supplied Jacobian approximation. The argument IER is an error return flag, which is 0 for success or non-zero if an error occurred.

Optional outputs specific to the BAND case are listed in Table 6.2.

[S][P] SPGMR treatment of the linear systems

For the Scaled Preconditioned GMRES solution of the linear systems, the user must make the call

```
CALL FIDASPGMR (MAXL, IGSTYPE, MAXRS, EPLIFAC, DQINCFAC, IER)
```

The arguments are as follows. MAXL is the maximum Krylov subspace dimension. IGSTYPE indicates the Gram-Schmidt process type: 1 for modified, or 2 for classical. MAXRS maximum number of restarts. EPLIFAC is the linear convergence tolerance factor. DQINCFAC is the optional increment factor used in the matrix-vector product Jv. For all the input arguments, a value of 0 or 0.0 indicates the default. IER is an error return flag, which is 0 to indicate success, -1 if a memory allocation failure occurred, or -2 to indicate an illegal input.

Optional outputs specific to the SPGMR case are listed in Table 6.2.

For descriptions of the relevant optional user-supplied routines, see **User-supplied routines for SPGMR/SPBCG/SPTFQMR** below.

[S][P] SPBCG treatment of the linear systems

For the Scaled Preconditioned Bi-CGStab solution of the linear systems, the user must make the call

```
CALL FIDASPBCG (MAXL, EPLIFAC, DQINCFAC, IER)
```

The arguments are as follows. MAXL is the maximum Krylov subspace dimension. EPLIFAC is the linear convergence tolerance factor. DQINCFAC is the optional increment factor used in the matrix-vector product Jv. For all the input arguments, a value of 0 or 0.0 indicates the default. IER is an error return flag, which is 0 to indicate success, -1 if a memory allocation failure occurred, or -2 to indicate an illegal input.

Optional outputs specific to the SPBCG case are listed in Table 6.2.

For descriptions of the relevant optional user-supplied routines, see **User-supplied routines for SPGMR/SPBCG/SPTFQMR** below.

[S][P] SPTFQMR treatment of the linear systems

For the Scaled Preconditioned Transpose-Free Quasi-Minimal Residual solution of the linear systems, the user must make the call

```
CALL FIDASPTFQMR (MAXL, EPLIFAC, DQINCFAC, IER)
```

The arguments are as follows. MAXL is the maximum Krylov subspace dimension. EPLIFAC is the linear convergence tolerance factor. DQINCFAC is the optional increment factor used in the matrix-vector product Jv. For all the input arguments, a value of 0 or 0.0 indicates the default. IER is an error return flag, which is 0 to indicate success, -1 if a memory allocation failure occurred, or -2 to indicate an illegal input.

Optional outputs specific to the SPTFQMR case are listed in Table 6.2.

For descriptions of the relevant optional user-supplied routines, see below.

[S][P] Functions used by SPGMR/SPBCG/SPTFQMR

An optional user-supplied routine, FIDAJTIMES, can be provided for Jacobian-vector products. If it is, then, following the call to FIDASPGMR, FIDASPBCG, or FIDASPTFQMR, the user must make the call:

```
CALL FIDASPILSSETJAC (FLAG, IER)
```

with $FLAG \neq 0$. The return flag IER is 0 if successful, or negative if a memory error occurred. If preconditioning is to be done, then the user must call

```
CALL FIDASPILSSETPREC (FLAG, IER)
```

with FLAG $\neq 0$. The return flag IER is 0 if successful, or negative if a memory error occurred. In addition, the user must supply preconditioner routines FIDAPSET and FIDAPSOL.

[S][P] User-supplied routines for SPGMR/SPBCG/SPTFQMR

With treatment of the linear systems by any of the Krylov iterative solvers, there are three optional user-supplied routines — FIDAJTIMES, FIDAPSOL, and FIDAPSET. The specifications for these routines are given below.

As an option when using any of the Krylov iterative solvers, the user may supply a routine that computes the product of the system Jacobian $J = \partial F/\partial y + \alpha \partial F/\partial y'$ and a given vector v. If supplied, it must have the following form:

```
SUBROUTINE FIDAJTIMES(T, Y, YP, R, V, FJV, CJ, EWT, H, & IPAR, RPAR, WK1, WK2, IER)

DIMENSION Y(*), YP(*), R(*), V(*), FJV(*), EWT(*), & IPAR(*), RPAR(*), WK1(*), WK2(*)
```

This routine must compute the product vector Jv, where the vector v is stored in V, and store the product in FJV. On return, set IER = 0 if FIDAJTIMES was successful, and nonzero otherwise. The vectors W1K and WK2, of length NEQ, are provided as work space for use in FIDAJTIMES. The input arguments T, Y, YP, R, and CJ are the current values of t, y, y', F(t, y, y'), and α , respectively. The arrays IPAR (of integers) and RPAR (of reals) contain user data and are the same as those passed to FIDAMALLOC.

If the user's FIDAJTIMES uses difference quotient approximations, it may need to use the error weight array EWT and current stepsize H in the calculation of suitable increments. It may also need the unit roundoff, which can be obtained as the optional output ROUT(6), passed from the calling program to this routine using COMMON.

If preconditioning is to be included, the following routine must be supplied, for solution of the preconditioner linear system:

```
SUBROUTINE FIDAPSOL(T, Y, YP, R, RV, ZV, CJ, DELTA, EWT, 

& IPAR, RPAR, WK1, IER)

DIMENSION Y(*), YP(*), R(*), RV(*), ZV(*), EWT(*), 

& IPAR(*), RPAR(*), WK1(*)
```

It must solve the preconditioner linear system Pz=r, where r=RV is input, and store the solution z in ZV. Here P is the left preconditioner if LR=1 and the right preconditioner if LR=2. The input arguments T, Y, YP, R, and CJ are the current values of t, y, y', F(t, y, y'), and α , respectively. On return, set IER = 0 if FIDAPSOL was successful, set IER positive if a recoverable error occurred, and set IER negative if a non-recoverable error occurred.

The arguments EWT and DELTA are input and provide the error weight array and a scalar tolerance, respectively, for use by FIDAPSOL if it uses an iterative method in its solution. In that case, the residual vector $\rho = r - Pz$ of the system should be made less than DELTA in weighted ℓ_2 norm, i.e. $\sqrt{\sum (\rho_i * \text{EWT}[i])^2} < \text{DELTA}$. The argument WK1 is a work array of length NEQ for use by this routine. The arrays IPAR (of integers) and RPAR (of reals) contain user data and are the same as those passed to FIDAMALLOC.

If the user's preconditioner requires that any Jacobian-related data be evaluated or preprocessed, then the following routine is to be used for the evaluation and preprocessing of the preconditioner:

```
SUBROUTINE FIDAPSET(T, Y, YP, R, CJ, EWT, H, & IPAR, RPAR, WK1, WK2, WK3, IER)
DIMENSION Y(*), YP(*), R(*), EWT(*), & IPAR(*), RPAR(*), WK1(*), WK2(*), WK3(*)
```

It must perform any evaluation of Jacobian-related data and preprocessing needed for the solution of the preconditioner linear systems by FIDAPSOL. The input arguments T, Y, YP, R, and CJ are the current values of t, y, y', F(t, y, y'), and α , respectively. On return, set IER = 0 if FIDAPSET was successful, set IER positive if a recoverable error occurred, and set IER negative if a non-recoverable error occurred. The arrays IPAR (of integers) and RPAR (of reals) contain user data and are the same as those passed to FIDAMALLOC.

If the user's FIDAPSET uses difference quotient approximations, it may need to use the error weight array EWT and current stepsize H in the calculation of suitable increments. It may also need the unit roundoff, which can be obtained as the optional output ROUT(6), passed from the calling program to this routine using COMMON.

If the user calls FIDASPILSSETPREC, the subroutine FIDAPSET must be provided, even if it is not needed and must return IER=0.

5. Correct initial values

Optionally, to correct the initial values y and/or y', make the call

```
CALL FIDACALCIC (TO, YO, YPO, ICOPT, TOUT1, IER)
```

(See §3.1 for details.) The arguments are as follows: T0 is t_0 . Y0 and YP0 are the initial guesses for y and y' at t_0 . ICOPT is 1 for initializing the algebraic components of y and differential components of y', or 2 for initializing all of y. IER is an error return flag, which is 0 for success, or negative for a failure (see IDACalcIC return values).

6. Problem solution

Carrying out the integration is accomplished by making calls as follows:

```
CALL FIDASOLVE (TOUT, T, Y, YP, ITASK, IER)
```

The arguments are as follows. TOUT specifies the next value of t at which a solution is desired (input). T is the value of t reached by the solver on output. Y is an array containing the computed solution vector y on output. YP is an array containing the computed solution vector y' on output. ITASK is a task indicator and should be set to 1 for normal mode (overshoot TOUT and interpolate), to 2 for one-step mode (return after each internal step taken), to 3 for normal mode with the additional tstop constraint, or to 4 for one-step mode with the additional constraint tstop. IER is a completion flag and will be set to a positive value upon successful return or to a negative value if an error occurred. These values correspond to the IDASolve returns (see §5.5.5 and §10.2). The current values of the optional outputs are available in IOUT and ROUT (see Table 6.2).

7. Additional solution output

After a successful return from FIDASOLVE, the routine FIDAGETSOL may be called to get interpolated values of y and y' for any value of t in the last internal step taken by IDA.

```
CALL FIDAGETSOL (T, Y, YP, IER)
```



where T is the input value of t at which solution derivative is desired, and Y and YP are arrays containing the computed vectors y and y' on return. The value T must lie between TCUR-HLAST and TCUR. The return flag IER is set to 0 upon successful return, or to a negative value to indicate an illegal input.

8. Problem reinitialization

To re-initialize the IDA solver for the solution of a new problem of the same size as one already solved, make the following call:

```
CALL FIDAREINIT (TO, YO, YPO, IATOL, RTOL, ATOL, IER)
```

The arguments have the same names and meanings as those of FIDAMALLOC. FIDAREINIT performs the same initializations as FIDAMALLOC, but does no memory allocation, using instead the existing internal memory created by the previous FIDAMALLOC call.

Following this call, a call to specify the linear system solver must be made if the choice of linear solver is being changed. Otherwise, a call to reinitialize the linear solver last used may or may not be needed, depending on changes in the inputs to it.

In the case of the BAND solver, for any change in the half-bandwidths, call FIDABAND as described above.

In the case of SPGMR, for a change of inputs other than MAXL, make the call

```
CALL FIDASPGMRREINIT (IGSTYPE, MAXRS, EPLIFAC, DQINCFAC, IER)
```

which reinitializes SPGMR without reallocating its memory. The arguments have the same names and meanings as those of FIDASPGMR. If MAXL is being changed, then call FIDASPGMR.

In the case of SPBCG, for a change in any inputs, make the call

```
CALL FIDASPBCGREINIT (MAXL, EPLIFAC, DQINCFAC, IER)
```

which reinitializes SPBCG without reallocating its memory. The arguments have the same names and meanings as those of FIDASPBCG.

In the case of SPTFQMR, for a change in any inputs, make the call

```
CALL FIDASPTFQMRREINIT (MAXL, EPLIFAC, DQINCFAC, IER)
```

which reinitializes SPTFQMR without reallocating its memory. The arguments have the same names and meanings as those of FIDASPTFQMR.

9. Memory deallocation

To free the internal memory created by the call to FIDAMALLOC, make the call

CALL FIDAFREE

6.3 FIDA optional input and output

In order to keep the number of user-callable FIDA interface routines to a minimum, optional inputs to the IDA solver are passed through only three routines: FIDASETIIN for integer optional inputs, FIDASETRIN for real optional inputs, and FIDASETVIN for real vector (array) optional inputs. These functions should be called as follows:

Integer optional inputs (FIDASETIIN)		
Key	Optional input	Default value
MAX_ORD	Maximum LMM method order	5
MAX_NSTEPS	Maximum no. of internal steps before t_{out}	500
MAX_ERRFAIL	Maximum no. of error test failures	10
MAX_NITERS	Maximum no. of nonlinear iterations	4
MAX_CONVFAIL	Maximum no. of convergence failures	10
SUPPRESS_ALG	Suppress alg. vars. from error test $(1 = TRUE)$	0 (= FALSE)
MAX_NSTEPS_IC	Maximum no. of steps for IC calc.	5
MAX_NITERS_IC	Maximum no. of Newton iterations for IC calc.	10
MAX_NJE_IC	Maximum no. of Jac. evals fo IC calc.	4
LS_OFF_IC	Turn off line search $(1 = TRUE)$	0 (= FALSE)

Table 6.1: Keys for setting FIDA optional inputs

Real optional inputs (FIDASETRIN)

Key	Optional input	Default value
INIT_STEP	Initial step size	estimated
MAX_STEP	Maximum absolute step size	∞
STOP_TIME	Value of t_{stop}	undefined
NLCONV_COEF	Coeff. in the nonlinear conv. test	0.33
NLCONV_COEF_IC	Coeff. in the nonlinear conv. test for IC calc.	0.0033
STEP_TOL_IC	Lower bound on Newton step for IC calc.	$uround^{2/3}$

Real vector optional inputs (FIDASETVIN)

	Key	Optional input	Default value
Γ	ID_VEC	Differential/algebraic component types	undefined
	CONSTR_VEC	Inequality constraints on solution	undefined

CALL FIDASETIIN(KEY, IVAL, IER)
CALL FIDASETRIN(KEY, RVAL, IER)

CALL FIDASETVIN(KEY, VVAL, IER)

where KEY is a quoted string indicating which optoinal input is set (see Table 6.1), IVAL is the input integer value, RVAL is the input real value (scalar), VVAL is the input real array, and IER is an integer return flag which is set to 0 on success and a negative value if a failure occurred.

When using FIDASETVIN to specify the variable types (KEY = 'ID_VEC') the components in the array VVAL must be 1.0 to indicate a differential variable, or 0.0 to indicate an algebraic variable. Note that this array is required only if FIDACALCIC is to be called with ICOPT = 1, or if algebraic variables are suppressed from the error test (indicated using FIDASETIIN with KEY = 'SUPPRESS_ALG'). When using FIDASETVIN to specify optional constraints on the solution vector (KEY = 'CONSTR_VEC') the components in the array VVAL should be one of -2.0, -1.0, 0.0, 1.0, or 2.0. See the description of IDASetConstraints (§5.5.6.1) for details.

The optional outputs from the IDA solver are accessed not through individual functions, but rather through a pair of arrays, IOUT (integer type) of dimension at least 21, and ROUT (real type) of dimension at least 6. These arrays are owned (and allocated) by the user and are passed as arguments to FIDAMALLOC. Table 6.2 lists the entries in these two arrays and specifies the optional variable as well as the IDA function which is actually called to extract the optional output.

For more details on the optional inputs and outputs, see §5.5.6 and §5.5.8.

In addition to the optional inputs communicated through FIDASET* calls and the optional outputs extracted from IOUT and ROUT, the following user-callable routines are available:

To reset the tolerances at any time, make the following call:

CALL FIDATOLREINIT (IATOL, RTOL, ATOL, IER)

Table 6.2: Description of the fida optional output arrays ${\tt IOUT}$ and ${\tt ROUT}$ Integer output array ${\tt IOUT}$

Index		IDA function	
	IDA main solver		
1	LENRW	IDAGetWorkSpace	
2	LENIW	IDAGetWorkSpace	
3	NST	IDAGetNumSteps	
4	NRE	IDAGetNumResEvals	
5	NETF	IDAGetNumErrTestFails	
6	NNCFAILS	IDAGetNonlinSolvConvFails	
7	NNI	IDAGetNumNonlinSolvIters	
8	NSETUPS	${\tt IDAGetNumLinSolvSetups}$	
9	QLAST	IDAGetLastOrder	
10	QCUR	IDAGetCurrentOrder	
11	NBCKTRKOPS	IDAGetNumBacktrackOps	
12	NGE	IDAGetNumGEvals	
	IDADENSE	linear solver	
13	LENRWLS	IDADenseGetWorkSpace	
14	LENIWLS	IDADenseGetWorkSpace	
15	LS_FLAG	${\tt IDADenseGetLastFlag}$	
16	NRELS	IDADenseGetNumResEvals	
17	NJE	IDADenseGetNumJacEvals	
	IDABAND	linear solver	
13	LENRWLS	IDABandGetWorkSpace	
14	LENIWLS	IDABandGetWorkSpace	
15	LS_FLAG	${\tt IDABandGetLastFlag}$	
16	NRELS	IDABandGetNumResEvals	
17	NJE	${\tt IDABandGetNumJacEvals}$	
ID.	IDASPGMR, IDASPBCG, IDASPTFQMR linear solvers		
13	LENRWLS	IDASpilsGetWorkSpace	
14	LENIWLS	IDASpilsGetWorkSpace	
15	LS_FLAG	IDASpilsGetLastFlag	
16	NRELS	IDASpilsGetNumResEvals	
17	NJE	IDASpilsGetNumJtimesEvals	
18	NPE	IDASpilsGetNumPrecEvals	
19	NPS	IDASpilsGetNumPrecSolves	
20	NLI	${\tt IDASpilsGetNumLinIters}$	
21	NCFL	IDASpilsGetNumConvFails	

Real output array \mathtt{ROUT}

Index	Optional output	IDA function
1	HO_USED	IDAGetActualInitStep
2	HLAST	IDAGetLastStep
3	HCUR	IDAGetCurrentStep
4	TCUR	IDAGetCurrentTime
5	TOLFACT	IDAGetTolScaleFactor
6	UROUND	unit roundoff

The tolerance arguments have the same names and meanings as those of FIDAMALLOC. The error return flag IER is 0 if successful, and negative if there was a memory failure or illegal input.

To obtain the error weight array EWT, containing the multiplicative error weights used the WRMS norms, make the following call:

```
CALL FIDAGETERRWEIGHTS (EWT, IER)
```

This computes the EWT array, normally defined by Eq. (3.6). The array EWT, of length NEQ or NLOCAL, must already have been declared by the user. The error return flag IER is zero if successful, and negative if there was a memory error.

To obtain the estimated local errors, following a successful call to FIDASOLVE, make the following call:

```
CALL FIDAGETESTLOCALERR (ELE, IER)
```

This computes the ELE array of estimated local errors as of the last step taken. The array ELE must already have been declared by the user. The error return flag IER is zero if successful, and negative if there was a memory error.

6.4 Usage of the FIDAROOT interface to rootfinding

The FIDAROOT interface package allows programs written in FORTRAN to use the rootfinding feature of the IDA solver module. The user-callable functions in FIDAROOT, with the corresponding IDA functions, are as follows:

- FIDAROOTINIT interfaces to IDARootInit.
- FIDAROOTINFO interfaces to IDAGetRootInfo.
- FIDAROOTFREE interfaces to IDARootFree.

In order to use the rootfinding feature of IDA, the following call must be made, after calling FIDAMALLOC but prior to calling FIDASOLVE, to allocate and initialize memory for the FIDAROOT module:

```
CALL FIDAROOTINIT (NRTFN, IER)
```

The arguments are as follows: NRTFN is the number of root functions. IER is a return completion flag; its values are 0 for success, -1 if the IDA memory was NULL, and -14 if a memory allocation failed.

To specify the functions whose roots are to be found, the user must define the following routine:

```
SUBROUTINE FIDAROOTFN (T, Y, YP, G, IPAR, RPAR, IER) DIMENSION Y(*), YP(*), G(*), IPAR(*), RPAR(*)
```

It must set the G array, of length NRTFN, with components $g_i(t, y, y')$, as a function of T = t and the arrays Y = y and YP = y'. The arrays IPAR (of integers) and RPAR (of reals) contain user data and are the same as those passed to FIDAMALLOC. Set IER on 0 if successful, or on a non-zero value if an error occurred.

When making calls to FIDASOLVE to solve the DAE system, the occurrence of a root is flagged by the return value IER = 2. In that case, if NRTFN > 1, the functions g_i which were found to have a root can be identified by making the following call:

```
CALL FIDAROOTINFO (NRTFN, INFO, IER)
```

The arguments are as follows: NRTFN is the number of root functions. INFO is an integer array of length NRTFN with root information. IER is a return completion flag; its values are 0 for success, negative if there was a memory failure. The returned values of INFO(i) (i=1,...,NRTFN) are 0 or 1, such that INFO(i) = 1 if g_i was found to have a root, and INFO(i) = 0 otherwise.

The total number of calls made to the root function FIDAROOTFN, denoted NGE, can be obtained from IOUT(12). If the FIDA/IDA memory block is reinitialized to solve a different problem via a call to FIDAREINIT, then the counter NGE is reset to zero.

To free the memory resources allocated by a prior call to FIDAROOTINIT make the following call:

CALL FIDAROOTFREE

See §5.7 for additional information on the rootfinding feature.

6.5 Usage of the FIDABBD interface to IDABBDPRE

The FIDABBD interface sub-module is a package of C functions which, as part of the FIDA interface module, support the use of the IDA solver with the parallel NVECTOR_PARALLEL module, in a combination of any of the Krylov iterative solver modules with the IDABBDPRE preconditioner module (see §5.8).

The user-callable functions in this package, with the corresponding IDA and IDABBDPRE functions, are as follows:

- FIDABBDINIT interfaces to IDABBDPrecAlloc.
- FIDABBDSPGMR interfaces to IDABBDSpgmr and SPGMR optional input functions.
- FIDABBDSPBCG interfaces to IDABBDSpbcg and SPBCG optional input functions.
- FIDABBDSPTFQMR interfaces to IDABBDSptfqmr and SPTFQMR optional input functions.
- FIDABBDREINIT interfaces to IDABBDPrecReInit.
- FIDABBDOPT interfaces to IDABBDPRE optional output functions.
- FIDABBDFREE interfaces to IDABBDPrecFree.

In addition to the FORTRAN residual function FIDARESFUN, the user-supplied functions used by this package, are listed below, each with the corresponding interface function which calls it (and its type within IDABBDPRE or IDA):

FIDABBD routine (FORTRAN)	IDA function (C)	IDA function type
FIDAGLOCFN	FIDAgloc	IDABBDLocalFn
FIDACOMMFN	FIDAcfn	IDABBDCommFn
FIDAJTIMES	FIDAJtimes	IDASpilsJacTimesVecFn

As with the rest of the FIDA routines, the names of all user-supplied routines here are fixed, in order to maximize portability for the resulting mixed-language program. Additionally, based on flags discussed above in §6.1, the names of the user-supplied routines are mapped to actual values through a series of definitions in the header file fidabbd.h.

The following is a summary of the usage of this module. Steps that are unchanged from the main program described in $\S6.2$ are grayed-out.

- 1. Residual function specification
- 2. NVECTOR module initialization
- 3. Problem specification

4. Linear solver specification

To initialize the IDABBDPRE preconditioner, make the following call:

```
CALL FIDABBDINIT (NLOCAL, MUDQ, MLDQ, MU, ML, DQRELY, IER)
```

The arguments are as follows. NLOCAL is the local size of vectors on this processor. MUDQ and MLDQ are the upper and lower half-bandwidths to be used in the computation of the local Jacobian blocks by difference quotients. These may be smaller than the true half-bandwidths of the Jacobian of the local block of G, when smaller values may provide greater efficiency. MU and ML are the upper

and lower half-bandwidths of the band matrix that is retained as an approximation of the local Jacobian block. These may be smaller than MUDQ and MLDQ. DQRELY is the relative increment factor in y for difference quotients (optional). A value of 0.0 indicates the default, $\sqrt{\text{unit roundoff. IER}}$ is a return completion flag. A value of 0 indicates success, while a value of -1 indicates that a memory failure occurred or that an input had an illegal value.

To specify the SPGMR linear system solver and use the IDABBDPRE preconditioner, make the following call:

```
CALL FIDABBDSPGMR (MAXL, IGSTYPE, MAXRS, EPLIFAC, DQINCFAC, IER)
```

Its arguments are the same as those of FIDASPGMR (see step 4 in §6.2).

To specify the SPBCG linear system solver and use the IDABBDPRE preconditioner, make the following call:

```
CALL FIDABBDSPBCG (MAXL, EPLIFAC, DQINCFAC, IER)
```

Its arguments are the same as those of FIDASPBCG (see step 4 in §6.2).

To specify the SPTFQMR linear system solver and use the IDABBDPRE preconditioner, make the following call:

```
CALL FIDABBDSPTFQMR (MAXL, EPLIFAC, DQINCFAC, IER)
```

Its arguments are the same as those of FIDASPTFQMR (see step 4 in §6.2).

Optionally, to specify that SPGMR, SPBCG, or SPTFQMR should use the supplied FIDAJTIMES, make the call

```
CALL FIDASPILSSETJAC (FLAG, IER)
```

with FLAG $\neq 0$ (see step 4 in §6.2 for details).

5. Problem solution

6. IDABBDPRE Optional outputs

Optional outputs specific to the SPGMR, SPBCG, or SPTFQMR solver are listed in Table 6.2. To obtain the optional outputs associated with the IDABBDPRE module, make the following call:

```
CALL FIDABBDOPT (LENRWBBD, LENIWBBD, NGEBBD)
```

The arguments returned are as follows. LENRWBBD is the length of real preconditioner work space, in realtype words. LENIWBBD is the length of integer preconditioner work space, in integer words. Both of these sizes are local to the current processor. NGEBBD is the number of G(t, y, y') evaluations (calls to FIDALOCFN) so far.

7. Problem reinitialization

If a sequence of problems of the same size is being solved using the SPGMR, SPBCG, or SPTFQMR linear solver in combination with the IDABBDPRE preconditioner, then the IDA package can be reinitialized for the second and subsequent problems by calling FIDAREINIT, following which a call to FIDABBDINIT may or may not be needed. If the input arguments are the same, no FIDABBDINIT call is needed. If there is a change in input arguments other than MU, ML, or MAXL, then the user program should make the call

```
CALL FIDABBDREINIT (NLOCAL, MUDQ, MLDQ, DQRELY, IER)
```

This reinitializes the IDABBDPRE preconditioner, but without reallocating its memory. The arguments of the FIDABBDREINIT routine have the same names and meanings as those of FIDABBDINIT. If the value of MU or ML is being changed, then a call to FIDABBDINIT must be made. Finally, if MAXL is being changed, then a call to FIDABBDSPGMR, FIDABBDSPBCG, or FIDASPTFQMR must be made; in this case the linear solver memory is reallocated.

8. Memory deallocation

To free the internal memory created by the call to FIDABBDINIT, before calling FIDAFREE, the user must call

CALL FIDABBDFREE

9. User-supplied routines

The following two routines must be supplied for use with the IDABBDPRE module:

```
SUBROUTINE FIDAGLOCFN (NLOC, T, YLOC, YPLOC, GLOC, IPAR, RPAR, IER)
DIMENSION YLOC(*), YPLOC(*), GLOC(*), IPAR(*), RPAR(*)
```

This routine is to evaluate the function G(t,y,y') approximating F (possibly identical to F), in terms of T=t, and the arrays YLOC and YPLOC (of length NLOC), which are the sub-vectors of y and y' local to this processor. The resulting (local) sub-vector is to be stored in the array GLOC. IER is a return flag that should be set to 0 if successful, to 1 (for a recoverable error), or to -1 (for a non-recoverable error). The arrays IPAR (of integers) and RPAR (of reals) contain user data and are the same as those passed to FIDAMALLOC.

```
SUBROUTINE FIDACOMMFN (NLOC, T, YLOC, YPLOC, IPAR, RPAR, IER)
DIMENSION YLOC(*), YPLOC(*), IPAR(*), RPAR(*)
```

This routine is to perform the inter-processor communication necessary for the FIDAGLOCFN routine. Each call to FIDACOMMFN is preceded by a call to the residual routine FIDARESFUN with the same arguments T, YLOC, and YPLOC. Thus FIDACOMMFN can omit any communications done by FIDARESFUN if relevant to the evaluation of GLOC. The arrays IPAR (of integers) and RPAR (of reals) contain user data and are the same as those passed to FIDAMALLOC. IER is a return flag that should be set to 0 if successful, to 1 (for a recoverable error), or to -1 (for a non-recoverable error).

The subroutine FIDACOMMFN must be supplied even if it is empty and it must return IER=0.

Optionally, the user can supply a routine FIDAJTIMES for the evaluation of Jacobian-vector products, as described above in step 4 in §6.2.



Chapter 7

Description of the NVECTOR module

The SUNDIALS solvers are written in a data-independent manner. They all operate on generic vectors (of type N_Vector) through a set of operations defined by the particular NVECTOR implementation. Users can provide their own specific implementation of the NVECTOR module or use one of two provided within SUNDIALS, a serial and an MPI parallel implementations.

The generic N_Vector type is a pointer to a structure that has an implementation-dependent content field containing the description and actual data of the vector, and an ops field pointing to a structure with generic vector operations. The type N_Vector is defined as

```
typedef struct _generic_N_Vector *N_Vector;
struct _generic_N_Vector {
    void *content;
    struct _generic_N_Vector_Ops *ops;
};
```

The _generic_N_Vector_Ops structure is essentially a list of pointers to the various actual vector operations, and is defined as

```
struct _generic_N_Vector_Ops {
  N_Vector
              (*nvclone)(N_Vector);
              (*nvcloneempty)(N_Vector);
  N_Vector
  void
              (*nvdestroy)(N_Vector);
              (*nvspace)(N_Vector, long int *, long int *);
  void
              (*nvgetarraypointer)(N_Vector);
  realtype*
              (*nvsetarraypointer)(realtype *, N_Vector);
  void
  void
              (*nvlinearsum)(realtype, N_Vector, realtype, N_Vector, N_Vector);
              (*nvconst)(realtype, N_Vector);
  void
              (*nvprod)(N_Vector, N_Vector, N_Vector);
  void
              (*nvdiv)(N_Vector, N_Vector, N_Vector);
  void
  void
              (*nvscale)(realtype, N_Vector, N_Vector);
              (*nvabs)(N_Vector, N_Vector);
  void
              (*nvinv)(N_Vector, N_Vector);
  void
  void
              (*nvaddconst)(N_Vector, realtype, N_Vector);
              (*nvdotprod)(N_Vector, N_Vector);
  realtype
  realtype
              (*nvmaxnorm)(N_Vector);
              (*nvwrmsnorm)(N_Vector, N_Vector);
  realtype
  realtype
              (*nvwrmsnormmask)(N_Vector, N_Vector, N_Vector);
  realtype
              (*nvmin)(N_Vector);
```

```
realtype (*nvwl2norm)(N_Vector, N_Vector);
realtype (*nvl1norm)(N_Vector);
void (*nvcompare)(realtype, N_Vector, N_Vector);
booleantype (*nvinvtest)(N_Vector, N_Vector);
booleantype (*nvconstrmask)(N_Vector, N_Vector, N_Vector);
realtype (*nvminquotient)(N_Vector, N_Vector);
};
```

The generic NVECTOR module defines and implements the vector operations acting on N_Vector. These routines are nothing but wrappers for the vector operations defined by a particular NVECTOR implementation, which are accessed through the *ops* field of the N_Vector structure. To illustrate this point we show below the implementation of a typical vector operation from the generic NVECTOR module, namely N_VScale, which performs the scaling of a vector x by a scalar c:

```
void N_VScale(realtype c, N_Vector x, N_Vector z)
{
   z->ops->nvscale(c, x, z);
}
```

Table 7.1 contains a complete list of all vector operations defined by the generic NVECTOR module.

Finally, note that the generic NVECTOR module defines the functions N_VCloneVectorArray and N_VCloneEmptyVectorArray. Both functions create (by cloning) an array of count variables of type N_Vector, each of the same type as an existing N_Vector. Their prototypes are

```
N_Vector *N_VCloneVectorArray(int count, N_Vector w);
N_Vector *N_VCloneEmptyVectorArray(int count, N_Vector w);
```

and their definitions are based on the implementation-specific N_VClone and N_VCloneEmpty operations, respectively.

An array of variables of type N_Vector can be destroyed by calling N_VDestroyVectorArray, whose prototype is

```
void N_VDestroyVectorArray(N_Vector *vs, int count);
```

and whose definition is based on the implementation-specific N_VDestroy operation.

A particular implementation of the NVECTOR module must:

- Specify the *content* field of N_Vector.
- Define and implement the vector operations. Note that the names of these routines should be unique to that implementation in order to permit using more than one NVECTOR module (each with different N_Vector internal data representations) in the same code.
- Define and implement user-callable constructor and destructor routines to create and free an N_Vector with the new *content* field and with *ops* pointing to the new vector operations.
- Optionally, define and implement additional user-callable routines acting on the newly defined N_Vector (e.g., a routine to print the content for debugging purposes).
- Optionally, provide accessor macros as needed for that particular implementation to be used to access different parts in the *content* field of the newly defined N_Vector.

Table 7.1: Description of the NVECTOR operations

Name	Usage and Description
N_VClone	<pre>v = N_VClone(w); Creates a new N_Vector of the same type as an existing vector w and sets the ops field. It does not copy the vector, but rather allocates storage for the new vector.</pre>
N_VCloneEmpty	<pre>v = N_VCloneEmpty(w); Creates a new N_Vector of the same type as an existing vector w and sets the ops field. It does not allocate storage for the data array.</pre>
N_VDestroy	N_VDestroy(v); Destroys the N_Vector v and frees memory allocated for its internal data.
N_VSpace	N_VSpace(nvSpec, &lrw, &liw); Returns storage requirements for one N_Vector. lrw contains the number of realtype words and liw contains the number of integer words.
N_VGetArrayPointer	<pre>vdata = N_VGetArrayPointer(v); Returns a pointer to a realtype array from the N_Vector v. Note that this assumes that the internal data in N_Vector is a contiguous array of realtype. This routine is only used in the solver-specific interfaces to the dense and banded linear solvers, as well as the interfaces to the banded preconditioners provided with SUNDIALS.</pre>
N_VSetArrayPointer	N_VSetArrayPointer(vdata, v); Overwrites the data in an N_Vector with a given array of realtype. Note that this assumes that the internal data in N_Vector is a contiguous array of realtype. This routine is only used in the interfaces to the dense linear solver.
N_VLinearSum	N_VLinearSum(a, x, b, y, z); Performs the operation $z = ax + by$, where a and b are scalars and x and y are of type N_Vector: $z_i = ax_i + by_i$, $i = 0, \ldots, n-1$.
N_VConst	N_VConst(c, z); Sets all components of the N_Vector z to c: $z_i=c,\ i=0,\dots,n-1.$
N_VProd	N_VProd(x, y, z); Sets the N_Vector z to be the component-wise product of the N_Vector inputs x and y: $z_i = x_i y_i$, $i = 0, \ldots, n-1$.
N_VDiv	N_VDiv(x, y, z); Sets the N_Vector z to be the component-wise ratio of the N_Vector inputs x and y: $z_i = x_i/y_i$, $i = 0, \ldots, n-1$. The y_i may not be tested for 0 values. It should only be called with an x that is guaranteed to have all nonzero components.
	continued on next page

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Name	Usage and Description
N_VScale	N_VScale(c, x, z); Scales the N_Vector x by the scalar c and returns the result in z: $z_i = cx_i$, $i = 0,, n-1$.
N_VAbs	N_VAbs(x, z); Sets the components of the N_Vector z to be the absolute values of the components of the N_Vector x: $y_i = x_i , i = 0, \ldots, n-1$.
N_VInv	N_VInv(x, z); Sets the components of the N_Vector z to be the inverses of the components of the N_Vector x: $z_i = 1.0/x_i, i = 0, \ldots, n-1$. This routine may not check for division by 0. It should be called only with an x which is guaranteed to have all nonzero components.
N_VAddConst	N_VAddConst(x, b, z); Adds the scalar b to all components of x and returns the result in the N_Vector z: $z_i = x_i + b, i = 0, \ldots, n-1$.
N_VDotProd	d = N_VDotProd(x, y); Returns the value of the ordinary dot product of x and y: $d = \sum_{i=0}^{n-1} x_i y_i$.
N_VMaxNorm	m = N_VMaxNorm(x); Returns the maximum norm of the N_Vector x: $m = \max_i x_i $.
N_VWrmsNorm	m = N_VWrmsNorm(x, w) Returns the weighted root-mean-square norm of the N_Vector x with weight vector w: $m = \sqrt{\left(\sum_{i=0}^{n-1} (x_i w_i)^2\right)/n}$.
N_VWrmsNormMask	m = N_VWrmsNormMask(x, w, id); Returns the weighted root mean square norm of the N_Vector x with weight vector w built using only the elements of x corresponding to nonzero elements of the N_Vector id:
N_VMin	$m = \sqrt{\left(\sum_{i=0}^{n-1} (x_i w_i \text{sign}(id_i))^2\right)/n}.$ $m = \text{N_VMin(x)};$ Returns the smallest element of the N_Vector x: $m = \min_i x_i$.
N_VWL2Norm	m = N_VWL2Norm(x, w); Returns the weighted Euclidean ℓ_2 norm of the N_Vector x with weight vector w: $m = \sqrt{\sum_{i=0}^{n-1} (x_i w_i)^2}$.
N_VL1Norm	m = N_VL1Norm(x); Returns the ℓ_1 norm of the N_Vector x: $m = \sum_{i=0}^{n-1} x_i $.
N_VCompare	N_VCompare(c, x, z); Compares the components of the N_Vector x to the scalar c and returns an N_Vector z such that: $z_i = 1.0$ if $ x_i \ge c$ and $z_i = 0.0$ otherwise.
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Name	Usage and Description
N_VInvTest	t = N_VInvTest(x, z); Sets the components of the N_Vector z to be the inverses of the components of the N_Vector x, with prior testing for zero values: $z_i = 1.0/x_i, i = 0, \ldots, n-1$. This routine returns TRUE if all components of x are nonzero (successful inversion) and returns FALSE otherwise.
N_VConstrMask	t = N_VConstrMask(c, x, m); Performs the following constraint tests: $x_i > 0$ if $c_i = 2$, $x_i \geq 0$ if $c_i = 1$, $x_i \leq 0$ if $c_i = -1$, $x_i < 0$ if $c_i = -2$. There is no constraint on x_i if $c_i = 0$. This routine returns FALSE if any element failed the constraint test, TRUE if all passed. It also sets a mask vector m, with elements equal to 1.0 where the constraint test failed, and 0.0 where the test passed. This routine is used only for constraint checking.
N_VMinQuotient	minq = N_VMinQuotient(num, denom); This routine returns the minimum of the quotients obtained by termwise dividing num _i by denom _i . A zero element in denom will be skipped. If no such quotients are found, then the large value BIG_REAL (defined in the header file sundials_types.h) is returned.

7.1 The NVECTOR_SERIAL implementation

The serial implementation of the NVECTOR module provided with SUNDIALS, NVECTOR_SERIAL, defines the *content* field of N_Vector to be a structure containing the length of the vector, a pointer to the beginning of a contiguous data array, and a boolean flag *own_data* which specifies the ownership of *data*.

```
struct _N_VectorContent_Serial {
  long int length;
  booleantype own_data;
  realtype *data;
};
```

The following five macros are provided to access the content of an NVECTOR_SERIAL vector. The suffix _S in the names denotes serial version.

• NV_CONTENT_S

This routine gives access to the contents of the serial vector N_Vector.

The assignment $v_cont = NV_CONTENT_S(v)$ sets v_cont to be a pointer to the serial N_Vector content structure.

Implementation:

```
#define NV_CONTENT_S(v) ( (N_VectorContent_Serial)(v->content) )
```

• NV_OWN_DATA_S, NV_DATA_S, NV_LENGTH_S

These macros give individual access to the parts of the content of a serial N_Vector.

The assignment $v_{data} = NV_DATA_S(v)$ sets v_{data} to be a pointer to the first component of the data for the $N_Vector v$. The assignment $NV_DATA_S(v) = v_{data}$ sets the component array of v to be v_{data} by storing the pointer v_{data} .

The assignment $v_len = NV_LENGTH_S(v)$ sets v_len to be the length of v. On the other hand, the call $NV_LENGTH_S(v) = len_v$ sets the length of v to be len_v .

Implementation:

```
#define NV_OWN_DATA_S(v) ( NV_CONTENT_S(v)->own_data )
#define NV_DATA_S(v) ( NV_CONTENT_S(v)->data )
#define NV_LENGTH_S(v) ( NV_CONTENT_S(v)->length )
```

• NV_Ith_S

This macro gives access to the individual components of the data array of an N_Vector.

The assignment $r = NV_{i,i}$ sets r to be the value of the i-th component of v. The assignment $NV_{i,i} = r$ sets the value of the i-th component of v to be r.

Here i ranges from 0 to n-1 for a vector of length n.

Implementation:

```
#define NV_Ith_S(v,i) ( NV_DATA_S(v)[i] )
```

The NVECTOR_SERIAL module defines serial implementations of all vector operations listed in Table 7.1. Their names are obtained from those in Table 7.1 by appending the suffix _Serial. The module NVECTOR_SERIAL provides the following additional user-callable routines:

• N_VNew_Serial

This function creates and allocates memory for a serial N_Vector. Its only argument is the vector length.

```
N_Vector N_VNew_Serial(long int vec_length);
```

• N_VNewEmpty_Serial

This function creates a new serial N_Vector with an empty (NULL) data array.

```
N_Vector N_VNewEmpty_Serial(long int vec_length);
```

• N_VMake_Serial

This function creates and allocates memory for a serial vector with user-provided data array.

```
N_Vector N_VMake_Serial(long int vec_length, realtype *v_data);
```

• N_VCloneVectorArray_Serial

This function creates (by cloning) an array of count serial vectors.

```
N_Vector *N_VCloneVectorArray_Serial(int count, N_Vector w);
```

• N_VCloneVectorArrayEmpty_Serial

This function creates (by cloning) an array of count serial vectors, each with an empty (NULL) data array.

```
N_Vector *N_VCloneVectorArrayEmpty_Serial(int count, N_Vector w);
```

• N_VDestroyVectorArray_Serial

This function frees memory allocated for the array of count variables of type N_Vector created with N_VCloneVectorArray_Serial or with N_VCloneVectorArrayEmpty_Serial.

```
void N_VDestroyVectorArray_Serial(N_Vector *vs, int count);
```

• N_VPrint_Serial

This function prints the content of a serial vector to stdout.

```
void N_VPrint_Serial(N_Vector v);
```

Notes

- When looping over the components of an N_Vector v, it is more efficient to first obtain the component array via v_data = NV_DATA_S(v) and then access v_data[i] within the loop than it is to use NV_Ith_S(v,i) within the loop.
- N_VNewEmpty_Serial, N_VMake_Serial, and N_VCloneVectorArrayEmpty_Serial set the field own_data = FALSE. N_VDestroy_Serial and N_VDestroyVectorArray_Serial will not attempt to free the pointer data for any N_Vector with own_data set to FALSE. In such a case, it is the user's responsibility to deallocate the data pointer.
- To maximize efficiency, vector operations in the NVECTOR_SERIAL implementation that have more than one N_Vector argument do not check for consistent internal representation of these vectors. It is the user's responsibility to ensure that such routines are called with N_Vector arguments that were all created with the same internal representations.





7.2 The NVECTOR_PARALLEL implementation

The parallel implementation of the NVECTOR module provided with SUNDIALS, NVECTOR_PARALLEL, defines the *content* field of N_Vector to be a structure containing the global and local lengths of the vector, a pointer to the beginning of a contiguous local data array, an MPI communicator, an a boolean flag own_data indicating ownership of the data array data.

```
struct _N_VectorContent_Parallel {
  long int local_length;
  long int global_length;
  booleantype own_data;
  realtype *data;
  MPI_Comm comm;
};
```

The following seven macros are provided to access the content of a NVECTOR_PARALLEL vector. The suffix _P in the names denotes parallel version.

• NV_CONTENT_P

This macro gives access to the contents of the parallel vector N_Vector.

The assignment $v_cont = NV_CONTENT_P(v)$ sets v_cont to be a pointer to the N_Vector content structure of type struct $_N_VectorParallelContent$.

Implementation:

```
#define NV_CONTENT_P(v) ( (N_VectorContent_Parallel)(v->content) )
```

• NV_OWN_DATA_P, NV_DATA_P, NV_LOCLENGTH_P, NV_GLOBLENGTH_P

These macros give individual access to the parts of the content of a parallel N_Vector.

The assignment $v_{data} = NV_DATA_P(v)$ sets v_{data} to be a pointer to the first component of the local data for the $N_Vector\ v$. The assignment $NV_DATA_P(v) = v_{data}$ sets the component array of v to be v_{data} by storing the pointer v_{data} .

The assignment v_llen = NV_LOCLENGTH_P(v) sets v_llen to be the length of the local part of v. The call NV_LENGTH_P(v) = llen_v sets the local length of v to be llen_v.

The assignment $v_glen = NV_GLOBLENGTH_P(v)$ sets v_glen to be the global length of the vector v. The call $NV_GLOBLENGTH_P(v) = glen_v$ sets the global length of v to be $glen_v$.

Implementation:

```
#define NV_OWN_DATA_P(v) ( NV_CONTENT_P(v)->own_data )
#define NV_DATA_P(v) ( NV_CONTENT_P(v)->data )
```

```
#define NV_LOCLENGTH_P(v) ( NV_CONTENT_P(v)->local_length )
#define NV_GLOBLENGTH_P(v) ( NV_CONTENT_P(v)->global_length )
```

• NV_COMM_P

This macro provides access to the MPI communicator used by the NVECTOR_PARALLEL vectors. Implementation:

```
#define NV_COMM_P(v) ( NV_CONTENT_P(v)->comm )
```

• NV_Ith_P

This macro gives access to the individual components of the local data array of an N-Vector.

The assignment $r = NV_i(v,i)$ sets r to be the value of the i-th component of the local part of v. The assignment $NV_i(v,i) = r$ sets the value of the i-th component of the local part of v to be r.

Here i ranges from 0 to n-1, where n is the local length.

Implementation:

```
#define NV_Ith_P(v,i) ( NV_DATA_P(v)[i] )
```

The NVECTOR_PARALLEL module defines parallel implementations of all vector operations listed in Table 7.1 Their names are obtained from those in Table 7.1 by appending the suffix _Parallel. The module NVECTOR_PARALLEL provides the following additional user-callable routines:

• N_VNew_Parallel

This function creates and allocates memory for a parallel vector.

• N_VNewEmpty_Parallel

This function creates a new parallel N_Vector with an empty (NULL) data array.

• N_VMake_Parallel

This function creates and allocates memory for a parallel vector with user-provided data array.

• N_VCloneVectorArray_Parallel

This function creates (by cloning) an array of count parallel vectors.

```
N_Vector *N_VCloneVectorArray_Parallel(int count, N_Vector w);
```

• N_VCloneVectorArrayEmpty_Parallel

This function creates (by cloning) an array of count parallel vectors, each with an empty (NULL) data array.

N_Vector *N_VCloneVectorArrayEmpty_Parallel(int count, N_Vector w);

• N_VDestroyVectorArray_Parallel

This function frees memory allocated for the array of count variables of type N_Vector created with N_VCloneVectorArray_Parallel or with N_VCloneVectorArrayEmpty_Parallel.

```
void N_VDestroyVectorArray_Parallel(N_Vector *vs, int count);
```

• N_VPrint_Parallel

```
This function prints the content of a parallel vector to stdout. void N_VPrint_Parallel(N_Vector v);
```

Notes

- When looping over the components of an N_Vector v, it is more efficient to first obtain the local component array via v_data = NV_DATA_P(v) and then access v_data[i] within the loop than it is to use NV_Ith_P(v,i) within the loop.
- N_VNewEmpty_Parallel, N_VMake_Parallel, and N_VCloneVectorArrayEmpty_Parallel set the field own_data = FALSE. N_VDestroy_Parallel and N_VDestroyVectorArray_Parallel will not attempt to free the pointer data for any N_Vector with own_data set to FALSE. In such a case, it is the user's responsibility to deallocate the data pointer.
- To maximize efficiency, vector operations in the NVECTOR_PARALLEL implementation that have more than one N_Vector argument do not check for consistent internal representation of these vectors. It is the user's responsibility to ensure that such routines are called with N_Vector arguments that were all created with the same internal representations.

7.3 NVECTOR functions used by IDA

In Table 7.2 below, we list the vector functions in the NVECTOR module used by the IDA package. The table also shows, for each function, which of the code modules uses the function. The IDA column shows function usage within the main integrator module, while the remaining five columns show function usage within each of the five IDA linear solvers (IDASPILS stands for any of IDASPGMR, IDASPBCG, or IDASPTFQMR), the IDABBDPRE preconditioner module, and the FIDA module.

There is one subtlety in the IDASPILS column hidden by the table, explained here for the case of the IDASPGMR module). The N_VDotProd function is called both within the implementation file ida_spgmr.c for the IDASPGMR solver and within the implementation files sundials_spgmr.c and iterative.c for the generic SPGMR solver upon which the IDASPGMR solver is implemented. Also, although N_VDiv and N_VProd are not called within the implementation file idaspgmr.c, they are called within the implementation file spgmr.c and so are required by the IDASPGMR solver module. This issue does not arise for the direct IDA linear solvers because the generic DENSE and BAND solvers (used in the implementation of IDADENSE and IDABAND) do not make calls to any vector functions.

Of the functions listed in Table 7.1, N_VWL2Norm, N_VL1Norm, N_VCloneEmpty, and N_VInvTest are not used by IDA. Therefore a user-supplied NVECTOR module for IDA could omit these four functions.





Table 7.2: List of vector functions usage by IDA code modules

	IDA	IDADENSE	IDABAND	IDASPILS	IDABBDPRE	FIDA
N_VClone	√			√	√	
N_VDestroy	√			√	√	
N_VSpace	√					
N_VGetArrayPointer		√	√		√	√
N_VSetArrayPointer		√				√
N_VLinearSum	√	√		√		
N_VConst	√			√		
N_VProd	√			√		
N_VDiv	√			√		
N_VScale	√	√	√	>	√	
N_VAbs	√					
N_VInv	√					
N_VAddConst	√					
N_VDotProd				>		
N_VMaxNorm	√					
N_VWrmsNorm	√					
N_VMin	√					
N_VMinQuotient	√					
N_VConstrMask	√					
N_VWrmsNormMask	√					
N_VCompare	√					

Chapter 8

Providing Alternate Linear Solver Modules

The central IDA module interfaces with the linear solver module to be used by way of calls to five routines. These are denoted here by linit, lsetup, lsolve, lperf, and lfree. Briefly, their purposes are as follows:

- linit: initialize and allocate memory specific to the linear solver;
- lsetup: evaluate and preprocess the Jacobian or preconditioner;
- lsolve: solve the linear system;
- lperf: monitor performance and issue warnings;
- lfree: free the linear solver memory.

A linear solver module must also provide a user-callable specification routine (like those described in §5.5.3) which will attach the above five routines to the main IDA memory block. The IDA memory block is a structure defined in the header file ida_impl.h. A pointer to such a structure is defined as the type IDAMem. The five fields in a IDAMem structure that must point to the linear solver's functions are ida_linit, ida_lsetup, ida_lsolve, ida_lperf, and ida_lfree, respectively. Note that of the four interface routines, only the lsolve routine is required. The lfree routine must be provided only if the solver specification routine makes any memory allocation. For consistency with the existing IDA linear solver modules, we recommend that the return value of the specification function be 0 for a successful return or a negative value if an error occurs (the pointer to the main IDA memory block is NULL, an input is illegal, the NVECTOR implementation is not compatible, a memory allocation fails, etc.)

To facilitate data exchange between the five interface functions, the field idalmem in the IDA memory block can be used to attach a linear solver-specific memory block.

These five routines, which interface between IDA and the linear solver module, necessarily have fixed call sequences. Thus a user wishing to implement another linear solver within the IDA package must adhere to this set of interfaces. The following is a complete description of the call list for each of these routines. Note that the call list of each routine includes a pointer to the main IDA memory block, by which the routine can access various data related to the IDA solution. The contents of this memory block are given in the file ida.h (but not reproduced here, for the sake of space).

8.1 Initialization function

linit

Definition int (*linit)(IDAMem IDA_mem);

Purpose The purpose of linit is to complete initializations for a specific linear solver, such as

counters and statistics.

Arguments IDA_mem is the IDA memory pointer of type IDAMem.

Return value An limit function should return 0 if it has successfully initialized the IDA linear solver

and a negative value otherwise.

8.2 Setup routine

The type definition of lsetup is

lsetup

Definition int (*lsetup)(IDAMem IDA_mem, N_Vector yyp, N_Vector ypp,

N_Vector resp,

N_Vector vtemp1, N_Vector vtemp2, N_Vector vtemp3);

Purpose The job of lsetup is to prepare the linear solver for subsequent calls to lsolve. It may

re-compute Jacobian-related data if it deems necessary.

Arguments IDA_mem is the IDA memory pointer of type IDAMem.

yyp is the predicted y vector for the current IDA internal step. ypp is the predicted y' vector for the current IDA internal step.

resp is the value of the residual function at yyp and ypp, i.e. $F(t_n, y_{pred}, y'_{pred})$.

vtemp1 vtemp2

vtemp3 are temporary variables of type N_Vector provided for use by lsetup.

Return value The lsetup routine should return 0 if successful, a positive value for a recoverable error, and a negative value for an unrecoverable error.

8.3 Solve routine

The type definition of lsolve is

lsolve

Definition int (*lsolve)(IDAMem IDA_mem, N_Vector b, N_Vector weight,

N_Vector ycur, N_Vector ypcur, N_Vector rescur);

Purpose The routine 1solve must solve the linear equation Mx = b, where M is some approxi-

mation to $J = \partial F/\partial y + c_j \partial F/\partial y'$ (see Eqn. (3.5)), and the right-hand side vector b is

input.

Arguments IDA_mem is the IDA memory pointer of type IDAMem.

b is the right-hand side vector b. The solution is to be returned in the vector b.

weight is a vector that contains the error weights. These are the W_i of (3.6).

ycur is a vector that contains the solver's current approximation to $y(t_n)$. ypcur is a vector that contains the solver's current approximation to $y'(t_n)$.

rescur is a vector that contains $F(t_n, y_{cur}, y'_{cur})$.

Return value lsolve returns a positive value for a recoverable error and a negative value for an unrecoverable error. Success is indicated by a 0 return value.

8.4 Performance monitoring routine

The type definition of lperf is

lperf

Definition int (*lperf)(IDAMem IDA_mem, int perftask);

Purpose The routine lperf is to monitor the performance of the linear solver.

Arguments IDA_mem is the IDA memory pointer of type IDAMem.

perftask is a task flag. perftask = 0 means initialize needed counters. perftask = 0

1 means evaluate performance and issue warnings if needed.

Return value The lperf return value is ignored.

8.5 Memory deallocation routine

The type definition of lfree is

lfree

Definition void (*lfree)(IDAMem IDA_mem);

Purpose The routine lfree should free up any memory allocated by the linear solver.

Arguments The argument IDa_mem is the IDA memory pointer of type IDAMem.

Return value This routine has no return value.

Notes This routine is called once a problem has been completed and the linear solver is no

longer needed.

Chapter 9

Generic Linear Solvers in SUNDIALS

In this section, we describe five generic linear solver code modules that are included in IDA, but which are of potential use as generic packages in themselves, either in conjunction with the use of IDA or separately. These modules are:

- The DENSE matrix package, which includes the matrix type DenseMat, macros and functions for DenseMat matrices, and functions for small dense matrices treated as simple array types.
- The BAND matrix package, which includes the matrix type BandMat, macros and functions for BandMat matrices.
- The SPGMR package, which includes a solver for the scaled preconditioned GMRES method.
- The SPBCG package, which includes a solver for the scaled preconditioned Bi-CGStab method.
- The SPTFQMR package, which includes a solver for the scaled preconditioned TFQMR method.

For reasons related to installation, the names of the files involved in these generic solvers begin with the prefix sundials. But despite this, each of the solvers is in fact generic, in that it is usable completely independently of SUNDIALS.

For the sake of space, the functions for DenseMat and BandMat matrices and the functions in SPGMR, SPBCG, and SPTFQMR are only summarized briefly, since they are less likely to be of direct use in connection with IDA. The functions for small dense matrices are fully described, because we expect that they will be useful in the implementation of preconditioners used with the combination of IDA and the IDASPGMR, IDASPBCG, or IDASPTFQMR solver.

9.1 The DENSE module

Relative to the SUNDIALS source_tree, the files comprising the DENSE generic linear solver are as follows:

- header files (located in source_tree/shared/include)
 sundials_dense.h sundials_smalldense.h
 sundials_types.h sundials_math.h sundials_config.h
- source files (located in source_tree/shared/source)
 sundials_dense.c sundials_smalldense.c sundials_math.c

Only two of the preprocessing directives in the header file sundials_config.h are relevant to the DENSE package by itself (see §2.5 for details):

• (required) definition of the precision of the SUNDIALS type realtype. One of the following lines must be present:

```
#define SUNDIALS_DOUBLE_PRECISION 1
#define SUNDIALS_SINGLE_PRECISION 1
#define SUNDIALS_EXTENDED_PRECISION 1
```

• (optional) use of generic math functions: #define SUNDIALS_USE_GENERIC_MATH 1

The sundials_types.h header file defines the SUNDIALS realtype and booleantype types and the macro RCONST, while the sundials_math.h header file is needed for the ABS macro and RAbs function. The eight files listed above can be extracted from the SUNDIALS source_tree and compiled by themselves into a DENSE library or into a larger user code.

9.1.1 Type DenseMat

The type DenseMat is defined to be a pointer to a structure with a size and a data field:

```
typedef struct {
  long int size;
  realtype **data;
} *DenseMat;
```

The *size* field indicates the number of columns (which is the same as the number of rows) of a dense matrix, while the *data* field is a two dimensional array used for component storage. The elements of a dense matrix are stored columnwise (i.e columns are stored one on top of the other in memory). If A is of type DenseMat, then the (i,j)-th element of A (with $0 \le i, j \le size-1$) is given by the expression (A->data)[j][i] or by the expression (A->data)[0][j*size+i]. The macros below allow a user to efficiently access individual matrix elements without writing out explicit data structure references and without knowing too much about the underlying element storage. The only storage assumption needed is that elements are stored columnwise and that a pointer to the j-th column of elements can be obtained via the DENSE_COL macro. Users should use these macros whenever possible.

9.1.2 Accessor Macros

The following two macros are defined by the DENSE module to provide access to data in the DenseMat type:

• DENSE_ELEM

```
Usage: DENSE_ELEM(A,i,j) = a_ij; or a_ij = DENSE_ELEM(A,i,j); DENSE_ELEM references the (i,j)-th element of the N \times N DenseMat A, 0 \le i, j \le N - 1.
```

• DENSE_COL

```
Usage : col_j = DENSE_COL(A,j);
```

DENSE_COL references the j-th column of the $N \times N$ DenseMat A, $0 \le j \le N-1$. The type of the expression DENSE_COL(A,j) is realtype *. After the assignment in the usage above, col_j may be treated as an array indexed from 0 to N-1. The (i, j)-th element of A is referenced by col_j[i].

9.1.3 Functions

The following functions for DenseMat matrices are available in the DENSE package. For full details, see the header file sundials_dense.h.

- DenseAllocMat: allocation of a DenseMat matrix;
- DenseAllocPiv: allocation of a pivot array for use with DenseFactor/DenseBacksolve;

- DenseFactor: LU factorization with partial pivoting;
- DenseBacksolve: solution of Ax = b using LU factorization;
- DenseZero: load a matrix with zeros;
- DenseCopy: copy one matrix to another;
- DenseScale: scale a matrix by a scalar;
- DenseAddI: increment a matrix by the identity matrix;
- DenseFreeMat: free memory for a DenseMat matrix;
- DenseFreePiv: free memory for a pivot array;
- DensePrint: print a DenseMat matrix to standard output.

9.1.4 Small Dense Matrix Functions

The following functions for small dense matrices are available in the DENSE package:

• denalloc

denalloc(n) allocates storage for an n by n dense matrix. It returns a pointer to the newly allocated storage if successful. If the memory request cannot be satisfied, then denalloc returns NULL. The underlying type of the dense matrix returned is realtype**. If we allocate a dense matrix realtype** a by a = denalloc(n), then a[j][i] references the (i,j)-th element of the matrix a, $0 \le i$, $j \le n-1$, and a[j] is a pointer to the first element in the j-th column of a. The location a[0] contains a pointer to n^2 contiguous locations which contain the elements of a.

• denallocpiv

denallocpiv(n) allocates an array of n integers. It returns a pointer to the first element in the array if successful. It returns NULL if the memory request could not be satisfied.

• gefa

gefa(a,n,p) factors the n by n dense matrix a. It overwrites the elements of a with its LU factors and keeps track of the pivot rows chosen in the pivot array p.

A successful LU factorization leaves the matrix a and the pivot array p with the following information:

- 1. p[k] contains the row number of the pivot element chosen at the beginning of elimination step k, k = 0, 1, ..., n-1.
- 2. If the unique LU factorization of a is given by Pa = LU, where P is a permutation matrix, L is a lower triangular matrix with all 1's on the diagonal, and U is an upper triangular matrix, then the upper triangular part of a (including its diagonal) contains U and the strictly lower triangular part of a contains the multipliers, I L.

gefa returns 0 if successful. Otherwise it encountered a zero diagonal element during the factorization. In this case it returns the column index (numbered from one) at which it encountered the zero.

• gesl

gesl(a,n,p,b) solves the n by n linear system ax = b. It assumes that a has been LU-factored and the pivot array p has been set by a successful call to gefa(a,n,p). The solution x is written into the b array.

• denzero

denzero(a,n) sets all the elements of the n by n dense matrix a to be 0.0;

• dencopy

dencopy(a,b,n) copies the n by n dense matrix a into the n by n dense matrix b;

• denscale

denscale(c,a,n) scales every element in the n by n dense matrix a by c;

denaddT

denaddI(a,n) increments the n by n dense matrix a by the identity matrix;

• denfreepiv

denfreepiv(p) frees the pivot array p allocated by denallocpiv;

• denfree

denfree(a) frees the dense matrix a allocated by denalloc;

• denprint

denprint(a,n) prints the n by n dense matrix a to standard output as it would normally appear on paper. It is intended as a debugging tool with small values of n. The elements are printed using the %g option. A blank line is printed before and after the matrix.

9.2 The BAND module

Relative to the SUNDIALS source_tree, the files comprising the BAND generic linear solver are as follows:

- header files (located in source_tree/shared/include) sundials_band.h sundials_types.h sundials_math.h sundials_config.h
- source files (located in *source_tree*/shared/source) sundials_band.c sundials_math.c

Only two of the preprocessing directives in the header file sundials_config.h are required to use the BAND package by itself (see §2.5 for details):

• (required) definition of the precision of the SUNDIALS type realtype. One of the following lines must be present:

```
#define SUNDIALS_DOUBLE_PRECISION 1
#define SUNDIALS_SINGLE_PRECISION 1
#define SUNDIALS_EXTENDED_PRECISION 1
```

• (optional) use of generic math functions: #define SUNDIALS_USE_GENERIC_MATH 1

The sundials_types.h header file defines of the SUNDIALS realtype and booleantype types and the macro RCONST, while the sundials_math.h header file is needed for the MIN, MAX, and ABS macros and RAbs function.

The six files listed above can be extracted from the SUNDIALS *source_tree* and compiled by themselves into a BAND library or into a larger user code.

9.2.1 Type BandMat

The type BandMat is the type of a large band matrix A (possibly distributed). It is defined to be a pointer to a structure defined by:

```
typedef struct {
  long int size;
  long int mu, ml, smu;
  realtype **data;
} *BandMat;
```

The fields in the above structure are:

- *size* is the number of columns (which is the same as the number of rows);
- mu is the upper half-bandwidth, $0 \le mu \le size-1$;
- ml is the lower half-bandwidth, $0 \le ml \le size-1$;
- smu is the storage upper half-bandwidth, $mu \le smu \le size-1$. The BandFactor routine writes the LU factors into the storage for A. The upper triangular factor U, however, may have an upper half-bandwidth as big as $\min(size-1, mu+ml)$ because of partial pivoting. The smu field holds the upper half-bandwidth allocated for A.
- data is a two dimensional array used for component storage. The elements of a band matrix of type BandMat are stored columnwise (i.e. columns are stored one on top of the other in memory).
 Only elements within the specified half-bandwidths are stored.

If we number rows and columns in the band matrix starting from 0, then

- data[0] is a pointer to (smu+ml+1)*size contiguous locations which hold the elements within the band of A
- data[j] is a pointer to the uppermost element within the band in the j-th column. This pointer may be treated as an array indexed from smu-mu (to access the uppermost element within the band in the j-th column) to smu+ml (to access the lowest element within the band in the j-th column). Indices from 0 to smu-mu-1 give access to extra storage elements required by BandFactor.
- data[j]/[i-j+smu] is the (i,j)-th element, $j-mu \le i \le j+ml$.

The macros below allow a user to access individual matrix elements without writing out explicit data structure references and without knowing too much about the underlying element storage. The only storage assumption needed is that elements are stored columnwise and that a pointer into the j-th column of elements can be obtained via the BAND_COL macro. Users should use these macros whenever possible.

See Figure 9.1 for a diagram of the BandMat type.

9.2.2 Accessor Macros

The following three macros are defined by the BAND module to provide access to data in the BandMat type:

• BAND_ELEM

```
Usage: BAND_ELEM(A,i,j) = a_ij; or a_ij = BAND_ELEM(A,i,j); 
BAND_ELEM references the (i,j)-th element of the N \times N band matrix A, where 0 \le i, j \le N-1. The location (i,j) should further satisfy j-(A->mu) \le i \le j+(A->m1).
```

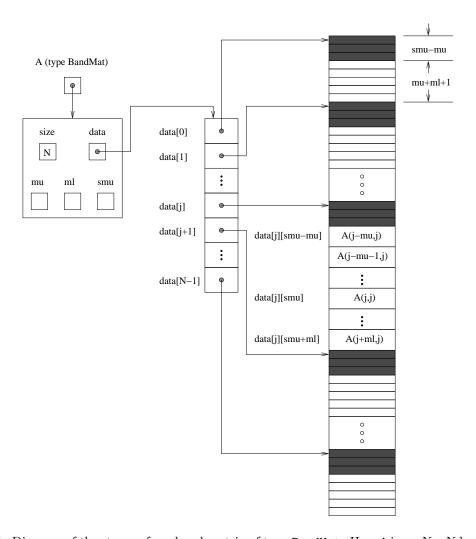


Figure 9.1: Diagram of the storage for a band matrix of type BandMat. Here A is an $N \times N$ band matrix of type BandMat with upper and lower half-bandwidths mu and ml, respectively. The rows and columns of A are numbered from 0 to N-1 and the (i,j)-th element of A is denoted A(i,j). The greyed out areas of the underlying component storage are used by the BandFactor and BandBacksolve routines.

• BAND_COL

```
Usage : col_j = BAND_COL(A,j);
```

BAND_COL references the diagonal element of the j-th column of the $N \times N$ band matrix A, $0 \le j \le N-1$. The type of the expression BAND_COL(A,j) is realtype *. The pointer returned by the call BAND_COL(A,j) can be treated as an array which is indexed from -(A-mu) to (A-ml).

• BAND_COL_ELEM

```
Usage : BAND_COL_ELEM(col_j,i,j) = a_ij; or a_ij = BAND_COL_ELEM(col_j,i,j);
```

This macro references the (i,j)-th entry of the band matrix A when used in conjunction with BAND_COL to reference the j-th column through col_j. The index (i,j) should satisfy $j-(A->mu) \le i \le j+(A->m1)$.

9.2.3 Functions

The following functions for BandMat matrices are available in the BAND package. For full details, see the header file sundials_band.h.

- BandAllocMat: allocation of a BandMat matrix;
- BandAllocPiv: allocation of a pivot array for use with BandFactor/BandBacksolve;
- BandFactor: LU factorization with partial pivoting;
- BandBacksolve: solution of Ax = b using LU factorization;
- BandZero: load a matrix with zeros;
- BandCopy: copy one matrix to another;
- BandScale: scale a matrix by a scalar;
- BandAddI: increment a matrix by the identity matrix;
- BandFreeMat: free memory for a BandMat matrix;
- BandFreePiv: free memory for a pivot array;
- BandPrint: print a BandMat matrix to standard output.

9.3 The SPGMR module

The SPGMR package, in the files sundials_spgmr.h and sundials_spgmr.c, includes an implementation of the scaled preconditioned GMRES method. A separate code module, implemented in sundials_iterative.(h,c), contains auxiliary functions that support SPGMR, as well as the other Krylov solvers in SUNDIALS (SPBCG and SPTFQMR). For full details, including usage instructions, see the header files sundials_spgmr.h and sundials_iterative.h.

Relative to the SUNDIALS *source_tree*, the files comprising the SPGMR generic linear solver are as follows:

- header files (located in source_tree/shared/include)
 sundials_spgmr.h sundials_iterative.h sundials_nvector.h
 sundials_types.h sundials_math.h sundials_config.h
- source files (located in source_tree/shared/source)
 sundials_spgmr.c sundials_iterative.c sundials_nvector.c

Only two of the preprocessing directives in the header file sundials_config.h are required to use the SPGMR package by itself (see §2.5 for details):

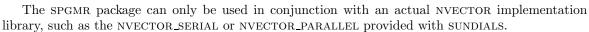
• (required) definition of the precision of the SUNDIALS type realtype. One of the following lines must be present:

```
#define SUNDIALS_DOUBLE_PRECISION 1
#define SUNDIALS_SINGLE_PRECISION 1
#define SUNDIALS_EXTENDED_PRECISION 1
```

(optional) use of generic math functions:
 #define SUNDIALS_USE_GENERIC_MATH 1

The sundials_types.h header file defines the SUNDIALS realtype and booleantype types and the macro RCONST, while the sundials_math.h header file is needed for the MAX and ABS macros and RAbs and RSqrt functions.

The generic NVECTOR files, sundials_nvector.(h,c) are needed for the definition of the generic N_Vector type and functions. The NVECTOR functions used by the SPGMR module are: N_VDotProd, N_VLinearSum, N_VScale, N_VProd, N_VDiv, N_VConst, N_VClone, N_VCloneVectorArray, N_VDestroy, and N_VDestroyVectorArray.



The nine files listed above can be extracted from the SUNDIALS *source_tree* and compiled by themselves into an SPGMR library or into a larger user code.

9.3.1 Functions

The following functions are available in the SPGMR package:

- SpgmrMalloc: allocation of memory for SpgmrSolve;
- SpgmrSolve: solution of Ax = b by the SPGMR method;
- SpgmrFree: free memory allocated by SpgmrMalloc.

The following functions are available in the support package sundials_iterative.(h,c):

- ModifiedGS: performs modified Gram-Schmidt procedure;
- ClassicalGS: performs classical Gram-Schmidt procedure;
- QRfact: performs QR factorization of Hessenberg matrix;
- QRsol: solves a least squares problem with a Hessenberg matrix factored by QRfact.

9.4 The SPBCG module

The SPBCG package, in the files sundials_spbcgs.h and sundials_spbcgs.c, includes an implementation of the scaled preconditioned Bi-CGStab method. For full details, including usage instructions, see the file sundials_spbcgs.h.

The SPBCG package can only be used in conjunction with an actual NVECTOR implementation library, such as the NVECTOR_SERIAL or NVECTOR_PARALLEL provided with SUNDIALS.

The files needed to use the SPBCG module by itself are the same as for the SPGMR module, with sundials_spbcgs.(h,c) replacing sundials_spgmr.(h,c).





9.4.1 Functions

The following functions are available in the SPBCG package:

- SpbcgMalloc: allocation of memory for SpbcgSolve;
- SpbcgSolve: solution of Ax = b by the SPBCG method;
- SpbcgFree: free memory allocated by SpbcgMalloc.

9.5 The SPTFQMR module

The SPTFQMR package, in the files sundials_sptfqmr.h and sundials_sptfqmr.c, includes an implementation of the scaled preconditioned TFQMR method. For full details, including usage instructions, see the file sundials_sptfqmr.h.

The SPTFQMR package can only be used in conjunction with an actual NVECTOR implementation library, such as the NVECTOR_SERIAL or NVECTOR_PARALLEL provided with SUNDIALS.

The files needed to use the SPTFQMR module by itself are the same as for the SPGMR module, with sundials_sptfqmr.(h,c) replacing sundials_spgmr.(h,c).

9.5.1 Functions

The following functions are available in the SPTFQMR package:

- SptfqmrMalloc: allocation of memory for SptfqmrSolve;
- SptfqmrSolve: solution of Ax = b by the SPTFQMR method;
- SptfqmrFree: free memory allocated by SptfqmrMalloc.



Chapter 10

IDA Constants

Below we list all input and output constants used by the main solver and linear solver modules, together with their numerical values and a short description of their meaning.

10.1 IDA input constants

IDA main solver module			
IDA_SS	1	Scalar relative tolerance, scalar absolute tolerance.	
IDA_SV	2	Scalar relative tolerance, vector absolute tolerance.	
IDA_NORMAL	1	Solver returns at specified output time.	
IDA_ONE_STEP	2	Solver returns after each successful step.	
IDA_NORMAL_TSTOP	3	Solver returns at specified output time, but does not proceed past the specified stopping time.	
IDA_ONE_STEP_TSTOP	4	Solver returns after each successful step, but does not proceed past the specified stopping time.	
IDA_YA_YDP_INIT	1	Compute y_a and y'_d , given y_d .	
IDA_Y_INIT	2	Compute y , given y' .	
	Ite	rative linear solver module	
PREC_NONE	0	No preconditioning	
PREC_LEFT	1	Preconditioning on the left.	
MODIFIED_GS	1	Use modified Gram-Schmidt procedure.	
CLASSICAL_GS	2	Use classical Gram-Schmidt procedure.	
OLADDIOAL_GD	2	ose classical Grain-Bellinius procedure.	

10.2 IDA output constants

IDA main solver module			
IDA_SUCCESS	0	Successful function return.	
IDA_TSTOP_RETURN	1	IDASolve succeeded by reaching the specified stopping point.	
IDA_ROOT_RETURN	2	IDASolve succeeded and found one or more roots.	
IDA_MEM_NULL	-1	The ida_mem argument was NULL.	
IDA_ILL_INPUT	-2	One of the function inputs is illegal.	
IDA_NO_MALLOC	-3	The IDA memory was not allocated by a call to IDAMalloc.	
IDA_TOO_MUCH_WORK	-4	The solver took mxstep internal steps but could not reach	
		tout.	

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IDA_TOO_MUCH_ACC	-5	The solver could not satisfy the accuracy demanded by the user for some internal step.
IDA_ERR_FAIL	-6	Error test failures occurred too many times during one inter-
	_	nal time step or minimum step size was reached.
IDA_CONV_FAIL	-7	Convergence test failures occurred too many times during one internal time step or minimum step size was reached.
IDA_LINIT_FAIL	-8	The linear solver's initialization function failed.
IDA_LSETUP_FAIL	-9	The linear solver's setup function failed in an unrecoverable
		manner.
IDA_LSOLVE_FAIL	-10	The linear solver's solve function failed in an unrecoverable
TDA DEG EATI	11	manner.
IDA_RES_FAIL	-11	The user-provided residual function failed in an unrecoverable
IDA_CONSTR_FAIL	-12	manner. The inequality constraints were violated and the solver was
IDA_CONSTR_I AIL	-12	unable to recover.
IDA_REP_RES_FAIL	-13	The user-provided residual function repeatedly returned a re-
		coverable error flag, but the solver was unable to recover.
IDA_MEM_FAIL	-14	A memory allocation failed.
IDA_BAD_T	-15	The time t s outside the last step taken.
IDA_BAD_EWT	-16	Zero value of some error weight component.
IDA_FIRST_RES_FAIL	-17	The user-provided residual function failed recoverably on the
		first call.
IDA_LINESEARCH_FAIL	-18	The line search failed.
IDA_NO_RECOVERY	-19	The residual function, linear solver setup function, or linear
		solver solve function had a recoverable failure, but IDACalcIC could not recover.
IDA_RTFUNC_FAIL	-20	The rootfinding function failed in an unrecoverable manner.
	-0	The recommendation range in an amount transfer incomment
	IDAI	DENSE linear solver module
IDADENSE_SUCCESS	0	Successful function return.
IDADENSE_MEM_NULL	-1	The ida_mem argument was NULL.
IDADENSE_LMEM_NULL	-2	The IDADENSE linear solver has not been initialized.
IDADENSE_ILL_INPUT	-3	The IDADENSE solver is not compatible with the current
		NVECTOR module.
IDADENSE_MEM_FAIL	-4	A memory allocation request failed.
IDADENSE_JACFUNC_UNRECVR	-5	The Jacobian function failed in an unrecoverable manner.
IDADENSE_JACFUNC_RECVR	-6	The Jacobian function had a recoverable error.
	IDA	BAND linear solver module
IDABAND_SUCCESS	0	Successful function return.
IDABAND_MEM_NULL	-1	The ida_mem argument was NULL.
IDABAND_LMEM_NULL IDABAND_ILL_INPUT	-2 -3	The IDABAND linear solver has not been initialized. The IDABAND solver is not compatible with the current NVEC-
TD4D4ND_TPP_TNL01	-0	TOR module.
IDABAND_MEM_FAIL	-4	A memory allocation request failed.
IDABAND_JACFUNC_UNRECVR	-5	The Jacobian function failed in an unrecoverable manner.
IDABAND_JACFUNC_RECVR	-6	The Jacobian function had a recoverable error.

	IDA	SPILS linear solver modules	
IDASPILS_SUCCESS	0	Successful function return.	
IDASPILS_MEM_NULL	-1	The ida_mem argument was NULL.	
IDASPILS_LMEM_NULL	-2	The linear solver has not been initialized.	
IDASPILS_ILL_INPUT	-3	The solver is not compatible with the current NVECTOR mod-	
151161 116_1111_1111 01	J	ule.	
IDASPILS_MEM_FAIL	-4	A memory allocation request failed.	
		1	
	SPGMR	generic linear solver module	
SPGMR_SUCCESS	0	Converged.	
SPGMR_RES_REDUCED	1	No convergence, but the residual norm was reduced.	
SPGMR_CONV_FAIL	2	Failure to converge.	
SPGMR_QRFACT_FAIL	3	A singular matrix was found during the QR factorization.	
SPGMR_PSOLVE_FAIL_REC	4	The preconditioner solve function failed recoverably.	
SPGMR_ATIMES_FAIL_REC	5	The Jacobian-times-vector function failed recoverably.	
SPGMR_PSET_FAIL_REC	6	The preconditioner setup function failed recoverably.	
SPGMR_MEM_NULL	-1	The SPGMR memory is NULL	
SPGMR_ATIMES_FAIL_UNREC	-2	The Jacobian-times-vector function failed unrecoverably.	
SPGMR_PSOLVE_FAIL_UNREC	-3	The preconditioner solve function failed unrecoverably.	
SPGMR_GS_FAIL	-4	Failure in the Gram-Schmidt procedure.	
SPGMR_QRSOL_FAIL	-5	The matrix R was found to be singular during the QR solve	
		phase.	
SPGMR_PSET_FAIL_UNREC	-6	The preconditioner setup function failed unrecoverably.	
	SPBCG	generic linear solver module	
SPBCG_SUCCESS	0	Converged.	
SPBCG_RES_REDUCED	1	No convergence, but the residual norm was reduced.	
SPBCG_CONV_FAIL	2	Failure to converge.	
SPBCG_PSOLVE_FAIL_REC	3	The preconditioner solve function failed recoverably.	
SPBCG_ATIMES_FAIL_REC	4	The Jacobian-times-vector function failed recoverably.	
SPBCG_PSET_FAIL_REC	5	The preconditioner setup function failed recoverably.	
SPBCG_MEM_NULL	-1	The SPBCG memory is NULL	
SPBCG_ATIMES_FAIL_UNREC	-2	The Jacobian-times-vector function failed unrecoverably.	
SPBCG_PSOLVE_FAIL_UNREC	-3	The preconditioner solve function failed unrecoverably.	
SPBCG_PSET_FAIL_UNREC	-4	The preconditioner setup function failed unrecoverably.	
SPTFQMR generic linear solver module			
SPTFQMR_SUCCESS	0	Converged.	
SPTFQMR_RES_REDUCED	1	No convergence, but the residual norm was reduced.	
CHARLES COMMANDER TO THE	2	Failure to converge.	
SPTFQMR_CONV_FAIL	^	TTI 11.1 1 C C 1 1	
SPTFQMR_PSOLVE_FAIL_REC	3	The preconditioner solve function failed recoverably.	
	3 4 5	The preconditioner solve function failed recoverably. The Jacobian-times-vector function failed recoverably. The preconditioner setup function failed recoverably.	

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SPTFQMR_MEM_NULL -1 The SPTFQMR memory is NULL
SPTFQMR_ATIMES_FAIL_UNREC -2 The Jacobian-times-vector function failed.
SPTFQMR_PSOLVE_FAIL_UNREC -3 The preconditioner solve function failed unrecoverably.
SPTFQMR_PSET_FAIL_UNREC -4 The preconditioner setup function failed unrecoverably.

IDABBDPRE preconditioner module

IDABBDPRE_SUCCESS 0 Successful function return.

IDABBDPRE_PDATA_NULL -11 The preconditioner module has not been initialized.

IDABBDPRE_FUNC_UNRECVR -12 A user supplied function failed unrecoverably.

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