Direct-space wavefunction

Reciprocal-space wavefunction

Indeed:

Overall wavefunction:

In reciprocal space:

Here, denotes the grid discretization

Schrodinger equation:

In real space:

(normalization)

In reciprocal space: