

Motion Planning

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1 Introduction

Motion planning is a very interesting problem in our realworld. One key issue here is that the metrics beacome infinite in real world, while computer can only handle finite number of states. In this report we introduce some planning methods that is able to build a search tree/graph for real world problem (here the problem is motion planning).

2 Probabilistic Roadmap (PRM)

2.1 Basic Idea

The basic idea of PRM is first sampling the real world and create a finite configuration space. Then we create a search graph based on the relationship of each configuration (usually a multi-dimensional distance). Then we use traditional path searching algorithm such as A* to find a solution from the start to the goal.

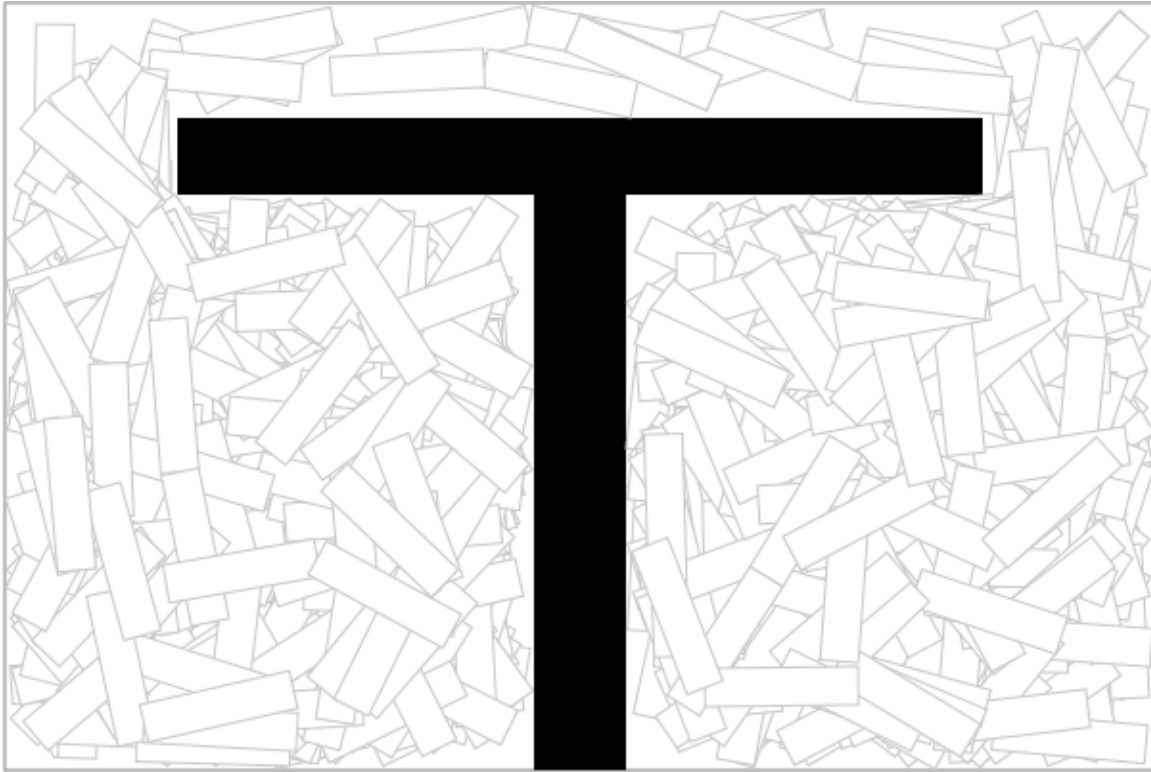


Figure 1: A demonstration of A* algorithm

Figure 1 demonstrate a sampling space, with all the random configuration of a two-links robot arm (gray rectagle). The black area is the obstable in the space.

2.2 Discussions

In this homework, in the sampling phase, an intuitive way is to randomly generate the configuration, and check whether it is a legal configuration. If not, dismiss it and keep generate another until a valid one occurs.

An issue we should concern about is, this method usually generate more configuration in a relatively large free space (in motion planning, meaning a space with a few obtacles). This would likely lead to a result that there are not enough configurations in the tricky space (such as a narrow corridor when referring to motion planning problem).

If you look at the figure 1, you will observe that there are significantly less configurations on the top because it is not easy to generat a legal configuration there.

Concerning this issue, we can propose some better sampling method. A simple idea is, every time when we detect a sampling collision, instead of simply dismiss it, we try to move the configuration in a random direction direction until it reaches the edge of the obstacles – becoming a legal configuration. By doing so,

we can make the density of narrow space higher than the normal open space, so that the computer can handle the corner case much better.

2.3 Code implementation

2.3.1 constructor

RoadMapProblem constructor gives you an outline of building the road map.

```
1 public RoadMapProblem(World m, Double[] config1, Double[] config2,  
    int density, int K) {  
3     // initiate the basic parameters  
    k_neighbour = K;  
5     map = m;  
    startArm = new ArmRobot(config1);  
7     goalArm = new ArmRobot(config2);  
    startNode = new RoadMapNode(startArm, 0.);  
9     // start sampling and generating the roadmap  
    getSampling(density);  
11    getConnected();  
}
```

2.3.2 getSampling

getSampling is used to create the sample configurations, preparing for roadmap generation.

Line 3: Generate the random configuration. **Line 5:** Check if the newly created configuration is legal. Noted that I modify the the armCollision function, so that the configuration will be confined into the world space. **Line 6:** Add the new configuration to the hash set.

```
public void getSampling(int density) {  
2     while (density > 0) {  
        Double[] rConfig = getRandCfg(startArm.links, map);  
4        ArmRobot toBeAdded = new ArmRobot(rConfig);  
        if (!map.armCollision(toBeAdded)) {  
6            samplings.add(toBeAdded);  
            density--;  
8        }  
    }  
10 }
```

2.3.3 getRandCfg

getRandCfg is used to generate the new random configuration.

Line 3: noted that the length of each arm is fixed.

```
private Double[] getRandCfg(int num, World map) {  
2     Random rd = new Random();  
    Double[] cfg = new Double[2 * num + 2];  
4     // randomize the start position  
    cfg[0] = rd.nextDouble() * map.getW();  
6     cfg[1] = rd.nextDouble() * map.getH();  
    // System.out.println(cfg[0]/map.getW() + "," + cfg[1]/map.getH());  
}
```

```

8   for (int i = 1; i <= num; i++) {
    // the length of each arm remains the same
10   cfg[2 * i] = startArm.config[2 * i];
    // randomize the angle
12   cfg[2 * i + 1] = rd.nextDouble() * Math.PI * 2;
    }
14   return cfg;
    }

```

2.3.4 getConnected

getConnected is used to connect the sampling. Basic idea is iterating through the samples and connect to k nearest vertex in the roadmap. The roadmap is implemented in adjacent linked list style.

```

1  public void getConnected() {
    // initiate the connecting with start arm
3  ArmLocalPlanner ap = new ArmLocalPlanner();
    PriorityQueue<AdjacentCfg> tmpq;
5  for (ArmRobot ar : samplings)
    roadmap.put(ar, new PriorityQueue<AdjacentCfg>());

7

    // add the start and goal to the roadmap
9  connected.add(startArm);
    connected.add(goalArm);
11 for (ArmRobot ar : samplings) {
    for (ArmRobot arOther : connected) {
13     if (ar != arOther
        && !map.armCollisionPath(ar, ar.config, arOther.config)) {
15         Double dis = ap.moveInParallel(ar.config, arOther.config);
        roadmap.get(ar).add(new AdjacentCfg(arOther, dis));
17         // make sure the configuration only points to k nearest neighbour
        if (roadmap.get(ar).size() > k_neighbour)
19             roadmap.get(ar).poll();
        // make sure that it an undirected graph
21         roadmap.get(arOther).add(new AdjacentCfg(ar, dis));
        if (roadmap.get(arOther).size() > k_neighbour)
23             roadmap.get(arOther).poll();
    }
25 }
    // keep track of the connected configurations
27 connected.add(ar);
    }
29 }

```

2.3.5 boundary detect

boundary detect makes sure that the configuration do not escape the world area.

```

1  ...
for (int j = 1; j <= p.getLinks(); j++) {
3  link_i = p.getLinkBox(j);

```

```

5   for(int i = 0; i < link_i.length; i++){
    if(link_i[i][0] < 0 || link_i[i][0] > window_width)
        return true;
7   if(link_i[i][1] < 0 || link_i[i][1] > window_height)
        return true;
9   }
   }
11  ...

```

2.4 Output demonstration

Figure 2 demonstrates the start and end configuration of my testing. Figure 3-5 presents 3 examples of the testing case, with increasing sampling difficulty. The number of sample configuration is 500, and k is 15.

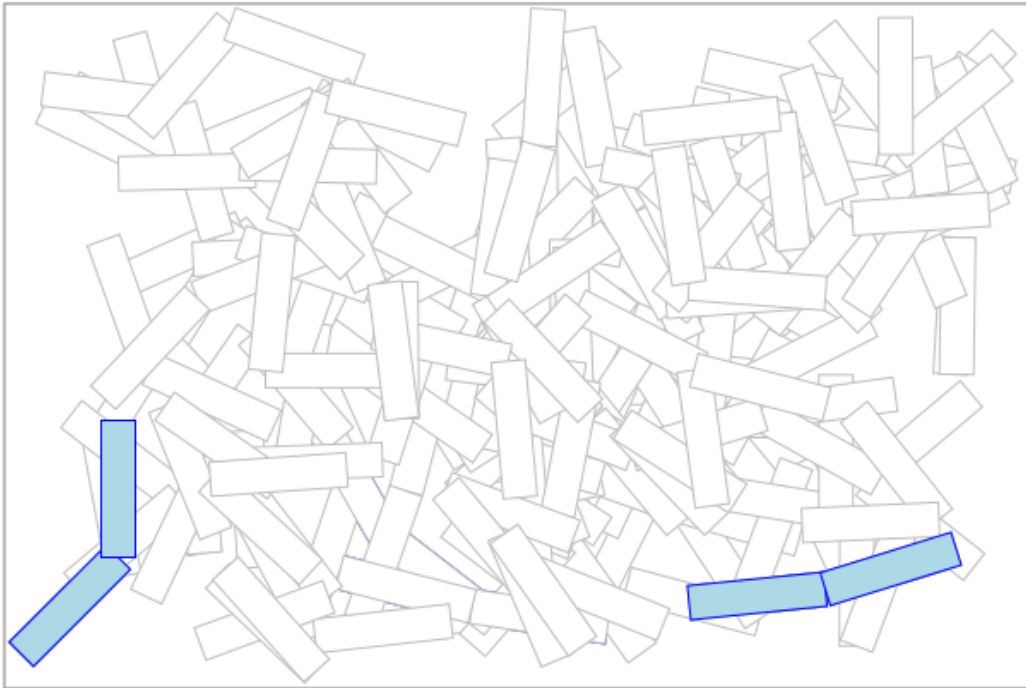


Figure 2: start and end of testing

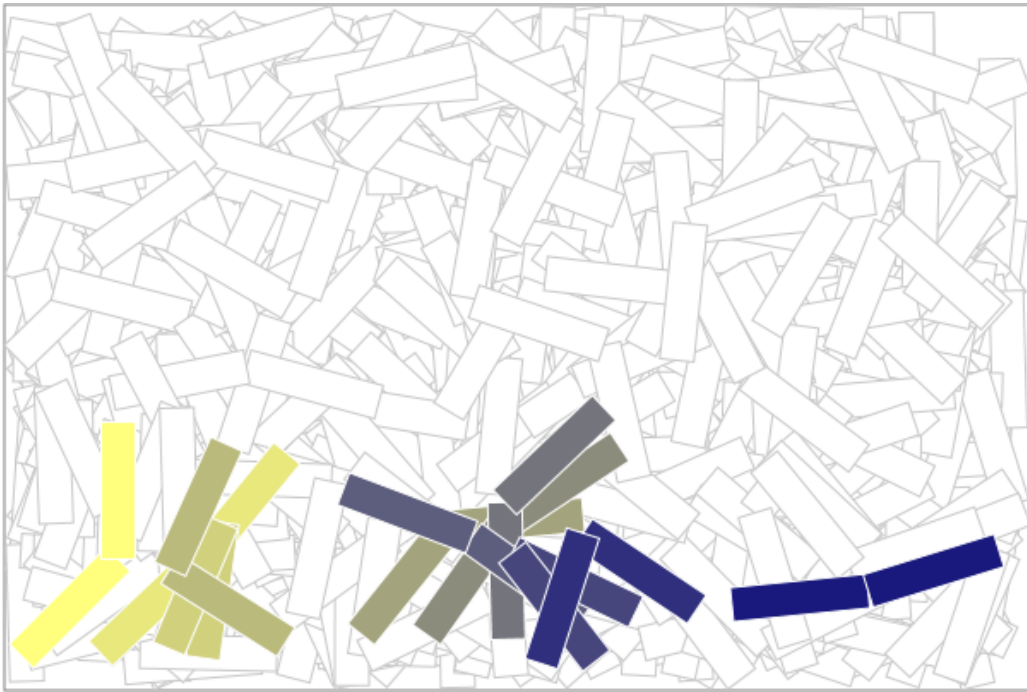


Figure 3: test in empty space

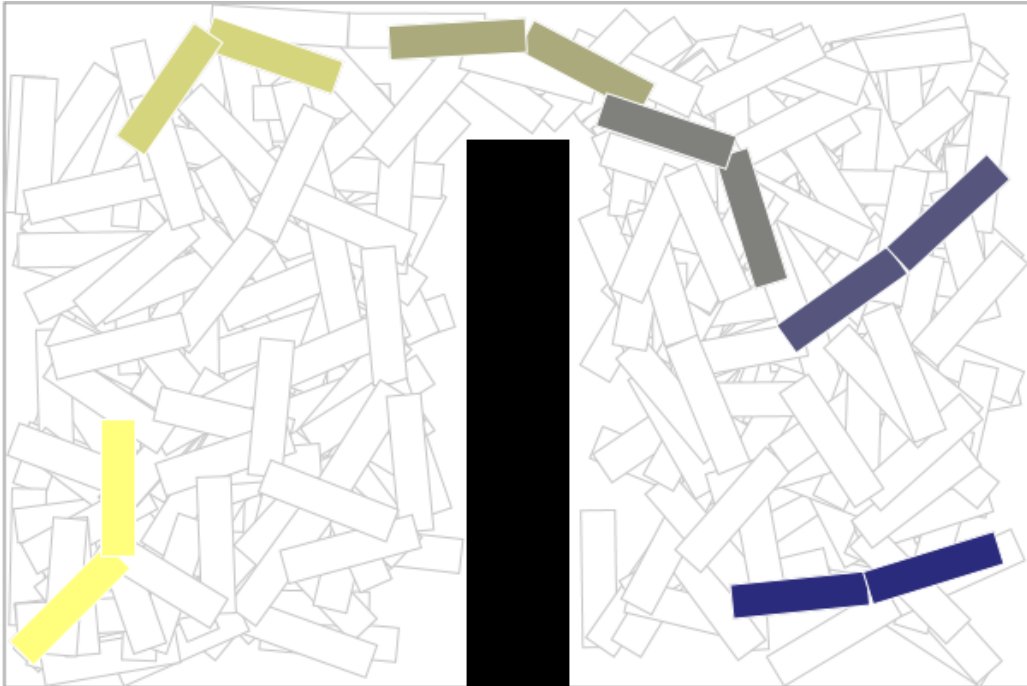


Figure 4: test with an obstacle.

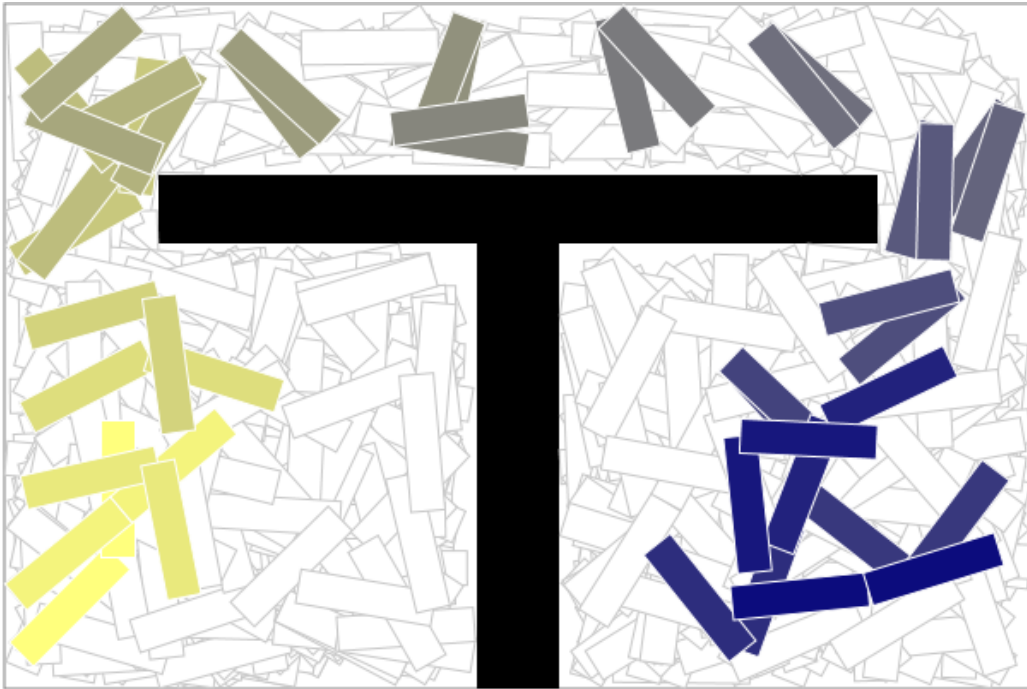


Figure 5: test with corridor. The movement becomes more tricky and complex

3 Rapidly Exploring Random Tree

3.1 Basic Idea

The basic idea of RRT is to grow a tree from the start, to fill up the infinite or over complex space. The most simple and intuitive way is to randomly generate legal configuration, and grow the tree towards the configuration.

3.2 Code implementation

3.2.1 growTree2Goal

growTree2Goal keeps iteratively expanding the tree until one of the node close to the goal. (I think the code is already quite self-explanatory, no further introduction is needed)

```
1 public void growTree2Goal(int num4grow) {
2     while (num4grow > 0) {
3         // generate new random car
4         CarRobot newRandCar = new CarRobot(getRandCfg(map));
5         // if the car is valid
6         if (!map.carCollision(newRandCar)) {
7             CarRobot nearest = findNearestInTree(newRandCar);
8             CarRobot newNearest = expandTree(newRandCar, nearest);
9             addNewNode2Tree(newNearest, nearest);
10            // terminate the iteration if reaching the goal
11            if (newNearest.getDistance(goalCar) < 20) {
12                addNewNode2Tree(goalCar, newNearest);
13                break;
14            }
15            num4grow--;
16        }
17    }
18 }
```

findNearestInTree finds the vertex that is nearest to the new randomly generated node.

```
1 private CarRobot findNearestInTree(CarRobot newRandCar) {
2     Double minDis = Double.MAX_VALUE;
3     CarRobot nearest = null;
4     for (CarRobot cr : connected) {
5         double dis = newRandCar.getDistance(cr);
6         if (minDis > dis) {
7             minDis = dis;
8             nearest = cr;
9         }
10    }
11    return nearest;
12 }
```

expandTree tries to expand to 6 different directions, and return the expansion that is nearest to the randomly generated node.

```
1 private CarRobot expandTree(CarRobot newRandCar, CarRobot nearest) {
2     // initiate the auxiliary object
```



```

4   Double minDis = Double.MAX_VALUE;
   SteeredCar sc = new SteeredCar();
   CarRobot newNearest = null, newCarRobot = new CarRobot();
6   // try to expand to 6 different directions
   for (int i = 0; i <= 5; i++) {
8       newCarRobot = new CarRobot(sc.move(nearest.getCarState(), i, 1.));
       // System.out.println("newCarRobot: " + newCarRobot);
10      if (!map.carCollision(newCarRobot)) {
           double dis = newCarRobot.getDistance(newRandCar);
12          if (minDis > dis) {
               minDis = dis;
14              newNearest = newCarRobot;
           }
16      }
   }
18   return newNearest;
}

```

addNewNode2Tree tries to expand to 6 different directions, and return the expansion that is nearest to the randomly generated node.

```

private void addNewNode2Tree(CarRobot newNode, CarRobot parentNode) {
2   connected.add(newNode);
   RRTree.get(parentNode).add(new AdjacentCfg(newNode, 1));
4   RRTree.put(newNode, new HashSet<AdjacentCfg>());
}

```

3.2.2 getSuccessors

getSuccessors is pretty simple. Simply return the children nodes in the exploring tree.

```

1   public ArrayList<SearchNode> getSuccessors() {
       ArrayList<SearchNode> successors = new ArrayList<SearchNode>();
3       for (AdjacentCfg adj : RRTree.get(car)) {
           successors.add(new RRTnode(adj.ar, adj.dis + cost));
5       }
       return successors;
7   }

```

3.3 Output demonstration

Figure 6-8 presents 3 examples of the testing case, with increasing sampling difficulty. From the last two case we can observe that, the tree on left part is much more complicate. This is because the left part has keep randomly generating the tree when one of the branch trying to explore through the corridor. I think using a bidirectional spanning can cut the expense of exploring corridor to half.

3.4 Extension: bidirectional search

4 Previous Work

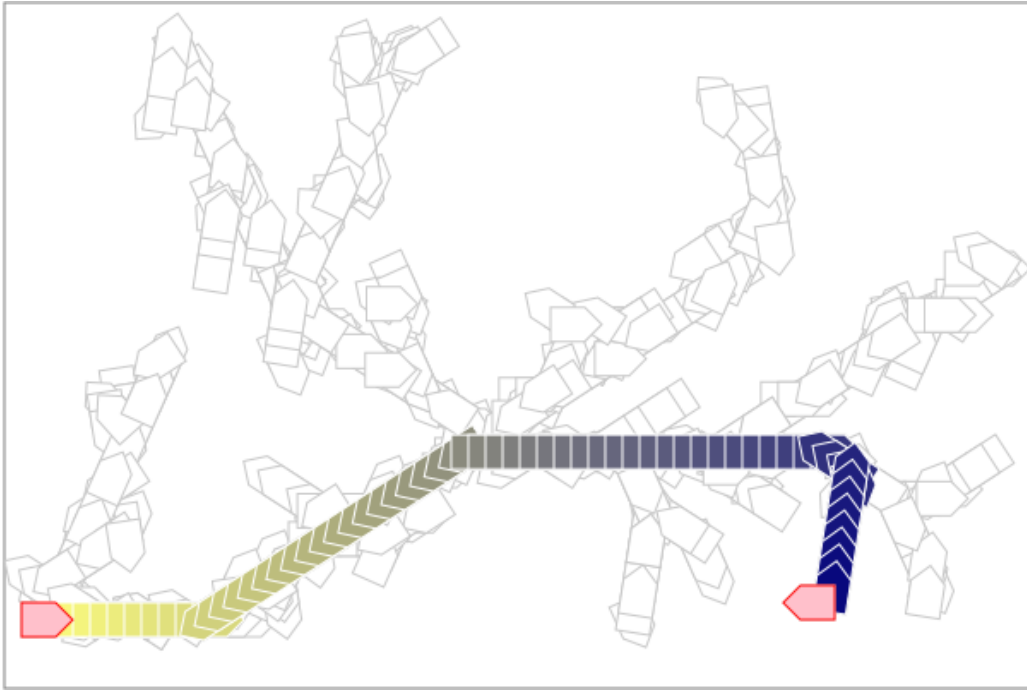


Figure 6: test in empty space

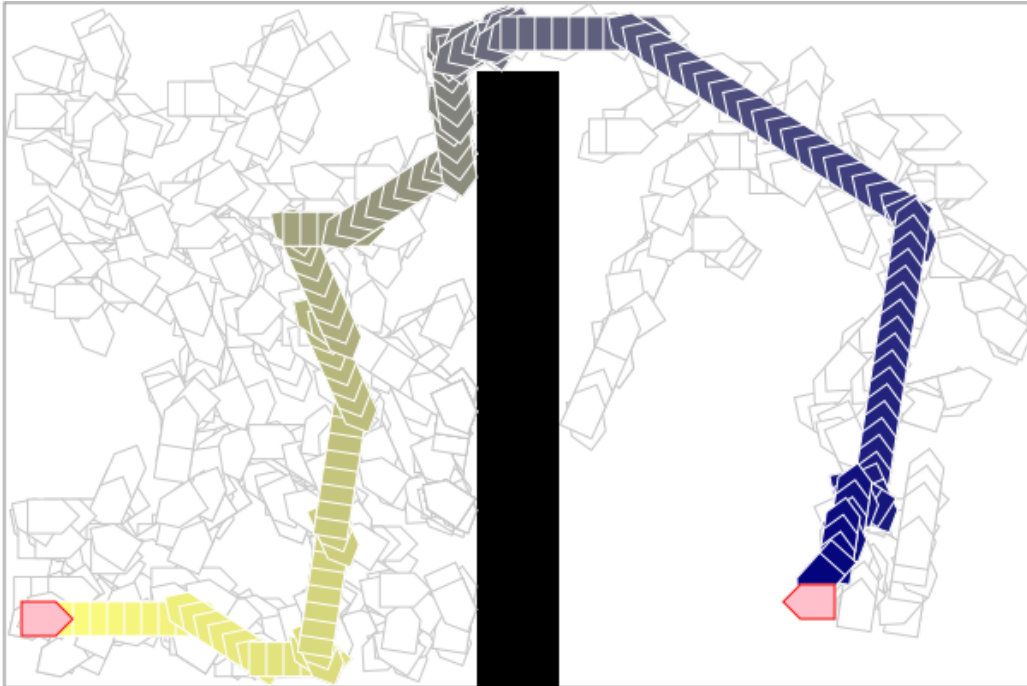


Figure 7: test with an obstacle.

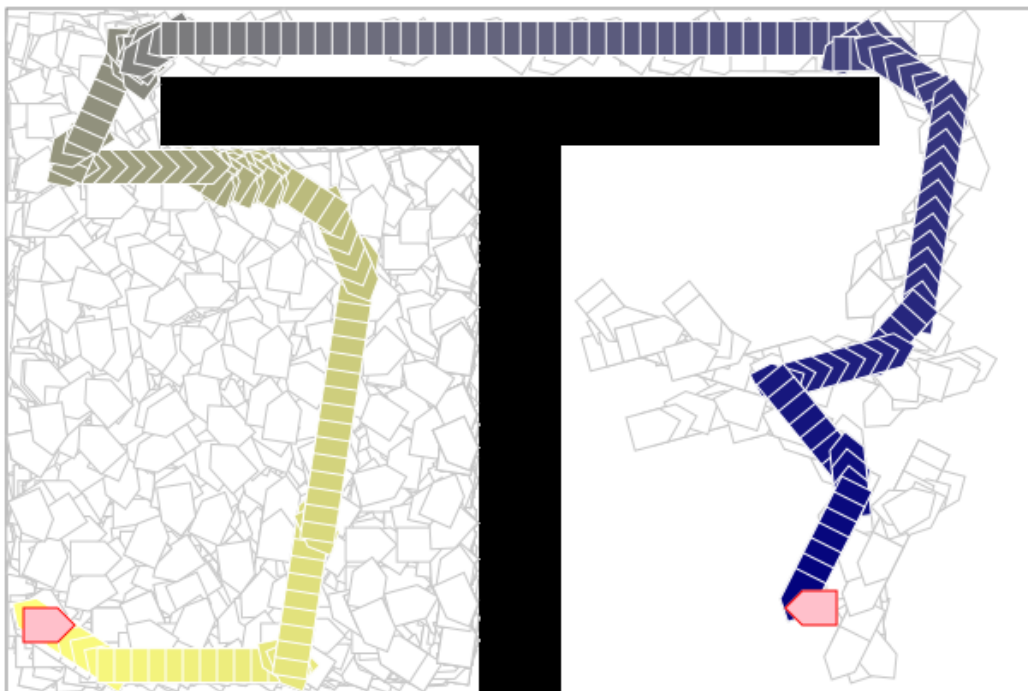


Figure 8: test with corridor. The movement becomes more tricky and complex