Chess AI

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1 Introduction

 $`Constraint\ satisfaction\ problems\ (CSPs)\ are\ mathematical\ problems\ defined\ as\ a\ set\ of\ objects\ whose\ state\ must\ satisfy\ a\ number\ of\ constraints\ or\ limitations.$

 $^{^1} Wikipedia: \ \mathtt{http://en.wikipedia.org/wiki/Constraint_satisfaction_problem}$

2 Solver design

2.1 Problem defination

CSP is usually defined with a tuple $\langle X, D, C \rangle$, as following:

$$X = \{X_1, ..., X_n\}$$

$$D = \{D_1, ..., D_k\}$$

$$C = \{C_1, ..., C_m\}$$

where X, D and C is a set of variables, domains and constraints. Our goal is to assign each variable a non-empty domain value from D, while satisfying all the constraints in C.

2.2 Design overview

Figure 1 is an overview my codes design. Basically it can be devided into 3 parts.

- The drivers contains the main function that read the input dataset and present the results/solutions.
- The second part is problem defination, theasf the asdf. It contains the basic definition of CSP problem. For example, the Variable, Constraints represent the the set I mentioned above, with necessary methods inside. Such as building constraints, validating the assignment, etc. I implement most of the method in a generic class, while I also extend the basic class for the needs of different problem. Despite of this, solver do not care about the specific problem. It only deal with those lower generic classes.
- The third part the problem solver, where I implement the CSP algorithm that solves the problem, as well as some helper methods such as heuristic computation.

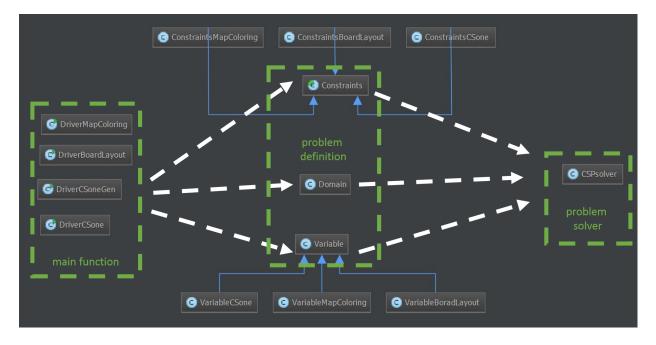


Figure 1: Overview of the design

3 CSP solver

3.1 back-tracking

cspDFS is a recursive style DFS method, which is the outline of the whole back-tracking. The basic procedure is,

- 1. Pick a variable from the unassigned variable set;
- 2. And then update all its valid domain values;
- 3. After preparation, it pick a *domain* value, and keep recursion of the remaining *variables*. Noted that if its successor report failure of DFS, it will iteratively choose the next *domain* values;
- 4. If it runs out of domain values, it will undo the assignemnt and report fail of search to its parent.

You may already notice some method names such as **pickMRV**, **sortLCV** and **MAC3Inference**. They are optimizations of the back-tracking algorithm, which will be explained in details later.

Listing 1: CSPsolver.class

```
/**
    * Oparam remain: list of variables that is not assigned yet
    * @return: whether the search is successful or not
   protected boolean cspDFS(LinkedList<Variable> remain) {
     // base case of recursion
     if (remain.size() == 0) return true;
     // pick a Minimum Remaining Variable
     Variable var = pickMRV(remain);
     // update domain and sort the values based on Least Constraining
10
     sortLCV(var, remain);
     // iterate all the valid domain
     for (Domain domain : var.getDomains()) {
       var.assign(domain);
14
       // try to assign the next variable in the remain
       if (MAC3Inference(var, remain)) {
16
         if (cspDFS(remain)) {
17
           return true; // solution found!
18
19
       }
20
     }
21
     // not found, reset assignment and put variable back to remain
     undoAssignment(var, remain);
23
     return false;
24
   }
25
```

3.2 pickMRV

The body of pickMRV is fairly simple: it returns the variable with min heuristic based on MRV heuristic.

Listing 2: CSPsolver.class

```
protected Variable pickMRV(LinkedList<Variable> remain) {
   Variable var = Collections.min(remain);
   remain.remove(var);
   return var;
}
```

The Main idea of MRV heuristic (minimum remaining values), is to find a variable with minimum remaining values, because these kind of value is most likely to cause a fail search. If two variable has the same amount of domain values, we pick the one with larger *degree*, because potentially it also more easy to fail.

Listing 3: CSPsolver.class

3.3 sortLCV

sortLCV is bascially sort all the valid domain values based LCV heuristic (least constraint value). The key idea is to left domains for the remaining variables as much as possible, so that the search is more likely to succeed earlier.

Listing 4: CSPsolver.class

```
protected void sortLCV(Variable var, LinkedList<Variable> remain) {
     // update the remaining domains based on constraints
     updateDomains(var);
     // compute value heuristic by trying
     for (Domain domain : var.getDomains()) {
       var.assign(domain);
       // try to assign the next variable in the remain
       domain.h = 0.;
       // compute its effect on the remaining varaibles
       for (Variable v : remain)
         domain.h += remainingDomains(v);
     }
     var.undoAssign();
     Collections.sort(var.getDomains());
14
15
   }
```

3.4 MAC3Inference

The body of MAC3Inference prunes the domains and forecast failure by checking arc consistency recursively. Supposed current variable is X_i . Line 5 means getting all the arcs $\langle X_i, X_j \rangle$, where $\{X_j\}$ is the neighbors of X_i . Line 13 means getting all the $\langle X_k, X_i \rangle$, where $\{X_k\}$ is the neighbors of X_i except X_j .

This recursion of inference is meant to converge / terminate at some point. Because it keeping pruning down the domains of the whole variables set, and stops recursion when no more domains can be pruned down. Since domain is a finite set, this inference is expected to terminate.

Listing 5: CSPsolver.class

```
protected boolean MAC3Inference(Variable thisVar,LinkedList<Variable> remain){
     // back up the properties of this variable
     Variable var = thisVar.snapshot();
     int backup = thisVar.getAssignment();
     LinkedList<Constraints.ArcPair> arcs = cons.getAdjArcs(var, remain);
     while (arcs != null && !arcs.isEmpty()) {
       Constraints.ArcPair arc = arcs.removeFirst();
       if (revise(arc.first, arc.second)) {
         if (var.getDomains().isEmpty())
11
           return false;
         arcs.addAll(cons.getAdjArcsInvert(arc.first, arc.second, remain));
13
     }
14
     // recover properties of this variable
15
     thisVar.assign(new Domain(backup));
16
17
     return true;
   }
18
```

The revise function prunes the domain when inconsistency occurs, and report the change of domains.

Listing 6: CSPsolver.class

```
protected boolean revise(Variable var, Variable adj) {
   for (Iterator<Domain> it = var.getDomains().iterator(); it.hasNext(); ) {
      // try to assign a domain and test if conflict exists
      var.assign(it.next());
      if (!cons.consistentTest(var, adj)) {
        it.remove();
      var.undoAssign();
      return true;
      }
   }
   var.undoAssign();
   return false;
}
```

4 Problem definition

Here I am presenting the outlines of two major classes that define the problem.

4.1 Variable.class

Here you can see the outline of **Variable**. Since most of the methods are very trivial, I am not presenting the details here.

Modifier and Type	Field and Description
protected int	assignment
protected Constraints	cons
protected int	degree
protected java.util.LinkedList <domain></domain>	domains
protected java.util.LinkedList <domain></domain>	domainsBackup
protected int	id

Table 1: Field Summary

Modifier and Type	Field and Description
protected int	assignment
boolean	assign(Domain domain)
int	compareTo(Variable o)
int	domainSize()
void	domainsRecover()
boolean	equals(java.lang.Object other)
int	getAssignment()
int	getDegree()
java.util.LinkedList <domain></domain>	getDomains()
int	$\operatorname{getId}()$
java.util.ArrayList <java.lang.integer></java.lang.integer>	getStates()
int	hashCode()
void	setDegree(int d)
void	$\operatorname{setDomainsBackup}()$
Variable	snapshot()
java.lang.String	toString()
void	undoAssign()

Table 2: Method Summary

4.2 Domain.class

Domains is very simple, basically just domain value along with a heuristic value.

4.3 Constraints.class

Here you can see the outline of **Variable**. There are two basic members in this class. **binaryAdjs** is used to store all the binary relationship, whole **binaryAdjs** is for global relationships. I don't store the relationship such as equal, greater, etc. Assuming that all the arcs/sets have the same relationship. Of course you can extend members base on your need of problem. For example, if different binary constraints have different relationship, you should implement a hashmap from collection of variables to their relationship.

Modifier and Type	Field and Description
static java.util.HashMap <variable,java.util.linkedlist<variable>></variable,java.util.linkedlist<variable>	binaryAdjs
static java.util.HashMap <java.lang.integer,java.util.hashset<variable>></java.lang.integer,java.util.hashset<variable>	globalAdjs

Table 3: Field Summary

Modifier and Type	Field and Description
void	addConstraint(Variable var1, Variable var2)
void	addGlobalVar(Variable var)
boolean	conflictTest(java.util.LinkedList <variable> vars)</variable>
boolean	conflictTest(Variable var)
boolean	consistentTest(Variable var, Variable adj)
LinkedList <constraints.arcpair></constraints.arcpair>	getAdjArcs(Variable var, LinkedList <variable> remain)</variable>
LinkedList <constraints.arcpair></constraints.arcpair>	getAdjArcsInvert(Variable var, Variable exclude, LinkedList <variable> remain)</variable>
abstract boolean	isSatisfied(Variable var1, Variable var2)
void	rmGlobalVar(Variable var)

Table 4: Method Summary

One major method is **conflictTest**. It is used to test conflict with the adjacent, after assigning values to a variable. The base method is written for binary constraint, because theoretically all problems can be represented by binary constraint problem. I will extend this for global constraints in some other problems, which makes the implementation and computation more easy.

Listing 7: Constraints.class

```
/***
    * Oparam var: the variable to be tested
    * Oreturn: whether the conflict exists
   public boolean conflictTest(Variable var) {
5
     LinkedList<Variable> adjs = binaryAdjs.get(var);
     if (adjs == null)
       return false; // no adjacent in constraint graph, no conflict
     for (Variable adj : adjs) {
9
       if (!isSatisfied(var, adj) )
10
         return true;
11
     }
12
     return false;
13
   }
```

Since most of the methods are not very crucial, I am not presenting the details here. The most important one is the **isSatisfied** method. It related to specific problem, I will present those extended codes when discussing real problem application later.

5 Map coloring problem

Map coloring is a very classic constraint satisfied problem. The basic idea is, any adjacent areas in the map should have different color, which forms a binary contraint.

5.1 Important methods

isSatisfied is method to determine whether two variables satisfied the bianry constraint. For each assignment, there can be a list of states corresponding to this vairble. The **getStates** is such a genric method in the base class. As you can see for map coloring problem, there is only one states, which is the assigned color.

Depending on the needs of the problem, I will override the **getStates** in **VariableExtendClass**, and wrote corresponding **isSatisfied** in the **ConstraintsExtendClass**

Listing 8: ConstraintsMapColoring.class

5.2 Testing

The following list the tresults of Austrilia coloring, with constriants described by figure 2^2

```
[WA->Yellow]
[NT->Red]
[SA->Green]
[Q->Yellow]
[NSW->Red]
[V->Yellow]
[T->Red]
```

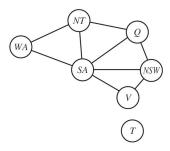


Figure 2: Constraint graph of Austrilia map coloring problem.

 $^{^2{\}rm from}$ Artificial Intelligence A Modern Approach 3rd Edition

I also test the solver on US States coloring. 3 Here comes the results.

```
[AK->Red]
   [AL->Yellow]
   [AR->Yellow]
   [AZ->Yellow]
   [CA->Red]
   [CO->Green]
   [CT->Green]
   [DC->Yellow]
   [DE->Green]
   [FL->Red]
10
   [GA->Green]
   [HI->Red]
   [IA->Yellow]
14
    [ID->Green]
   [IL->Red]
15
   [IN->Green]
16
   [KS->Yellow]
17
   [KY->Yellow]
   [LA->Red]
   [MA->Yellow]
20
   [MD->Red]
21
   [ME->Yellow]
22
   [MI->Yellow]
   [MN->Red]
   [MO->Green]
   [MS->Green]
27
   [MT->Red]
    [NC->Yellow]
28
   [ND->Yellow]
29
   [NE->Red]
30
   [NH->Red]
31
   [NJ->blue]
   [NM->blue]
   [NV->blue]
34
   [NY->Red]
35
   [OH->Red]
36
   [OK->Red]
   [OR->Yellow]
   [PA->Yellow]
40
   [RI->Red]
    [SC->Red]
41
   [SD->Green]
42
   [TN->Red]
43
   [TX->Green]
44
   [UT->Red]
   [VA->Green]
   [VT->Green]
47
   [WA->Red]
48
   [WI->Green]
49
   [WV->blue]
   [WY->Yellow]
```

 $^{^3}$ thanks to data this website help me to build the constraint graph. http://writeonly.wordpress.com/2009/03/20/adjacency-list-of-states-of-the-united-states-us/

This is a much more complex coloring problem, where I can give more analysis on the performance of my CSP solver, as figure 3 shows.

To my surprise, using LCV alone makes the search twice as worse as back tracking. But combining MRV and LCV heuristic together does get the best performance, indicating that LCV can have positive influence. I guess the reason why LCV alone performance worst, is because it keep using the values that is least likely to cause failure. Turn out that it waste too much time on those variables that needs massive search while being exploered too early. (Because I am not using MRV here).

As you can see, MAC3 explore the same amount of nodes as back tracking does. However it cause slightly more time because it needs to compute the inference. The reason that MAC3 has no effect is because arc consistency is not effective on map coloring problem. In this case we should use other method such as path consistency. I will leave to future work.

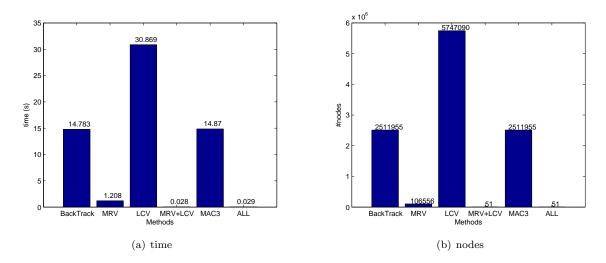


Figure 3: Performance comparison between different methods.

6 Circuit board layout problem

Circuit board is another classic problem that can be described by binary constraints. The basic idea is that two layouts should not *overlap* with each other. So, based on my previous work on map coloring, the only thing I need to do is to add a few members and methods to *VariableBoardLayout*, as well as implement the **isSatisfied** abstract method.

6.1 Important methods

As you can see, is Satisfied and get States are more complex than the previous one. The basic

Listing 10: ConstraintsBoardLayout.class

```
@Override
   public boolean isSatisfied(Variable var1, Variable var2){
     HashSet<Integer> overlap = new HashSet<>();
     ArrayList<Integer> states1 = var1.getStates();
     ArrayList<Integer> states2 = var2.getStates();
     for(Iterator<Integer> it = states1.iterator(); it.hasNext();){
       overlap.add(it.next());
     for(Iterator<Integer> it = states2.iterator(); it.hasNext();){
       if(overlap.contains(it.next()))
10
         return false;
11
     }
12
     return true;
13
   }
14
```

Listing 11: VariableBoradLayout.class

```
public ArrayList<Integer> getStates() {
    return new ArrayList<>(Arrays.asList(getAssignment()));
}
```

6.2 Testing

7 CS 1 section assignment problem

8 Map coloring problem

Map coloring is a very classic constraint satisfied problem. The basic idea is, any adjacent areas in the map should have different color, which forms a binary contraint.

8.1 Important methods

isSatisfied is method to determine whether two variables satisfied the bianry constraint. For each assignment, there can be a list of states corresponding to this vairble. The **getStates** is such a genric method in the base class. As you can see for map coloring problem, there is only one states, which is the assigned color.

Depending on the needs of the problem, I will override the **getStates** in **VariableExtendClass**, and wrote corresponding **isSatisfied** in the **ConstraintsExtendClass**

```
00verride
public boolean isSatisfied(Variable var1, Variable var2){
```

```
return var1.getStates().get(0) != var2.getStates().get(0);
}
```

8.1.1 minimaxIDS

minimaxIDS initializes the search using iterative-depending strategy.

```
private short minimaxIDS(Position position, int maxDepth)
throws IllegalMoveException{
this.terminalFound = false;
MoveValuePair bestMove = new MoveValuePair();
for (int d = 1; d <= maxDepth && !this.terminalFound; d++) {
   bestMove = maxMinValue(position, maxDepth - 1, MAX_TURN);
}
return bestMove.move;
}</pre>
```

8.1.2 maxMinValue

maxMinValue is an recursive function that keep searching in the tree. I write it in a compact way by mering min and max procedure in this one method, which turns out to be a big mistake for future when I try to implement more fancy mechansim for the searching. This design makes the codes a little messy.

There is also another better way to implement the search in a compact way, which is called *Nagamax*. However it was too late for me to discover it so I leave it to my future work.

```
private MoveValuePair maxMinValue(Position position, int depth,
       boolean maxTurn) throws IllegalMoveException{
     if (depth <= 0 || position.isTerminal()) {</pre>
       // the base case of recursion
       return handleTerminal(position, maxTurn);
     } else {
       // get all the legal moves
       MoveValuePair bestMove = new MoveValuePair();
       for (short move : position.getAllMoves()) {
         // collect values from further moves by recursion
         position.doMove(move);
11
         MoveValuePair childMove = maxMinValue(position, depth - 1, !maxTurn);
         bestMove.updateMinMax(move, childMove.eval, maxTurn);
13
         position.undoMove();
14
       return bestMove;
16
17
   }
18
```

8.1.3 handleTerminal

handleTerminal is used to terminate the searching by returning an evalution value, when either reaching the maximum depth or check mate or draw. Noted that getMaterial evalutes the weighted sum of the stones, while getDominant evaluates the distribution of the stones.

```
private MoveValuePair handleTerminal(Position position, boolean maxTurn) {
    MoveValuePair finalMove = new MoveValuePair();
    if (position.isTerminal() && position.isMate()) {
```

```
this.terminalFound = position.isTerminal();
finalMove.eval = (maxTurn ? BE_MATED : MATE);
} else if (position.isTerminal() && position.isStaleMate())
finalMove.eval = 0;
else {
finalMove.eval = (int) ( (maxTurn ? 1 : -1) * (position.getMaterial() + position.getDomination()));
}
return finalMove;
}
```

8.1.4 helper class

MoveValuePair help me to store the move and corresponding evaluation value. Also it has a generalized method that help me to find the max value for maximum search, or vise versa.

```
private MoveValuePair handleTerminal(Position position, boolean maxTurn) {
    MoveValuePair finalMove = new MoveValuePair();
    if (position.isTerminal() && position.isMate()) {
        this.terminalFound = position.isTerminal();
        finalMove.eval = (maxTurn ? BE_MATED : MATE);
    } else if (position.isTerminal() && position.isStaleMate())
        finalMove.eval = 0;
    else {
        finalMove.eval = (maxTurn ? 1 : -1) * position.getMaterial();
    }
    return finalMove;
}
```

9 Results demonstration

I did a lot of testing, turn out that I don't leave myself much time to organize how to present them. Here I am going to focus on computation time of each step. I create a fix random seed for the random AI, and let my AI play with it.

Figure 4 demonstrate the step and time curve, with my Minimax against Random AI (blue curve), $\alpha\beta$ pruning against Random AI respectively (green curve). The left figure is a normal plot, while y axis of the right one is set to log scale (Noted that logy scale will shrink the difference on y direction!). Considering sometimes the computation time grows exponentially with depth, this can provide a better observation. As you can see, the $\alpha\beta$ pruning finish the game using exact same amount of steps, while taking much less computation time.

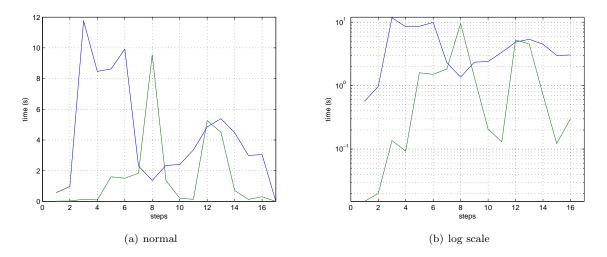


Figure 4: step and time curve of Random MinimaxAI and $\alpha\beta$ pruning.

Figure 5 demonstrate the step and time curve difference when there exists a transposition table. As expected, the time conusmption is lower when implemented with transposition table. What's more, with transposition table it actually finish the game even fater! Because sometimes the table provider more depth of information than current node, which might lead to a bette decision.

Figure 6 demonstrate the step and time curve difference when there exists a transposition table. Though the time decrease even more significantly, the takes more steps for some unknown reason. I also test ordering enhancement against pure transposition table, it shows that after reodering it becomes a little more stupid. This leave as my future work.

Figure 7 demonstrate mean time of different methods. It seems that null-move actually takes more time. I think it because although it reduce depth of search occassionally, it actually increase searching times on the same depth. May be I haven't tuned it properly.

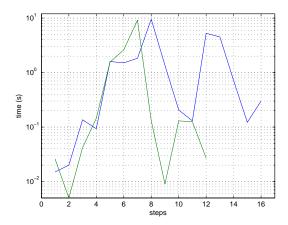


Figure 5: step and time curve of $\alpha\beta$ pruning and $\alpha\beta$ enhanced with transposition table

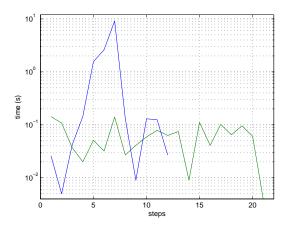


Figure 6: step and time curve of transposition table and $\alpha\beta$ enhanced with re-ordering

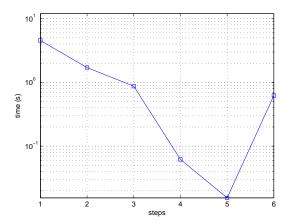


Figure 7: mean time regards to Minimax, Alpha-beta pruning, transposition table, moves reodering, quiescence search and null move heuristic repectively

10 Some related work

Null move strategy can be very tricky. Adaptive Null-Move Pruning 4 prose some good suggestions. 1) when depth is less or equal to 6, use R=2. When Depth is larger than 8, use R=3. When depth is 6 or 7, and both sides has more than 3 stones, then R=3. Otherwise, R=2.

⁴Heinz, Ernst A. "Adaptive null-move pruning." Scalable Search in Computer Chess. Vieweg+ Teubner Verlag, 2000. 29-40.