

Practical Concurrent and Parallel Programming XII

Testing & Verification

Raúl Pardo

Remember



"Program **testing** can be used to **show the presence of bugs**, but **never to show their absence**!"

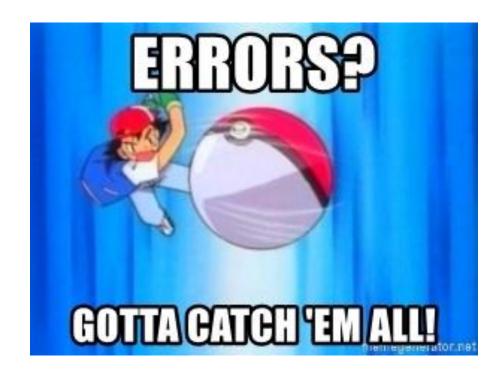
Edsger W. Dijkstra



Agenda



- Intro to concurrency properties
- Testing
 - Intro to JUnit 5
 - Counter
 - Bounded Buffer
 - Deadlocks
- Formal Verification
 - Java Path Finder



Concurrency properties



- Traditionally, properties of concurrent programs are split into:
 - Safety "Something bad never happens"

Ex. 1: Two intersection traffic light never are green at the same time Ex. 2: The field size of a collection is never less than 0

Liveness – "Something good will eventually happen"

Ex. 1: The traffic light will eventually switch to red

Ex. 2: It should always be possible to eventually add elements to the collection

Ex. 3: If an actor sends message to another actor, the latter will eventually receive the message



- The statements in a thread are executed when the thread is in its "running" state
- An interleaving is a possible sequence of operations for a concurrent program
 - Note this: <u>a sequence of operations for a concurrent program</u>, not for a thread. Concurrent programs are composed by 2 or more threads.

Interleavings



```
// shared variable
int counter = 0;
// two threads
for(int i=0; i<2; i++){
  new Thread(() -> {
    while(true) {
                             (1)
      int temp = counter;
      temp = counter + 1;
                            (2)
                             (3)
      counter = temp;
  }).start();
```

What are possible interleavings for this program? (assuming that (1),(2) and (3) are atomic operations)

Interleavings

Assuming that (1), (2) and (3) are atomic.

```
// shared variable
int counter = 0;
```

Some interleavings are 1. (1), (2), (3), (1), (2), (3),...

2. (1), (2), (3), (1), (2), (3),...

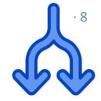
```
// two threads
for(int i=0; i<2; i++){
  new Thread(() -> {
    while(true) {
                             (1)
      int temp = counter;
      temp = counter + 1;
                             (2)
      counter = temp;
                             (3)
  }).start();
```

3. (1), (2), (3), (1), (2), (3),... 4. (1), (2), (3), (1), (2), (3),... But we also have

1. (1), (1), (2), (2), (3), (3),... 2. (1), (2), (1), (2), (3), (3),...

These produce race conditions

Testing concurrent programs



- Testing concurrent programs is about writing tests to find undesired interleavings (if any)
 - These are commonly known as counterexamples

 2. (1), (2), (1), (2), (3), (3),...

 These produce race conditions
 - They show an interleaving that violates a property
- Since concurrent execution is non-deterministic, it is not guaranteed that tests will trigger undesired interleavings
- Today we will see strategies to design tests to find interleavings that violate a property

1. (1), (1), (2), (2), (3), (3),...

Structure of counterexamples



- The type of counterexample we are looking for, depends on the type of property
 - Safety
 - Liveness

Counterexamples in safety properties



- Safety property
 - A counterexample is a <u>finite</u> interleaving where the property does not hold
- <u>Ex. 1</u>: Two intersection traffic light never are green at the same time
 - Counterexample: a finite interleaving that result in having two green lights at the same time
- Ex. 2: The field size of a collection is never less than 0
 - Counterexample: Can you give a cou

Can you give a counterexample for this property?

- Liveness property
 - A counterexample is an <u>infinite</u> interleaving where the property never holds
- Ex. 1: The traffic light will eventually switch to red
 - Counterexample: an infinite interleaving when lights never go green, or yellow
- <u>Ex. 2</u>: It should always be possible to eventually add elements to the collection
 - Counterexample: an infinite interleaving when a thread can never add an element to the collection
- <u>Ex. 3</u>: If an actor sends message to another actor, the latter will eventually receive the message (more a distributed systems property)
 - Counterexample:

Can you give a counterexample for this property?



- The type of counterexample we are looking for, depends on the type of property
 - Safety
 - Liveness

Today we focus only on safety properties



Testing Concurrent Programs (Counter)



Functional Correctness tests

- These tests focus on testing that program behaves (functions) correctly when executed concurrently
- For instance, data structures
- This lecture focuses on this type of tests
- Performance tests
 - These tests focus on measuring the execution performance of concurrent programs
 - We saw in week 3 a more accurate (and statistically stronger) method to measure performance



- JUnit is a popular unit test framework for Java programs
- It makes it easy to implement and run tests
- Some useful features are:
 - Execute initialization tasks
 - Running tests repeatedly
 - Define and automatically execute sets of input parameters for a test
 - Compatibility with build tools, such as Gradle







```
•19
```

```
Class to test
```

```
class CounterDR implements Counter {
    private int count;
    public CounterDR() {
        count = 0;
    public void inc() {
        count++;
    public int get() {
       return count;
```

```
// several imports
public class CounterTest {
    private Counter count;
    @BeforeEach
    public void initialize() {
      count = new CounterDR();
    @RepeatedTest(10)
    @DisplayName("Counter Sequential")
    public void testingCounterSequential()
      int localSum = 0;
      for (int i = 0; i < 10 000; i++) {
        count.inc();
        localSum++;
      assertTrue(count.get() == localSum);
    // other tests
```

19

Class to test

```
class CounterDR implements Counter {
    private int count;
                              Counter variable that will
                                 be used in the tests
    public CounterDR() {
        count = 0;
    public void inc() {
        count++;
    public int get() {
        return count;
```

```
// several imports
public class CounterTest {
    private Counter count;
    @BeforeEach
    public void initialize() {
      count = new CounterDR();
    @RepeatedTest(10)
    @DisplayName("Counter Sequential")
    public void testingCounterSequential()
      int localSum = 0;
      for (int i = 0; i < 10 000; i++) {
        count.inc();
        localSum++;
      assertTrue(count.get() == localSum);
    // other tests
```

Class to test

class CounterDR implements Counter {
 private int count;
 public CounterDR() {
 count = 0;
 }
 public void inc() {
 count++;
 }
 public int get() {
 return count;
 }
}
This method before a useful to object the count of the count of the count of the count;
 counter value of the counter of the counter

Counter variable that will be used in the tests

This method is executed before each test. It is useful to initialize the objects to test

```
// several imports
public class CounterTest {
    private Counter count;
    @BeforeEach
    public void initialize() {
      count = new CounterDR();
    @RepeatedTest(10)
    @DisplayName("Counter Sequential")
    public void testingCounterSequential()
      int localSum = 0;
      for (int i = 0; i < 10 000; i++) {
        count.inc();
        localSum++;
      assertTrue(count.get() == localSum);
    // other tests
```

•19

Class to test

```
class CounterDR implements Counter {
    private int count;
                                  Counter variable that will
                                     be used in the tests
    public CounterDR() {
         count = 0;
                                   This method is executed
                                    before each test. It is
    public void inc() {
                                    useful to initialize the
         count++;
                                       objects to test
    pu
           First, we define the type of test. One might use
          @Test (regular test), @RepeatedTest(X) the test is
          executed X times, or @ParameterizedTest with an
                  input generator (see next slides)
```

```
// several imports
public class CounterTest {
    private Counter count;
    @BeforeEach
    public void initialize() {
      count = new CounterDR();
    @RepeatedTest(10)
    @DisplayName("Counter Sequential")
    public void testingCounterSequential()
      int localSum = 0;
      for (int i = 0; i < 10 000; i++) {
        count.inc();
        localSum++;
      assertTrue(count.get() == localSum);
    // other tests
```

- 19

Class to test

```
class CounterDR implements Counter {
    private int count;
                                  Counter variable that will
                                     be used in the tests
    public CounterDR() {
         count = 0;
                                   This method is executed
                                    before each test. It is
    public void inc() {
                                    useful to initialize the
         count++;
                                       objects to test
    pu
           First, we define the type of test. One might use
          @Test (regular test), @RepeatedTest(X) the test is
          executed X times, or @ParameterizedTest with an
                  input generator (see next slides)
```

```
// several imports
public class CounterTest {
    private Counter count;
                                   Some text to
    @BeforeEach
                                   display when
    public void initialize() {
      count = new CounterDR();
                                    printing the
                                  result of the test
    @RepeatedTest(10)
    @DisplayName("Counter Sequential")
    public void testingCounterSequential()
      int localSum = 0;
      for (int i = 0; i < 10 000; i++) {
        count.inc();
        localSum++;
      assertTrue(count.get() == localSum);
    // other tests
```

• 19

Class to test

```
class CounterDR implements Counter {
    private int count;
                                  Counter variable that will
                                     be used in the tests
    public CounterDR() {
         count = 0;
                                   This method is executed
                                    before each test. It is
    public void inc() {
                                    useful to initialize the
         count++;
                                       objects to test
    pu
           First, we define the type of test. One might use
          @Test (regular test), @RepeatedTest(X) the test is
          executed X times, or @ParameterizedTest with an
                  input generator (see next slides)
```

Body of the test. In this case we execute inc() 10000 times

```
Test Class
```

```
// several imports
public class CounterTest {
    private Counter count;
                                   Some text to
    @BeforeEach
                                   display when
    public void initialize() {
      count = new CounterDR();
                                    printing the
                                  result of the test
    @RepeatedTest(10)
    @DisplayName("Counter Sequential")
    public void testingCounterSequential()
      int localSum = 0:
      for (int i = 0; i < 10 000; i++) {
        count.inc();
        localSum++;
      assertTrue(count.get() == localSum);
    // other tests
```

Test

```
. 20
```

```
Class to test
```

```
class CounterDR implements Counter {
    private int count;
    public CounterDR() {
        count = 0;
    public void inc() {
        count++;
    pr-h1:- --+ --+ /\
```

The test finishes with some assertions. Here we check that the final value of count equals our local sum.

You may also add assertions during the execution of the test.

```
// several imports
public class CounterTest {
    private Counter count;
    @BeforeEach
    public void initialize() {
      count = new CounterDR();
    @RepeatedTest(10)
    @DisplayName("Counter Sequential")
    public void testingCounterSequential()
      int localSum = 0;
      for (int i = 0; i < 10 000; i++) {
        count.inc();
        localSum++;
      assertTrue(count.get() == localSum);
    // other tests
```

Sequential tests in JUnit 5

Class to test

```
class CounterDR implements Counter {
   private int count;

   public CounterDR() {
      count = 0;
   }

   public void inc() {
      count++;
   }
```

```
To run tests in gradle we use:

$ gradle cleanTest test --tests <package>.<test_class>
In this example,

$ gradle cleanTest test --tests testingconcurrency.CounterTest
(cleanTest ensures a fresh environment for running the test, it is not always necessary)
```

Test



```
// several imports
public class CounterTest {
    private Counter count;
    @BeforeEach
    public void initialize() {
      count = new CounterDR();
    @RepeatedTest(10)
    @DisplayName("Counter Sequential")
    public void testingCounterSequential()
      int localSum = 0:
      for (int i = 0; i < 10 000; i++) {
        count.inc();
        localSum++;
      assertTrue(count.get() == localSum);
    // other tests
```



 Now we extend the test to multiple threads (or turnstiles)









- Some advise to take into account when developing a test:
- 1. Precisely define the property you want to test
- 2. If you are going to test multiple implementations, it is useful to define an *interface* for the class you are testing
- 3. Concurrent tests require a setup for starting and running multiple threads
 - Maximize contention to avoid a sequential execution of the threads
 - You may need to define thread classes
- 4. Run the tests multiple times and with different setups to try to maximize the number of interleavings tested



- Precisely define the property you want to test
- "after N threads execute inc() X times, the value of the counter must be equal to N*X"

```
Class CounterTest {
   Counter count;
   ...
   public void testingCounterParallel(int nrThreads, int N) {
      // body of the test
      assert(N*nrThreads == count.get());
   }
   ...
}
```



- Precisely define the property you want to test
- "after N threads execute inc() X times, the value of the counter must be equal to N*X"

```
Class CounterTest {
   Counter count;
   ...
   public void testingCounterParallel(int nrThreads, int N) {
        // body of the test
        assert(N*nrThreads == count.get());
   }
   ...
}

Is this a safety or liveness property?
```

 If you are going to test multiple implementations, it is useful to define an interface for the class you are testing

```
public interface Counter {
    public void inc();
    public int get();
}
```

```
class CounterDR implements Counter {
    private int count;

    public CounterDR() {
        count = 0;
    }

    public void inc() {
        count++;
    }

    public int get() {
        return count;
    }
}
```

```
class CounterSync implements Counter {
   private int count;

   public CounterSync() {
      count = 0;
   }

   public synchronized void inc() {
      count++;
   }

   public int get() {
      return count;
   }
}
```

Barriers Intuition (revisited)



 Barriers are synchronization primitives used to wait until several thread reach some point in their computation (marked by executing await())









Barriers | Intuition (revisited)

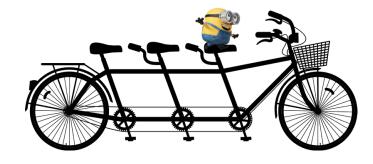


 Barriers are synchronization primitives used to wait until several thread reach some point in their computation (marked by executing await())









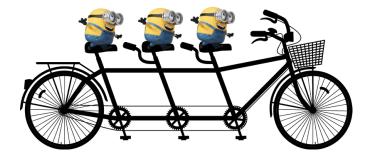


 Barriers are synchronization primitives used to wait until several thread reach some point in their computation (marked by executing await())











- Barriers are synchronization primitives used to wait until several thread reach some point in their computation
- Barriers consists of
 - A number parties to wait for
 - A method await()
 - If the number of waiting threads is less than parties, then the calling thread blocks, otherwise all waiting threads wake up and the calling thread is allowed to make progress
- Java includes the class CyclicBarrier
 - After parties called await(), then the state is reset and the barrier behaves as initially

- Maximize contention (e.g., using a cyclic barrier) to avoid a sequential execution of the threads
 - Use a cyclic barrier to reduce the likelihood that threads are executed in a sequence

```
class TestCounter {
  // Shared variable for the tests
 CyclicBarrier barrier;
public void testingCounterParallel(int nrThreads, int N) {
     // init barrier
     barrier = new CyclicBarrier(nrThreads + 1);
     for (int i = 0; i < nrThreads; i++) {</pre>
      new Thread(() -> {
       barrier.await(); // wait until all threads are ready
      // thread execution
       barrier.await(); // wait until all threads are finished
      }).start();
     try
         barrier.await();
         barrier.await();
     } catch (InterruptedException | BrokenBarrierException e) {
         e.printStackTrace();
```

.30

- Maximize contention (e.g., using a cyclic barrier) to avoid a sequential execution of the threads
 - Use a cyclic barrier to reduce the likelihood that threads are executed in a sequence

```
class TestCounter {
  // Shared variable for the tes
 CyclicBarrier barrier;
                                    Why do we
                                  need this +1?
public void testingCounterParal
    // init barrier
    barrier = new CyclicBarrier(nrThreads + 1);
    for (int i = 0; i < nrThreads; i++) {</pre>
      new Thread(() -> {
      barrier.await(); // wait until all threads are ready
      // thread execution
      barrier.await(); // wait until all threads are finished
     }).start();
    try
        barrier.await();
        barrier.await();
    } catch (InterruptedException | BrokenBarrierException e) {
        e.printStackTrace();
```



You may need to define thread classes

```
class TestCounter {
Counter count;
public class Turnstile extends Thread {
    private final int N;
    public Turnstile(int N) { this.N = N; }
    public void run() {
                                Note that the thread includes
         try {
                                     the barrier.await()s
      barrier.await():
      IntStream
           .range(0,N)
           .forEach(x -> count.inc());
      barrier.await();
         } catch (InterruptedException | BrokenBarrierException e) {
      e.printStackTrace();
```

Concurrent Correctness Test – Counter



You may need to define thread classes

```
class TestCounter {
Counter count;
public class Turnstile extends Thread {
    private final int N;
    public Turnstile(int N) { this.N = N; }
     public void run() {
                                Note that the thread includes
         try {
                                     the barrier.await()s
      barrier.await():
      IntStream
           .range(0,N)
           .forEach(x -> count.inc());
      barrier.await();
         } catch (InterruptedException | BrokenBarrierException e) {
      e.printStackTrace();
```

```
class TestCounter {
  // Shared variable for the tests
  CyclicBarrier barrier;
public void testingCounterParallel(int nrThreads,
                                     int N) {
     // init barrier
    barrier = new CyclicBarrier(nrThreads + 1);
     for (int i = 0; i < nrThreads; i++) {</pre>
      new Turnstile(N).start();
     try {
                        Now we can simply start the
         barrier.awai
         barrier.awai
                             thread in the test
     } catch (Interru
    BrokenBarrierException e) {
         e.printStackTrace();
```

<u>Concurrent Correctness</u> Test – Counter



You may need to define thread classes

```
class TestCounter {
Counter count;
public class Turnstile extends Thread {
    private final int N;
    public Turnstile(int N) { this.N = N; }
     public void run() {
                                Note that the thread includes
         try {
                                     the barrier.await()s
      barrier.await();
      IntStream
           .range(0,N)
           .forEach(x -> count.inc());
      barrier.await();
         } catch (InterruptedException | BrokenBarrierException e) {
      e.printStackTrace();
```

```
class TestCounter {
  // Shared variable for the tests
 CyclicBarrier barrier;
   private final static ExecutorService pool
     = Executors.newCachedThreadPool();
public void testingCounterParallel(int nrThreads,
                                     int N) {
     // init barrier
    barrier = new CyclicBarrier(nrThreads + 1);
     for (int i = 0; i < nrThreads; i++) {</pre>
      pool.execute(new Turnstile(N));
     try {
                         Alternatively, we can use a
         barrier.awai
         barrier.awai
                          thread pool as in Goetz
     } catch (Interru
    BrokenBarrierException e) {
         e.printStackTrace();
```

Concurrent Correctness Test – Counter



- Optionally (though encouraged), one may generate input parameters using JUnit (@ParameterizedTest)
 - Note that the test method takes as input two integer parameters
 - Using @MethodSoucer we can specify a method that provides a collection of parameters (known as arguments)

```
private static List<Arguments> argsGeneration() {
    // Max number of increments
    final int I = 50 000;
    final int iInit = 10 000;
    final int iIncrement = 10 000;
    // Max exponent number of threads (2^J)
    final int J = 6;
    final int jInit = 1;
    final int jIncrement = 1;
    // List to add each parameters entry
    List<Arguments> list = new
    ArrayList<Arguments>();
    // Loop to generate each parameter entry
    // (2<sup>j</sup>, i) for j \in {10 000,20 000,...,J}
                and j \in {1,..,I}
    for (int i = iInit; i <= I; i += iIncrement)</pre>
        for (int j = jInit; j < J; j += jIncrement) {</pre>
     list.add(Arguments.of((int) Math.pow(2,j),i));
    // Return the list
    return list;
```

Concurrent Correctness Test – Counter



- Optionally (though encouraged), one may generate input parameters using JUnit (@ParameterizedTest)
 - Note that the test method takes as input two integer parameters
 - Using @MethodSoucer we can specify a method that provides a collection of parameters (known as arguments)

```
private static List<Arguments> argsGeneration() {
    // Max number of increments
    final int I = 50 000;
    final int iInit = 10 000;
    final int iIncrement = 10 000;
    // Max exponent number of threads (2^J)
    final int J = 6;
    final int jInit = 1;
    final int jIncrement = 1;
    // List to add each parameters entry
    List<Arguments> list = new
    ArrayList<Arguments>();
    // Loop to generate each parameter entry
    // (2<sup>j</sup>, i) for j \in {10 000,20 000,...,J}
                 and j \in {1,..,I}
    for (int i = iInit; i <= I; i += iIncrement)</pre>
        for (int j = jInit; j < J; j += jIncrement) {</pre>
     list.add(Arguments.of((int) Math.pow(2,j),i));
                                 Arguments is a JUnit class that
                                  can be seen as a collection of
    // Return the list
    return list;
                                    objects of different type
```



- Let's look at all together in code-lecture directory
- Note that Gradle requires test classes to be placed in the folder app/src/test/java/<package>/
- We look at three different implementations
 - CounterDR
 - CounterSync
 - CounterCAS
- JUnit produces a nice HTML report in build/reports/tests/test/classes/<package>.<class>.html
 - It includes outputs and running times



- Remember that some interleavings are difficult to trigger
- Let's look at the test testingCounterParallelConstant()
 - It is hard to find the interleavings that violate our property
 - Executing the test multiple times increases your chances of triggering the interleavings you are looking for
 - Remember @RepeatedTest()



Testing a Bounded Buffer



Now we turn our attention to a Bounded Buffer

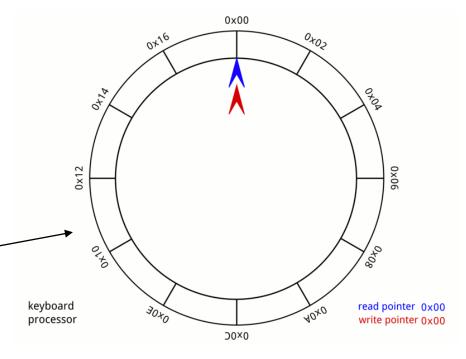


Producers

© Raúl Pardo Jimenez and Jørgen Staunstrup – F2021



- We study a functional correctness property of a bounded buffer that may be accessed by producers and consumers concurrently
- Producers may put elements in the buffer as long as there is space.
 Otherwise they must wait.
- Consumers can take elements from the buffer as long as it is not empty. Otherwise they must wait.
- The buffer is implemented as a circular buffer
- Synchronization is implemented using semaphores





```
@ThreadSafe
public class BoundedBuffer<E> {
    private final Semaphore availableItems, availableSpaces;
    @GuardedBy("this") private final E[] items;
    @GuardedBy("this") private int putPosition = 0, takePosition = 0;
    public BoundedBuffer(int capacity) {
        availableItems = new Semaphore(0);
        availableSpaces = new Semaphore(capacity);
        items = (E[]) new Object[capacity];
    public boolean isEmpty() {
        return availableItems.availablePermits() == 0;
    public boolean isFull() {
        return availableSpaces.availablePermits() == 0;
    public void put(E x) throws InterruptedException {
        availableSpaces.acquire();
        doInsert(x);
        availableItems.release();
    public E take() throws InterruptedException {
        availableItems.acquire();
        E item = doExtract();
        availableSpaces.release();
        return item;
```

Here is the implementation in Goetz p.
 249

```
private synchronized void doInsert(E x) {
   int i = putPosition;
   items[i] = x;
   putPosition = (++i == items.length)? 0 : i;
}
private synchronized E doExtract() {
   int i = takePosition;
   E x = items[i];
   items[i] = null;
   takePosition = (++i == items.length)? 0 : i;
   return x;
}
```

```
•41
```

```
@ThreadSafe
public class BoundedBuffer<E> {
    private final Semaphore availableItems, availableSpaces;
    @GuardedBy("this") private final E[] items;
    @GuardedBy("this") private int putPosition = 0, takePosition = 0;
    public BoundedBuffer(int capacity) {
        availableItems = new Semaphore(0);
        availableSpaces = new Semaphore(capacity);
        items = (E[]) new Object[capacity];
    public boolean isEmpty() {
        return availableItems.availablePermits() == 0;
    public boolean isFull() {
        return availableSpaces.availablePermits() == 0;
    public void put(E x) throws InterruptedException {
        availableSpaces.acquire();
        doInsert(x);
        availableItems.release():
    public E take() throws InterruptedException {
        availableItems.acquire();
        E item = doExtract();
        availableSpaces.release();
        return item;
```

- Here is the implementation in Goetz p.
 249
- It uses two semaphores to block threads when the buffer is full or empty

```
private synchronized void doInsert(E x) {
    int i = putPosition;
    items[i] = x;
    putPosition = (++i == items.length)? 0 : i;
}
private synchronized E doExtract() {
    int i = takePosition;
    E x = items[i];
    items[i] = null;
    takePosition = (++i == items.length)? 0 : i;
    return x;
}
```

```
•42
```

```
@ThreadSafe
public class BoundedBuffer<E> {
    private final Semaphore availableItems, availableSpaces;
    @GuardedBy("this") private final E[] items;
    @GuardedBy("this") private int putPosition = 0, takePosition = 0;
    public BoundedBuffer(int capacity) {
        availableItems = new Semaphore(0);
        availableSpaces = new Semaphore(capacity);
        items = (E[]) new Object[capacity];
    public boolean isEmpty() {
        return availableItems.availablePermits() == 0;
    public boolean isFull() {
        return availableSpaces.availablePermits() == 0;
    public void put(E x) throws InterruptedException {
        availableSpaces.acquire();
        doInsert(x);
        availableItems.release();
    public E take() throws InterruptedException {
        availableItems.acquire();
        E item = doExtract();
        availableSpaces.release();
        return item;
```

- Here is the implementation in Goetz p.
 249
- It uses two semaphores to block threads when the buffer is full or empty
- It uses intrinsic locks to ensure mutual exclusion when accessing the buffer

```
private synchronized void doInsert(E x) {
   int i = putPosition;
   items[i] = x;
   putPosition = (++i == items.length)? 0 : i;
}
private synchronized E doExtract() {
   int i = takePosition;
   E x = items[i];
   items[i] = null;
   takePosition = (++i == items.length)? 0 : i;
   return x;
}
```



```
@ThreadSafe
public class BoundedBuffer<E> {
    private final Semaphore availableItems, availableSpaces;
    @GuardedBy("this") private final E[] items;
    @GuardedBy("this") private int putPosition = 0, takePosition = 0;

public BoundedBuffer(int capacity) {
        availableItems = new Semaphore(0);
        availableSpaces = new Semaphore(capacity);
        items = (E[]) new Object[capacity];
    }
    public boolean isEmpty() {
        return availableItems.availablePermits() == 0;
    }
    public boolean isFull() {
        return availableSpaces.availablePermits() == 0;
}
```

Why is it necessary to use the intrinsic locks if we are already using semaphores to control access to the buffer?

- Here is the implementation in Goetz p.
 249
- It uses two semaphores to block threads when the buffer is full or empty
- It uses intrinsic locks to ensure mutual exclusion when accessing the buffer

```
private synchronized void doInsert(E x) {
   int i = putPosition;
   items[i] = x;
   putPosition = (++i == items.length)? 0 : i;
}
private synchronized E doExtract() {
   int i = takePosition;
   E x = items[i];
   items[i] = null;
   takePosition = (++i == items.length)? 0 : i;
   return x;
}
```



1. Property to check

- "after several producers put integers $x_1, ..., x_N$ to the buffer and several consumers take integers $y_1, ..., y_N$ from the buffer, it must hold that $\sum_{i=1}^N x_i = \sum_{i=1}^N y_i$ "
- More informally: "If several threads put and take the same number of elements, the sum of the put elements and the sum of the taken elements must be equal"
- A producer may add more than one integer in the buffer and a consumer may take more than one integer
 - The only constraint is that the combined number of puts and takes is the same for all producers and consumers



1. Property to check

- "after several producers put integers $x_1, ..., x_N$ to the buffer and several consumers take integers $y_1, ..., y_N$ from the buffer, it must hold that $\sum_{i=1}^N x_i = \sum_{i=1}^N y_i$ "
- More informally: "If several threads put and take the same number of elements, the sum of the put elements and the sum of the taken elements must be equal"

What should go wrong in the buffer for this property to be violated?

Or, assume a wrongly implemented buffer, can you give an interleaving that violates the property?

er and a consumer

ts and takes is the

•44

2. Testing setup (producer)

```
Class BoundedBufferTest {
 BoundedBuffer buffer:
AtomicInteger putSum; // global sum of put numbers
AtomicInteger takeSum; // global sum of taken numbers
 class Producer extends Thread {
     int nrTrials:
     int localSum;
     public Producer(int nrTrials) {
         this.nrTrials = nrTrials;
         this.localSum = 0;
     public void run() {
         try {
      barrier.await();
       for (int i = 0; i < nrTrials; i++) {
           Random r = new Random();
           int toPut = r.nextInt();
           buffer.put(toPut);
          localSum += toPut;
      putSum.addAndGet(localSum);
      barrier.await();
         } catch (InterruptedException |
     BrokenBarrierException e) {
       e.printStackTrace();
```

.44

2. Testing setup (producer)

We have use two global AtomicIntegers to keep track of the global sum of put/remove

```
Class BoundedBufferTest {
 BoundedBuffer buffer:
AtomicInteger putSum; // global sum of put numbers
AtomicInteger takeSum; // global sum of taken numbers
 class Producer extends Thread {
     int nrTrials:
     int localSum;
     public Producer(int nrTrials) {
         this.nrTrials = nrTrials;
         this.localSum = 0;
     public void run() {
         try {
      barrier.await();
      for (int i = 0; i < nrTrials; i++) {
          Random r = new Random();
          int toPut = r.nextInt();
          buffer.put(toPut);
          localSum += toPut;
      putSum.addAndGet(localSum);
      barrier.await();
         } catch (InterruptedException |
     BrokenBarrierException e) {
      e.printStackTrace();
```

•44

2. Testing setup (producer)

We have use two global AtomicIntegers to keep track of the global sum of put/remove

The producer is initialized with the number of integers it should put in the buffer. I also has a local sum of put numbers.

```
Class BoundedBufferTest {
 BoundedBuffer buffer:
AtomicInteger putSum; // global sum of put numbers
AtomicInteger takeSum; // global sum of taken numbers
 class Producer extends Thread {
     int nrTrials:
     int localSum;
     public Producer(int nrTrials) {
         this.nrTrials = nrTrials;
         this.localSum = 0;
     public void run() {
         try {
      barrier.await();
      for (int i = 0; i < nrTrials; i++) {
          Random r = new Random();
          int toPut = r.nextInt();
          buffer.put(toPut);
          localSum += toPut;
      putSum.addAndGet(localSum);
      barrier.await();
         } catch (InterruptedException |
     BrokenBarrierException e) {
      e.printStackTrace();
```



2. Testing setup (producer)

We have use two global AtomicIntegers to keep track of the global sum of put/remove

The producer is initialized with the number of integers it should put in the buffer. I also has a local sum of put numbers.

The producer generates a local random number to puts it in the buffer. Then it updates the local sum of put numbers

```
Class BoundedBufferTest {
 BoundedBuffer buffer:
AtomicInteger putSum; // global sum of put numbers
AtomicInteger takeSum; // global sum of taken numbers
 class Producer extends Thread {
     int nrTrials:
     int localSum;
     public Producer(int nrTrials) {
         this.nrTrials = nrTrials;
         this.localSum = 0;
     public void run() {
         try {
      barrier.await();
      for (int i = 0; i < nrTrials; i++) {
          Random r = new Random();
          int toPut = r.nextInt();
          buffer.put(toPut);
          localSum += toPut;
      putSum.addAndGet(localSum);
      barrier.await();
         } catch (InterruptedException |
     BrokenBarrierException e) {
      e.printStackTrace();
```

•44

2. Testing setup (producer)

We have use two global AtomicIntegers to keep track of the global sum of put/remove

The producer is initialized with the number of integers it should put in the buffer. I also has a local sum of put numbers.

The producer generates a local random number to puts it in the buffer. Then it updates the local sum of put numbers

Finally, the global put sum is updated with the local sum of the producer.

```
Class BoundedBufferTest {
 BoundedBuffer buffer:
AtomicInteger putSum; // global sum of put numbers
AtomicInteger takeSum; // global sum of taken numbers
 class Producer extends Thread {
     int nrTrials:
     int localSum;
     public Producer(int nrTrials) {
         this.nrTrials = nrTrials;
         this.localSum = 0;
     public void run() {
         try {
      barrier.await();
      for (int i = 0; i < nrTrials; i++) {
          Random r = new Random();
          int toPut = r.nextInt();
          buffer.put(toPut);
          localSum += toPut;
      putSum.addAndGet(localSum);
      barrier.await();
         } catch (InterruptedException |
     BrokenBarrierException e) {
      e.printStackTrace();
```

maximize

2. Testing setup (producer)

We have use two global AtomicIntegers to keep track of the global sum of put/remove

The producer is initialized with the number of integers it should put in the buffer. I also has a local sum of put numbers.

The producer generates a local random number to puts it in the buffer. Then it updates the local sum of put numbers

Finally, the global put sum is updated with the local sum of the producer.

```
Class BoundedBufferTest {
BoundedBuffer buffer:
AtomicInteger putSum; // global sum of put numbers
AtomicInteger takeSum; // global sum of taken numbers
 class Producer extends Thread {
     int nrTrials:
     int localSum;
                                         As expected, we
    public Producer(int nrTrials) {
         this.nrTrials = nrTrials;
                                          use a barrier to
         this.localSum = 0;
                                            contention.
    public void run() {
         try {
      barrier.await();
      for (int i = 0; i < nrTrials; i++) {
          Random r = new Random();
          int toPut = r.nextInt();
          buffer.put(toPut);
          localSum += toPut;
      putSum.addAndGet(localSum);
      barrier.await();
         } catch (InterruptedException |
    BrokenBarrierException e) {
      e.printStackTrace();
```

© Raúl Pardo Jimenez and Jørgen Staunstrup – F2021

.45

2. Testing setup (consumer)

```
Class BoundedBufferTest {
 BoundedBuffer buffer:
AtomicInteger putSum; // global sum of put numbers
AtomicInteger takeSum; // global sum of taken numbers
  class Consumer extends Thread {
     int nrTrials:
     int localSum;
     public Consumer(int nrTrials) {
         this.nrTrials = nrTrials;
         this.localSum = 0;
     public void run() {
         try {
      barrier.await();
      for (int i = 0; i < nrTrials; i++) {
          localSum += buffer.take();
      takeSum.addAndGet(localSum);
      barrier.await();
         } catch (InterruptedException |
     BrokenBarrierException e) {
      e.printStackTrace();
```

. 45

2. Testing setup (consumer)

The consumer is initialized with the number of integers it should take from the buffer. I also has a local sum of taken numbers.

```
Class BoundedBufferTest {
 BoundedBuffer buffer:
AtomicInteger putSum; // global sum of put numbers
AtomicInteger takeSum; // global sum of taken numbers
  class Consumer extends Thread {
     int nrTrials:
     int localSum;
     public Consumer(int nrTrials) {
         this.nrTrials = nrTrials;
         this.localSum = 0;
     public void run() {
         try {
      barrier.await();
      for (int i = 0; i < nrTrials; i++) {
          localSum += buffer.take();
      takeSum.addAndGet(localSum);
      barrier.await();
         } catch (InterruptedException |
     BrokenBarrierException e) {
      e.printStackTrace();
```

6

2. Testing setup (consumer)

The consumer is initialized with the number of integers it should take from the buffer. I also has a local sum of taken numbers.

The consumer takes an element from the buffer and it updates the local sum of taken integers

```
Class BoundedBufferTest {
 BoundedBuffer buffer:
AtomicInteger putSum; // global sum of put numbers
AtomicInteger takeSum; // global sum of taken numbers
  class Consumer extends Thread {
     int nrTrials:
     int localSum;
     public Consumer(int nrTrials) {
         this.nrTrials = nrTrials;
         this.localSum = 0;
     public void run() {
         try {
      barrier.await();
      for (int i = 0; i < nrTrials; i++) {
          localSum += buffer.take();
      takeSum.addAndGet(localSum);
      barrier.await();
         } catch (InterruptedException |
     BrokenBarrierException e) {
      e.printStackTrace();
```

2. Testing setup (consumer)

The consumer is initialized with the number of integers it should take from the buffer. I also has a local sum of taken numbers.

The consumer takes an element from the buffer and it updates the local sum of taken integers

Finally, the global taken sum is updated with the local sum of the consumer.

```
Class BoundedBufferTest {
 BoundedBuffer buffer:
AtomicInteger putSum; // global sum of put numbers
AtomicInteger takeSum; // global sum of taken numbers
  class Consumer extends Thread {
     int nrTrials:
     int localSum;
     public Consumer(int nrTrials) {
         this.nrTrials = nrTrials;
         this.localSum = 0;
     public void run() {
         try {
      barrier.await();
      for (int i = 0; i < nrTrials; i++) {
          localSum += buffer.take();
      takeSum.addAndGet(localSum);
      barrier.await();
         } catch (InterruptedException |
     BrokenBarrierException e) {
      e.printStackTrace();
```

2. Testing setup (consumer)

The consumer is initialized with the number of integers it should take from the buffer. I also has a local sum of taken numbers.

The consumer takes an element from the buffer and it updates the local sum of taken integers

Finally, the global taken sum is updated with the local sum of the consumer.

```
Class BoundedBufferTest {
BoundedBuffer buffer:
AtomicInteger putSum; // global sum of put numbers
AtomicInteger takeSum; // global sum of taken numbers
  class Consumer extends Thread {
     int nrTrials:
     int localSum;
                                         As expected, we
    public Consumer(int nrTrials) {
         this.nrTrials = nrTrials;
                                         use a barrier to
         this.localSum = 0;
                                             maximize
                                           contention.
    public void run() {
         try {
      barrier.await();
      for (int i = 0; i < nrTrials; i++) {
          localSum += buffer.take();
      takeSum.addAndGet(localSum);
      barrier.await();
         } catch (InterruptedException |
    BrokenBarrierException e) {
      e.printStackTrace();
```



2. Testing setup (test)

```
public void putTakeTest(int nrThreads,
                int nrTrials,
                 int bufferSize) {
    // init buffer
    buffer = new BoundedBufferSemaphore<Integer>(bufferSize);
    // init barrier
    barrier = new CyclicBarrier((nrThreads*2) + 1);
    for (int i = 0; i < nrThreads; i++) {
        pool.execute(new Producer(nrTrials));
        pool.execute(new Consumer(nrTrials));
    try {
        barrier.await():
        barrier.await();
    } catch (InterruptedException | BrokenBarrierException e)
        e.printStackTrace();
    assert(putSum.get() == takeSum.get());
```



2. Testing setup (test)

The test has 3 parameters: the number of pairs of producer consumers, the number of put/take that each producer/consumer must perform and the size of the buffer

```
public void putTakeTest(int nrThreads,
                 int nrTrials,
                 int bufferSize) {
    // init buffer
    buffer = new BoundedBufferSemaphore<Integer>(bufferSize);
    // init barrier
    barrier = new CyclicBarrier((nrThreads*2) + 1);
    for (int i = 0; i < nrThreads; i++) {
        pool.execute(new Producer(nrTrials));
        pool.execute(new Consumer(nrTrials));
    try {
        barrier.await();
        barrier.await();
    } catch (InterruptedException | BrokenBarrierException e)
        e.printStackTrace();
    assert(putSum.get() == takeSum.get());
```



2. Testing setup (test)

The test has 3 parameters: the number of pairs of producer consumers, the number of put/take that each producer/consumer must perform and the size of the buffer

We initialize the buffer and the barrier

```
public void putTakeTest(int nrThreads,
                 int nrTrials,
                int bufferSize) {
    // init buffer
    buffer = new BoundedBufferSemaphore<Integer>(bufferSize);
    // init barrier
    barrier = new CyclicBarrier((nrThreads*2) + 1);
    for (int i = 0; i < nrThreads; i++) {
        pool.execute(new Producer(nrTrials));
        pool.execute(new Consumer(nrTrials));
    try {
        barrier.await();
        barrier.await();
    } catch (InterruptedException | BrokenBarrierException e)
        e.printStackTrace();
    assert(putSum.get() == takeSum.get());
```



2. Testing setup (test)

The test has 3 parameters: the number of pairs of producer consumers, the number of put/take that each producer/consumer must perform and the size of the buffer

We initialize the buffer and the barrier

```
public void putTakeTest(int nrThreads,
                int nrTrials,
                int bufferSize) {
    // init buffer
    buffer = new BoundedBufferSemaphore<Integer>(bufferSize);
    // init barrier
   barrier = new CyclicBarrier((nrThreads*2) + 1);
    for (int i = 0; i < nrThreads; i++) {
                                                  We execute a
        pool.execute(new Producer(nrTrials));
                                                  producer and
        pool.execute(new Consumer(nrTrials));
                                                   consumer in
                                                  each iteration
    try {
        barrier.await();
        barrier.await();
    } catch (InterruptedException | BrokenBarrierException e)
        e.printStackTrace();
    assert(putSum.get() == takeSum.get());
```



2. Testing setup (test)

The test has 3 parameters: the number of pairs of producer consumers, the number of put/take that each producer/consumer must perform and the size of the buffer

We initialize the buffer and the barrier

As a reminder, the first await is to maximize contention, and the second to wait for all threads to finish execution

```
public void putTakeTest(int nrThreads,
                int nrTrials,
                int bufferSize) {
    // init buffer
    buffer = new BoundedBufferSemaphore<Integer>(bufferSize);
    // init barrier
    barrier = new CyclicBarrier((nrThreads*2) + 1);
    for (int i = 0; i < nrThreads; i++) {
                                                  We execute a
        pool.execute(new Producer(nrTrials));
                                                   producer and
        pool.execute(new Consumer(nrTrials));
                                                   consumer in
                                                  each iteration
    try {
        barrier.await();
        barrier.await();
    } catch (InterruptedException | BrokenBarrierException e)
        e.printStackTrace();
    assert(putSum.get() == takeSum.get());
```



2. Testing setup (test)

The test has 3 parameters: the number of pairs of producer consumers, the number of put/take that each producer/consumer must perform and the size of the buffer

We initialize the buffer and the barrier

As a reminder, the first await is to maximize contention, and the second to wait for all threads to finish execution

Finally, we check that our property holds after executing the test. The test relies on the correctness of AtomicInteger.

```
public void putTakeTest(int nrThreads,
                int nrTrials,
                int bufferSize) {
    // init buffer
    buffer = new BoundedBufferSemaphore<Integer>(bufferSize);
    // init barrier
    barrier = new CyclicBarrier((nrThreads*2) + 1);
    for (int i = 0; i < nrThreads; i++) {
                                                   We execute a
        pool.execute(new Producer(nrTrials));
                                                   producer and
        pool.execute(new Consumer(nrTrials));
                                                   consumer in
                                                  each iteration
    try {
        barrier.await();
        barrier.await();
    } catch (InterruptedException | BrokenBarrierException e)
        e.printStackTrace();
    assert(putSum.get() == takeSum.get());
```

© Raúl Pardo Jimenez and Jørgen Staunstrup – F2021 IT UNIVERSITY OF COPENHAGEN



2. Testing setup (test)

The test has 3 parameters: the number of pairs of producer consumers, the number of put/take that each producer/consumer must perform and the size of the buffer

We initialize the buffer and the barrier

As a reminder, the first await is to maximize contention, and the second to wait for all threads to finish execution

Finally, we check that our property holds after executing the test. The test relies on the correctness of AtomicInteger.

```
public void putTakeTest(int nrThreads,
                int nrTrials,
                int bufferSize) {
    // init buffer
    buffer = new BoundedBufferSemaphore<Integer>(bufferSize);
    // init barrier
   barrier = new CyclicBarrier((nrThreads*2) + 1);
    for (int i = 0; i < nrThreads; i++) {
                                                  We execute a
        pool.execute(new Producer(nrTrials));
                                                   producer and
        pool.execute(new Consumer(nrTrials));
                                                   consumer in
                                                  each iteration
    try {
        barrier.await();
        barrier.await();
    } catch (InterruptedException | BrokenBarrierException e)
        e.printStackTrace();
    assert(putSum.get() == takeSum.get());
```

Let's run the tests!

© Raúl Pardo Jimenez and Jørgen Staunstrup – F2021



```
@ThreadSafe
public class BoundedBuffer<E> {
    private final Semaphore availableItems, availableSpaces;
    @GuardedBy("this") private final E[] items;
    @GuardedBv("this") private int putPosition = 0. takePosition = 0:
    public BoundedBuffer(int capacity) {
        availableItems = new Semaphore(0);
        availableSpaces = new Semaphore(capacity);
        items = (E[]) new Object[capacity];
    public boolean isEmpty() {
        return availableItems.availablePermits() == 0;
    public boolean isFull() {
        return availableSpaces.availablePermits() == 0;
    public void put(E x) throws InterruptedException {
        availableSpaces.acquire();
        doInsert(x);
        availableItems.release();
    public E take() throws InterruptedException {
        availableItems.acquire();
        E item = doExtract();
        availableSpaces.release();
        return item;
```

 Here is the implementation in Goetz p. 249

```
private synchronized void doInsert(E x) {
    int i = putPosition;
    items[i] = x;
    putPosition = (++i == items.length)? 0 : i;
}
private synchronized E doExtract() {
    int i = takePosition;
    E x = items[i];
    items[i] = null;
    takePosition = (++i == items.length)? 0 : i;
    return x;
}
```



```
@ThreadSafe
public class BoundedBuffer<E> {
    private final Semaphore availableItems, availableSpaces;
    @GuardedBy("this") private final E[] items;
    @GuardedBy("this") private int putPosition = 0, takePosition = 0;
    public BoundedBuffer(int capacity) {
        availableItems = new Semaphore(0);
        availableSpaces = new Semaphore(capacity);
        items = (E[]) new Object[capacity];
    public boolean isEmpty() {
        return availableItems.availablePermits() == 0;
    public boolean isFull() {
        return availableSpaces.availablePermits() == 0;
    public void put(E x) throws InterruptedException {
        availableSpaces.acquire();
        doInsert(x);
        availableItems.release();
    public E take() throws InterruptedException {
        availableItems.acquire();
        E item = doExtract();
        availableSpaces.release();
        return item;
```

Here is the implementation in Goetz p.
 249

Do you think these methods are thread-safe?
(the question is a bit ambiguous on purpose, you can try asking me to be more precise if you will)

```
}
private synchronized E doExtract() {
   int i = takePosition;
   E x = items[i];
   items[i] = null;
   takePosition = (++i == items.length)? 0 : i;
   return x;
}
```

Deadlocks



- A deadlock occurs when all threads are waiting locks hold by other threads
 - which will never happen as all threads are waiting
- Standard (but not very realistic) example:
 - Dinning philosophers by E.W. Dijkstra
 - Philosophers only think and eat
 - A philosopher must pick both left and right forks to start eating

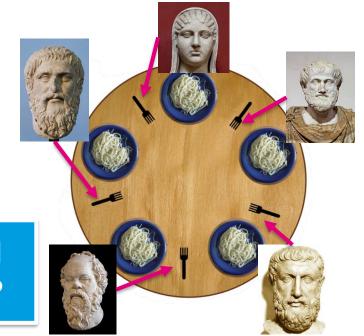


Deadlocks



- A deadlock occurs when all threads are waiting locks hold by other threads
 - which will never happen as all threads are waiting
- Standard (but not very realistic) example:
 - Dinning philosophers by E.W. Dijkstra
 - Philosophers only think and eat
 - A philosopher must pick both left and right forks to start eating

What happens if we reach a state where all philosophers have grabbed their right fork?



Testing deadlocks



Testing for deadlocks is not really possible

Testing deadlocks

.49

Testing for deadlocks is not really possible

Why?



Formal Verification

Limitations of testing



- Testing is a extremely useful technique, which is the de-facto approach in industry
 - You should extensively tests all your programs!
- However, it cannot be used to prove the absence bugs (remember the first slides)
- Tests can be seen as random interleaving generators ©
 - They stimulate the system to produce different interleavings
 - For most systems, it is virtually impossible to write a set of tests that cover all possible interleavings in the system



- Formal verification is a technology that aims to prove that a program satisfy a specification (properties)
- It treats programs and properties as mathematical objects
- Using mathematical reasoning it is possible to prove that programs satisfy their specifications (i.e., for all possible interleavings)
 - Manually: Proof assistants (Coq, Isabelle, etc.)
 - Automatically: SAT solvers, SMT solvers, <u>model-checking</u>, static verification, symbolic execution, etc.



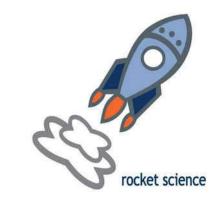
- Model-checking transforms programs into a finite-state models that encapsulate all possible interleavings in the system
 - Automata, Kripke structures, binary decision diagrams, etc.
- Properties are specified in some type of logic
 - Linear Temporal Logic (LTL), Computational Tree Logic (CTL), First-Order Logic (FOL), propositional logic, etc.
- The model of the program and the property are typically expressed in the same language so it is possible to automatically check whether they are satisfied
- Model-checking has been very successful in hardware verification at Intel

JavaPathFinder (switch to rocket science)

JavaPathFinder is (among other things) a model-checker for Java programs

- It is developed at the Jet Propulsion Lab (JPL) at NASA
 - It was used to verify part of the system in the Curiosity rover that landed in Mars in 2012

Let's look at a few examples of using **JavaPathFinder**







 Altogether (not executa the executable program **VERY HARD**: What is the minimum value of **counter** that this program can print?



```
long counter = 0;
final long PEOPLE = 10 000;
Turnstile turnstile1 = new Turnstile();
Turnstile turnstile2 = new Turnstile();
turnstile1.start();turnstile2.start();
turnstile2.join();turnstile2.join();
System.out.println(counter+" people entered");
public class Turnstile extends Thread {
   public void run() {
       for (int i = 0; i < PEOPLE; i++) {
          counter++;
```

Another déjà vu?

Let's use javapathfinder to automatically get the answer



 Altogether (not executa the executable program **VERY HARD**: What is the minimum value of **counter** that this program can print?

Can testing be used to answer this question?



```
Turnstile turnstile1 = new Turnstile();
Turnstile turnstile2 = new Turnstile();
turnstile1.start();turnstile2.start();
turnstile2.join();turnstile2.join();
System.out.println(counter+" people entered");

public class Turnstile extends Thread {
   public void run() {
      for (int i = 0; i < PEOPLE; i++) {
         counter++;
      }
   }
}</pre>
```

Another déjà vu?

Let's use javapathfinder to automatically get the answer

© Raúl Pardo Jimenez and Jørgen Staunstrup – F2021

Bounded Buffer in JavaPathFinder



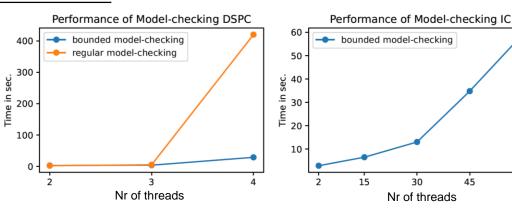
 Let's now look at an example of finding deadlocks with JavaPathFinder in a buggy implementation of a bounded buffer

Too good to be true...

45

60

- Ok Raúl, if formal verification is so good, why isn't everyone using it all the time?
 - Welcome to the state explosion problem! (among other things)
 - Even for small programs the computational cost of proving that the system satisfies its specification can be astronomically expensive
- The use of abstractions and/or narrow down the problem domain, has helped formal verification to scale better
 - Example: Proving that an IoT system satisfies a privacy requirement (my own work-in-progress paper)



Formal Verification – In Industry and at ITU



 Many companies have started to use formal verification in their software development process, so it might be a good asset to have in your toolbox





- At ITU, you can learn more about formal verification in the software analysis specialization, e.g., in the courses
 - Advanced Software Analysis
 - Program verification
 - ...
- I believe modern software engineers should be aware of this technology and trained to use it (warning: personal opinion)

MSc thesis in Formal Verification



- Formal verification is an active topic of research
- If you found this topic interesting, feel free to contact me regarding MSc thesis projects
 - Also keep an eye on people working at the Software Quality Group (SQUARE), the Centre of Security and Trust (CISAT) and the Programming, Logic and Semantics (PLS) group
- My interests focus on using formal verification to
 - Prove that systems satisfy legal privacy requirements (e.g., GDPR)
 - Quantify privacy risks in ML
 - Prove properties in probabilistic programs

Agenda



- Intro to concurrency properties
- Testing
 - Intro to JUnit 5
 - Counter
 - Bounded Buffer
 - Deadlocks
- Formal Verification
 - Java Path Finder

