

Modeling of Thermo-Fluid Systems with Modelica

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Content

- Introduction
- Separation of Component and Medium
- Property models in Media: main concepts
- Components, control volumes and ports
- Balance equations
- Index reduction and state selection
- Numerical regularization
- Exercises

Separate Medium from Component

- Independent components for very different types of media (only constants or based on Helmholtz function)
- Introduce “Thermodynamic State” concept: minimal and *replaceable* set of variables needed to compute all properties
- Calls to functions take a state-record as input and are therefore identical for e.g. **Ideal gas mixtures** and **Water**

```

redeclare record extends ThermodynamicState "thermo state variables"
  AbsolutePressure p "Absolute pressure of medium";
  Temperature T "Temperature of medium";
  MassFraction X[nS] "Mass fractions (= (comp. mass)/total mass)";
end ThermodynamicState;

```

```

redeclare record extends ThermodynamicState "thermo state variables"
  AbsolutePressure p "Absolute pressure of medium";
  SpecificEnthalpy h "specific enthalpy of medium";
end ThermodynamicState;

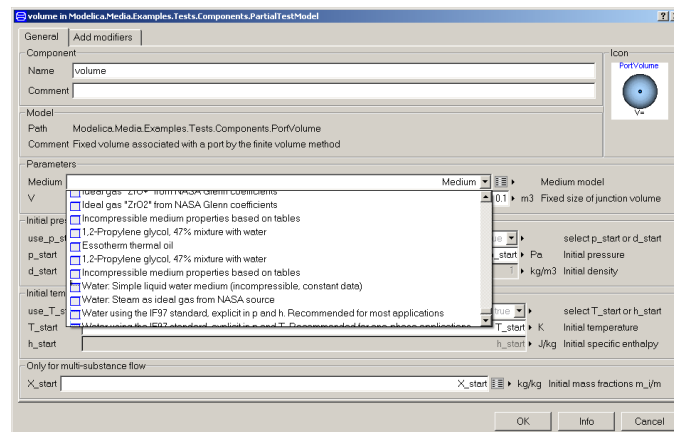
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Separate Medium from Component

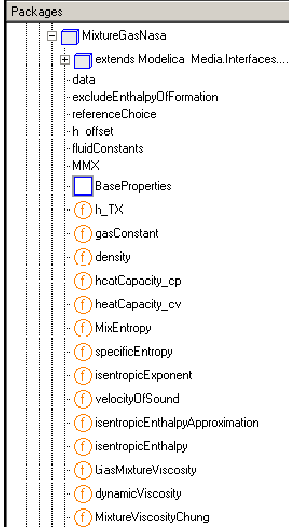
- Medium models are “replaceable packages” in Modelica, selected via drop-down menus in Dymola



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Media Models



Medium property definitions for

- Single and **multiple substances**
- Single and **multiple phases**
(all phases have same speed)
- **free** selection of **independent variables**
(p,T or p,h, T,p,T, Mx or p, T, X_i)

Media mostly adapted from ThermoFluid:

- 1241 ideal gases (NASA source) and their mixtures
- IF97 water (high precision)
- Moist air
- Incompressible media defined by tabular data
- simple air, and water models (for machine cooling)

- Every medium model provides **3 equations** for **5 + nX variables**

Variable	Unit	Description
T	K	temperature
p	Pa	absolute pressure
d	kg/m ³	density
u	J/kg	specific internal energy
h	J/kg	specific enthalpy (h = u + p/d)
X _i [nX _i]	kg/kg	independent mass fractions m _i /m
X[nX]	kg/kg	All mass fractions m _i /m. X is defined in BaseProperties by: X = if reducedX then vector([X _i ; 1-sum(X _i)]) else X _i

Two variables out of p, d, h, or u, as well as the mass fractions X_i are the **independent** variables and the medium model basically provides equations to compute the remaining variables, including the full mass fraction vector X

- A medium model might provide **optional functions**

Function call	Unit	Description
Medium.dynamicViscosity(medium.state)	Pa.s	dynamic viscosity
Medium.thermalConductivity(medium.state)	W/(m.K)	thermal conductivity
Medium.prandtlNumber(medium.state)	1	Prandtl number
Medium.specificEntropy(medium.state)	J/(kg.K)	specific entropy
Medium.heatCapacity_cp(medium.state)	J/(kg.K)	specific heat capacity at constant pressure
Medium.heatCapacity_cv(medium.state)	J/(kg.K)	specific heat capacity at constant density
Medium.isentropicExponent(medium.state)	1	isentropic exponent
Medium.isentropicEnthalpy(pressure, medium.state)	J/kg	isentropic enthalpy
Medium.velocityOfSound(medium.state)	m/s	velocity of sound
Medium.isobaricExpansionCoefficient(medium.state)	1/K	isobaric expansion coefficient
Medium.isothermalCompressibility(medium.state)	1/Pa	isothermal compressibility
Medium.density_der_p(medium.state)	kg/(m3.Pa)	derivative of density by pressure at constant enthalpy
Medium.density_der_h_p(medium.state)	kg2/(m3.J)	derivative of density by enthalpy at constant pressure
Medium.density_der_p_T(medium.state)	kg/(m3.Pa)	derivative of density by pressure at constant temperature
Medium.density_der_T_p(medium.state)	kg/(m3.K)	derivative of density by temperature at constant pressure
Medium.density_der_X(medium.state)	kg/m3	derivative of density by mass fraction
Medium.molarMass(medium.state)	kg/mol	molar mass

Medium package

```

package SimpleAir
...
constant Integer nX = 0 // the independent mass fractions;
model BaseProperties
  constant SpecificHeatCapacity cp_air=1005.45
  "Specific heat capacity of dry air";
  AbsolutePressure      p;
  Temperature           T;
  Density               d;
  SpecificInternalEnergy u;
  SpecificEnthalpy      h;
  MassFraction          X[nX];
  constant MolarMass MM_air=0.0289651159 "Molar mass";
  constant SpecificHeatCapacity R_air=Constants.R/MM_air
equation
  d = p/(R_air*T);
  h = cp_air*T + h0;
  u = h - p/d;
  state.T = T;
  state.p = p;
end BaseProperties;
...
end SimpleAir;

```

Separate Medium from Component, II

How should components be written that are independent of the medium (and its independent variables)?

```
.....
package Medium = Modelica.Media.Interfaces.PartialMedium;
    Medium.BaseProperties medium;
equation
    // mass balances
    der(m) = port_a.m_flow + port_b.m_flow;
    der(mXi) = port_a.mXi_flow + port_b.mXi_flow;
        m = V*medium.d;
        mXi = M*medium.Xi; //only the independent ones, nS-1!
    // Energy balance
        U = M*medium.u;
    der(U) = port_a.H_flow+port_b.H_flow;
```

Important note: only 1 less mXi then components are integrated.
 “i” stands for “independent”!

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Balance Equations and Media Models are decoupled

```
// Balance equations in volume for single substance:
    m = V*d;           // mass of fluid in volume
    U = m*u;           // internal energy in volume
der(m) = port.m_flow; // mass balance
der(U) = port.H_flow; // energy balance

// Equations in medium (independent of balance equations)
    d = f_d(p,T);
    h = f_h(p,T);
    u = h - p/d;
```

Assume m, U are selected as states, i.e., m, U are assumed to be known:

```
u := U/m;
d := m/V;
res1 := d - f_d(p,T)
res2 := u + p/d - f_h(p,T) }
```

As a result, **non-linear equations** have to be solved for p and T:

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Use preferred states

the independent variables in media models are declared as preferred states:

AbsolutePressure p(stateSelect = StateSelect.prefer)
Tool will select p as state, if this is possible

<pre>d := f_d(p,T); h := f_h(p,T); u := h - p/d; m := V*d; U := m*u;</pre>	→	<pre>der(U) = der(m)*u + m*der(u) der(m) = V*der(d) der(u) = der(h) - der(p)/d + p/d^2*der(d) der(d) = der(f_d,p)*der(p) + der(f_d,T)*der(T) der(h) = der(f_h,p)*der(p) + der(f_h,T)*der(T)</pre>
--	---	---

der(f_d, p) is the partial derivative of f_d w.r.t. p

- index reduction is automatically applied by tool to rewrite the equations using p, T as states (linear system in **der(p)** and **der(T)**)
- no non-linear systems of equations anymore
- different independent variables are possible (tool just performs different index reductions)

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Incompressible Media

Same balance equations + special medium model:

- Equation stating that density is constant ($d = d_{\text{const}}$) or that density is a function of T, ($d = d(T)$)
- User-provided initial value for p or d is used as guess value (i.e. 1 initial equation and not 2 initial equations)

Automatic index reduction transforms differential equation for mass balance into algebraic equation:

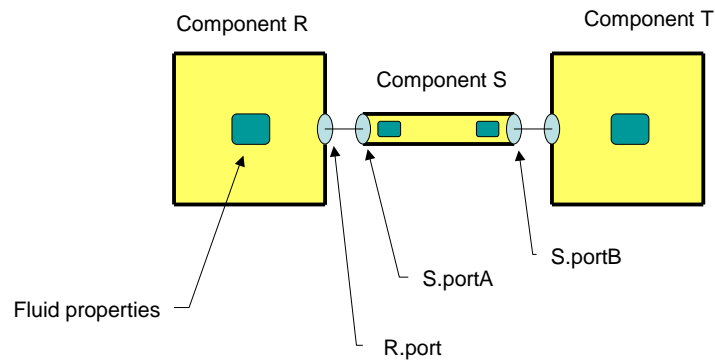
<pre>m = V*d; der(m) = port.m_flow;</pre>	→	<pre>der(m) = V*der(d);</pre>	→	<pre>0 = port.m_flow;</pre>
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Connectors and Reversible flow

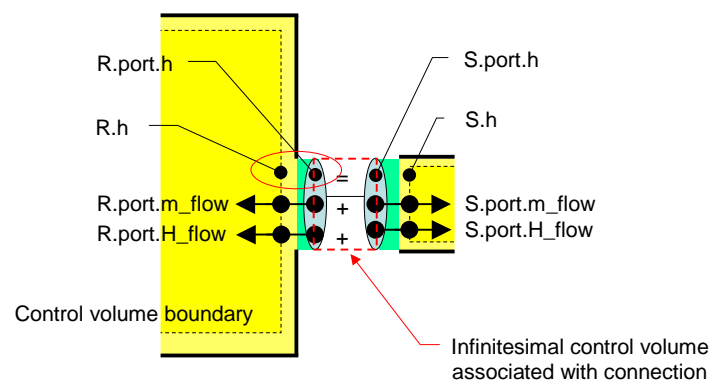
- Compressible and non-compressible fluids
- Reversing flows
- Ideal mixing



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The details – boundary conditions



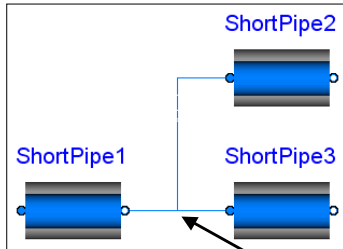
$$\dot{H} = \begin{cases} \dot{m}h_{port} & \dot{m} > 0 \\ \dot{m}h & \text{otherwise} \end{cases}$$

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2. Modelica.Fluid Connector Definition

The interfaces (connector **FluidPort**) are defined, so that arbitrary components can be connected together



- correct for **all media** of Modelica_Media (incompressible/compressible, one/multiple substance, one/multiple phases)
- **Diffusion not included**

- Infinitesimal small volume in connection point.
- **Mass- and energy balance** are always **fulfilled** (= ideal mixing).
- If "ideal mixing is not sufficient", a special component to define the mixing must be introduced. This is an advantage in many cases, and is thus available in Modelica.Fluid

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Connector

Infinitesimal control volume associated with connection

- **flow** variables give mass- and energy-balances
- Momentum balance not considered – forces on junction gives balance

Medium in connector allows to check that only valid connections can be made!

```
connector FluidPort
  replaceable package Medium =
    Modelica_Media.Interfaces.PartialMedium;

  Medium.AbsolutePressure p;
  flow Medium.MassFlowRate m_flow;

  Medium.SpecificEnthalpy h;
  flow Medium.EnthalpyFlowRate H_flow;

  Medium.MassFraction Xi [Medium.nXi]
  flow Medium.MassFlowRate mXi_flow[Medium.nXi]
end FluidPort;
```

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Balance equations for infinitesimal balance volume without mass/energy/momentum storage:

Intensive variables (since ideal mixing):
 $p_1=p_2=p_3$; $h_1=h_2=h_3$;

Mass balance:
 $0 = m_flow1 + m_flow2 + m_flow3$

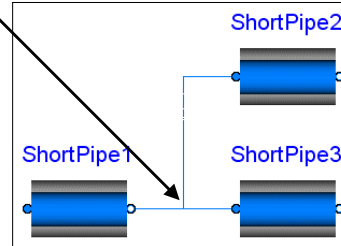
Energy balance:
 $0 = H_flow1 + H_flow2 + H_flow3$

{Momentum balance ($v=v_1=v_2=v_3$; i.e., velocity vectors are parallel)

$$0 = m_flow1 \cdot v_1 + m_flow2 \cdot v_2 + m_flow3 \cdot v_3 \\ = v \cdot (m_flow1 + m_flow2 + m_flow3)$$

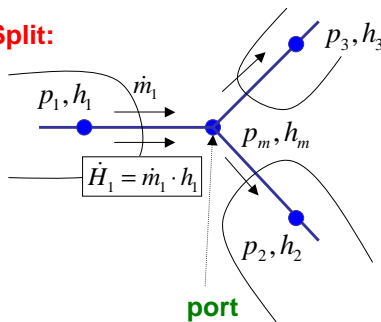
Conclusion:

Connectors must have "**m_flow**" and "**H_flow**" and define them as "**flow**" variable since the default connection equations generate the mass/energy/momentum balance!

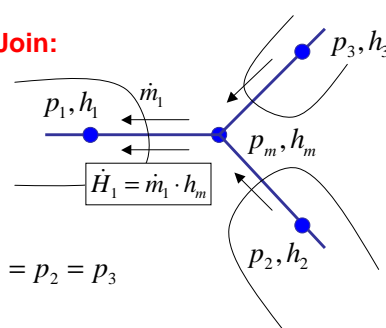


2.1 "Upstream" discretisation + flow direction unknown

Split:



Join:



Variables in connector
port of component 1:

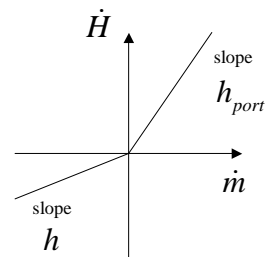
$$p_m, h_m, \dot{m}_1, \dot{H}_1$$

connector FluidPort

```
SI.Pressure           p; // p_m
SI.SpecificEnthalpy   h; // h_m
flow SI.MassFlowRate  m_flow;
flow SI.EnthalpyFlowRate H_flow;
end FluidPort;
```

Energy flow rate and port specific enthalpy

$$\dot{H} = \begin{cases} \dot{m}h_{port} & \dot{m} > 0 \\ \dot{m}h & \text{otherwise} \end{cases}$$

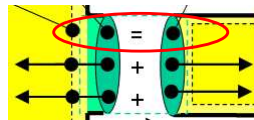


`H_flow=semiLinear(m_flow, h_port, h)`

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Solving semiLinear equations



```
R.H_flow=semiLinear(R.m_flow, R.h_port, R.h)
```

```
S.H_flow=semiLinear(S.m_flow, S.h_port, S.h)
```

```
// Connection equations
```

```
R.e_port = S.e_port
```

```
R.m_flow + S.m_flow = 0
```

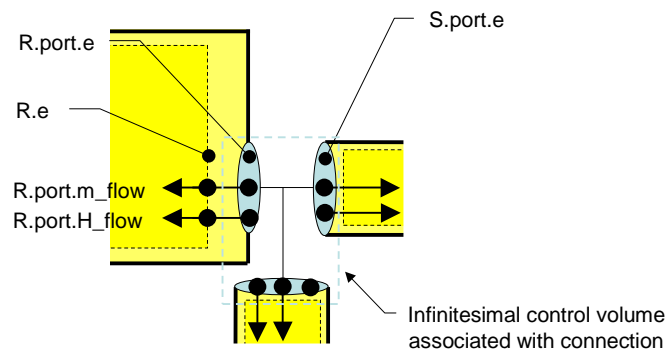
```
R.H_flow + S.H_flow = 0
```

$$e_{port} = \begin{cases} e_S & \dot{m}_R > 0 \\ e_R & \dot{m}_R < 0 \\ \text{undefined} & \dot{m}_R = 0 \end{cases}$$

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Three connected components



- Use of semiLinear() results in systems of equations with many if-statements.
- In many situations, these equations can be solved symbolically

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Splitting flow

- For a *splitting* flow from R to S and T
($R.port.m_flow < 0$, $S.port.m_flow > 0$ and $T.port.m_flow > 0$)
- $$h = -R.port.m_flow * R.h / (S.port.m_flow + T.port.m_flow)$$
- $h = R.h$

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Mixing flow

- For a *mixing* flow from R and T into S
(R.port.m_flow < 0, S.port.m_flow < 0 and T.port.m_flow > 0)
$$h = -(R.port.m_flow \cdot R.h + S.port.m_flow \cdot S.h) / T.port.m_flow$$
- or
$$h = (R.port.m_flow \cdot R.h + S.port.m_flow \cdot S.h) / (R.port.m_flow + S.port.m_flow)$$
- Perfect mixing condition

Mass- momentum- and energy-balances

$$\begin{aligned} \frac{\partial(\rho A)}{\partial t} + \frac{\partial(\rho A v)}{\partial x} &= 0 \\ \frac{\partial(\rho v A)}{\partial t} + \frac{\partial(\rho v^2 A)}{\partial x} &= -A \frac{\partial p}{\partial x} - F_F - A \rho g \frac{\partial z}{\partial x} \\ \frac{\partial(\rho(u + \frac{v^2}{2})A)}{\partial t} + \frac{\partial(\rho v(u + \frac{p}{\rho} + \frac{v^2}{2})A)}{\partial x} &= -A \rho v g \frac{\partial z}{\partial x} + \frac{\partial}{\partial x} (kA \frac{\partial T}{\partial x}) \\ F_F &= \frac{1}{2} \rho v |v| f S \end{aligned}$$

Alternative energy equation

- Subtract v times momentum equation

$$\frac{\partial(\rho u A)}{\partial t} + \frac{\partial(\rho v(u + \frac{p}{\rho})A)}{\partial x} = vA \frac{\partial p}{\partial x} + vF_F + \frac{\partial}{\partial x}(kA \frac{\partial T}{\partial x})$$

Finite volume method

- Integrate equations over small segment
- Introduce appropriate mean values

$$\int_a^b \frac{\partial(\rho A)}{\partial t} dx + \rho A v|_{x=b} - \rho A v|_{x=a} = 0$$

$$\frac{dm}{dt} = \dot{m}_a + \dot{m}_b$$

$$m = \rho_m A_m L$$

Index reduction and state selection

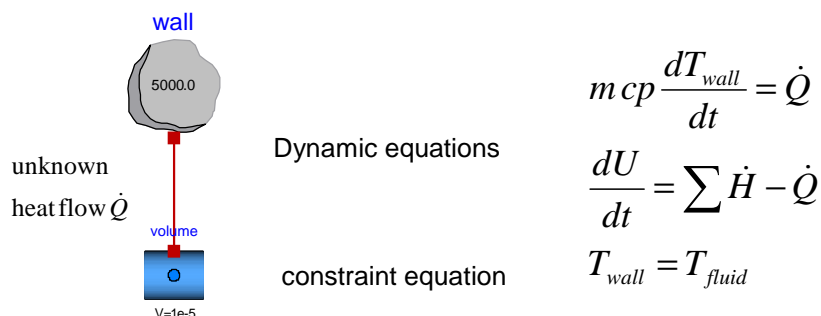
- Component oriented modeling needs to have maximum number of differential equations in components
- Constraints are introduced through connections or simplifying assumptions (e.g. density=constant)
- Tool needs to figure out how many states are independent
- Common situation in mechanics, not common in fluid in thermodynamic modeling
- Very useful also in thermo-fluid systems
 - Unify models for compressible/incompressible fluids
 - High efficiency of models independent from input variables of property computation

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Index reduction and state selection

- Example: connect an incompressible medium to a metal body under the assumption of infinite heat conduction (Exercise 3-1).
- Realistic real-world example: model of slow dynamics in risers and drum in a drum boiler (justified simplification used in practice)



→ unknown heat flow keeps temperatures equal

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Index reduction and state selection

Differentiate the constraint equation: $\frac{dT_{wall}}{dt} = \frac{dT_{fluid}}{dt}$

$$U = u m$$

Definition of u for simple
Incompressible fluid

$$h(T, p) = h(T) + \frac{p - p_0}{\rho}$$

$$u(T) = h(T) - \frac{p_0}{\rho}$$

Expand fluid definition

$$\frac{dh(T)}{dT} \frac{dT_{fluid}}{dt} - \frac{p_0}{\rho} = cp(T) \frac{dT_{fluid}}{dt} - \frac{p_0}{\rho}$$

Re-write energy
balance with T as state

$$\frac{dU}{dt} = m \left(cp(T) \frac{dT_{fluid}}{dt} - \frac{p_0}{\rho} \right)$$

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Index reduction and state selection

Using $\frac{dT_{wall}}{dt} = \frac{dT_{fluid}}{dt}$

Some rearranging yields:

$$(m_{wall} cp_{wall} + m_{fluid} cp_{fluid}) \frac{dT}{dt} = \sum \dot{H} + \frac{p_0}{\rho}$$

→ Combined energy balance for metal and fluid

$$\dot{Q} = \sum \dot{H} - m_{fluid} cp_{fluid} \frac{dT}{dt} - \frac{p_0}{\rho}$$

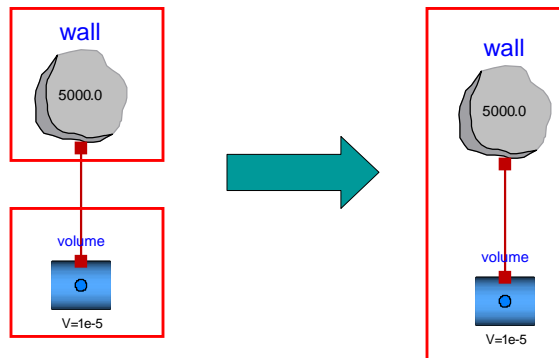
Unknown flow Q computed from temperature derivative

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Index reduction and state selection

- Because temperatures are forced to be equal, we get to one lumped energy balance for volume and wall instead of 2
- Side effect: the independent state variable is now T , not U any more
- Heavily used in Modelica.Media and Fluid to get efficient dynamic models



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Index reduction and state selection

- Many other situations:
 - 2 volumes are connected
 - Tanks have equal pressure at bottom
 - Change of independent variables, though not originally a high index problem, uses the same mechanism (see also slide 11)
- Big advantage in most cases:
 - Independence of fluid and plant model
 - Highly efficient
 - More versatile models
- Potential drawbacks
 - All functions have to be symbolically differentiable
 - Complex manipulations
 - If manipulations not right, model can have unnecessary non-linear equations – potentially slow simulation
 - See exercises

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Regularizing Numerical Expressions

- Robustness: reliable solutions wanted
in the complete operating range!
- Difference between static and dynamic models
 - Dynamic models are used in much wider operating range
- Empirical correlations not adapted to robust numerical solutions (only locally valid)
- Non-linear equation systems or functions
- Singularities
- Handling of discontinuities

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Singularities

- *functions with singular points or singular derivatives should be regularized.*
 - Empirical functions are often used outside their region of validity to simplify models.
 - Most common problem: infinite derivative, causing *inflection*.

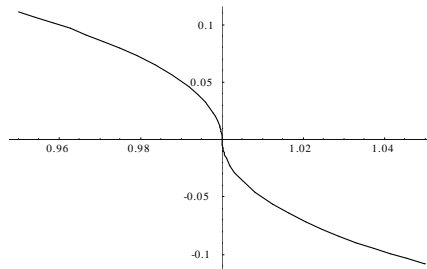
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Root function Example

- Textbook form of turbulent flow resistance

$$\dot{m} - k \operatorname{sign}(\Delta p) \sqrt{\rho \operatorname{abs}(\Delta p)} = 0$$



→ Infinite derivative at origin

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Singularities

- Infinite derivative causes trouble with Newton-Raphson type solvers:
Solutions are obtained from following iteration:

$$z^{j+1} = z^j + \frac{f(z^j)}{\frac{\partial f(z^j)}{\partial z^j}} \approx \Delta z^j + \frac{f(z^j)}{\frac{\Delta f(z^j)}{\Delta z^j}}$$

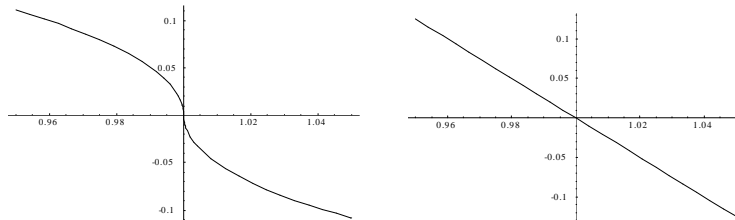
For $\frac{\partial f(z^j)}{\partial z^j} \rightarrow \infty$, the step size goes to 0.

This is called *inflection problem*

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Root function remedy



- Replace singular part with local, non-singular substitute
 - result should be **qualitatively** correct
 - the overall function should be C^1 continuous
 - No singular derivatives should remain!

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Log-mean Temperature

Log-mean Temperature
$$\Delta T_{lm} = \frac{\Delta T_1 - \Delta T_2}{\ln(\Delta T_1 / \Delta T_2)}$$

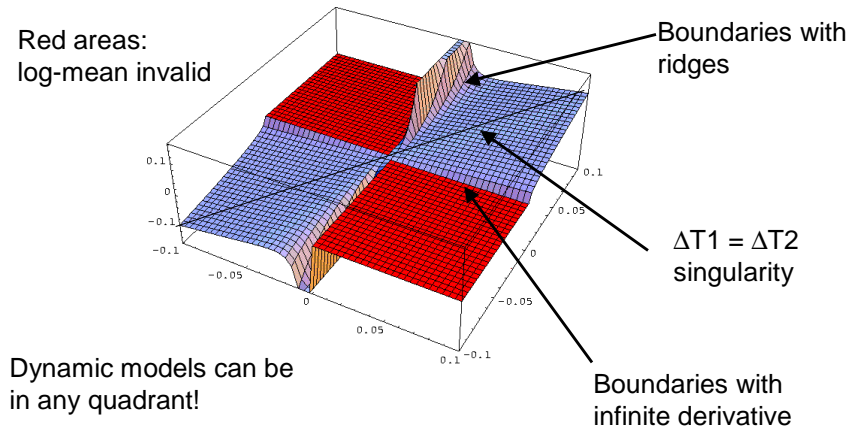
- Invalid for all $\text{sign}(\Delta T_1) \times \text{sign}(\Delta T_2) < 0$
- numerical singularities for

$$\Delta T_1 = \Delta T_2, \Delta T_1 \rightarrow 0, \Delta T_2 \rightarrow 0$$

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Log-mean Temperature Difference



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Scaling

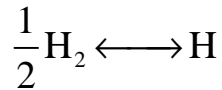
- *Scale extremely nonlinear functions to improve numerical behavior.*
- *Use min, max and nominal attributes so that the solver can scale.*

```
Real myVar(min = 1.0e-10, max =  
          1.0, nominal = 1e-3)
```

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Scaling: chemical equilibrium of dissociation of Hydrogen



$$x_{\text{H}} = \frac{\sqrt{x_{\text{H}_2}}}{\sqrt{p}} \exp(k)$$

$$k = 2.6727 - \frac{11.247}{T} - 0.0743T + 0.4317 \log(T) + 0.002407T^2$$

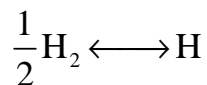
Take the log of the equation and variables:

$$\log(x_{\text{H}}) = \frac{1}{2} (\log(x_{\text{H}_2}) - \log(p)) + k$$

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Scaling: chemical equilibrium of dissociation of Hydrogen



Effect of log at 280K: ratio of $\frac{x_{\text{H}_2}}{x_{\text{H}}} = 1.3 \times 10^{75}$

ratio of $\frac{\log(x_{\text{H}_2})}{\log(x_{\text{H}})} = 172$

Experiences tested with several non-linear solvers:

22 simultaneous, similar equilibrium reactions

exp form: solvable if $T > 1200 \text{ K}$

log form: solvable if $T > 250 \text{ K}$

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Smoothing

- *Piece-wise and discontinuous function approximations which should be continuous for physical reasons shall be smoothened.*

Smoothing example: Heat transfer equations

- Convective heat transfer with flow perpendicular to a cylinder. Two Nusselt numbers for laminar and turbulent flow

$$Nu_{lam} = 0.664 Re^{1/2} Pr^{1/3}$$

$$Nu_{turb} = \frac{0.037 Re^{0.8} Pr}{1 + 2.443 Re^{-0.1} (Pr^{2/3} - 1)}$$

For $Re < 10$ we have to take care of the root function singularity as well!

- Combine as:

$$Nu = 0.3 + \sqrt{Nu_{lam}^2 + Nu_{turb}^2}$$

$$10 < Re < 10^7, \quad 0.6 < Pr < 1000$$

Summary

Framework for object-oriented fluid modeling

- Media and component models decoupled
- Reversing flows
- Ideal models for mixing and separation
- Index reduction for
 - transformations of media equations
 - handling of incompressible media
 - Index reduction for combining volumes
- Some issues in numerical regularization

Exercises

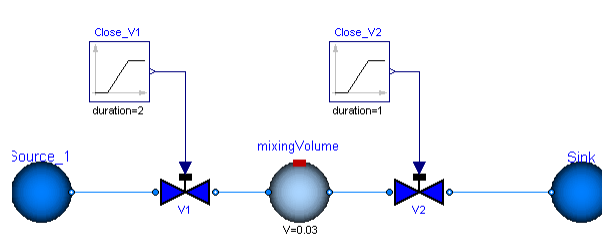
1. Build up small model and run with different media
 - Look at state selection
 - Check non-linear equation systems
 - Test different options for incompressible media
2. Reversing flow and singularity treatment
 - Build up model with potential backflow
 - Test with regularized and Text-book version of pressure drop
3. Index reduction and efficient state selection with fluid models, 3 different examples
 1. Index reduction through temperature constraint of solid body and fluid volume (used in power plant modeling)
 2. Index reduction between 2 well mixed volumes
 3. Index reduction between tanks without a pressure drop in between.
4. Non-linear equation systems in networks of simple pressure losses
5. Reversing and 0-flow with liquid valve models

Exercises

- All exercises are explained step by step in the info-layer in Dymola of the corresponding exercise models.
- All models are prepared and can be run directly, the the exercises modify and explore the models

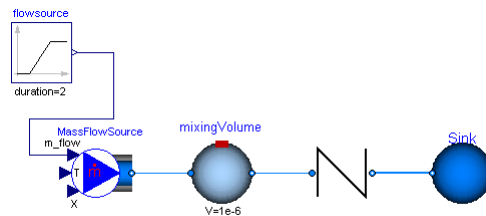
Exercise 1

- Using different Media with the same plant and test of 0-flow conditions



Exercise 2

- Effect of Square root singularity

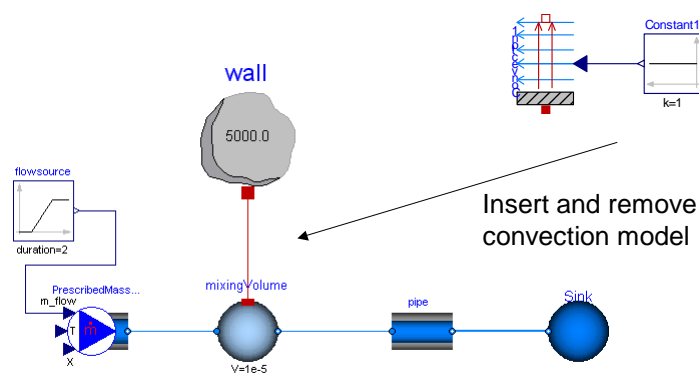


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Exercise 3-1

- Index reduction between solid body and fluid volume

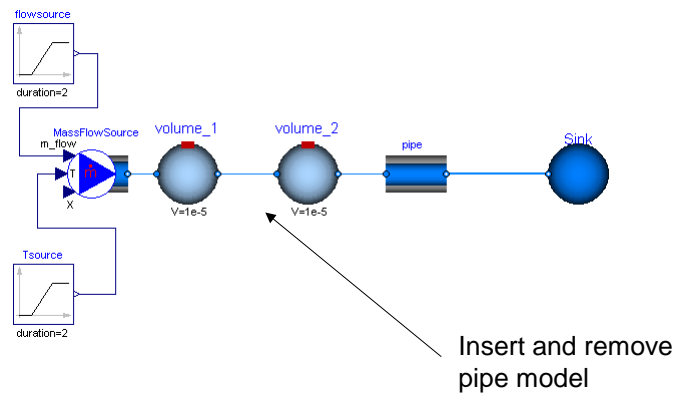


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Exercise 3-2

- Index reduction between 2 well mixed fluid volumes

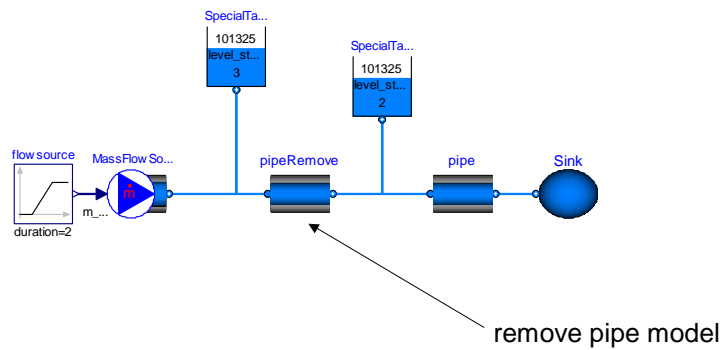


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Exercise 3-3

- Index reduction of one state only between 2 tank models

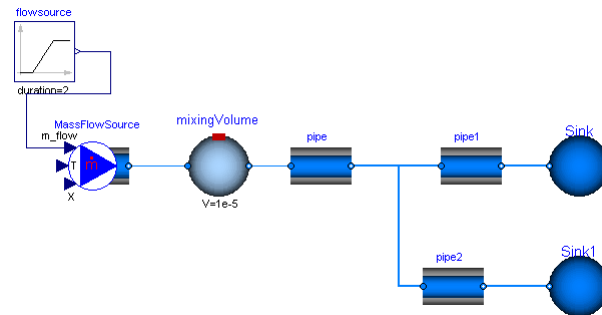


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Exercise 4

- Non-linear equations in pipe network models

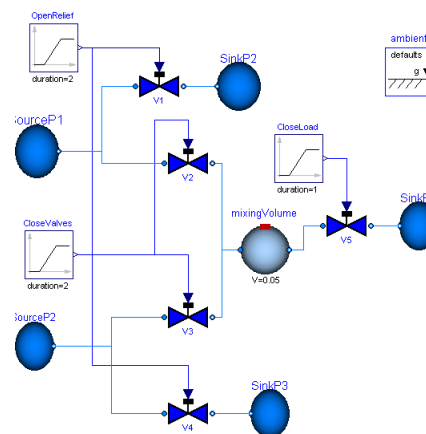


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Exercise 5

- Reversing flow for a liquid valve



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