

Abstract

Inclusion Dynamics proposes that the foundations of physics arise from a single axiom: *information cannot vanish and cannot be infinitely sharp*.

From this principle, a conserved information density — the *inclusion field* — gives rise to the familiar equations of modern physics as different limits of one variational structure.

By adding a finite Fisher-information stiffness to the action of this field, we recover:

- the **Schrödinger equation** as the dynamics of information flow;
- **Einstein's equation** as the thermodynamic closure of inclusion entropy across local horizons;
- the **Navier–Stokes–Korteweg system** describing macroscopic fluids and turbulence with built-in dispersive regularization.

A discrete microscopic scale a sets both the quantum of action ($\hbar = m \sqrt{\chi} a$) and the strength of gravity ($1/G \propto 1/a^2$), unifying constants that normally appear unrelated.

Gauge fields and spin emerge naturally as symmetries of information redundancy.

At cosmological scales, the same framework predicts correlated variations in spectral lines, gravitational-wave amplitudes, and dark-energy drift — a falsifiable “triangle” linking all three observations.

Inclusion Dynamics therefore reframes physics as the geometry of finite information and resolves the apparent fine-tuning of constants by deriving them from a single microscopic consistency condition.

1 Introduction

Modern physics is built from several extraordinary but seemingly independent frameworks.

Quantum mechanics describes microscopic behavior through complex amplitudes and probabilities.

General relativity explains gravity as the curvature of spacetime produced by energy and momentum.

Fluid mechanics governs collective motion at large scales.

Each theory is successful in its domain, yet their mathematical languages remain fundamentally distinct.

No single principle connects them.

The purpose of this work is to show that they all arise from one universal statement about *information*.

Everything that exists can be represented as an information density — a measure of how much “being” occupies a region of reality.

This density can flow, interact, and evolve, but it cannot disappear entirely and it cannot be compressed into infinite sharpness.

That simple rule already contains the seeds of quantum behavior, gravitational curvature, and thermodynamic irreversibility.

I call this framework **Inclusion Dynamics** because every part of reality is included in a continuous field of existence whose local density is conserved.

When the field varies smoothly, it behaves like a classical fluid.

When its variations are restricted by finite information stiffness, it reproduces the probabilistic structure of quantum mechanics.

And when it is viewed thermodynamically, the curvature of its information geometry becomes the curvature of spacetime itself.

1.1 Motivation

The fragmentation of modern theory into separate regimes is partly historical.

Quantum mechanics was built from the postulate of a universal constant \hbar ; relativity was built from the invariance of c and the equivalence principle.

Both constants appear inserted by hand, with no deeper explanation.

Similarly, the fine-tuning of cosmological parameters — the balance that allows matter, structure, and life — has no fundamental reason within existing frameworks.

Inclusion Dynamics aims to supply that reason by deriving all constants and laws from one informational principle.

1.2 Core axiom

The axiom is minimal:

Inclusion Axiom — Information density ρ is conserved and cannot be infinitely sharp.

Mathematically this introduces two requirements:

1. **Continuity:** $\partial\rho/\partial t + \nabla \cdot (\rho \mathbf{v}) = 0$.
2. **Finite roughness:** There is an energetic cost for large spatial gradients, measured by the *Fisher information*
$$I[\rho] = \int |\nabla \sqrt{\rho}|^2 d^3x.$$

Together these constraints form the skeleton of every dynamical law that follows.

1.3 What this paper does

Starting from the inclusion axiom, we construct a single action functional containing both conservation and Fisher stiffness.

By varying that action we obtain:

- The **Schrödinger equation** as the canonical form of inclusion dynamics at microscopic scales.
- **Einstein's field equations** as the thermodynamic equation of state of inclusion entropy near local horizons.
- The **Navier–Stokes–Korteweg** equations governing macroscopic flow and turbulence, where the Fisher term appears as a dispersive stress that regularizes shocks.
- A quantitative relationship linking **Planck's constant** (\hbar) and the **gravitational constant** (G) to the same microscopic grain size a of information.
- Natural emergence of **gauge fields** and **spin** from local redundancies of phase and frame.
- Observable predictions in cosmology and turbulence that can falsify the theory.

1.4 Relation to earlier work

This approach connects to several historical ideas while unifying them into one consistent structure:

- **Entropic and thermodynamic gravity** — Jacobson (1995) and Padmanabhan (2010) showed that Einstein's equation follows from horizon thermodynamics.
Inclusion Dynamics reproduces this derivation while identifying the entropy as Fisher information of the inclusion field.
- **Quantum Fisher information** — Frieden, Reginatto, and others derived wave mechanics from information optimization.
Here that principle is embedded directly into spacetime dynamics.
- **Hydrodynamic and quantum-fluid analogies** — Madelung's and Bohm's formulations of quantum mechanics hint that quantum behavior is fluid-like.
Inclusion Dynamics formalizes this insight, deriving the same stress term that appears in Korteweg or Gross–Pitaevskii fluids.

- **Information geometry** — The Fisher metric defines a curvature on probability space. In this theory that curvature *is* spacetime curvature at macroscopic scale.

1.5 Outline of the paper

Section 2 defines the axioms and constructs the master action that governs inclusion fields.

Section 3 derives quantum mechanics from finite information and explains the physical meaning of Planck's constant.

Section 4 shows how gravitational dynamics emerge from inclusion entropy via the Clausius relation.

Section 5 establishes the microscopic origin of both \hbar and G in a common grain size.

Section 6 describes the fluid and turbulent regimes and their testable signatures.

Section 7 develops the role of gauge and spin symmetries.

Section 8 presents cosmological evolution and falsifiable correlations between observables.

Section 9 reframes fine-tuning as a structural self-consistency condition.

Section 10 concludes with discussion and future directions.

Appendices provide full derivations and supporting calculations.

2 Axioms and Master Action

The Inclusion Dynamics framework begins with a single substance — the **inclusion field**, described by two variables:

- **$\rho(\mathbf{x}, \mathbf{t})$** : the local inclusion density, representing how much “being” or information occupies a region.
- **$\mathbf{S}(\mathbf{x}, \mathbf{t})$** : a phase or potential that generates the flow of inclusion through space and time.

Together, these variables define the informational state of reality at every point.

2.1 Axiom 1 — Conservation of Inclusion

The first axiom states that inclusion (information) cannot vanish or be created from nothing. It can only flow or redistribute, which leads to the standard **continuity equation**:

$$(1) \quad \partial \rho / \partial t + \nabla \cdot (\rho \mathbf{v}) = 0$$

Here $\mathbf{v} = \nabla S / m$ represents the mean flow velocity of inclusion, and m is an inertial parameter that connects gradients of S to physical motion.

Equation (1) ensures that the total amount of inclusion $\int \rho \, d^3x$ remains constant over time. It is the same mathematical statement that underlies probability conservation in quantum mechanics and mass conservation in fluid dynamics.

2.2 Axiom 2 — Finite Roughness

The second axiom expresses the finiteness of information density.

Reality resists being infinitely “jagged” — there is an energetic cost to compressing inclusion into sharp spikes or discontinuities.

This penalty is quantified by the **Fisher information functional**:

$$(2) \quad I[\rho] = \int (|\nabla \rho|^2 / \rho) \, d^3x = 4 \int |\nabla \sqrt{\rho}|^2 \, d^3x$$

This is the only local, positive, and scale-invariant measure of informational roughness.

It ensures that inclusion fields remain smooth at small scales, preventing singularities and providing a natural ultraviolet cutoff.

2.3 Building the Action

The simplest action that incorporates both conservation and finite roughness combines three parts:

1. A kinetic term representing the classical drift of inclusion through the potential S .
2. A potential energy term $V(\rho, x, t)$ representing external influences.
3. A Fisher-information penalty weighted by a stiffness coefficient proportional to $\hbar^2 / (8m)$.

The full **action functional** is therefore

(3)

$$A[\rho, S] = \int \rho \left[\partial S / \partial t + |\nabla S|^2 / (2m) + V \right] d^3x \, dt + (\hbar^2 / 8m) \int (|\nabla \rho|^2 / \rho) \, d^3x \, dt$$

The first bracket is the standard Hamilton–Jacobi term describing motion under potential V .

The second integral adds the finite-information correction.

2.4 Variation of the Action

We now obtain the dynamical equations by extremizing A with respect to S and ρ .

1. Variation with respect to S:

$$\delta A / \delta S = 0 \rightarrow \partial \rho / \partial t + \nabla \cdot (\rho \nabla S / m) = 0$$

which is exactly the continuity equation (1).

2. Variation with respect to ρ :

$$\delta A / \delta \rho = 0 \rightarrow \partial S / \partial t + |\nabla S|^2 / (2m) + V - (\hbar^2 / 2m) (\nabla^2 \sqrt{\rho} / \sqrt{\rho}) = 0$$

This second equation is a modified Hamilton–Jacobi equation that includes an additional term, often called the **quantum potential**:

$$(4) \quad Q = - (\hbar^2 / 2m) (\nabla^2 \sqrt{\rho} / \sqrt{\rho})$$

The presence of Q distinguishes inclusion dynamics from classical mechanics.

It encodes the finite-information correction to classical motion — the resistance of the inclusion field to infinite localization.

2.5 Physical interpretation

Equations (1) and (4) together describe the exact motion of inclusion density under a potential V.

They contain no quantum postulates or probabilistic assumptions — only the conservation of finite information.

However, when expressed in a single complex field variable, these equations transform into the standard form of quantum mechanics.

2.6 The canonical substitution

Define the complex inclusion wavefunction:

$$(5) \quad \psi(x, t) = \sqrt{\rho(x, t)} \cdot \exp(i S(x, t) / \hbar)$$

Substituting this into equations (1) and (4) yields:

$$(6) \quad i \hbar \partial \psi / \partial t = - (\hbar^2 / 2m) \nabla^2 \psi + V \psi$$

which is precisely the **Schrödinger equation**.

This result shows that quantum mechanics is not a separate postulate but an inevitable outcome of inclusion conservation and finite information stiffness.

The “wavefunction” ψ simply encodes the inclusion density ρ and its flow potential S in a compact complex form.

2.7 Summary of this section

- The two axioms — conservation and finite roughness — completely determine the form of physical dynamics.
- The resulting variational principle naturally yields quantum mechanics as its canonical limit.
- The Fisher information acts as the universal regulator that prevents infinite compression and defines the scale of \hbar .
- This same formalism will later reproduce gravity, fluids, and thermodynamics when viewed through different coarse-graining regimes.

3 Quantum Mechanics from Finite Information

The derivation in the previous section shows that once inclusion density is conserved and resists infinite compression, the mathematical structure of quantum mechanics appears automatically.

This section interprets that result and explores its consequences.

3.1 From inclusion flow to wave dynamics

The continuity equation ($\partial\rho/\partial t + \nabla \cdot (\rho \mathbf{v}) = 0$) describes how inclusion moves through space, just like a fluid.

The Hamilton–Jacobi equation with the additional quantum potential,

$$\partial S/\partial t + |\nabla S|^2 / (2m) + V - (\hbar^2 / 2m) (\nabla^2 \sqrt{\rho} / \sqrt{\rho}) = 0,$$

describes how the potential S evolves in time.

Together, these two real equations fully determine the dynamics of the pair (ρ, S) .

The substitution $\psi = \sqrt{\rho} \exp(iS/\hbar)$ combines these into a single complex equation:

$$i \hbar \partial \psi / \partial t = - (\hbar^2 / 2m) \nabla^2 \psi + V \psi.$$

This is not an arbitrary rewriting — it is the unique way to combine ρ and S such that their evolution remains self-consistent under information conservation.

Inclusion Dynamics therefore provides a deterministic foundation for the origin of the wavefunction.

3.2 The meaning of Planck's constant

In this framework, Planck's constant \hbar is not a separate postulate or mysterious quantum of nature.

It is the direct measure of **information granularity** — the stiffness of the inclusion field.

At the microscopic level, there exists a minimal length a that defines the smallest distinguishable region of information.

From the discrete-to-continuum analysis (derived later in Section 5), we obtain

$$\hbar = m \sqrt{\chi} a,$$

where:

- m is the inertial scale relating flow velocity to momentum,
- χ is a geometric factor depending on lattice or network structure, and
- a is the grain size of inclusion.

This equation says that \hbar is proportional to the product of mass scale and information grain size. Quantum effects arise because inclusion cannot vary more sharply than this microscopic limit.

3.3 The quantum potential as informational pressure

The extra term

$$Q = - (\hbar^2 / 2m) (\nabla^2 \sqrt{\rho} / \sqrt{\rho})$$

can be interpreted as an **information pressure** or **entropic force**.

Where ρ changes rapidly, $\nabla^2 \sqrt{\rho}$ becomes large, and Q introduces a restoring effect that smooths the distribution.

This behavior is mathematically identical to the dispersive pressure that appears in Korteweg or Gross–Pitaevskii fluids, but here it arises from information geometry rather than molecular interactions.

The quantum potential therefore represents a universal tendency of reality to avoid infinite information density.

At large scales (slow variation of ρ), Q becomes negligible and the system obeys classical mechanics.

At small scales, Q dominates and produces quantum interference and wave–particle duality.

3.4 Information–theoretic interpretation

The Fisher information term

$$I[\rho] = \int |\nabla \sqrt{\rho}|^2 d^3x$$

is proportional to the curvature of the probability manifold defined by ρ .

In information geometry, this curvature measures how distinguishable nearby states are.

High curvature corresponds to high precision or “sharpness” of information, which costs energy.

Inclusion Dynamics simply includes that cost in the fundamental action.

Thus, the energy of a system is directly related to the distinguishability of its informational configuration.

This viewpoint clarifies several quantum phenomena:

- **Uncertainty principle:**
Limiting the sharpness of ρ automatically produces a lower bound on the product of position and momentum uncertainties.
The inequality $\Delta x \cdot \Delta p \geq \hbar/2$ is an expression of finite Fisher curvature.
 - **Wave–particle duality:**
The wavefunction encodes both density and flow.
Regions where ρ is high correspond to probable particle positions, while the phase S/\hbar controls interference through coherent flow.
 - **Superposition and interference:**
Because ψ combines both ρ and S into one complex field, linear combinations of ψ correspond to overlapping information flows.
Interference patterns arise from constructive or destructive addition of inclusion flow potentials.
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3.5 Quantum measurement as information equilibration

Measurement in this framework is not collapse but **information equilibration**.

When an inclusion system interacts with an environment or detector, their information densities

combine.

The composite system evolves toward a new macrostate that maximizes entropy under the joint constraints — the classical limit of the inclusion field.

This process naturally reproduces decoherence: the apparent collapse of a superposition corresponds to the system's inclusion density distributing itself over accessible environmental configurations.

No additional postulate or observer mechanism is required.

3.6 Classical limit

In regions where the Fisher stiffness is negligible — equivalently, when $|\nabla \rho| / \rho$ is small compared to $1/a$ —

the quantum potential Q becomes insignificant.

Equation (4) then reduces to the standard Hamilton–Jacobi equation of classical mechanics:

$$\partial S / \partial t + |\nabla S|^2 / (2m) + V = 0.$$

This limit confirms that classical physics is just the smooth, low-curvature regime of finite information dynamics.

Quantum behavior appears when the information curvature cannot be ignored.

3.7 Summary of this section

- The Schrödinger equation emerges directly from inclusion conservation and finite Fisher stiffness.
- The quantum potential Q represents the energetic cost of finite information curvature.
- Planck's constant \hbar quantifies the minimal granularity of inclusion and connects microscopic geometry to macroscopic observables.
- Measurement and decoherence are forms of information exchange leading to equilibrium.
- Classical mechanics is the limit where the Fisher term vanishes.

4 Gravity from Inclusion Entropy

If inclusion dynamics is the foundation of all physical law, then gravity must also arise from the same informational principle.

In this section, we show that spacetime curvature is the large-scale geometry of inclusion information and that Einstein's equations emerge from the Clausius relation between heat, entropy, and energy flow.

This builds on earlier insights by Jacobson (1995) and Padmanabhan (2010), but now the entropy and temperature originate from the microphysics of the inclusion field.

4.1 Local horizon thermodynamics

Consider a small region of spacetime around an arbitrary event.

In that infinitesimal neighborhood, we can always construct a **local Rindler horizon** — the surface that separates accessible and inaccessible regions for an observer undergoing uniform acceleration.

Let:

- k^a denote the null vector tangent to the horizon generators,
- κ be the surface gravity associated with the local acceleration, and
- χ^a be the approximate boost Killing vector that generates local time translations.

An observer with acceleration κ experiences a temperature known as the **Unruh temperature**:

$$(7) \quad T = (\hbar \kappa) / (2\pi)$$

Thus, even a vacuum possesses an effective thermal temperature when seen by an accelerated observer.

If the inclusion field carries an entropy per unit area $\eta(\rho_I)$, then an infinitesimal patch of horizon with area A has entropy

$$(8) \quad dS_H = \eta(\rho_I) \cdot dA$$

where ρ_I is the local inclusion density evaluated at the horizon.

4.2 The Clausius relation

The Clausius relation connects energy flow (heat) across the horizon to the change in entropy:

$$(9) \quad \delta Q = T \delta S_H$$

Here δQ is the energy flux across the horizon patch, measured by the local boost Killing vector:

$$(10) \quad \delta Q = \int T_{\{\mu\nu\}}^{\{\text{matter}\}} \chi^u d\Sigma^v$$

→ On the horizon, $\chi^u \approx \kappa \lambda k^u$, so

$$\delta Q \approx \int T_{\{\mu\nu\}}^{\{\text{matter}\}} k^u k^v \lambda d\lambda dA_0$$

where λ is an affine parameter along the null generator k^u , and $T_{\{\mu\nu\}}$ is the matter stress-energy tensor.

At the same time, the area of the horizon changes due to spacetime curvature, as given by the **Raychaudhuri equation** for null geodesic congruences:

$$(11) \quad d\theta/d\lambda = - (1/2) \theta^2 - R_{\{\mu\nu\}} k^u k^v$$

Near equilibrium, shear and expansion vanish, so approximately

$$d\theta/d\lambda \approx - R_{\{\mu\nu\}} k^u k^v$$

Integrating this gives the fractional change in area:

$$(12) \quad \delta A \approx - \int R_{\{\mu\nu\}} k^u k^v \lambda d\lambda dA_0$$

and thus the entropy change

$$(13) \quad \delta S_H = \eta \delta A = - \eta \int R_{\{\mu\nu\}} k^u k^v \lambda d\lambda dA_0.$$

4.3 Equating flux and entropy change

Combining equations (9), (10), and (13) using the Unruh temperature (7), we find:

$$(\hbar \kappa / 2\pi) \eta R_{\{\mu\nu\}} k^u k^v = T_{\{\mu\nu\}}^{\{\text{matter}\}} k^u k^v.$$

Because this relation holds for all null vectors k^u at any spacetime point, it must hold tensorially (up to a cosmological constant term).

Therefore,

$$(14) \quad (\hbar \kappa / 2\pi) \eta (R_{\{\mu\nu\}} - \frac{1}{2} R g_{\{\mu\nu\}}) + \Lambda g_{\{\mu\nu\}} = T_{\{\mu\nu\}}^{\{\text{matter}\}}.$$

Identifying the proportionality constant gives the **Einstein field equations**:

$$(15) \quad G_{\{\mu\nu\}} + \Lambda g_{\{\mu\nu\}} = 8\pi G T_{\{\mu\nu\}}^{\{\text{matter}\}}.$$

The Newton constant G is determined by the combination of microscopic parameters that appear in η and κ .

4.4 Determining the entropy density

Inclusion Dynamics provides a microscopic expression for the entropy density η .

At the informational level, the inclusion entropy is given by the integral

$$S = \int \sqrt{-g} [s(\rho_I) - (\kappa_F / 2) (\nabla \rho_I)^2 + \dots] d^4x,$$

where the first term $s(\rho_I)$ is a local entropy density and the second term is a gradient (Fisher) correction.

The horizon contribution arises from the area term in this functional:

$$(16) \quad S_H = \int \sqrt{\sigma} [\eta_0 + \eta_1 \delta \rho_I + \eta_2 (\nabla \rho_I)^2 + \dots] dA,$$

where σ is the determinant of the induced metric on the horizon.

To leading order, the coefficient η_0 corresponds to the Bekenstein–Hawking value:

$$(17) \quad \eta_0 = 1 / (4 \hbar G).$$

When inclusion density is locally homogeneous on horizon scales, η becomes effectively constant and reproduces standard general relativity exactly.

4.5 Inclusion corrections to gravity

If ρ_I varies across the horizon, η acquires small spatial dependence, leading to non-equilibrium corrections:

$$(18) \quad G_{\{\mu\nu\}} + \Lambda g_{\{\mu\nu\}} = 8\pi G [T_{\{\mu\nu\}}^{\{\text{matter}\}} + T_{\{\mu\nu\}}^{\{\text{l, diss}\}}].$$

The additional term $T_{\{\mu\nu\}}^{\{\text{l, diss}\}}$ arises from the gradient and non-equilibrium parts of the inclusion entropy.

It can be interpreted as an effective stress-energy tensor describing small dissipative or viscous effects of inclusion flow.

These corrections are tiny in equilibrium conditions (recovering standard GR) but may produce detectable effects in cosmological or high-curvature regimes.

They provide a natural mechanism for dark-energy drift and late-time deviations from $w = -1$.

4.6 Geometric interpretation

Einstein's equations now have a clear informational meaning:

- The **geometry** of spacetime ($R_{\{\mu\nu\}}$) describes how inclusion information curves in response to energy and matter.
- The **stress-energy tensor** represents the flux of inclusion through spacetime.
- The **entropy–area relation** ensures that the total information on causal horizons remains finite and consistent with the inclusion axiom.

In other words, gravity is not a fundamental force but the emergent thermodynamic geometry of finite information.

4.7 Summary of this section

1. The Unruh temperature ($T = \hbar \kappa / 2\pi$) connects acceleration to inclusion microphysics.
2. The Clausius relation $\delta Q = T \delta S_H$ reproduces Einstein's equations when the entropy per area is finite and proportional to $1 / (4 \hbar G)$.
3. The entropy density η originates from the inclusion field's Fisher information.
4. Small gradients of inclusion generate higher-order corrections, offering a testable path beyond general relativity.
5. Spacetime curvature is literally the curvature of the inclusion-information manifold.

5 Micro–Macro Link: Common Origin of \hbar and G

Having derived both quantum and gravitational dynamics from the same informational framework, we now connect them quantitatively.

Inclusion Dynamics predicts that the fundamental constants of nature—Planck's constant \hbar and Newton's constant G —arise from a single microscopic length scale a that characterizes the granularity of information.

5.1 Microscopic model of inclusion stiffness

At the smallest level, inclusion can be modeled as a network or lattice of nodes separated by distance a , each carrying a scalar amplitude ψ that represents $\sqrt{\rho}$.

The simplest measure of roughness is a quadratic energy cost between neighboring nodes:

$$(19) \quad E_{\text{a}} = (\kappa_0 / 2) \sum_{\langle i, j \rangle} (\psi_i - \psi_j)^2,$$

where the sum runs over neighboring pairs and κ_0 is the spring-like stiffness of each connection.

Expanding ψ in a Taylor series, $\psi_j = \psi(\mathbf{x} + a \hat{\mathbf{e}}_i) \approx \psi + a \hat{\mathbf{e}}_i \cdot \nabla \psi + (1/2) a^2 \hat{\mathbf{e}}_i \hat{\mathbf{e}}_i \partial_i \partial_i \psi$, and summing over the coordination number z gives the continuum limit:

$$(20) \quad E_{\text{a}} \approx (1/2) \kappa_0 z a^2 \int |\nabla \psi|^2 d^3x.$$

Comparing this with the Fisher-information energy

$$E_{\text{F}} = (1/2) \kappa \int |\nabla \psi|^2 d^3x,$$

we identify the continuum coefficient

$$(21) \quad \kappa = \chi a^2, \quad \text{where } \chi = (1/2) z \kappa_0 / m^2 \text{ is a dimensionless geometry factor.}$$

5.2 Matching the quantum pressure

In the Madelung equations of quantum mechanics, the quantum potential

$$Q = - (\hbar^2 / 2m) (\nabla^2 \sqrt{\rho} / \sqrt{\rho})$$

acts as a Fisher-type pressure with effective stiffness $\kappa = \hbar^2 / m^2$.

Equating this to the microscopic coefficient (21) gives the relation

$$(22) \quad \hbar = m \sqrt{\chi} a.$$

This identifies Planck's constant as the product of the inertial mass scale m , the geometric factor $\sqrt{\chi}$, and the fundamental inclusion grain size a .

Quantum mechanics therefore arises whenever the granularity a is finite; taking $a \rightarrow 0$ recovers the classical continuum.

5.3 Induced gravity from the same microstructure

The same microscopic network also generates an area–entropy term when its degrees of freedom are traced over.

Using the replica or heat-kernel method, the entanglement entropy per unit horizon area is approximately

$$(23) \quad \sigma_I = (\alpha_I / 48\pi) \Lambda^2 + \dots, \quad \text{with } \Lambda \approx \pi / a.$$

Here α_I counts the effective number of inclusion modes.

This area term renormalizes the Einstein–Hilbert action, giving an effective gravitational coupling

$$(24) \quad 1 / G_{\text{ren}} = 1 / G_{\text{bare}} + c_I \Lambda^2 = 1 / G_{\text{bare}} + (\alpha_I \pi / 12) (1 / a^2).$$

If the bare term is small compared to the induced contribution (the “induced gravity” limit), the observed Newton constant is controlled directly by the inclusion grain size:

$$(25) \quad G \approx 12 a^2 / (\alpha_I \pi).$$

5.4 Eliminating a and linking \hbar and G

Eliminating a between equations (22) and (24) gives a direct relationship between the two constants:

$$(26) \quad 1 / G = 1 / G_{\text{bare}} + (\alpha_I \pi / 12 \chi) (m^2 / \hbar^2).$$

If G_{bare} is negligible, then

$$(27) \quad G \approx (12 \chi / \alpha_I \pi) (\hbar^2 / m^2).$$

Thus, once the micro-mass m and lattice geometry χ are chosen, both \hbar and G follow automatically.

They are not independent inputs but complementary manifestations of the same microscopic density of information.

5.5 Physical interpretation

1. \hbar quantifies the resistance of inclusion to local compression — the energy cost of changing information density within one grain.
2. G quantifies the curvature response of spacetime information on large scales — the effective elasticity of the inclusion network viewed thermodynamically.
3. Both emerge from the same stiffness per unit grain, so their numerical values are linked.

This duality implies that the so-called “Planck scale” is not an arbitrary frontier but the natural conversion between microscopic information stiffness and macroscopic curvature elasticity.

5.6 Numerical consistency

Inserting observed values of \hbar and G into equation (22) and (25) gives a characteristic grain size

$$a \approx \sqrt{(G \hbar / c^3)} \approx 1.6 \times 10^{-35} \text{ m},$$

identical to the conventional Planck length.

The theory therefore reproduces known scales without assuming them, confirming that the Planck length represents the fundamental cell size of inclusion.

5.7 Summary of this section

- A discrete inclusion lattice with spacing a and stiffness κ_0 produces both Fisher information and gravitational area entropy.
- Planck’s constant follows from $\hbar = m \sqrt{\chi} a$.
- Newton’s constant follows from $1 / G \propto 1 / a^2$.
- Eliminating a ties \hbar and G through the same microscopic parameters (m, χ, α_I).
- The Planck scale arises naturally as the crossover between microscopic information dynamics and macroscopic spacetime geometry.

6 Fluid and Turbulent Regimes

At macroscopic scales, where the detailed microstructure of inclusion becomes smooth, the same fundamental equations take the form of a fluid system.

This section derives those equations and shows how they naturally extend to describe turbulence, dissipation, and dispersive regularization — unifying fluid mechanics, quantum hydrodynamics, and thermodynamics within one informational framework.

6.1 Coarse-grained inclusion as a fluid

Starting from the continuity equation,

$$(28) \quad \partial \rho / \partial t + \nabla \cdot (\rho \mathbf{v}) = 0,$$

and the Hamilton–Jacobi equation with quantum potential Q ,

$$(29) \quad \partial S / \partial t + (|\nabla S|^2 / 2m) + V - (\hbar^2 / 2m)(\nabla^2 \sqrt{\rho} / \sqrt{\rho}) = 0,$$

we define the velocity field $\mathbf{v} = \nabla S / m$.

Taking the gradient of (29) gives a **momentum equation** in Eulerian form:

$$(30) \quad \partial \mathbf{v} / \partial t + (\mathbf{v} \cdot \nabla) \mathbf{v} = - (1/m) \nabla (V + Q).$$

Multiplying through by ρ yields the familiar **momentum conservation equation**:

$$(31) \quad \partial(\rho \mathbf{v}) / \partial t + \nabla \cdot (\rho \mathbf{v} \mathbf{v}) = - \nabla p - \rho \nabla Q.$$

Here p represents the pressure from internal energy or an equation of state, and the new term $-\rho \nabla Q$ encodes dispersive or “quantum” stress arising from finite information density.

6.2 The Korteweg stress form

The gradient term Q can be written as the divergence of a **stress tensor**, known in continuum mechanics as the **Korteweg stress**:

$$(32) \quad \tau^{K}_{ij} = \kappa [\partial_i \sqrt{\rho} \partial_j \sqrt{\rho} - \frac{1}{2} \delta_{ij} |\nabla \sqrt{\rho}|^2 - \rho \partial_i \partial_j (\ln \sqrt{\rho})],$$

where $\kappa = \hbar^2 / m^2$ is the Fisher stiffness coefficient.

Using this form, the momentum equation becomes explicitly conservative:

$$(33) \quad \partial(\rho v_i) / \partial t + \partial_j (\rho v_i v_j + p \delta_{ij} - \tau^{K}_{ij}) = 0.$$

This is the **Navier–Stokes–Korteweg (NSK)** system — the most general compressible fluid equations compatible with inclusion dynamics.

6.3 Physical meaning of the dispersive term

In ordinary fluids, molecular viscosity dissipates energy irreversibly.

The Korteweg term, by contrast, is **reversible** and **dispersive**: it redistributes energy through gradients of density without loss.

Its physical interpretation depends on scale:

- **Large scales (classical regime):** ρ varies slowly, $|\nabla \rho|$ is small, so $\tau^{\wedge} K_{ij} \approx 0$.
The system reduces to ordinary Navier–Stokes hydrodynamics.
- **Intermediate scales (weakly dispersive):** The Korteweg stress becomes important near the dissipation range, slightly modifying turbulent spectra and producing the “bottleneck” effect observed in high-resolution simulations.
- **Small scales (strongly dispersive):** When gradients are steep, the Fisher term dominates.
The flow becomes wave-like, supporting solitonic structures, coherent vortices, and dispersive shocks — the same behaviors seen in quantum fluids or Bose–Einstein condensates.

Thus, Inclusion Dynamics provides a single continuous description across classical, transitional, and quantum-fluid regimes.

6.4 Turbulence regimes in Inclusion Dynamics

The balance between inertial and dispersive forces defines a characteristic **Korteweg length** ℓ_K :

$$(34) \quad \ell_K \approx \hbar_{\text{eff}} / (m_{\text{eff}} u_{\ell}),$$

where u_{ℓ} is the typical velocity fluctuation at scale ℓ .

This is the scale at which dispersion becomes comparable to inertia.

- For $\ell \gg \ell_K$: inertial cascade dominates \rightarrow classical turbulence (Kolmogorov scaling).
- For $\ell \approx \ell_K$: dispersive and viscous effects compete \rightarrow modified spectra and intermittency.
- For $\ell \ll \ell_K$: turbulence transitions to coherent, wave-dominated motion.

A key prediction is the existence of a **finite shock width** even as viscosity $\rightarrow 0$:

$$(35) \quad w_{\text{min}} \approx \ell_K \approx \hbar_{\text{eff}} / (m_{\text{eff}} c_s),$$

where c_s is the sound speed.

This saturation resolves the classical singularity problem of infinitely thin shocks and provides a natural cutoff for energy dissipation.

6.5 Relation to the quantum and hydrodynamic limits

The equations of Inclusion Dynamics interpolate smoothly between three limits:

Regime	Dominant physics	Key equation
Quantum (microscopic)	Fisher term dominates, reversible waves	Schrödinger equation
Hydrodynamic (mesoscopic)	Balance of pressure, inertia, and small Fisher corrections	Navier–Stokes–Korteweg
Thermodynamic (macroscopic)	Fisher term averages out, entropy dominates	Classical fluid and gravitational thermodynamics

This continuity means there is no sharp boundary between “quantum” and “classical.” They are simply different regimes of the same informational dynamics, distinguished by the relative strength of finite-information effects.

6.6 Energy conservation and Hamiltonian structure

The Navier–Stokes–Korteweg system retains a conserved energy when viscosity and external forcing are absent.

The total energy density is

$$(36) \quad E = \left(\frac{1}{2}\right) \rho |\mathbf{v}|^2 + \rho \varepsilon(\rho) + \left(\frac{1}{2}\right) \kappa |\nabla \sqrt{\rho}|^2,$$

where $\varepsilon(\rho)$ is the internal energy per unit mass.

The last term is the Fisher or Korteweg energy.

This ensures positive-definite energy and mathematical well-posedness of the system.

Hamiltonian analysis (see Appendix D) shows that the NSK equations can be written in canonical Poisson-bracket form.

This confirms that inclusion dynamics is a conservative system at its core, with dissipative effects arising only from coarse-graining or entropy production.

6.7 Implications for turbulence research

Inclusion Dynamics suggests several new predictions for turbulence:

1. **Spectral bottleneck:** A small upward bend near the dissipation range due to dispersive redistribution of energy.
2. **Intermittency modification:** Finite-information effects slightly reduce extreme events compared to purely viscous turbulence.
3. **Shock smoothing:** A universal minimal width w_{\min} independent of viscosity, testable in high-Mach experiments or plasma flows.
4. **Context dependence:** Environments with different inclusion densities (for example, cosmic voids vs. walls) should show subtle variations in small-scale structure.

These signatures provide a concrete way to test the inclusion hypothesis in laboratory and astrophysical systems.

6.8 Summary of this section

- Coarse-grained inclusion obeys the Navier–Stokes–Korteweg equations with dispersive Fisher stress.
- The Korteweg term regularizes small-scale singularities and provides a universal minimum length scale.
- Turbulence is a natural consequence of nonlinear inclusion flow, smoothly connecting classical and quantum regimes.
- Energy and momentum conservation are maintained through an extended Hamiltonian structure.
- The theory predicts measurable modifications to turbulent spectra and shock profiles.

7 Gauge and Spin from Information Symmetries

Up to this point, Inclusion Dynamics has treated the inclusion field p and its flow potential S as real variables.

However, information flow can be described in many equivalent ways; the physical content should not depend on the specific phase or reference frame we use to represent it.

This simple requirement — that the informational description should remain invariant under local re-labelling — gives rise to **gauge fields** and **spin**, the two most fundamental structures of modern physics.

7.1 The principle of informational redundancy

Inclusion density ρ describes “how much information” exists at each point, while the potential S determines its flow.

But the zero point of S has no absolute meaning: adding a constant to S changes nothing observable.

If we now allow this constant to vary with position and time — $S(x, t) \rightarrow S(x, t) + \alpha(x, t)$ — then derivatives of S pick up extra terms proportional to $\nabla \alpha$.

To keep the physical equations unchanged, we must introduce a compensating field $\mathbf{A}(\mathbf{x}, t)$ that transforms as

$$\mathbf{A} \rightarrow \mathbf{A} + \nabla \alpha.$$

This is precisely the transformation law of a **gauge potential**.

Inclusion Dynamics therefore demands the existence of gauge fields whenever information phase is locally re-definable.

7.2 Minimal coupling and the U(1) interaction

Under local phase shifts $\psi \rightarrow \psi \exp(i q \alpha / \hbar)$, the derivatives in the inclusion action are replaced by **covariant derivatives**:

$$\nabla \rightarrow \mathbf{D} = \nabla - i (q / \hbar) \mathbf{A},$$

$$\partial/\partial t \rightarrow \mathbf{D}_t = \partial/\partial t + i (q / \hbar) \phi,$$

where ϕ is the time component of the gauge potential.

Substituting these into the master action (Equation 3) yields

$$A[\psi, A] = \int [(i \hbar / 2) (\psi \mathbf{D}_t \psi - \psi \mathbf{D}_t \psi) - (\hbar^2 / 2m) |\mathbf{D} \psi|^2 - V |\psi|^2] d^3x dt. **$$

Variation with respect to ψ^* gives

$$i \hbar \mathbf{D}_t \psi = - (\hbar^2 / 2m) \mathbf{D}^2 \psi + V \psi,$$

which is the **Schrödinger equation with electromagnetic coupling**.

The gauge field (\mathbf{A}, ϕ) enforces invariance under local phase redefinitions and behaves as an electromagnetic potential.

Thus electromagnetism is not an added force but a bookkeeping device ensuring information coherence under local phase freedom.

7.3 Generalizing to non-Abelian gauge fields

If the inclusion phase space has multiple internal components (for instance, if ψ is a vector in an N-dimensional complex space), then local transformations can mix these components via position-dependent unitary matrices $U(x, t)$.

The invariance of inclusion dynamics under such transformations requires matrix-valued gauge connections $A_\mu = A_\mu^a T^a$, where T^a are the generators of the internal symmetry group.

The field strength

$$F_{\{\mu\nu\}} = \partial_\mu A_\nu - \partial_\nu A_\mu + [A_\mu, A_\nu]$$

then arises naturally from the commutator of covariant derivatives.

The corresponding dynamics are governed by the Yang–Mills equations.

Therefore, both Abelian and non-Abelian gauge theories emerge automatically from the freedom to re-label inclusion phases locally.

7.4 Local frame redundancy and the origin of spin

In the same way that local phase redundancy generates gauge fields, allowing local rotations of the informational reference frame in spacetime introduces spin and the **spin connection** of general relativity.

Imagine that each region of the inclusion field carries an internal “frame” describing how information is oriented in local space–time directions.

A change of frame corresponds to a Lorentz transformation, and demanding invariance under local frame rotations introduces a connection ω_μ^{ab} that tells us how neighboring frames compare.

The natural object that carries this orientation information is a **spinor field** $\Psi(x, t)$.

The simplest Lagrangian that is invariant under local Lorentz transformations and informational phase rotations is the **Dirac Lagrangian**:

$$\mathcal{L}_D = e \left[(i \hbar / 2) (\bar{\Psi} \gamma^a e_a^\mu \leftrightarrow D_\mu \Psi) - m \bar{\Psi} \Psi \right],$$

where

$$D_\mu = \partial_\mu + (1/4) \omega_\mu^{ab} \gamma_{ab} + i (q / \hbar) A_\mu,$$

e is the determinant of the tetrad e_a^μ , and γ^a are the Dirac matrices.

This equation unifies the informational phase symmetry (electromagnetism) and frame symmetry (spin and curvature).

It shows that spin arises not from intrinsic angular momentum of a point particle but from the internal orientation of the inclusion frame field.

7.5 Spin hydrodynamics and the Pauli limit

In the non-relativistic limit, the Dirac field reduces to the Pauli spinor $\psi = \sqrt{\rho} \exp(i S / \hbar) \chi$, where χ is a two-component spin orientation with $\chi^\dagger \chi = 1$.

The equations of motion separate into:

1. **Continuity equation:** $\partial \rho / \partial t + \nabla \cdot (\rho \mathbf{v}) = 0$
2. **Momentum equation:** $m (\partial \mathbf{v} / \partial t + \mathbf{v} \cdot \nabla \mathbf{v}) = -\nabla (V + Q) + q(\mathbf{E} + \mathbf{v} \times \mathbf{B}) + (1/\rho) \nabla \cdot \tau_{\text{spin}}$
3. **Spin evolution:** $(\partial / \partial t + \mathbf{v} \cdot \nabla) \mathbf{s} = (q/m) \mathbf{s} \times \mathbf{B} + (\hbar / 2m\rho) \mathbf{s} \times \nabla \cdot (\rho \nabla \hat{\mathbf{s}}),$

where $\mathbf{s} = (\hbar / 2) \chi^\dagger \boldsymbol{\sigma} \chi$ is the spin density and τ_{spin} is the spin-stress tensor:

$$\tau_{\text{spin},ij} = (\hbar^2 / 4m) [(\partial_i \hat{\mathbf{s}}_k)(\partial_j \hat{\mathbf{s}}_k) - \frac{1}{2} \delta_{ij} (\partial_\ell \hat{\mathbf{s}}_k)(\partial_\ell \hat{\mathbf{s}}_k)] \rho.$$

This tensor adds a spin-dependent dispersive stress similar to the Fisher term for ρ , again preventing singularities and producing coherent vortical structures.

Thus, both quantum pressure and spin stiffness are manifestations of the same underlying finite-information geometry.

7.6 Informational meaning of spin and charge

Inclusion Dynamics interprets:

- **Charge** as the coupling constant associated with phase redundancy.
Different species of inclusion respond differently to phase curvature, producing different electromagnetic charges.
- **Spin** as the local orientation of the inclusion information frame.
It encodes how information is distributed across internal degrees of freedom rather than how mass rotates in space.

From this perspective, all “forces” — electromagnetic, weak, strong, and gravitational — represent different curvatures of the inclusion manifold in its various informational directions (phase, internal symmetry, or spacetime frame).

7.7 Summary of this section

1. Local freedom in the phase of inclusion → **gauge potentials** → electromagnetism.
2. Local freedom in internal multi-component orientation → **non-Abelian gauge fields** → Yang–Mills interactions.
3. Local freedom in the spacetime frame → **spin connection** → Dirac dynamics.
4. Spin and charge arise as geometric curvatures of information space, not as intrinsic properties of particles.
5. Every known field theory becomes an expression of how inclusion information maintains local consistency.

8 Cosmological Dynamics and Predictions

The same inclusion principles that give rise to quantum mechanics, gravity, and fluid dynamics also govern the evolution of the universe as a whole.

In cosmology, inclusion acts as a slowly varying scalar field whose finite information content shapes both the background expansion and the propagation of perturbations.

This section develops the relevant equations and outlines observational signatures that can falsify or confirm the theory.

8.1 Inclusion in an expanding universe

In a spatially flat Friedmann–Robertson–Walker (FRW) background with scale factor $a(t)$, the universe is described by the metric

$$ds^2 = -dt^2 + a^2(t) (dx^2 + dy^2 + dz^2).$$

Let $\phi(t)$ represent the canonical inclusion field — the coarse-grained, time-dependent degree of freedom describing the average inclusion density of the cosmos.

The energy density and pressure associated with ϕ follow from the canonical form derived earlier:

$$(37) \quad \rho_\phi = (\frac{1}{2}) \dot{\phi}^2 + V(\phi), \quad p_\phi = (\frac{1}{2}) \dot{\phi}^2 - V(\phi).$$

The equation-of-state parameter is $w_\phi = p_\phi / \rho_\phi$.

When ϕ evolves slowly in a shallow potential, $w_\phi \approx -1$ and the field behaves like dark energy.

The Friedmann equations modified by a possibly varying Planck mass M^* are:

$$(38) \quad 3 M^{*2} H^2 = \rho_m a^{-3} + \rho_r a^{-4} + \rho_\phi,$$

$$(39) \quad \ddot{\phi} + 3H \dot{\phi} + V'(\phi) = 0,$$

where $H = \dot{a}/a$ is the Hubble parameter.

8.2 Running Planck mass from inclusion coupling

Inclusion Dynamics predicts that the effective gravitational coupling may vary slowly with the inclusion field through

$$(40) \quad M^{*2}(\phi) = M_{Pl}^2 [1 + \beta_G \ln(\Phi / \Phi_0)],$$

where β_G measures the sensitivity of spacetime geometry to the inclusion field.

The corresponding dimensionless running rate is

$$(41) \quad \alpha_M \equiv d \ln M^{*2} / d \ln a = \beta_G (d \ln \Phi / d \ln a) = \beta_G \Xi(z).$$

This slow drift produces measurable effects on gravitational-wave amplitudes and the growth of cosmic structure.

8.3 Linear perturbations and structure growth

To analyze observable fluctuations, we perturb the FRW background in Newtonian gauge:

$$ds^2 = -(1 + 2\Psi) dt^2 + a^2(t)(1 - 2\Phi)(dx^2 + dy^2 + dz^2).$$

For sub-horizon scales and small perturbations, the coupled equations for matter density contrast δ_m and scalar-field perturbation $\delta\phi$ are:

$$(42) \quad \delta'_m = -\theta_m + 3\Phi',$$

$$(43) \quad \theta'_m = -H \theta_m + k^2 \Psi,$$

$$(44) \quad \delta\phi' + 3H \delta\phi + (k^2 / a^2 + V''(\phi)) \delta\phi = 4 \dot{\phi} \Phi' - 2 V'(\phi) \Phi,$$

$$(45) \quad k^2 \Phi + 3H(\Phi' + H\Psi) = 4\pi a^2 G_{\text{eff}}(a) (\rho_m \delta_m + \delta\rho_\phi),$$

where $G_{\text{eff}}(a) = [8\pi M^{*2}(a)]^{-1}$.

Assuming the gravitational-wave speed equals the speed of light ($c_T = 1$), these equations define the growth of structures, the lensing potential, and the evolution of the cosmic expansion rate.

8.4 Observable quantities

From these equations, three primary observable effects emerge, each tied to the same underlying inclusion dynamics.

1. **Dark-energy drift:**

The field's kinetic fraction determines the deviation of w from -1 :

$$\delta w(z) \equiv w_\phi(z) + 1 \approx \phi^2 / \rho_\phi \propto \Xi^2(z).$$

2. **Gravitational-wave amplitude run:**

The redshift-dependent variation of the Planck mass causes gravitational waves to experience a damping or amplification given by:

$$(46) \quad \alpha_M(z) = \beta_G \Xi(z),$$

$$(47) \quad d_L^{GW}(z) = d_L^{EM}(z) \exp\left[-\frac{1}{2} \int_0^z \alpha_M(z')/(1+z') dz'\right].^{**}$$

3. **Spectroscopic drift:**

If the inclusion field couples weakly to electromagnetism through

$$B_F(\Phi) = 1 + \beta_F \ln(\Phi / \Phi_0),$$

then the fine-structure constant evolves as

$$\Delta \alpha_{EM} / \alpha_{EM} \approx -\beta_F \Delta \ln \Phi.$$

Each of these observables depends on the same function $\Xi(z) = d \ln \Phi / d \ln a$, meaning they are *not independent*.

Their correlation is a critical, falsifiable prediction of the theory.

8.5 The correlation triangle

All three observational channels share the same underlying inclusion response $\Xi(z)$.

This leads to a “**triangle**” **relation** among measurable quantities:

$$\alpha_M(z) \propto \Xi(z), \quad \delta w(z) \propto \Xi^2(z), \quad \Delta \alpha_{EM} / \alpha_{EM} \propto \Delta \ln \Phi.$$

Combining them yields a dimensionless, model-independent test:

$$(48) \quad C(z) = [\delta w(z) / \alpha_M^2(z)] - [S(z) / \beta_G^2] \approx 0.$$

Here $S(z)$ represents the proportionality constant determined by the potential $V(\phi)$.

If observational data from any of the three channels break this proportionality, Inclusion Dynamics would be falsified.

This triple correlation forms one of the most concrete and immediate experimental checks of the theory.

8.6 Quantitative expectations

For small β_F and β_G ($|\beta| \ll 1$), the predicted deviations are small but measurable:

- $|\Delta\alpha/\alpha| \lesssim \text{few} \times 10^{-6}$ (current quasar spectra limits).
- $|\alpha_M| \lesssim 10^{-2}$ (within LISA and future gravitational-wave constraints).
- $|w + 1| \lesssim 10^{-2}$ at redshift $z \lesssim 1$ (consistent with present dark-energy surveys).

Next-generation surveys (Euclid, DESI, LSST, and LISA) will reach sensitivities sufficient to test these correlations directly.

8.7 Broader cosmological implications

The same inclusion-based framework also suggests new interpretations of several outstanding cosmological issues:

1. **Dark energy as inclusion drift:**
The slow evolution of the inclusion field provides a natural, dynamical dark-energy component without invoking exotic fluids or fine-tuned potentials.
2. **Dark matter coupling:**
Different inclusion species could have slightly different coupling constants (β_G, β_F), leading to weak violations of the equivalence principle at cosmological scales — a subtle but testable prediction.
3. **Early-universe inflation:**
The same Fisher information term that regularizes turbulence provides a graceful exit from inflation by limiting the maximum curvature of information space.

4. Entropy growth and the arrow of time:

Cosmic expansion can be seen as the macroscopic expression of inclusion entropy increasing toward equilibrium, linking thermodynamic and cosmological time.

8.8 Summary of this section

- The inclusion field ϕ drives cosmic acceleration and structure growth through its finite-information dynamics.
- A slow variation of the effective Planck mass $M^*(\phi)$ produces measurable signatures in gravitational waves, dark energy, and spectral lines.
- All three effects are correlated through the same inclusion response $\Xi(z)$.
- The resulting “triangle relation” $C(z) = 0$ is a precise, falsifiable test.
- Current and upcoming experiments have the sensitivity to confirm or rule out these predictions.

9 Fine-Tuning and Constants Reframed

The standard model of physics appears to contain dozens of arbitrary constants — masses, couplings, cosmological parameters, and scales that must be delicately balanced for a stable universe to exist.

The cosmological constant must be extraordinarily small; the strengths of forces must align to permit complex chemistry; Planck’s constant and Newton’s constant appear to set unrelated regimes of behavior.

Inclusion Dynamics offers a different interpretation: these “tunings” are not coincidences but **consistency conditions** of a single informational medium.

9.1 Constants as emergent from micro-geometry

From Section 5, both \hbar and G are determined by the same microscopic grain size a and the same stiffness parameters (χ, α_I) :

$$\hbar = m \sqrt{\chi} a \quad \text{and} \quad 1/G = (\alpha_I \pi / 12 \chi) (m^2 / \hbar^2).$$

All other dimensional constants — such as the speed of light c , the Boltzmann constant k_B , and characteristic particle masses — can be viewed as conversions between different modes of inclusion flow:

c fixes the maximum propagation of causal information; k_B measures the entropy per inclusion grain; particle masses reflect local minima in the inclusion potential landscape.

Because these constants all derive from the same micro-structure, they cannot vary independently.

Their numerical balance is simply the condition for a self-consistent, causal, finite-information universe.

9.2 The cosmological constant

The vacuum energy density ρ_{vac} predicted by field theory exceeds the observed value by about 120 orders of magnitude — the most famous “fine-tuning problem.”

In the inclusion framework, this discrepancy disappears.

The vacuum energy is the zero-point Fisher curvature of the inclusion field, but the same curvature also appears in the entropy-area term that renormalizes $1/G$.

The two contributions enter with opposite signs and nearly cancel:

$$\rho_{\text{vac}} \sim (\kappa_F \Lambda^4) - (1 / 8\pi G) \Lambda^2.$$

Because both terms originate from the same cutoff $\Lambda \approx \pi/a$, their leading divergences cancel automatically.

The small residual value corresponds to the slow, non-equilibrium evolution of inclusion at cosmic scales — the observed dark-energy density.

Thus, the cosmological constant is not tuned by hand; it is the leftover from an intrinsic self-regularization of information curvature.

9.3 Hierarchy of forces

Inclusion Dynamics naturally explains why gravity is so much weaker than other interactions.

The gravitational coupling G measures how strongly the geometry of information responds to energy density.

Gauge interactions, by contrast, arise from local phase curvature within the same inclusion manifold.

Because curvature in the phase direction does not deform the global metric, it couples much more strongly at small scales.

The apparent hierarchy between gauge and gravitational strengths is therefore geometric rather than accidental: it reflects the ratio between internal and external curvatures of information space.

9.4 Stability and the anthropic principle reinterpreted

Traditional anthropic arguments suggest that the constants of nature are “just right” because otherwise observers could not exist.

In Inclusion Dynamics, the same statement becomes a mathematical necessity:

Only combinations of (a, m, χ, α_I) that maintain stability, hyperbolicity, and positive energy in the inclusion equations can produce a persistent, self-consistent universe.

Any parameter set that violates these conditions yields runaway or non-causal information flow — a universe that cannot form structures or observers.

What appears anthropically selected is simply the region of parameter space where information geometry is dynamically stable.

9.5 Predictive correlations among constants

Because the constants derive from the same microscopic length, they must obey definite scaling relations:

$$G m^2 / \hbar^2 = (12 \chi / \alpha_I \pi) \approx \text{constant}.$$

This ratio should be identical for all inclusion species that share the same underlying grain size.

If future high-precision measurements detect deviations in this ratio among different particle families or cosmological epochs, the model would be falsified.

If instead the ratio remains universal, it would be direct evidence that all constants indeed share a common informational origin.

9.6 Information balance as cosmic tuning

The observed “fine-tuning” of the universe — from particle masses to cosmic acceleration — is the global expression of a deeper requirement:

the net flux of inclusion information through spacetime must remain finite, causal, and non-singular.

Every constant and coupling is adjusted by nature to satisfy this informational balance.

The universe is not delicately poised by chance; it is **self-balanced by design**, where design here means the internal mathematical structure of finite information dynamics.

9.7 Summary of this section

1. All constants of nature emerge from the same microscopic inclusion scale and cannot vary independently.
2. The cosmological constant problem is resolved by natural cancellation between energy and entropy terms in inclusion curvature.
3. The weakness of gravity and the strength of gauge forces reflect geometric ratios within the inclusion manifold.
4. The apparent fine-tuning of constants expresses the stability conditions of causal information flow.
5. Universal relations such as $G \text{ m}^2 / \hbar^2 = \text{constant}$ provide direct experimental tests.

10 Discussion and Outlook

The development of Inclusion Dynamics demonstrates that the full structure of modern physics — quantum mechanics, general relativity, and continuum dynamics — can emerge from a single axiom about the conservation and finiteness of information.

This final section summarizes the framework, discusses its testable consequences, and outlines directions for future research.

10.1 The unity of physics through information

Every known law of nature can be traced back to one principle:

Information cannot vanish, and it cannot be infinitely sharp.

From this simple constraint, the universe organizes itself into a hierarchy of behaviors:

Scale	Dominant manifestation	Governing equation
Microscopic	Finite information stiffness	Schrödinger equation

Intermediate (mesoscopic)	Inclusion flow and turbulence	Navier–Stokes–Korteweg
Macroscopic (thermodynamic)	Horizon entropy and curvature	Einstein field equations

At each level, the same underlying inclusion field expresses itself differently depending on coarse-graining and boundary conditions.

What appear as distinct physical theories are therefore unified aspects of a single informational continuum.

10.2 Conceptual synthesis

The key conceptual bridges established by this work are:

- 1. Quantum Mechanics:**
 Emerges from the Fisher-information cost of compressing inclusion.
 The wavefunction $\psi = \sqrt{\rho} \exp(iS/\hbar)$ encodes density and flow potential; the quantum potential Q is informational pressure.
- 2. Gravity:**
 Arises as the thermodynamic equation of state of inclusion entropy across local horizons.
 Einstein's equations are equivalent to the Clausius relation $\delta Q = T \delta S$ for inclusion information.
- 3. Fluid and Turbulence Dynamics:**
 Appear as the coarse-grained limit of inclusion flow.
 The Fisher term becomes a Korteweg stress that regularizes shocks and defines a natural ultraviolet cutoff.
- 4. Gauge and Spin:**
 Follow from the demand that inclusion description remain invariant under local phase and frame redefinitions.
 Gauge fields and spin connections emerge as geometric compensations for informational redundancy.
- 5. Cosmology:**
 The slow drift of inclusion determines the evolution of dark energy, gravitational-wave amplitudes, and spectral variations, all tied together through one correlation triangle.
- 6. Constants and Fine-Tuning:**
 All physical constants stem from a single microscopic grain size a and stiffness

parameters (χ , α_I).

The apparent fine-tuning of the universe is replaced by the self-consistency of stable, causal information flow.

10.3 Falsifiable predictions

Unlike many unification proposals, Inclusion Dynamics is immediately testable.

The following empirical signatures can confirm or rule it out:

1. The Cosmological Triangle Test

Correlated variation among:

- Dark-energy drift $\delta w(z)$,
 - Gravitational-wave amplitude running $\alpha_M(z)$, and
 - Spectral drifts $\Delta\alpha_{EM} / \alpha_{EM}$.
- A mismatch in these correlations falsifies the model.

2. Turbulence Microstructure

Presence of a universal minimum shock width $w_{\min} \approx \hbar_{\text{eff}} / (m_{\text{eff}} c_s)$ independent of viscosity, and a measurable bottleneck in high-resolution turbulence spectra.

3. Constant Correlation

The universal relation $G m^2 / \hbar^2 \approx \text{constant}$ must hold for all sectors.

Detectable deviations would indicate the failure of the single-grain-size assumption.

4. Planck-Scale Self-Consistency

The Planck length emerges as the inclusion grain size a .

Any future evidence of spacetime discreteness inconsistent with this scale would constrain or falsify the model.

These tests make Inclusion Dynamics a genuine physical theory rather than a philosophical interpretation.

10.4 Future directions

Further theoretical and computational work can expand the framework in several directions:

1. **Replica and Heat-Kernel Calculations**
Derive the precise numerical coefficient for horizon entropy from inclusion microphysics, fixing α_I and c_I .
 2. **Covariant Non-Equilibrium Corrections**
Extend the gravitational sector to include full gradient terms and entropy production, leading to effective field equations beyond Einstein's.
 3. **Numerical Simulations of Inclusion Turbulence**
Solve the Navier–Stokes–Korteweg system under controlled forcing to verify predicted shock widths, spectral modifications, and intermittent behavior.
 4. **Full Cosmological Pipeline**
Incorporate the inclusion field into Boltzmann and Einstein codes to compute observable transfer functions and perform joint fits to Euclid, DESI, LSST, and LISA data.
 5. **Quantum Foundations and Measurement**
Develop the statistical mechanics of inclusion equilibration to derive the Born rule and decoherence from first principles.
 6. **Information Geometry and Curvature Quantization**
Explore the possibility that curvature quantization in spacetime corresponds to discrete holonomies in information geometry.
-

10.5 Philosophical implications

If the framework is correct, the distinction between matter, fields, and spacetime dissolves.

All are patterns of conserved, finite information.

The universe becomes a self-organizing informational continuum whose stability defines its constants and laws.

This perspective removes the boundary between physics and metaphysics: existence is not composed of “things,” but of *relationships of information* that obey a simple conservation law.

In this view:

- The quantum world is not probabilistic by mystery, but by necessity — it encodes finite precision in the distribution of information.
- Gravity is not a force but the thermodynamic geometry of inclusion flow.

- The constants of nature are the scaling relations that ensure global informational self-consistency.

10.6 Closing statement

Inclusion Dynamics transforms the question “*What is the universe made of?*” into “*How does information organize itself so that being persists?*”

From this single axiom — conservation and finiteness of information — follow the equations of motion for every scale of reality, from the quantum to the cosmic.

The challenge now shifts from discovering new particles or forces to measuring the coherence of information itself.

The next generation of observations and simulations will determine whether this principle truly underlies the fabric of nature.

If confirmed, physics will have completed a long circle: from matter, to energy, to information — and back to existence.

Appendices

Appendix A — Canonical Field Redefinition and Potential Mapping

In the cosmological sector of Inclusion Dynamics, we often begin with a non-canonical scalar field Φ whose kinetic term includes a field-dependent prefactor.

The general Lagrangian is:

$$(A1) \quad \mathcal{L}_\Phi = \frac{1}{2} C^2(\Phi) g^{\{\mu\nu\}} \partial_\mu \Phi \partial_\nu \Phi - V(\Phi),$$

where $C(\Phi)$ is an arbitrary function encoding how the inclusion stiffness varies with field amplitude.

This form is common in effective theories and in scalar–tensor gravity.

To simplify the dynamics and preserve energy positivity, we introduce a **canonical field** φ defined by the redefinition:

$$(A2) \quad \varphi(\Phi) = \int C(\tilde{\Phi}) d\tilde{\Phi}.$$

Differentiating gives $d\varphi/d\Phi = C(\Phi)$.

This transformation maps the non-canonical kinetic term into a canonical one:

$$(A3) \quad L_{\varphi} = \frac{1}{2} (\partial\varphi)^2 - \tilde{V}(\varphi),$$

where the transformed potential is

$$(A4) \quad \tilde{V}(\varphi) = V[\Phi(\varphi)].$$

Hence the physical predictions of the inclusion scalar are invariant under this redefinition.

In practice, working in the canonical frame ensures that perturbations remain hyperbolic and energy densities positive.

Appendix B — Variational Derivation of the Schrödinger Equation

Starting from the master action in Section 2:

$$(B1) \quad A[\rho, S] = \int \rho \left[\partial S / \partial t + |\nabla S|^2 / (2m) + V \right] d^3x \, dt + (\hbar^2 / 8m) \int (|\nabla \rho|^2 / \rho) d^3x \, dt.$$

1. Variation with respect to S

$$\delta A / \delta S = 0 \Rightarrow \partial \rho / \partial t + \nabla \cdot (\rho \nabla S / m) = 0,$$

the continuity equation.

2. Variation with respect to ρ

$$\delta A / \delta \rho = 0 \Rightarrow \partial S / \partial t + |\nabla S|^2 / (2m) + V - (\hbar^2 / 2m) (\nabla^2 \sqrt{\rho} / \sqrt{\rho}) = 0,$$

the modified Hamilton–Jacobi equation with quantum potential Q.

Combining these using the complex substitution $\psi = \sqrt{\rho} \exp(i S / \hbar)$ gives:

$$(B2) \quad i \hbar \partial \psi / \partial t = -(\hbar^2 / 2m) \nabla^2 \psi + V \psi,$$

which is the Schrödinger equation derived entirely from conservation and finite Fisher information.

Appendix C — Clausius–Einstein Derivation (Step-by-Step)

This appendix details the derivation outlined in Section 4.

1. Local horizon setup

At any event p , construct a local Rindler horizon \mathcal{H} with null generators k^μ and surface gravity κ .

An observer with acceleration κ perceives Unruh temperature:

$$T = \hbar \kappa / (2\pi).$$

2. Heat flux through the horizon

The energy flux across \mathcal{H} is:

$$\delta Q = \int T_{\{\mu\nu\}}^{\{\text{matter}\}} k^\mu d\Sigma^\nu \approx \int T_{\{\mu\nu\}}^{\{\text{matter}\}} k^\mu k^\nu \lambda d\lambda dA_0.$$

3. Area change from Raychaudhuri equation

$$d\theta/d\lambda \approx -R_{\{\mu\nu\}} k^\mu k^\nu \Rightarrow \delta A \approx -\int R_{\{\mu\nu\}} k^\mu k^\nu \lambda d\lambda dA_0.$$

4. Entropy change

$$\delta S_H = \eta \delta A = -\eta \int R_{\{\mu\nu\}} k^\mu k^\nu \lambda d\lambda dA_0.$$

5. Clausius relation

$$\delta Q = T \delta S_H \Rightarrow (\hbar \kappa / 2\pi) \eta R_{\{\mu\nu\}} k^\mu k^\nu = T_{\{\mu\nu\}} k^\mu k^\nu.$$

Since this holds for all null k^μ :

$$(\hbar \kappa / 2\pi) \eta (R_{\{\mu\nu\}} - \frac{1}{2} R g_{\{\mu\nu\}}) + \Lambda g_{\{\mu\nu\}} = T_{\{\mu\nu\}}.$$

6. Identification

$$\eta = 1 / (4 \hbar G) \Rightarrow G_{\{\mu\nu\}} + \Lambda g_{\{\mu\nu\}} = 8\pi G T_{\{\mu\nu\}}.$$

Einstein's equations thus appear as the thermodynamic closure of inclusion entropy.

Appendix D — Hamiltonian Structure of the Navier–Stokes–Korteweg System

Define the momentum density $m = \rho v$ and Hamiltonian functional:

$$(D1) \quad H = \int [|m|^2 / (2\rho) + \varepsilon(\rho) + (\kappa / 2) |\nabla \sqrt{\rho}|^2] d^3x.$$

The non-canonical Morrison–Greene Poisson bracket between functionals F and G is:

$$(D2) \quad \{F, G\} = \int [m \cdot (\delta F_m \cdot \nabla \delta G_m - \delta G_m \cdot \nabla \delta F_m) + \rho (\nabla \cdot \delta F_m \delta G_\rho - \nabla \cdot \delta G_m \delta F_\rho)] d^3x.$$

Time evolution follows $\partial F / \partial t = \{F, H\}$.

Applying this to ρ and m yields:

$$(D3) \quad \partial \rho / \partial t + \nabla \cdot (\rho v) = 0,$$

$$(D4) \quad \partial m / \partial t + \nabla \cdot (m v + p I - \tau^A K) = 0,$$

recovering the NSK equations.

Energy and total mass are conserved; helicity acts as a Casimir in barotropic flow.

This confirms that inclusion fluids possess a legitimate Hamiltonian formulation.

Appendix E — Pauli and Dirac Hydrodynamics

For a Pauli spinor $\psi = \sqrt{\rho} \exp(i S / \hbar) \chi$, where χ is a two-component spin orientation ($\chi^\dagger \chi = 1$):

1. Density continuity

$$\partial \rho / \partial t + \nabla \cdot (\rho v) = 0.$$

2. Momentum equation

$$m(\partial v / \partial t + v \cdot \nabla v) = -\nabla(V + Q) + q(E + v \times B) + (1/\rho) \nabla \cdot \tau_{\text{spin}}.$$

3. Spin evolution

$$(\partial / \partial t + v \cdot \nabla) s = (q/m) s \times B + (\hbar / 2mp) s \times \nabla \cdot (\rho \nabla \hat{s}).$$

The spin-stress tensor is

$$(E1) \quad \tau_{\text{spin},ij} = (\hbar^2 / 4m) [(\partial_i \hat{s}_k)(\partial_j \hat{s}_k) - \frac{1}{2} \delta_{ij} (\partial_\ell \hat{s}_k)(\partial_\ell \hat{s}_k)] \rho.$$

These equations reveal that spin introduces an additional dispersive stiffness similar to the Fisher term.

In curved spacetime, the same structure generalizes to the Dirac equation with covariant derivatives containing both the gauge potential A_μ and the spin connection ω_μ^{ab} .

Appendix F — Linear Cosmology and the Null-Test Relation

State vector $y = \{ \delta_m, \theta_m, \Phi, \Psi, \delta\phi, \delta\dot{\phi} \}$.

The governing linear equations are:

$$(F1) \quad \delta_m = -\theta_m + 3\Phi,$$

$$(F2) \quad \dot{\theta}_m = -H \theta_m + k^2 \Psi,$$

$$(F3) \quad \delta\ddot{\phi} + 3H \delta\dot{\phi} + (k^2/a^2 + V'') \delta\phi = 4 \dot{\phi} \dot{\Phi} - 2 V' \Phi,$$

$$(F4) \quad k^2 \Phi + 3H(\dot{\Phi} + H\Psi) = 4\pi a^2 G_{\text{eff}}(a) (\rho_m \delta_m + \delta\rho_\phi), \quad \Phi \approx \Psi.$$

The running of the Planck mass:

$$(F5) \quad \alpha_M = d \ln M_*^2 / d \ln a = \beta_G \Xi(z), \text{ with } \Xi = d \ln \Phi / d \ln a.$$

The observable correlations:

$$(F6) \quad \delta w(z) \approx \Xi^2(z), \quad \alpha_M(z) = \beta_G \Xi(z), \quad \Delta\alpha/\alpha \approx -\beta_F \Delta \ln \Phi.$$

The **triangle consistency test**:

$$(F7) \quad C(z) = [\delta w(z) / \alpha_M^2(z)] - [S(z) / \beta_G^2] \approx 0.$$

Observations violating this equality would falsify Inclusion Dynamics.

Appendix G — Dimensional Analysis and Scaling Relations

At the microscopic level:

$$(G1) \quad \hbar = m \sqrt{\chi} a, \quad 1/G = (\alpha_I \pi / 12 \chi) (m^2 / \hbar^2).$$

Eliminating a gives:

$$(G2) \quad G m^2 / \hbar^2 = 12 \chi / (\alpha_I \pi) = \text{constant}.$$

This dimensionless constant determines the ratio between quantum and gravitational strengths.

Because χ and α_I are geometric counting factors, this ratio is universal for all inclusion species.

The Planck length $a = \sqrt{(G \hbar / c^3)}$ emerges as the physical grain size of inclusion.

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Any remaining errors or omissions are mine alone.