

Covid-19-data Analysis

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Objective of this analysis

I will analyze Covid-19 data. Data is read from the Johns Hopkins University Github site. I will visualize the data grouped by country and, for the US, by state. Then I am going to analyze correlations between Covid-19 cases and deaths. In addition, I will analyze autocorrelation and partial autocorrelation for new patients and try to fit them to a time-series model.

Clear memory

At first, I clear memories in advance.

```
rm(list=ls())
gc();gc()
```

```
##           used (Mb) gc trigger (Mb) max used (Mb)
## Ncells 472897 25.3   1029034   55   644200 34.5
## Vcells 858071  6.6    8388608   64  1635000 12.5
```

```
##           used (Mb) gc trigger (Mb) max used (Mb)
## Ncells 473292 25.3   1029034   55   644200 34.5
## Vcells 859004  6.6    8388608   64  1635000 12.5
```

Import libraries

I import libraries to use this analysis.

```
Sys.setenv(LANGUAGE="en")
library(tidyverse)
```

```
## -- Attaching packages ----- tidyverse 1.3.2 --
## v ggplot2 3.3.6      v purrr   0.3.4
## v tibble  3.1.8      v dplyr  1.0.9
## v tidyr   1.2.0      v stringr 1.4.1
## v readr   2.1.2      v forcats 0.5.2
## -- Conflicts ----- tidyverse_conflicts() --
## x dplyr::filter() masks stats::filter()
## x dplyr::lag()    masks stats::lag()
```

```
library(lubridate)

##
## Attaching package: 'lubridate'
##
## The following objects are masked from 'package:base':
##
##     date, intersect, setdiff, union

# If you haven't installed 'forecast' yet, please do so.
# >install.packages('forecast', dependencies = TRUE)
library(forecast)

## Registered S3 method overwritten by 'quantmod':
##   method      from
##   as.zoo.data.frame zoo
```

Step 1 - Identify and import the data

I will start by reading in the data from the four main csv files.

```
# Get current Data in the four files
# They all begin the same way
url_in <- "https://raw.githubusercontent.com/CSSEGISandData/COVID-19/master/csse_covid_19_data/csse_cov
file_names <- c("time_series_covid19_confirmed_global.csv",
               "time_series_covid19_deaths_global.csv",
               "time_series_covid19_confirmed_US.csv",
               "time_series_covid19_deaths_US.csv")
urls <- str_c(url_in, file_names)
```

Let's read in the data and see what we have.

```
global_cases <- read_csv(urls[1])
global_deaths <- read_csv(urls[2])
US_cases <- read_csv(urls[3])
US_deaths <- read_csv(urls[4])
```

Step 2 - Tidy and Transform Data

After looking at global_cases and global_deaths, I would like to tidy those datasets and put each variable (date, cases, deaths) in their own colum. Also, I don't need Lat and Long for the analysis I am planning, so I will get rid of those and rename Region and State to be more R friendly.

```
global_cases <- global_cases %>%
  pivot_longer(cols = -c(`Province/State`, `Country/Region`, Lat, Long),
               names_to = "date",
               values_to = "cases") %>%
  select(-c(Lat, Long))

global_deaths <- global_deaths %>%
```

```

pivot_longer(cols = -c(`Province/State`, `Country/Region`, Lat, Long),
             names_to = "date",
             values_to = "deaths") %>%
select(-c(Lat, Long))

global <- global_cases %>%
  full_join(global_deaths) %>%
  rename(Country_Region = `Country/Region`,
         Province_state = `Province/State`) %>%
  mutate(date = mdy(date))

```

```
## Joining, by = c("Province/State", "Country/Region", "date")
```

```

global <- global %>% filter(cases > 0)

summary(global)

```

```

## Province_state      Country_Region      date      cases
## Length:268656      Length:268656      Min.   :2020-01-22      Min.   :      1
## Class :character    Class :character    1st Qu.:2020-11-07      1st Qu.:     991
## Mode  :character    Mode  :character    Median :2021-07-09      Median :    15550
##                                     Mean  :2021-07-05      Mean   :   853931
##                                     3rd Qu.:2022-03-06      3rd Qu.:  224610
##                                     Max.   :2022-10-27      Max.   : 97409772
##
## deaths
## Min.   :      0
## 1st Qu.:      6
## Median :    174
## Mean   :   13119
## 3rd Qu.:   3138
## Max.   : 1070055

```

```

US_cases <- US_cases %>%
  pivot_longer(cols = -c(UID:Combined_Key),
               names_to = "date",
               values_to = "cases") %>%
  select(Admin2:cases) %>%
  mutate(date = mdy(date)) %>%
  select(-c(Lat, Long_))

US_deaths <- US_deaths %>%
  pivot_longer(cols = -(UID:Population),
               names_to = "date",
               values_to = "deaths") %>%
  select(Admin2:deaths) %>%
  mutate(date = mdy(date)) %>%
  select(-c(Lat, Long_))

US <- US_cases %>%
  full_join(US_deaths)

```

```

## Joining, by = c("Admin2", "Province_State", "Country_Region", "Combined_Key",
## "date")

```

```
summary(US)
```

```
##      Admin2      Province_State      Country_Region      Combined_Key
## Length:3375420 Length:3375420      Length:3375420      Length:3375420
## Class :character Class :character Class :character Class :character
## Mode  :character Mode  :character Mode  :character Mode  :character
##
##
##
##      date      cases      Population      deaths
## Min.   :2020-01-22 Min.   : -3073 Min.   :      0 Min.   : -82.0
## 1st Qu.:2020-09-30 1st Qu.:   227 1st Qu.:   9917 1st Qu.:    2.0
## Median :2021-06-09 Median :   1846 Median :   24892 Median :   31.0
## Mean   :2021-06-09 Mean   :  11974 Mean   :   99604 Mean   :  168.3
## 3rd Qu.:2022-02-17 3rd Qu.:   6809 3rd Qu.:   64979 3rd Qu.:  107.0
## Max.   :2022-10-27 Max.   :3484615 Max.   :10039107 Max.   :33945.0
```

```
global <- global %>%
  unite("Combined_Key",
        c(Province_state, Country_Region),
        sep = ", ",
        na.rm = TRUE,
        remove = FALSE)
```

```
summary(global)
```

```
## Combined_Key      Province_state      Country_Region      date
## Length:268656      Length:268656      Length:268656      Min.   :2020-01-22
## Class :character   Class :character   Class :character   1st Qu.:2020-11-07
## Mode  :character   Mode  :character   Mode  :character   Median :2021-07-09
##                                     Mean  :2021-07-05
##                                     3rd Qu.:2022-03-06
##                                     Max.   :2022-10-27
##      cases      deaths
## Min.   :      1 Min.   :      0
## 1st Qu.:    991 1st Qu.:      6
## Median : 15550 Median :    174
## Mean   : 853931 Mean   :  13119
## 3rd Qu.: 224610 3rd Qu.:   3138
## Max.   :97409772 Max.   :1070055
```

```
uid_lookup_url <- "https://raw.githubusercontent.com/CSSEGISandData/COVID-19/master/csse_covid_19_data/"
uid <- read_csv(uid_lookup_url) %>%
  select(-c(Lat, Long_, Combined_Key, code3, iso2, iso3, Admin2))
```

```
## Rows: 4321 Columns: 12
## -- Column specification -----
## Delimiter: ","
## chr (7): iso2, iso3, FIPS, Admin2, Province_State, Country_Region, Combined_Key
## dbl (5): UID, code3, Lat, Long_, Population
##
## i Use 'spec()' to retrieve the full column specification for this data.
## i Specify the column types or set 'show_col_types = FALSE' to quiet this message.
```

Step 3 - Visualizing Data

I will visualize the data. First, draw a time series graph of cases and deaths across the US. Then plot the time series data for each state (here, New York and Colorado). I also shows a bar chart of total cases and deaths by state.

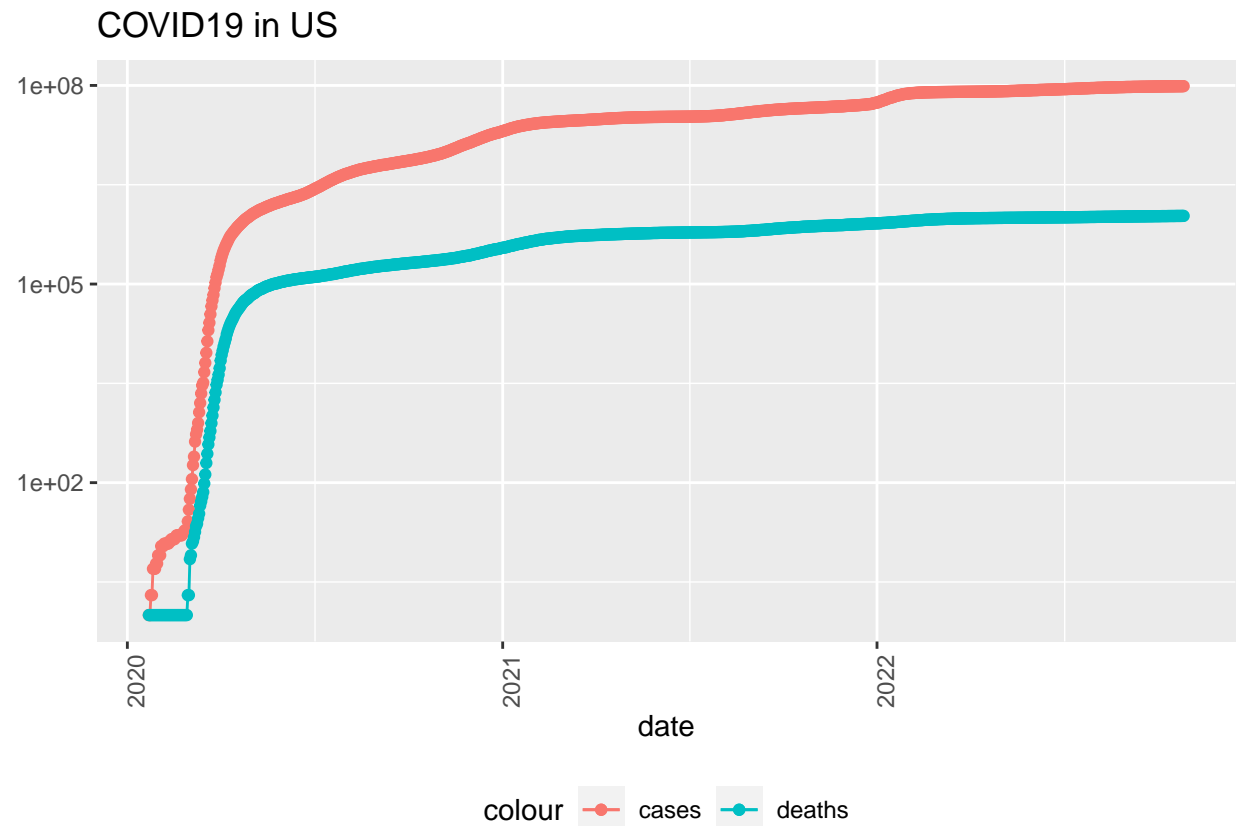
```
US_by_state <- US %>%
  group_by(Province_State, Country_Region, date) %>%
  summarise(cases = sum(cases), deaths = sum(deaths),
            Population = sum(Population)) %>%
  mutate(deaths_per_mill = deaths * 1000000 / Population) %>%
  select(Province_State, Country_Region, date,
         cases, deaths, deaths_per_mill, Population) %>%
  ungroup()
```

'summarise()' has grouped output by 'Province_State', 'Country_Region'. You can
override using the '.groups' argument.

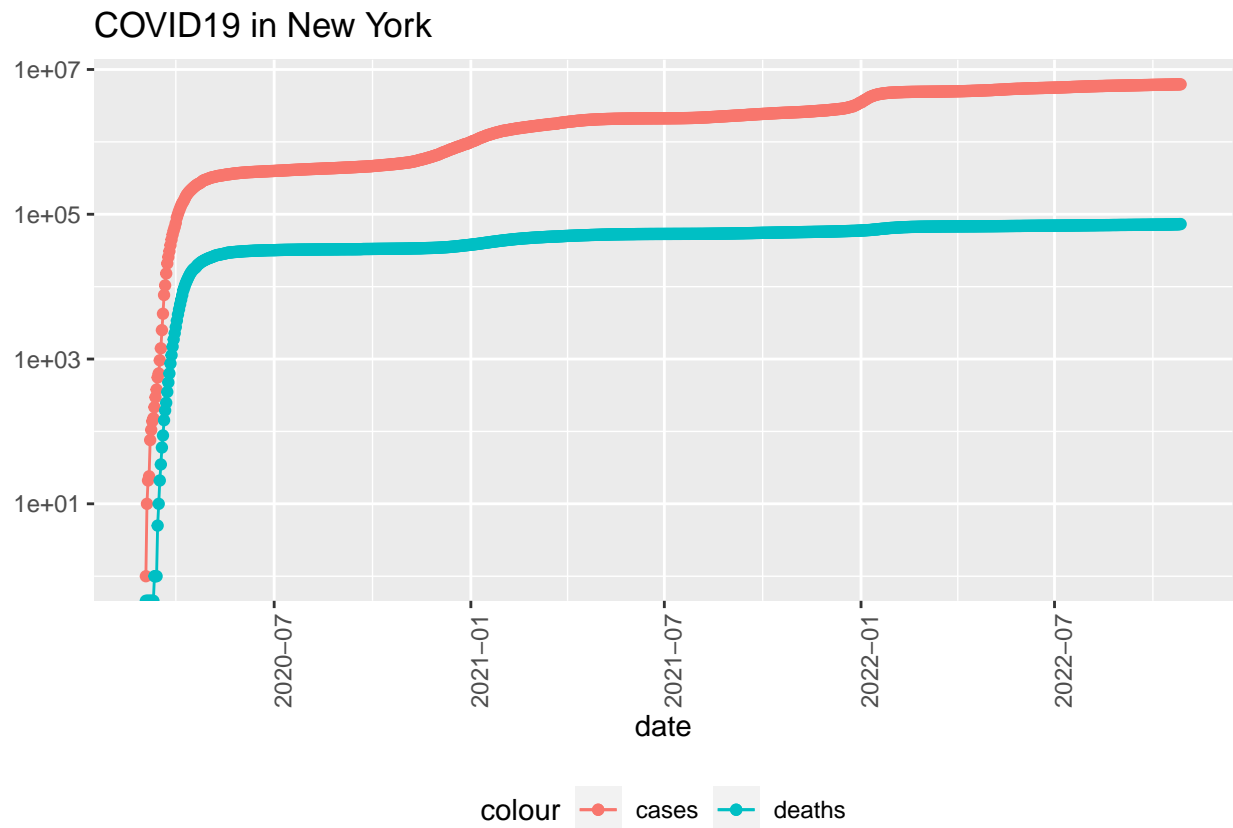
```
US_totals <- US_by_state %>%
  group_by(Country_Region, date) %>%
  summarise(cases = sum(cases), deaths = sum(deaths),
            Population = sum(Population)) %>%
  mutate(deaths_by_mill = deaths * 1000000 / Population) %>%
  ungroup()
```

'summarise()' has grouped output by 'Country_Region'. You can override using
the '.groups' argument.

```
US_totals %>%
  filter(cases > 0) %>%
  ggplot(aes(x = date, y = cases)) +
  geom_line(aes(color = "cases")) +
  geom_point(aes(color = "cases")) +
  geom_line(aes(y = deaths, color = "deaths")) +
  geom_point(aes(y = deaths, color = "deaths")) +
  scale_y_log10() +
  theme(legend.position = "bottom",
        axis.text.x = element_text(angle = 90)) +
  labs(title = "COVID19 in US", y = NULL)
```

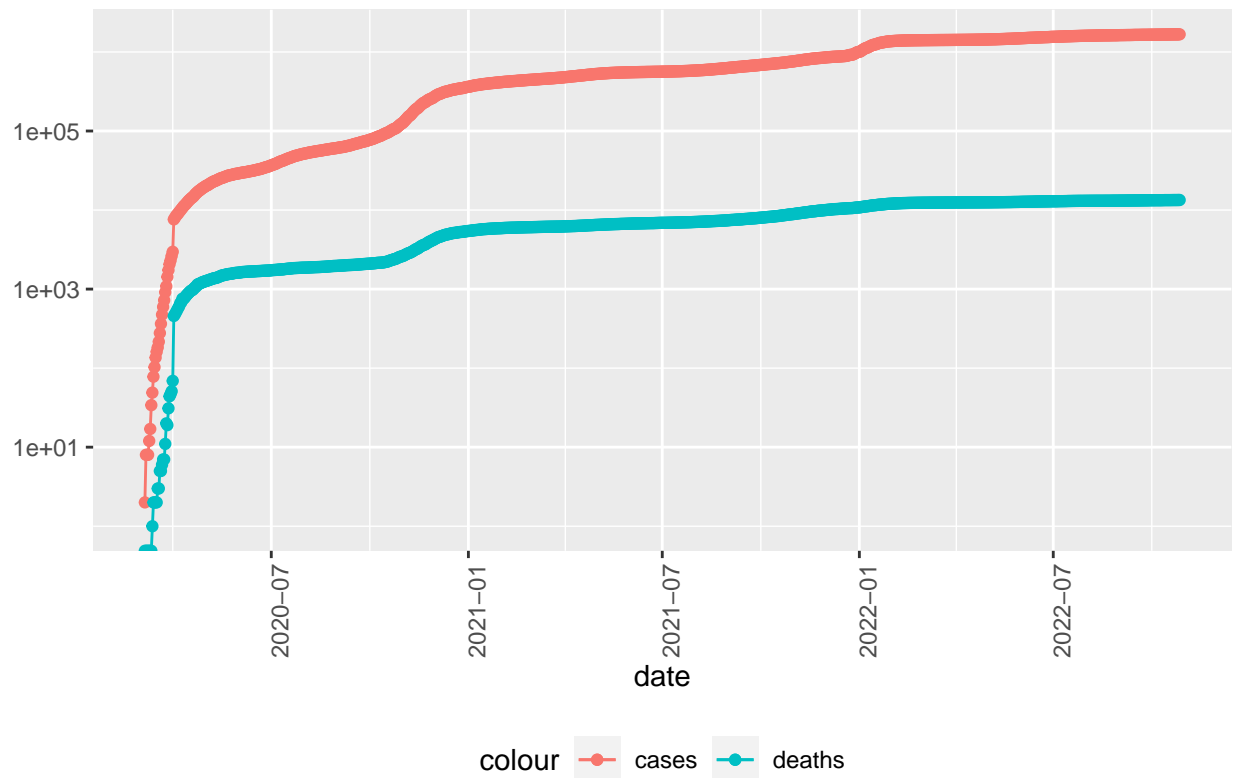


```
state <- "New York"
US_by_state %>%
  filter(Province_State == state) %>%
  filter(cases > 0) %>%
  ggplot(aes(x = date, y = cases)) +
  geom_line(aes(color = "cases")) +
  geom_point(aes(color = "cases")) +
  geom_line(aes(y = deaths, color = "deaths")) +
  geom_point(aes(y = deaths, color = "deaths")) +
  scale_y_log10() +
  theme(legend.position = "bottom",
        axis.text.x = element_text(angle = 90)) +
  labs(title = str_c("COVID19 in ", state), y = NULL)
```



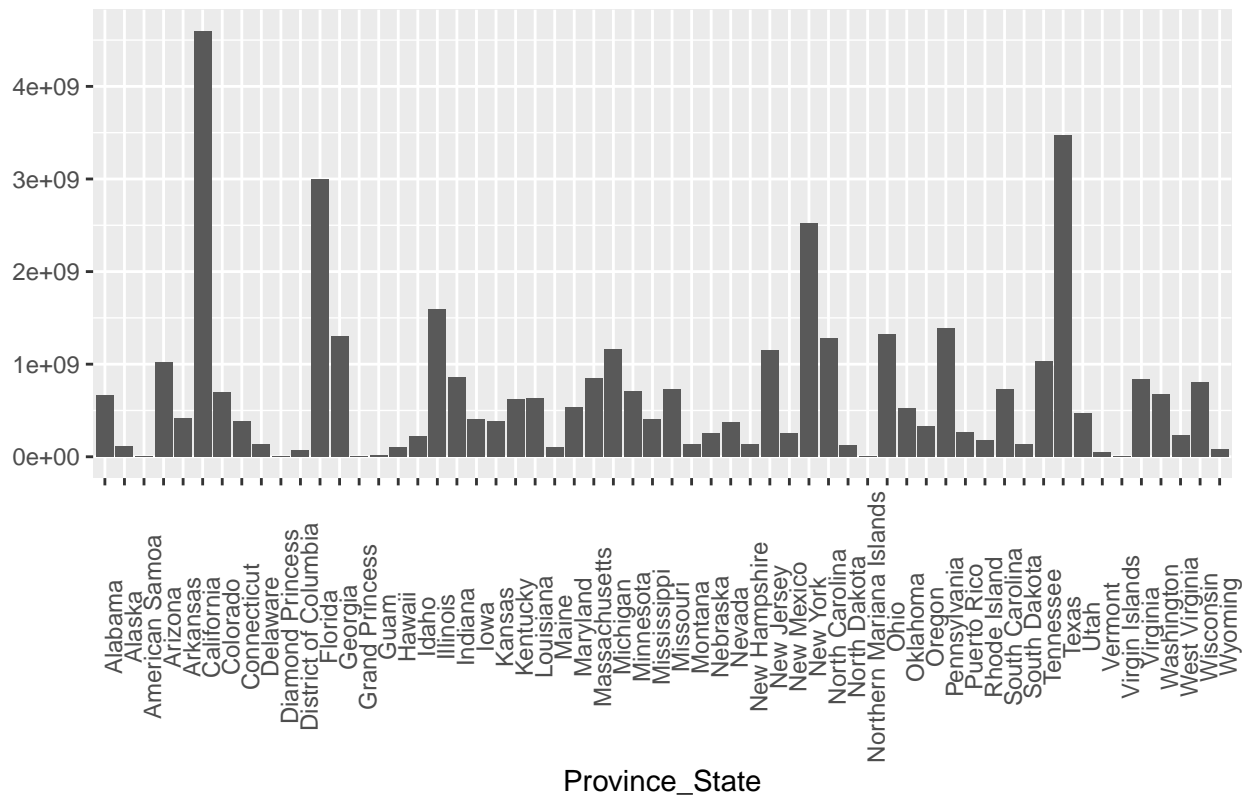
```
state <- "Colorado"
US_by_state %>%
  filter(Province_State == state) %>%
  filter(cases > 0) %>%
  ggplot(aes(x = date, y = cases)) +
  geom_line(aes(color = "cases")) +
  geom_point(aes(color = "cases")) +
  geom_line(aes(y = deaths, color = "deaths")) +
  geom_point(aes(y = deaths, color = "deaths")) +
  scale_y_log10() +
  theme(legend.position = "bottom",
        axis.text.x = element_text(angle = 90)) +
  labs(title = str_c("COVID19 in ", state), y = NULL)
```

COVID19 in Colorado



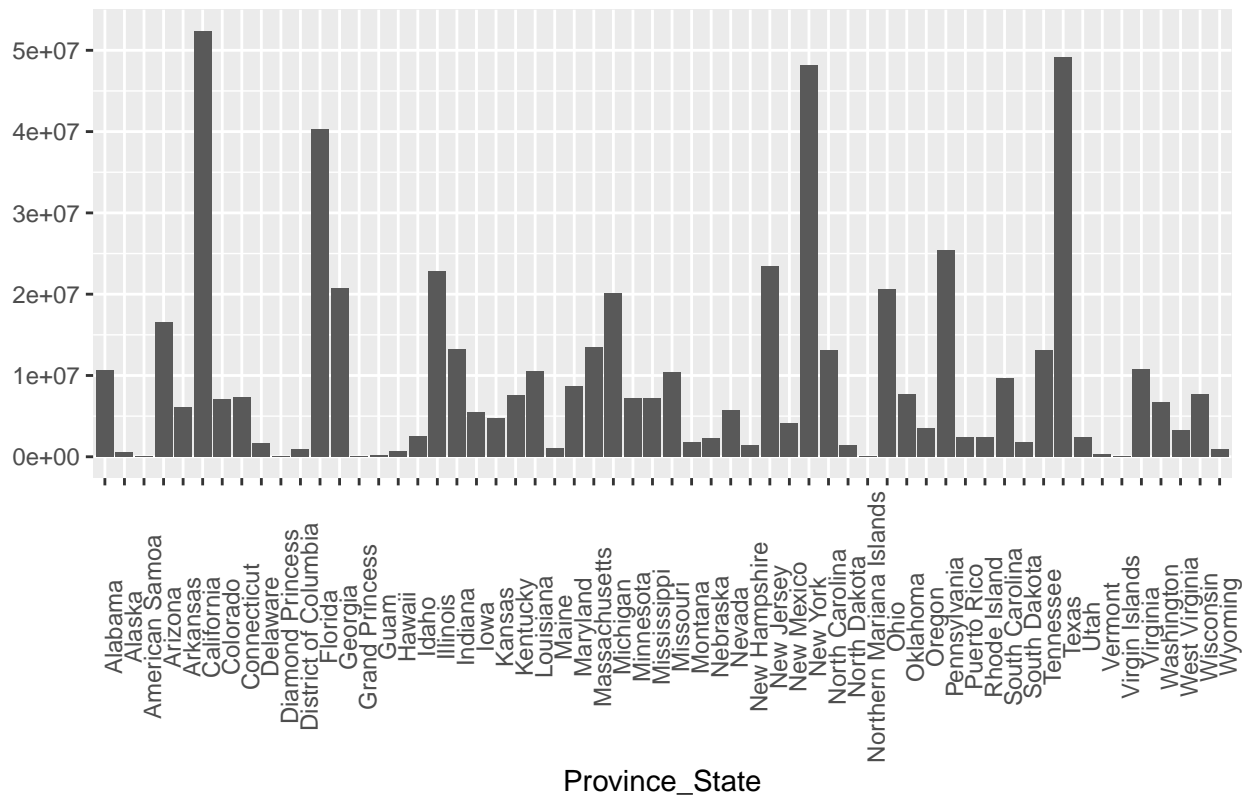
```
g_cases <- ggplot(US_by_state, aes(x = Province_State, y = cases)) +  
  geom_bar(stat = "identity") +  
  theme(axis.text.x = element_text(angle = 90)) +  
  labs(title = "Cases of COVID19 by States", y = NULL)  
plot(g_cases)
```


Cases of COVID19 by States



```
g_deaths <- ggplot(US_by_state, aes(x = Province_State, y = deaths)) +
  geom_bar(stat = "identity") +
  theme(axis.text.x = element_text(angle = 90)) +
  labs(title = "Deaths of COVID19 by States", y = NULL)
plot(g_deaths)
```

Deaths of COVID19 by States



Step 4 - Analyzing Data

I will analyze new cases and deaths for the entire US and New York.

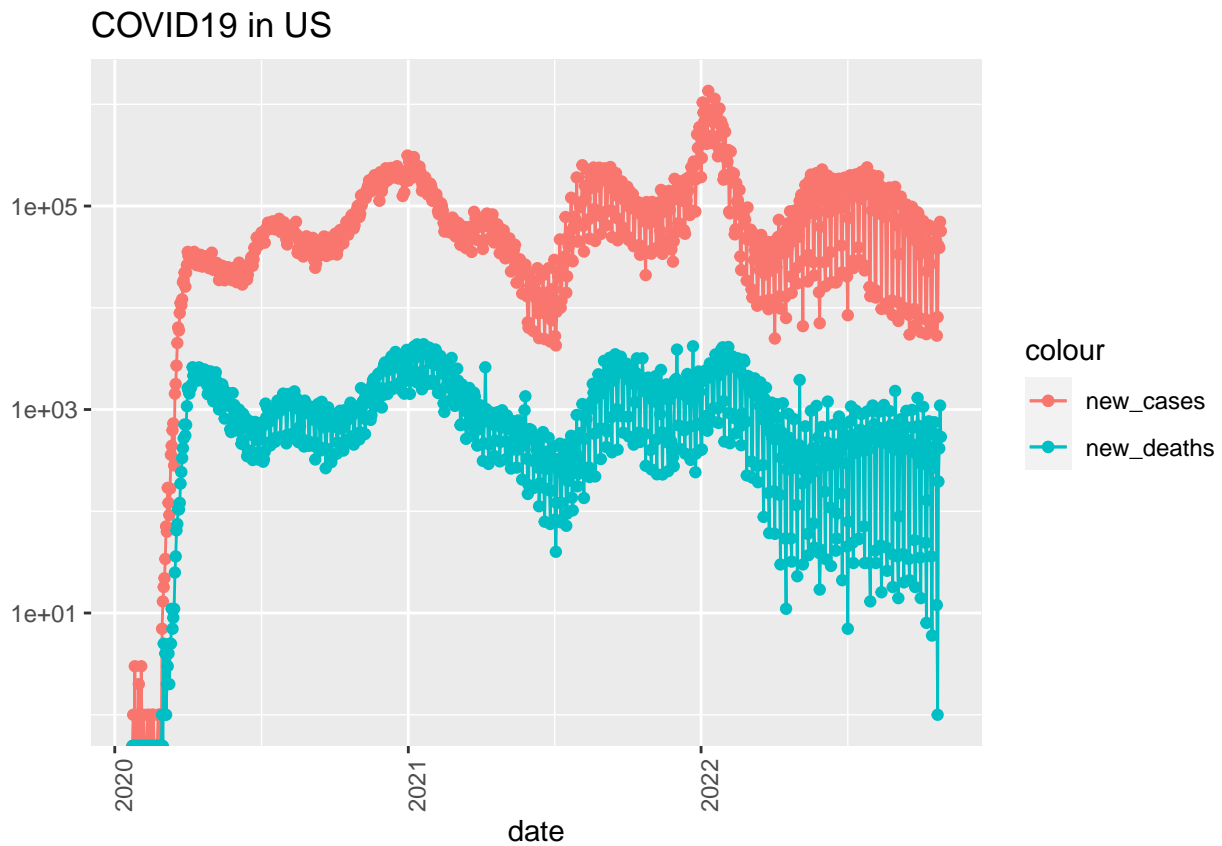
```
uid <- read_csv(uid_lookup_url) %>%
  select(-c(Lat, Long_, Combined_Key, code3, iso2, iso3, Admin2))
```

```
## Rows: 4321 Columns: 12
## -- Column specification -----
## Delimiter: ","
## chr (7): iso2, iso3, FIPS, Admin2, Province_State, Country_Region, Combined_Key
## dbl (5): UID, code3, Lat, Long_, Population
##
## i Use 'spec()' to retrieve the full column specification for this data.
## i Specify the column types or set 'show_col_types = FALSE' to quiet this message.
```

```
US_by_state <- US_by_state %>%
  mutate(new_cases = cases - lag(cases),
         new_deaths = deaths - lag(deaths))
US_totals <- US_totals %>%
  mutate(new_cases = cases - lag(cases),
         new_deaths = deaths - lag(deaths))

US_totals %>%
```

```
ggplot(aes(x = date, y = new_cases)) +
  geom_line(aes(color = "new_cases")) +
  geom_point(aes(color = "new_cases")) +
  geom_line(aes(y = new_deaths, color = "new_deaths")) +
  geom_point(aes(y = new_deaths, color = "new_deaths")) +
  scale_y_log10() +
  theme(axis.text.x = element_text(angle = 90)) +
  labs(title = "COVID19 in US", y = NULL)
```



```
state <- "New York"
US_by_state %>%
  filter(Province_State == state) %>%
  ggplot(aes(x = date, y = new_cases)) +
  geom_line(aes(color = "new_cases")) +
  geom_point(aes(color = "new_cases")) +
  geom_line(aes(y = new_deaths, color = "new_deaths")) +
  geom_point(aes(y = new_deaths, color = "new_deaths")) +
  scale_y_log10() +
  theme(legend.position = "bottom",
        axis.text.x = element_text(angle = 90)) +
  labs(title = str_c("COVID19 in ", state), y = NULL)
```

COVID19 in New York



```
US_state_totals <- US_by_state %>%
  group_by(Province_State) %>%
  summarise(deaths = max(deaths), cases = max(cases),
            Population = max(Population),
            cases_per_thou = 1000 * cases / Population,
            deaths_per_thou = 1000 * deaths / Population) %>%
  filter(cases > 0, Population > 0)

US_state_totals %>%
  slice_min(deaths_per_thou, n = 10) %>%
  select(deaths_per_thou, cases_per_thou, everything())
```

```
## # A tibble: 10 x 6
##   deaths_per_thou cases_per_thou Province_State deaths cases Popul~1
##   <dbl>          <dbl> <chr>          <dbl> <dbl> <dbl>
## 1 0.611          148. American Samoa      34 8.26e3 55641
## 2 0.725          239. Northern Mariana Islands 40 1.32e4 55144
## 3 1.16           217. Virgin Islands      124 2.33e4 107268
## 4 1.19           232. Vermont              740 1.45e5 623989
## 5 1.20           256. Hawaii              1704 3.62e5 1415872
## 6 1.40           261. Puerto Rico         5248 9.79e5 3754939
## 7 1.58           326. Utah                5056 1.05e6 3205958
## 8 1.91           405. Alaska              1413 3.00e5 740995
## 9 1.91           241. Washington         14550 1.84e6 7614893
## 10 1.97           221. Maine               2642 2.97e5 1344212
## # ... with abbreviated variable name 1: Population
```

```
US_state_totals %>%
  slice_max(deaths_per_thou, n = 10) %>%
  select(deaths_per_thou, cases_per_thou, everything())
```

```
## # A tibble: 10 x 6
##   deaths_per_thou cases_per_thou Province_State deaths    cases Population
##           <dbl>         <dbl> <chr>          <dbl>    <dbl>      <dbl>
## 1             4.36           314. Mississippi  12968  933065   2976149
## 2             4.33           314. Arizona      31548 2287886   7278717
## 3             4.32           305. Oklahoma    17100 1208316   3956971
## 4             4.19           313. Alabama     20558 1534287   4903185
## 5             4.19           339. West Virginia  7513  607087   1792147
## 6             4.13           318. Arkansas    12462  959014   3017804
## 7             4.12           299. New Mexico    8633  626714   2096829
## 8             4.11           345. Tennessee   28074 2357243   6829174
## 9             3.93           289. Michigan    39250 2886176   9986857
## 10            3.93           314. New Jersey   34889 2789256   8882190
```

Step 5 - Modeling Data

I will do modeling. First, we perform a correlation analysis between cases and deaths. I also fit the correlation with a linear model. Next, I analyze the autocorrelations and partial autocorrelations of the time series data of new-affected individuals and fit them with a time series model (ARIMA model).

```
mod <- lm(deaths_per_thou ~ cases_per_thou, data = US_state_totals)
summary(mod)
```

```
##
## Call:
## lm(formula = deaths_per_thou ~ cases_per_thou, data = US_state_totals)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -2.3470 -0.6060  0.1230  0.6736  1.1851
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)  -0.285191   0.716159  -0.398   0.692
## cases_per_thou  0.011205   0.002431   4.609 2.52e-05 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.8518 on 54 degrees of freedom
## Multiple R-squared:  0.2823, Adjusted R-squared:  0.269
## F-statistic: 21.24 on 1 and 54 DF,  p-value: 2.518e-05
```

```
US_state_totals %>% slice_min(cases_per_thou)
```

```
## # A tibble: 1 x 6
##   Province_State deaths cases Population cases_per_thou deaths_per_thou
##   <chr>          <dbl> <dbl>    <dbl>          <dbl>          <dbl>
## 1 American Samoa    34  8257    55641          148.           0.611
```

```
US_state_totals %>% slice_max(cases_per_thou)
```

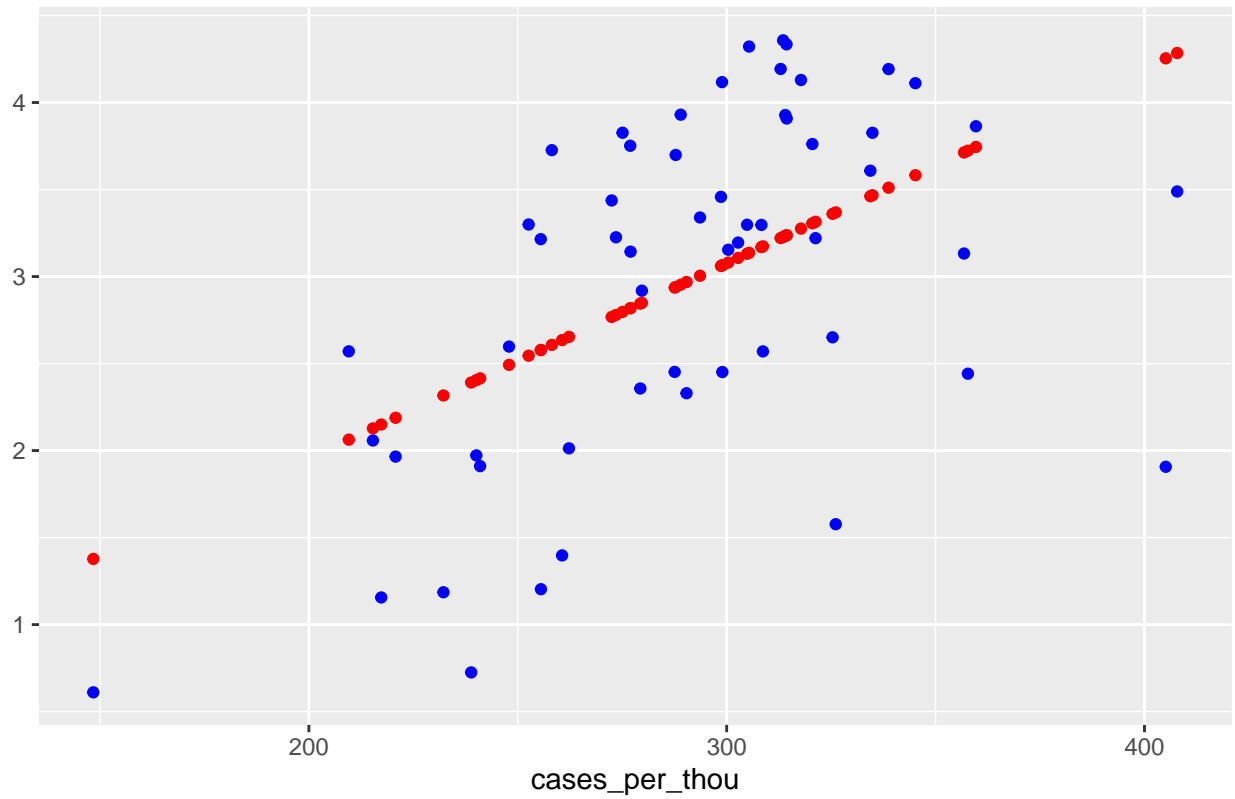
```
## # A tibble: 1 x 6
##   Province_State deaths   cases Population cases_per_thou deaths_per_thou
##   <chr>          <dbl>  <dbl>      <dbl>          <dbl>          <dbl>
## 1 Rhode Island    3696 432042   1059361          408.            3.49
```

```
x_grid <- seq(1, 451)
new_df <- tibble(cases_per_thou = x_grid)
US_state_totals %>% mutate(pred = predict(mod))
```

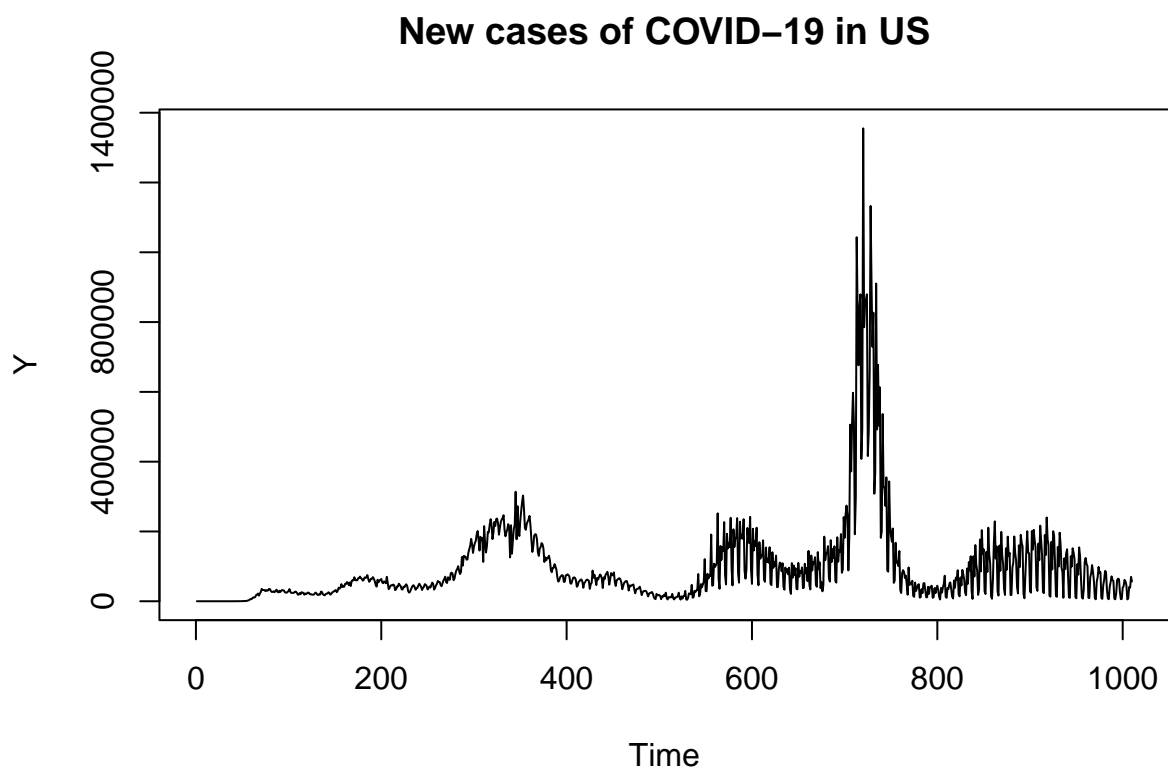
```
## # A tibble: 56 x 7
##   Province_State   deaths   cases Population cases_per_thou deaths~1  pred
##   <chr>          <dbl>   <dbl>      <dbl>          <dbl>    <dbl> <dbl>
## 1 Alabama        20558 1534287   4903185          313.     4.19  3.22
## 2 Alaska          1413   300177    740995          405.     1.91  4.25
## 3 American Samoa     34    8257     55641          148.     0.611 1.38
## 4 Arizona        31548 2287886   7278717          314.     4.33  3.24
## 5 Arkansas        12462  959014   3017804          318.     4.13  3.28
## 6 California       96886 11362031  39512223          288.     2.45  2.94
## 7 Colorado        13415 1672312   5758736          290.     2.33  2.97
## 8 Connecticut     11462  910919   3565287          255.     3.21  2.58
## 9 Delaware         3136  312850   973764          321.     3.22  3.31
## 10 District of Columbia 1392  169436   705749          240.     1.97  2.40
## # ... with 46 more rows, and abbreviated variable name 1: deaths_per_thou
```

```
US_tot_w_pred <- US_state_totals %>% mutate(pred = predict(mod))
US_tot_w_pred %>% ggplot() +
  geom_point(aes(x = cases_per_thou, y = deaths_per_thou), color = "blue") +
  geom_point(aes(x = cases_per_thou, y = pred), color = "red") +
  labs(title = "Linear Modeling of Cases and Deaths of COVID19", y = NULL)
```

Linear Modeling of Cases and Deaths of COVID19

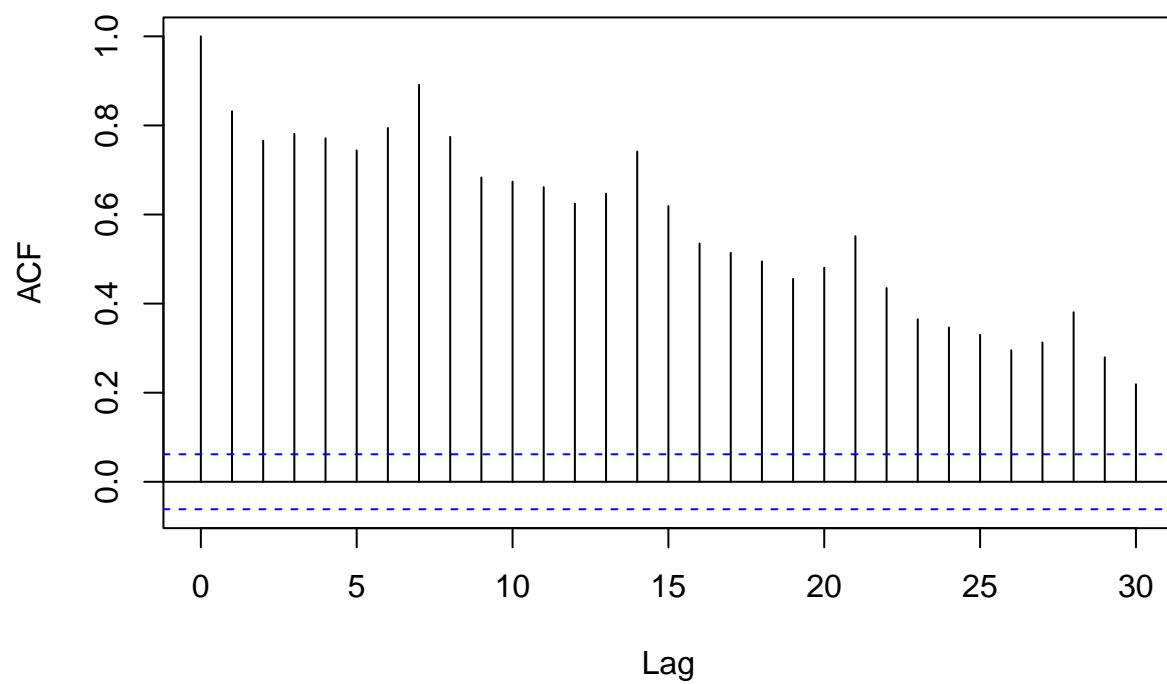


```
Y <- US_totals$new_cases  
Y[is.na(Y)] <- 0  
ts.plot(Y, main = "New cases of COVID-19 in US")
```



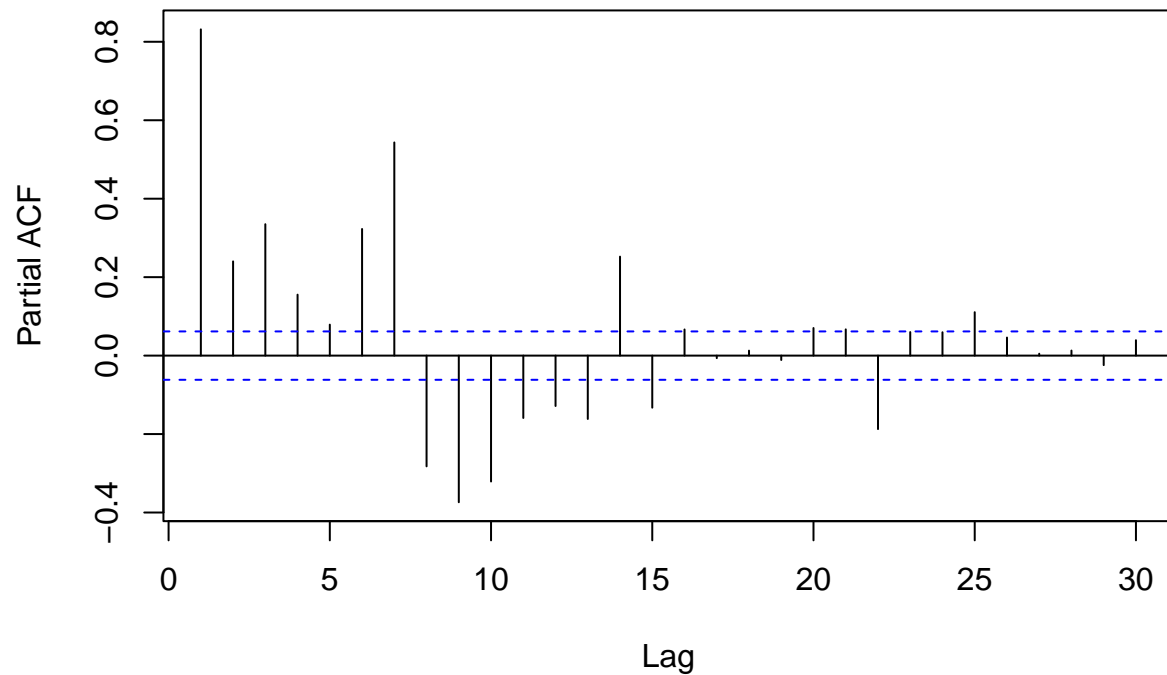
```
acf(Y, main = "Auto-correlation of New cases")
```


Auto-correlation of New cases



```
pacf(Y, main = "Partial Auto-correlation of New cases")
```

Partial Auto-correlation of New cases



```
auto.arima(Y, ic="aic", stepwise=T, trace=T)
```

```
##
## Fitting models using approximations to speed things up...
##
## ARIMA(2,1,2) with drift      : 24991.5
## ARIMA(0,1,0) with drift      : 25550.64
## ARIMA(1,1,0) with drift      : 25455.35
## ARIMA(0,1,1) with drift      : 25254.16
## ARIMA(0,1,0)                 : 25548.64
## ARIMA(1,1,2) with drift      : 25212.4
## ARIMA(2,1,1) with drift      : 25204.45
## ARIMA(3,1,2) with drift      : Inf
## ARIMA(2,1,3) with drift      : 25043.07
## ARIMA(1,1,1) with drift      : 25240.45
## ARIMA(1,1,3) with drift      : 25043.83
## ARIMA(3,1,1) with drift      : 25206.84
## ARIMA(3,1,3) with drift      : 24994.04
## ARIMA(2,1,2)                 : 24989.5
## ARIMA(1,1,2)                 : 25210.41
## ARIMA(2,1,1)                 : 25202.45
## ARIMA(3,1,2)                 : Inf
## ARIMA(2,1,3)                 : 25041.08
## ARIMA(1,1,1)                 : 25238.46
## ARIMA(1,1,3)                 : 25041.83
```

```
## ARIMA(3,1,1) : 25204.85
## ARIMA(3,1,3) : 24992.04
##
## Now re-fitting the best model(s) without approximations...
##
## ARIMA(2,1,2) : 25013.06
##
## Best model: ARIMA(2,1,2)

## Series: Y
## ARIMA(2,1,2)
##
## Coefficients:
##          ar1          ar2          ma1          ma2
##          0.9311   -0.5715   -1.6357   0.9001
## s.e.    0.0290    0.0335    0.0129   0.0161
##
## sigma^2 = 3.387e+09: log likelihood = -12501.53
## AIC=25013.06 AICc=25013.12 BIC=25037.64
```

Conclusions

- US COVID-19 cases are increasing exponentially, and so are the deaths. Since the middle of 2020, it has been increasing continuously, although not exponentially.
- I looked at the cases in New York and Colorado, the trend is similar across the US.
- By state, California, Texas, New York, and Florida have the most cases and deaths.
- Focusing on new cases and deaths, both will level off from the middle of 2020.
- There is a loose positive correlation between the cases and the deaths.
- From ACF, the order of the MR model is likely to be more than 30 days, and the order of the AR model is likely to be more than half a month. However, the best ARIMA model was (2, 1, 2).

Bias include the distribution of PCR test kits. In developed countries such as the US, it is possible to receive sufficient PCR tests and measure the number of infected people, but in developing countries, there is a possibility that accurate numbers cannot be obtained due to the lack of PCR test kits. Also, within the US, it is conceivable that the status of COVID-19 testing will change as a function of income. A certain number of low-income people are likely to be sick or die without being tested for COVID-19.

Therefore, for a more objective analysis, it is necessary to correct the bias while looking at trends in the number of deaths other than COVID-19 in the future.

```
sessionInfo()
```

```
## R version 4.2.1 (2022-06-23 ucrt)
## Platform: x86_64-w64-mingw32/x64 (64-bit)
## Running under: Windows 10 x64 (build 22621)
##
## Matrix products: default
##
## locale:
## [1] LC_COLLATE=Japanese_Japan.utf8 LC_CTYPE=Japanese_Japan.utf8
## [3] LC_MONETARY=Japanese_Japan.utf8 LC_NUMERIC=C
## [5] LC_TIME=Japanese_Japan.utf8
##
```

```

## attached base packages:
## [1] stats      graphics  grDevices utils      datasets  methods   base
##
## other attached packages:
## [1] forecast_8.18  lubridate_1.8.0 forcats_0.5.2  stringr_1.4.1
## [5] dplyr_1.0.9    purrr_0.3.4    readr_2.1.2    tidyr_1.2.0
## [9] tibble_3.1.8   ggplot2_3.3.6  tidyverse_1.3.2
##
## loaded via a namespace (and not attached):
## [1] tseries_0.10-52  httr_1.4.4      bit64_4.0.5
## [4] vroom_1.5.7      jsonlite_1.8.0  modelr_0.1.9
## [7] assertthat_0.2.1 TTR_0.24.3      highr_0.9
## [10] googlesheets4_1.0.1 cellranger_1.1.0 yaml_2.3.5
## [13] pillar_1.8.1     backports_1.4.1 lattice_0.20-45
## [16] glue_1.6.2       quadprog_1.5-8  digest_0.6.29
## [19] rvest_1.0.3      colorspace_2.0-3 htmltools_0.5.3
## [22] timeDate_4021.106 pkgconfig_2.0.3 broom_1.0.1
## [25] haven_2.5.1      scales_1.2.1    tzdb_0.3.0
## [28] googledrive_2.0.0 farver_2.1.1     generics_0.1.3
## [31] ellipsis_0.3.2   withr_2.5.0     urca_1.3-3
## [34] nnet_7.3-17      cli_3.3.0       quantmod_0.4.20
## [37] magrittr_2.0.3   crayon_1.5.1    readxl_1.4.1
## [40] evaluate_0.16    fs_1.5.2        fansi_1.0.3
## [43] nlme_3.1-157     xts_0.12.1      xml2_1.3.3
## [46] tools_4.2.1      hms_1.1.2       gargle_1.2.0
## [49] lifecycle_1.0.1  munsell_0.5.0   reprex_2.0.2
## [52] compiler_4.2.1   rlang_1.0.4     grid_4.2.1
## [55] rstudioapi_0.14  labeling_0.4.2  rmarkdown_2.16
## [58] gtable_0.3.0     fracdiff_1.5-1  DBI_1.1.3
## [61] curl_4.3.2       R6_2.5.1        zoo_1.8-11
## [64] knitr_1.40       bit_4.0.4       fastmap_1.1.0
## [67] utf8_1.2.2       stringi_1.7.8   parallel_4.2.1
## [70] Rcpp_1.0.9       vctrs_0.4.1     dbplyr_2.2.1
## [73] tidyselect_1.1.2 xfun_0.32       lmtest_0.9-40

```