## **030 Partial Computations**

This exercise set assumes that you have read chapters 1–4 of [Chiusano, Bjarnason 2015]. Exercises marked [–] are meant to be easy, and can be skipped by students that already know functional programming and feel comfortable.

Solve the exercises in the file Exercises.scala, inline. This is the only file you shall need to hand in. Uncomment function declarations as you proceed. In the bottom of the file you can find tests, to check your solutions. Uncomment them as you go. Make sure that you understand the test cases, and try to add some yourself to confirm understanding.

We start with few simple exercises on ADTs and traits (Chapter 3), before we proceed to Chapter 4. First, we see how to use traits to implement dependency injection in existing code base. Then, we have a second look at simple ADTs using trees. In Chapter 4, we experience advanced functional programming for the first time (especially using map, flatMap, for-comprehensions, sequence and traverse with partial computations encapsulated in Option values).

As usual, do not use variables, side effects, exceptions or return statements. Additionally, avoid using pattern matching in Exercises from Chapter 4, if possible. Once you implemented monadic API for your ADT, you should not need to use pattern matching much.

The entire exercise set is normed to take about **4-6 hours** of intensive and focused programming. All functions are very short (most of them one line long, but require careful attention to formulate).

**Exercise 1.** This exercise is not about functional programming, but about traits (a feature of Scala that is independent of functional programming). We will use it to obtain a simple form of dependency injection. We will extend an existing class java.awt.Point with a new set of operators (comparisons).

Define a trait OrderedPoint extending the generic scala.math.Ordered[Point]. Implement the missing method compare from Ordered[Point], using the lexicographic ordering, i.e. (x,y) < (x',y') iff x < x' or  $x = x' \land y < y'$ .

You will need to restrict the trait to only be allowed to be mixed into subclassess of java.awt.Point to access the x and y components of the objects. This is done by inserting the following constraint in the beginning of the trait block: "this :java.awt.Point =>" (Google for trait's self-types if you want to know more about these constraints).

Now mix the new java.awt.Point into java.awt.Point and create some ad hoc point objects using this mixin. Test the extension in the Scala REPL by comparing some point instances using the less than (<) operator.<sup>1</sup>

This way, we can use infix comparison operators this way with classes that were defined in the java.awt package long before Scala existed, without modifying their source or recompiling them.

Exercise 2[-]. Write a function size that counts the number of nodes (leaves and branches) in a tree.<sup>2</sup>

Exercise 3[-]. Write a function maximum that returns the maximum element in a Tree[Int]. Note: In Scala, you can use x.max(y) or x max y to compute the maximum of two integers x and y.

<sup>&</sup>lt;sup>1</sup>A variation of Exercise 10.2 [Horstmann 2012]

<sup>&</sup>lt;sup>2</sup>Exercise 3.25 [Chiusano, Bjarnason 2014]

<sup>&</sup>lt;sup>3</sup>Exercise 3.26 [Chiusano, Bjarnason 2014]

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Exercise 4 [–]. Write a function map, analogous to the method of the same name on List, that modifies each element in a tree with a given function.<sup>4</sup>

**Exercise 5.** Generalize size, maximum, and map, writing a new function fold that abstracts over their similarities. Reimplement them in terms of this more general function.<sup>5</sup>

**Exercise 6.** Implement map, getOrElse, flatMap, orElse, filter on Option. As you implement each function, try to think about what it means and in what situations you'd use it. Refer to the book's Chapter 4, and Exercise 4.1 for hints and context information, if you do not know what to do.<sup>6</sup>

Exercise 7. Implement the variance function in terms of flatMap. If the mean of a sequence is m, the variance is the mean of math.pow(x - m, 2) for each element x in the sequence.

This is a realistic exercise, in the sense that a variance computation, is something that you could need to implement in a machine learning or a data analytics application. Don't use pattern matching in this exercise (use the isEmpty method if you need to see if a sequence is empty). You will have (likely your first) chance to experience a computation in a monad.

If you feel comfortable with functional programming this is a good point to start experimenting with for-comprehensions. Try to write your implementation using for-comprehensions, without using flatMap (using List.map is OK to use here). Once succeeded, reflect whether this code is more readable than the code using flatMap directly. Notice that, it looks strangely similar to imperative code in Scala/Java/C#...

On the other hand, if you are overwhelmed, you can skip the for-comprehensions for now, and revisit this (and similar exercises) in a week or two.

**Exercise 8.** Write a generic function map2 that combines two Option values using a binary function. If either Option value is None, then the return value is None too. Do not use pattern matching in this exercise.<sup>8</sup>

The exercise makes much more sense if you read section 4.3.2 in the book, until the Exercise 4.3.

After you are done, have a look in the end of Section 4.3 in how this can be rewritten using for-comprehensions in Scala.

**Exercise 9.** Write a function sequence that combines a list of Options into one Option containing a list of all the Some values in the original list. If the original list contains None even once, the result of the function should be None; otherwise the result should be Some with a list of all the values. Do not use pattern matching, and recall that you have foldRight available on lists. A solution fits a (longish) single line.

NB1. This function captures a very realistic situation, where you have a bunch of results from computations that may fail, and the entire list has no value to you, if at least one of these has failed. So sequence handles 'exceptions' in bulk in functional style. This function sequences computations in the Option monad. We shall see more interesting instances of sequencing later on, and eventually a formal definition of a monad in the end of the course.

<sup>&</sup>lt;sup>4</sup>Exercise 3.28 [Chiusano, Bjarnason 2014]

<sup>&</sup>lt;sup>5</sup>Exercise 3.29 [Chiusano, Bjarnason 2014]

<sup>&</sup>lt;sup>6</sup>Exercise 4.1 [Chiusano, Bjarnason 2014]

<sup>&</sup>lt;sup>7</sup>Exercise 4.2 [Chiusano, Bjarnason 2014]

<sup>&</sup>lt;sup>8</sup>Exercise 4.3 [Chiusano, Bjarnason 2014]

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NB2. This is an example, where it seems inappropriate to define the function as a method in the object-oriented style. The function sequence likely should not be a method on a List, as this would tangle List to Option, which appears not very natural. Sequencing partial computations belongs better with Option, which is concerned with partial computations. However, sequence cannot be a method on Option as its argument is List! Thus we put it in companion object of Option.<sup>9</sup>

## **Exercise 10.** Implement function traverse:

```
def traverse[A,B] (a: List[A]) (f: A =>Option[B]) :Option[List[B]]
```

The function should behave like a map executed sequentially on the list a, but in this case the mapped function f can fail. If at least one application fails, then the entire computation of the mapping (traversal) should fail.

It is straightforward to do using map and sequence, but try for a more efficient implementation that only looks at the list once (Incidentally, sequence can be implemented in terms traverse, but we shall skip that part of the exercise from the textbook).<sup>10</sup>

<sup>&</sup>lt;sup>9</sup>Exercise 4.4 [Chiusano, Bjarnason 2014]

<sup>&</sup>lt;sup>10</sup>Exercise 4.5 [Chiusano, Bjarnason 2014]