# Lecture 10: Recurrent Neural Networks

### Administrative

- Project proposal grades should be out by now
  - If concerned, come to my office hours.

### Administrative

- A2 is due Friday April 30th, 11:59pm

### Administrative: Midterm

Covers material through Lecture 10 (Thu April 29).

- Tues, **May 4** and is worth **15%** of your grade.
- available for **24 hours** on Gradescope from May 4, **12PM PDT** to May 5, 11:59 AM PDT.
- 3-hour consecutive timeframe
- Exam will be designed for **1.5 hours**.
- Open book and open internet but no collaboration
- Only make private posts during those 24 hours

### Administrative

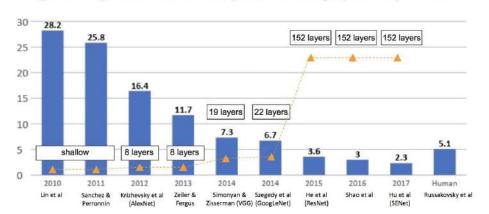
Midterm review session: Fri April 30th discussion section

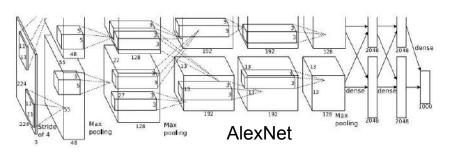
Sample midterm has been released on Piazza.

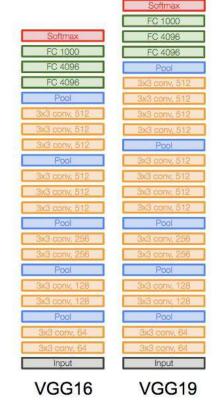
**OAE accommodations**: If you have not received an email from us, please reach out to the staff mailing list ASAP.

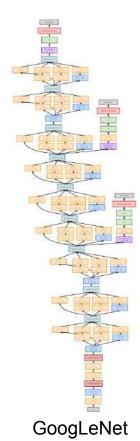
#### Last Time: CNN Architectures

ImageNet Large Scale Visual Recognition Challenge (ILSVRC) winners





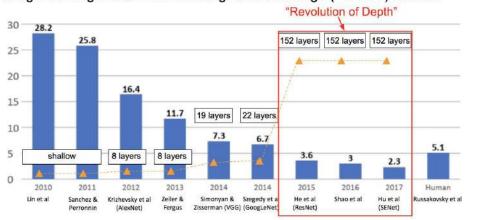


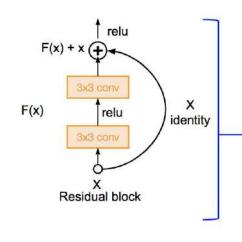


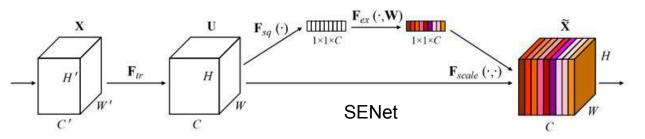
Let's jump to lecture 9 - slide 106

#### Last Time: CNN Architectures

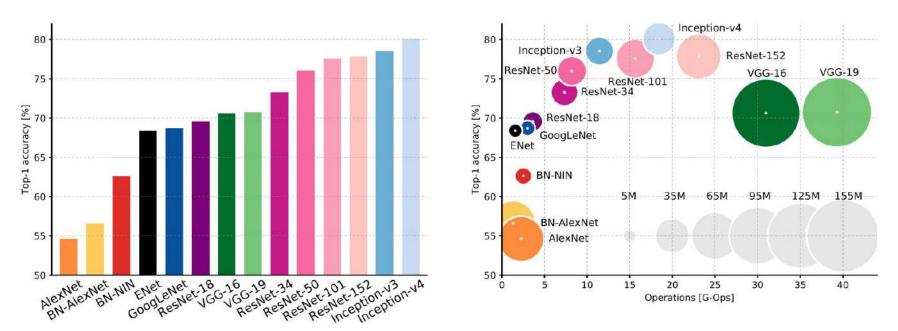
ImageNet Large Scale Visual Recognition Challenge (ILSVRC) winners







#### Comparing complexity...

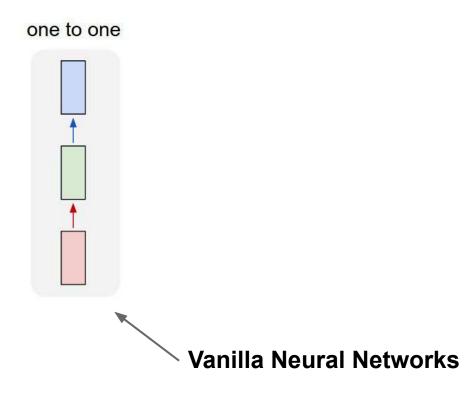


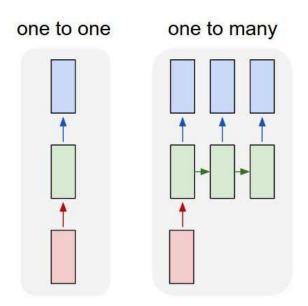
An Analysis of Deep Neural Network Models for Practical Applications, 2017.

Figures copyright Alfredo Canziani, Adam Paszke, Eugenio Culurciello, 2017. Reproduced with permission.

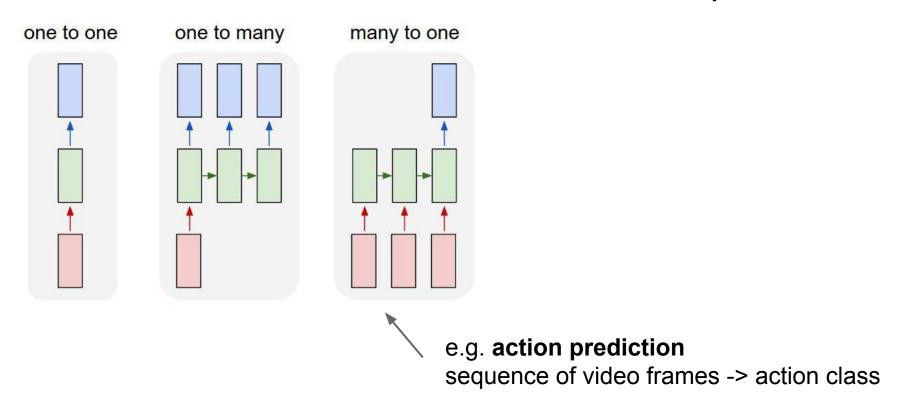
Today: Recurrent Neural Networks

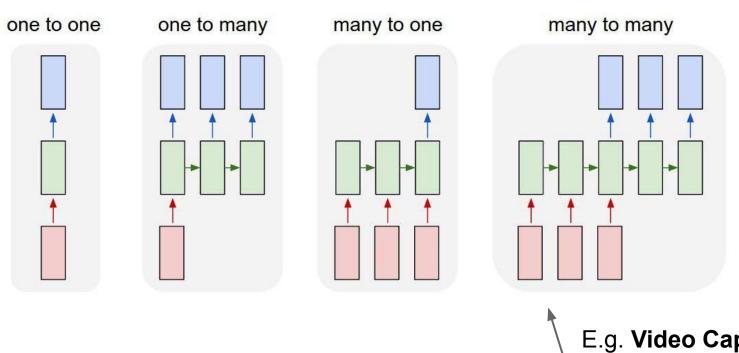
#### "Vanilla" Neural Network



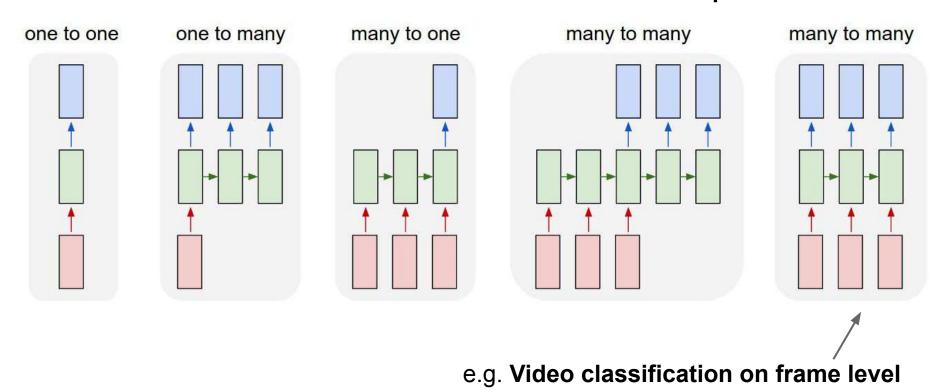


e.g. **Image Captioning** image -> sequence of words





E.g. **Video Captioning**Sequence of video frames -> caption



#### Sequential Processing of Non-Sequence Data

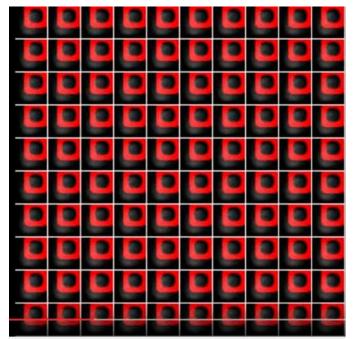
Classify images by taking a series of "glimpses"

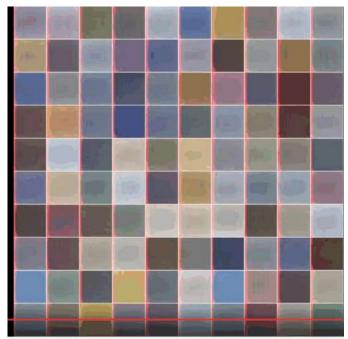


Ba, Mnih, and Kavukcuoglu, "Multiple Object Recognition with Visual Attention", ICLR 2015. Gregor et al, "DRAW: A Recurrent Neural Network For Image Generation", ICML 2015 Figure copyright Karol Gregor, Ivo Danihelka, Alex Graves, Danilo Jimenez Rezende, and Daan Wierstra, 2015. Reproduced with permission.

#### Sequential Processing of Non-Sequence Data

Generate images one piece at a time!





Gregor et al, "DRAW: A Recurrent Neural Network For Image Generation", ICML 2015 Figure copyright Karol Gregor, Ivo Danihelka, Alex Graves, Danilo Jimenez Rezende, and Daan Wierstra, 2015. Reproduced with permission.

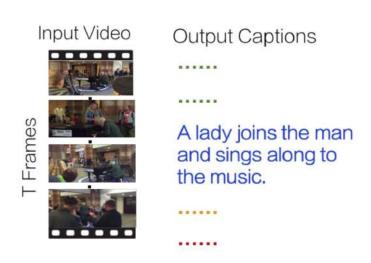
## Why existing convnets are insufficient?

Variable sequence length inputs and outputs!

Example task: video captioning

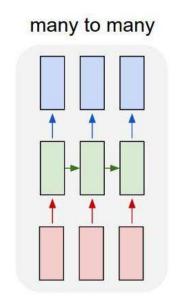
**Input** video can have variable number of frames

Output captions can be variable length.

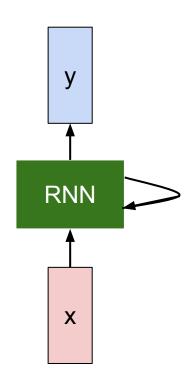


Krishna, Hata, Ren, Fei-Fei, Niebles. Dense captioning Events in Videos. ICCV 2019

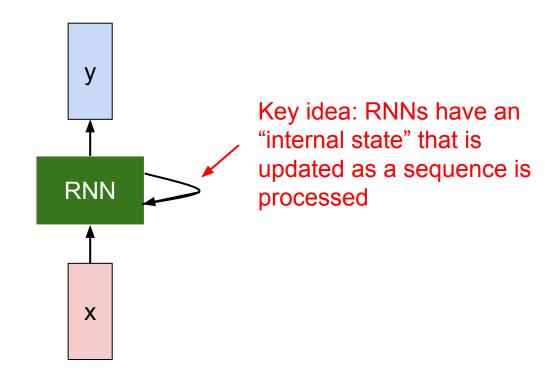
Let's start with a task that takes a variable input and produces an output at every step



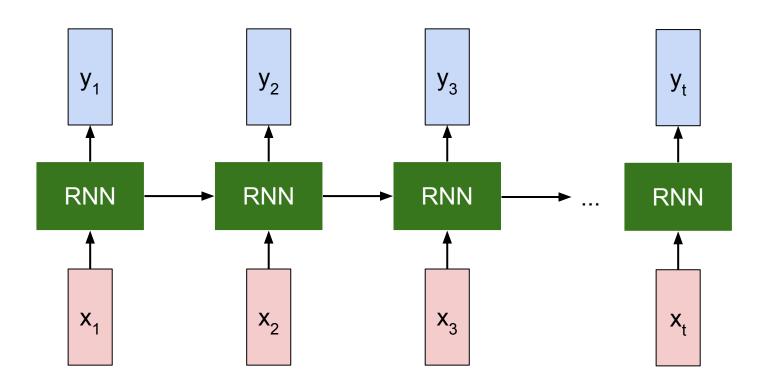
### Recurrent Neural Network



#### Recurrent Neural Network



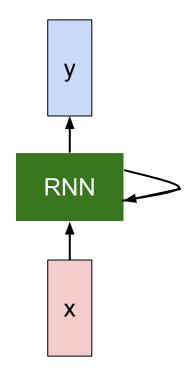
### **Unrolled RNN**



# RNN hidden state update

We can process a sequence of vectors **x** by applying a **recurrence formula** at every time step:

$$h_t = f_W(h_{t-1}, x_t)$$
 new state  $\int$  old state input vector at some time step some function with parameters W

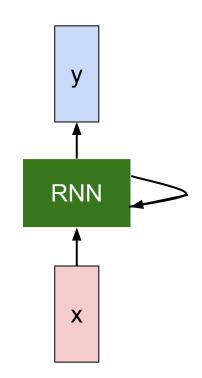


# RNN output generation

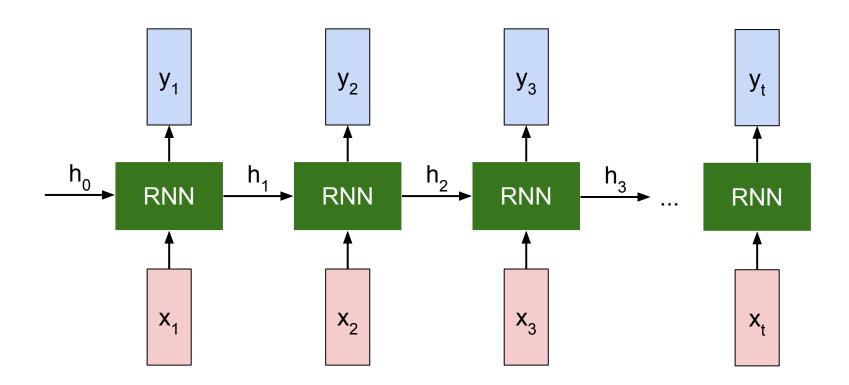
We can process a sequence of vectors **x** by applying a **recurrence formula** at every time step:

output = 
$$f_{W_{hy}}(h_t)$$
output new state

another function
with parameters  $W_0$ 



#### Recurrent Neural Network

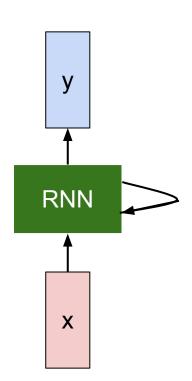


#### Recurrent Neural Network

We can process a sequence of vectors **x** by applying a **recurrence formula** at every time step:

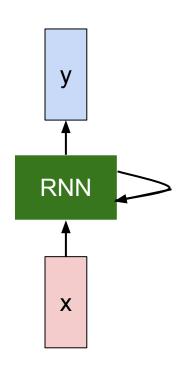
$$h_t = f_W(h_{t-1}, x_t)$$

Notice: the same function and the same set of parameters are used at every time step.



# (Simple) Recurrent Neural Network

The state consists of a single "hidden" vector h:

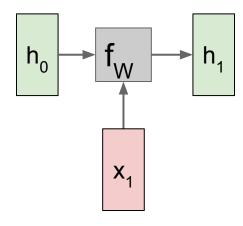


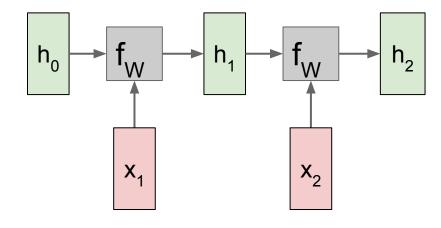
$$h_t = f_W(h_{t-1}, x_t)$$

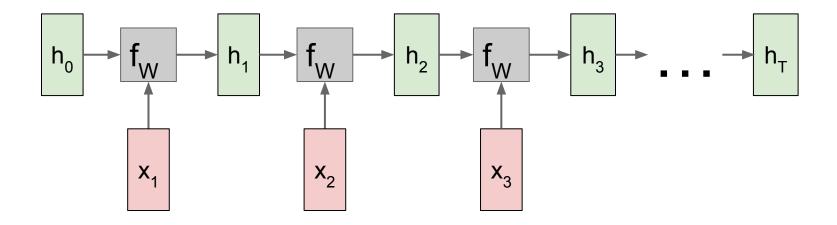
$$h_t = anh(W_{hh}h_{t-1} + W_{xh}x_t)$$

$$y_t = W_{hy} h_t$$

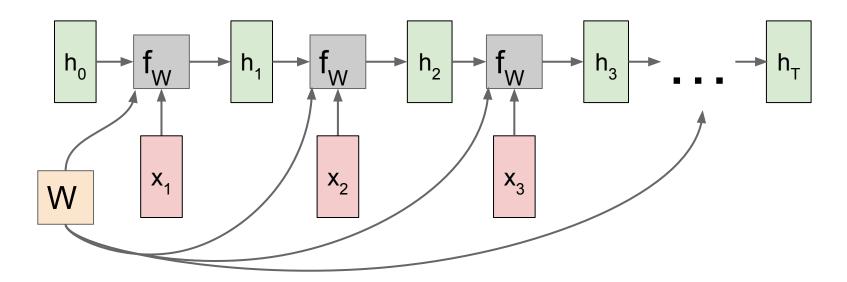
Sometimes called a "Vanilla RNN" or an "Elman RNN" after Prof. Jeffrey Elman



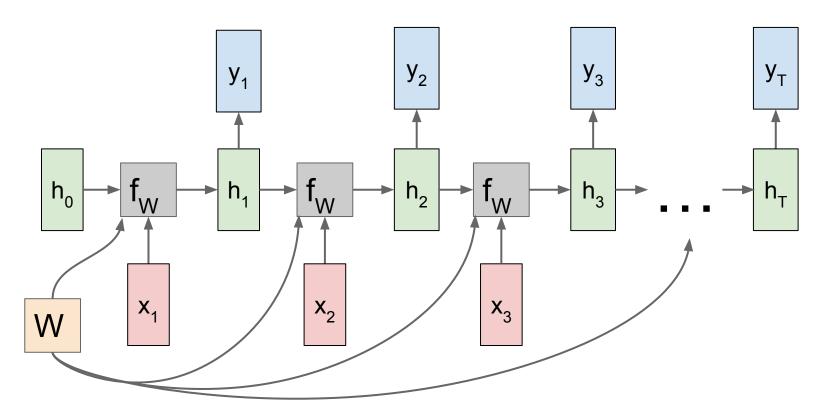




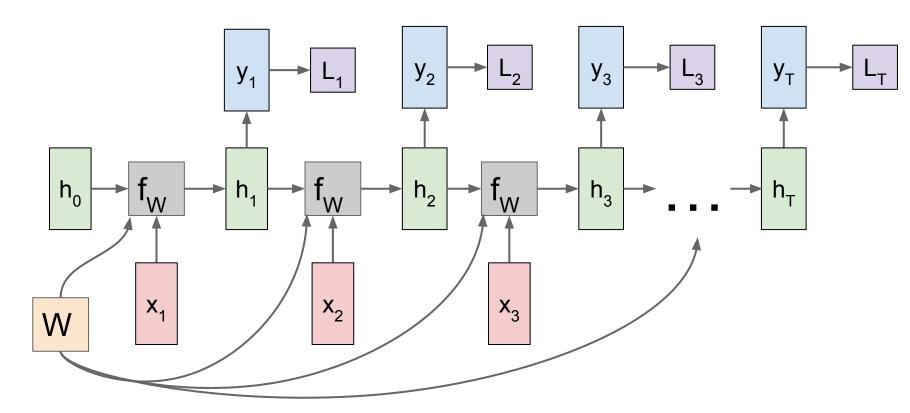
Re-use the same weight matrix at every time-step

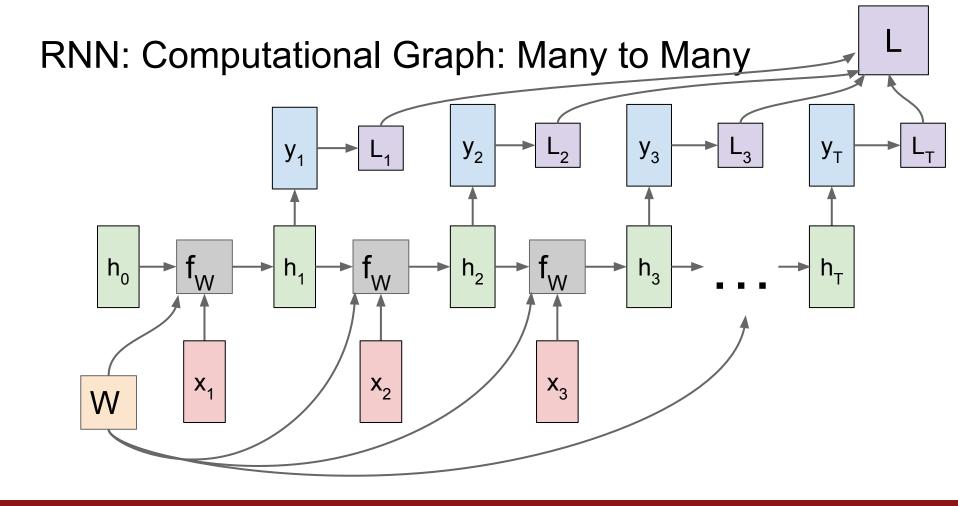


#### RNN: Computational Graph: Many to Many

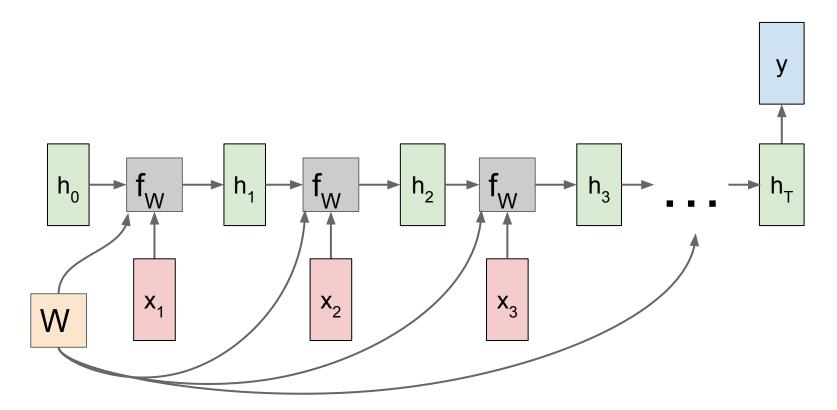


#### RNN: Computational Graph: Many to Many

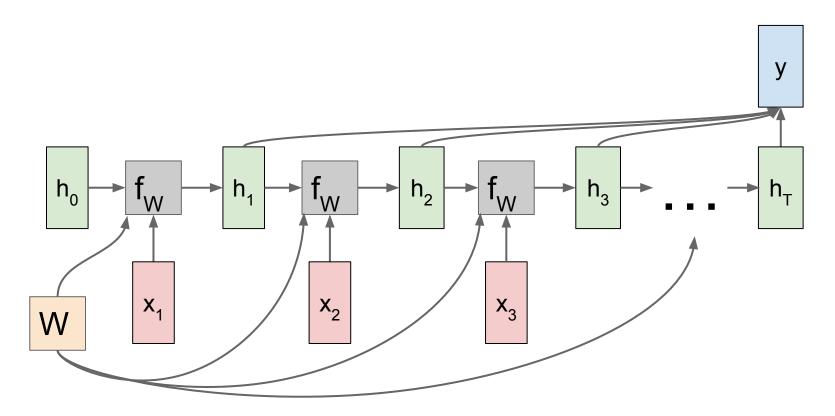


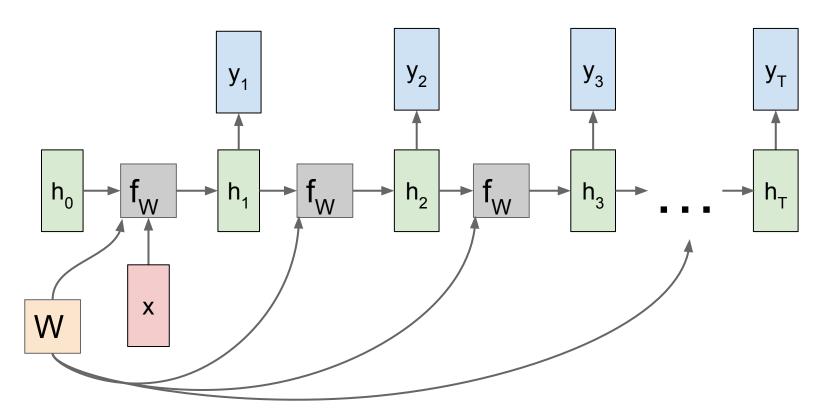


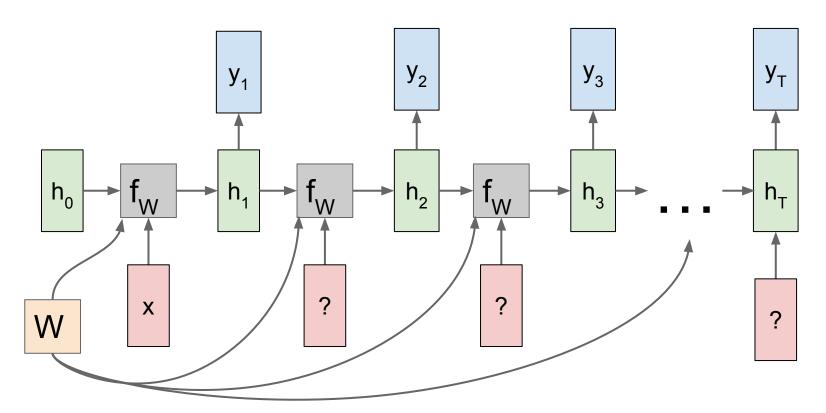
#### RNN: Computational Graph: Many to One

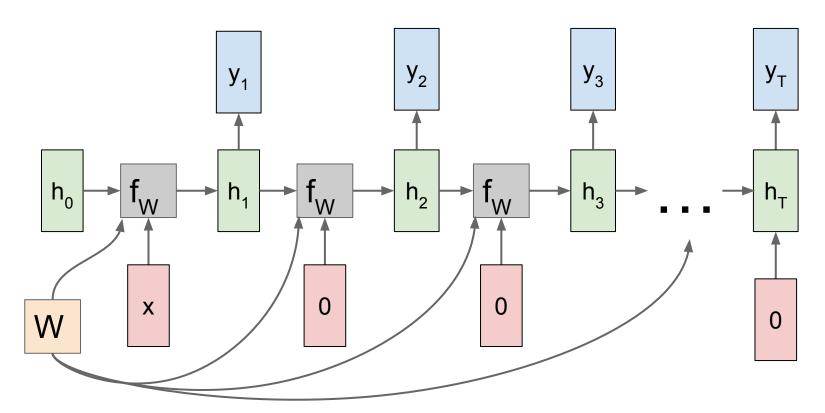


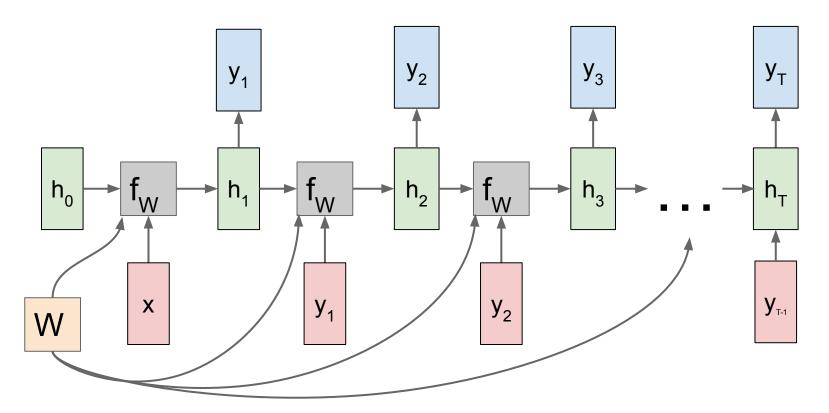
#### RNN: Computational Graph: Many to One





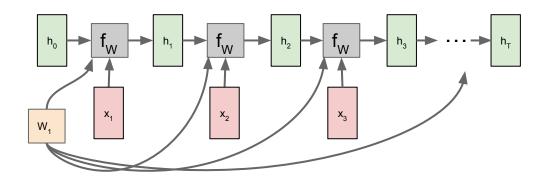






## Sequence to Sequence: Many-to-one + one-to-many

Many to one: Encode input sequence in a single vector



Sutskever et al, "Sequence to Sequence Learning with Neural Networks", NIPS 2014

## Sequence to Sequence: Many-to-one + one-to-many

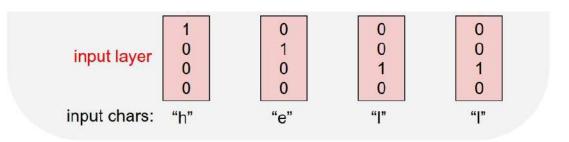
sequence from single input vector Many to one: Encode input sequence in a single vector  $y_2$ W,  $W_{2}$ 

Sutskever et al, "Sequence to Sequence Learning with Neural Networks", NIPS 2014

One to many: Produce output

Vocabulary: [h,e,l,o]

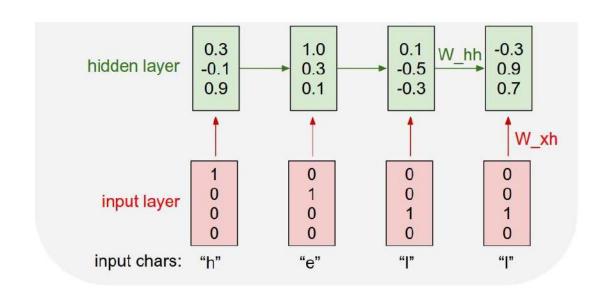
Example training sequence: "hello"



$$h_t = anh(W_{hh}h_{t-1} + W_{xh}x_t)$$

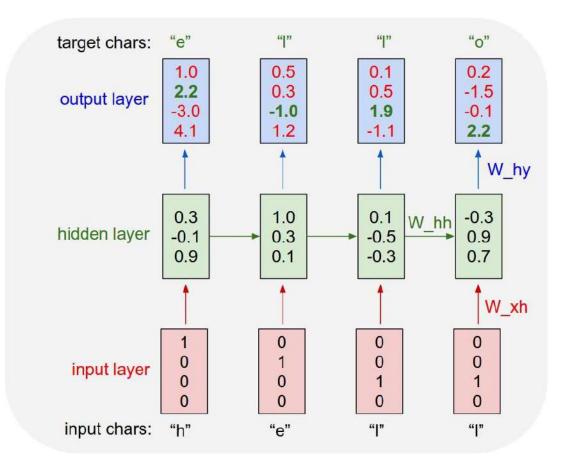
Vocabulary: [h,e,l,o]

Example training sequence: "hello"

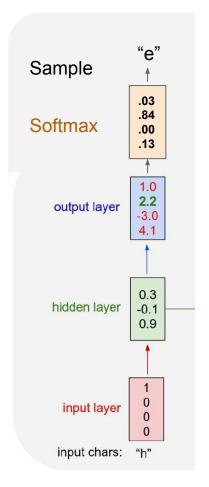


Vocabulary: [h,e,l,o]

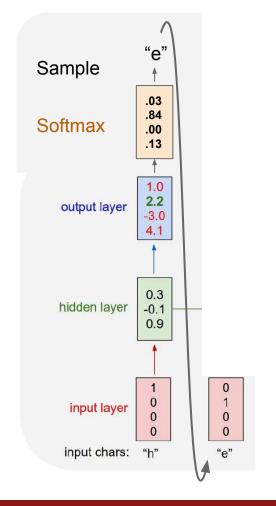
Example training sequence: "hello"



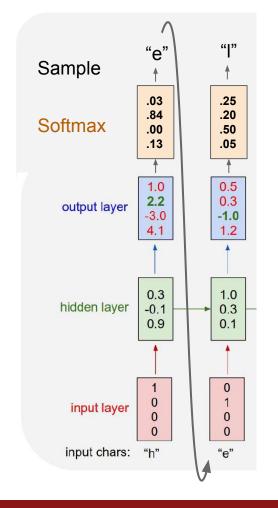
Vocabulary: [h,e,l,o]



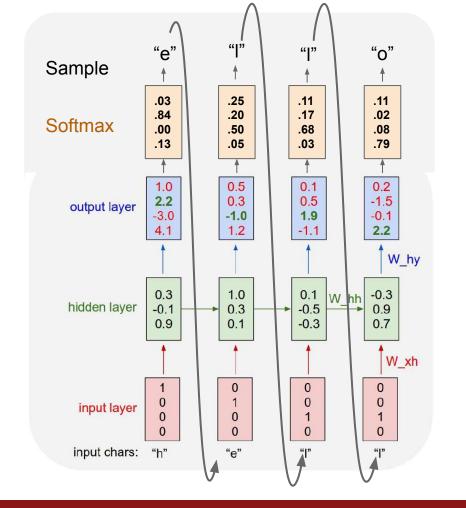
Vocabulary: [h,e,l,o]

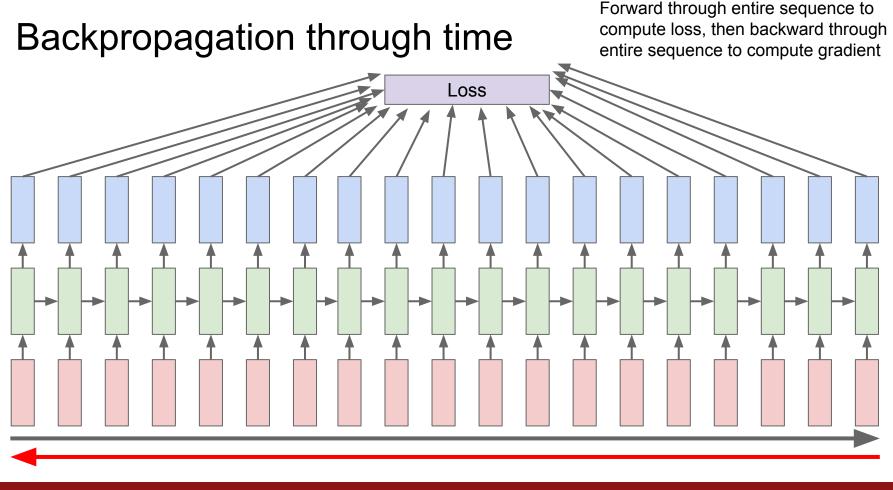


Vocabulary: [h,e,l,o]

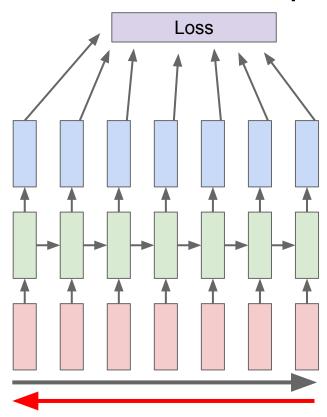


Vocabulary: [h,e,l,o]



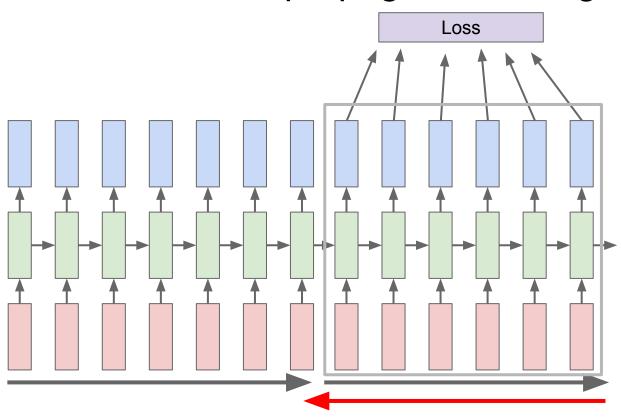


## Truncated Backpropagation through time



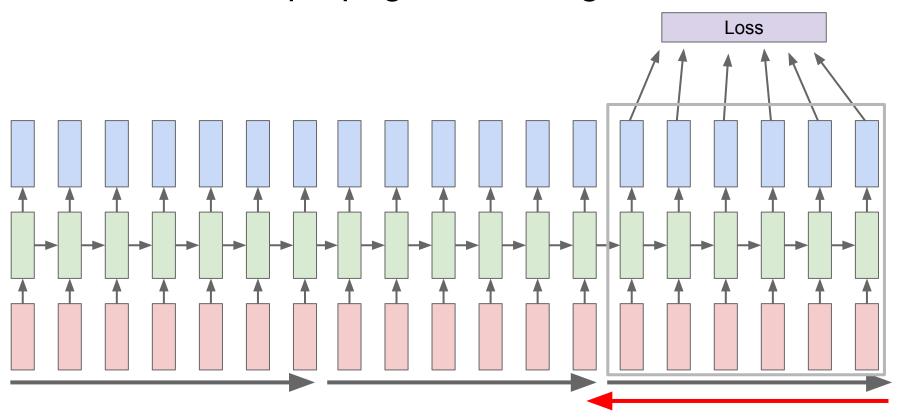
Run forward and backward through chunks of the sequence instead of whole sequence

## Truncated Backpropagation through time



Carry hidden states forward in time forever, but only backpropagate for some smaller number of steps

## Truncated Backpropagation through time



#### min-char-rnn.py gist: 112 lines of Python

```
Minimal character-level Vanilla RNN model, Written by Andrej Karpathy (@Karpathy)
    BSD License
 s import numby as no
 7 - 6 data 1/0
# data = open('input,txt', 'r'),read() # should be simple plain text file
chars = list(set(datal)
data_size, vocab_size = len(data), len(chars)
print 'data has %d characters, %d unique,' % (data size, vocab size)
char_to_ix = { ch:1 for i,ch in enumerate(chars) }
ix_to_char = { 1:ch for 1,ch in enumerate(chars) }
is # hyperparameters
in hidden_size = 100 = size of hidden layer of neurons
if seq_length = 25 # number of steps to unroll the Row for
IN learning_rate = 1e-1
21 With = np_random_rando(hidden_size, votab_size)*0.81 # input to hidden
pp Whit = np.random.rando(hidden_size, hidden_size)*8.01 # hidden to hidden
ys | why = np.random.random(vocab_size, hidden_size)'e.el = hidden to output
24 bh = np.zeros((hidden_size, 1)) + hidden bias
ps by = np.zeros((vocab_size, 1)) = output bias
    def lossFun(inputs, targets, horev);
      inputs, targets are both list of integers.
      hprev is Hx1 arrny of initial hidden state
      returns the loss, gradients on model parameters, and last hidden state
     xs, hs, ys, ps = {}, {}, {}, {}, {}
     hs[-1] = np.copy(hprey)
on # forward pass
      for t in xrange(len(inputa));
       xs[t] = np.zerqs((vocab_size,1)) + encode in 1-pf-# representation
        xs[t][inputs[t]] = 1
        hs[t] = np.tanh(np.dot(wxh, xs[t]) + np.dot(whh, hs[t-1]) + bh) + hidden state
       ys[t] = np.dot(Why, hs[t]) + by + uncormulized log probabilities for next chars
       ps[t] = np.exp(ys[t]) / np.sun(np.exp(ys[t])) # probabilities for next chara
       loss += -np.log(ps[t][targets[t], 8]) # softmax (orens-entropy loss)
44 # backward pass: compute gradients going backwards
datch, dwhh, dwhy = np.zeros_like(Wch), np.zeros_like(Whh), np.zeros_like(Why)
    dbh, dby = np.zeros_like(bh), np.zeros_like(by)
      dbnext = np.zeros like(hs[0])
      for t in reversed(xrange(len(inputs))):
        dy = np.copy(ps[t])
        dy[targets[t]] == 1 % backprop into y
       cheby += np.dot(dy, hs[t].T)
ns dh = np.dot(Why.T, dy) + dhnext # Backprup into h
54 dhraw = (1 - hs[t] * hs[t]) * dh = backgrop through tanh boolinearity
       dWxh += np.dot(dhraw, xs[t].T)
       dwhh += np.dot(dhraw, hs[t-1].t)
       dhnext = np.dot(Whh.T, dhraw)
      for dparam in [dwxh, dwhh, dwhy, dbh, dby]:
       op.clip(dparam, -5, 5, out=dparam) * clip to minigate exploding gradients
     return loss, dwsh, dwsh, dwsy, dbh, dby, hs[len(inputs)-1]
```

```
def sample(h, seed_ix, n):
       sample a sequence of integers from the model
       h is memory state, seed is is seed letter for first time step
x = np.zeros((vocab size, 1))
x[seed_ix] = 1
      1xes = []
71 for t in wrange(n):
        h = np.tanh(np.dot(Wxh, x) + np.dot(Whh, h) + bh)
         y = np.dot(Why, h) + by
         p = np.exp(y) / np.sum(np.exp(y))
        ix = np.random.choice(range(vocab_size), p=p.ravel())
        x = np.zeros((vocab size, 1))
         x[ix] = 1
         lxes.append(lx)
wwxh, mwhh, mwhy = np.zeros_like(wxh), np.zeros_like(whh), np.zeros_like(why)
up mbh. mby = np.zeros like(bh), np.zeros like(by) = memory variables for educad
smooth_loss = -np.log(1.0/vocnb_size)*seq_length # Inss at iteration #
     s prepare loputs (we're sweeping from left to right in steps seg length long)
       if p-seq_length+1 >= len(data) or n == n;
        hprev = np.zeros((hidden_size,i)) + reset fill propery
       p = 0 = us from start of data
       inputs = [char_to_ix[ch] for ch in data[p:p-seq_length]]
       targets = [char_to_ix[ch] for ch in data[p+1:p+seq_length+1]]
21 * sample from the model now and then
if n % 198 = 0:
        sample_ix = sample(hprev, imputs[8], 208)
         txt = ''.loinfix_to_charfix1 for ix in sample_lx)
        print '----\n %s \n----' % (txt, )
       # forward seg langth characters through the net and fetch gradient
       loss, wwxh, dwhh, dwhy, dbh, dby, hprev = lossFun(inputs, targets, hprev)
       swooth_loss = smooth_loss * 8.899 + loss * 8.801
       if n % 100 = 0: print 'iter Nd, loss: Nf' N (n, sapoth_loss) # print progress
       for param, dparam, men in zip([wkh, Whh, Why, bh, by],
                                   [dMxh, dWhh, dWhy, dbh, dby]
                                   [mixh, mishh, mishy, mbh, mby]);
         param += -learning_rate * dparam / np.sgrt(mem + 1e-8) # adaprad update
      p += sed length # mave date bointer
in a 1 * iteration counter
```

(https://gist.github.com/karpathy/d4dee 566867f8291f086)

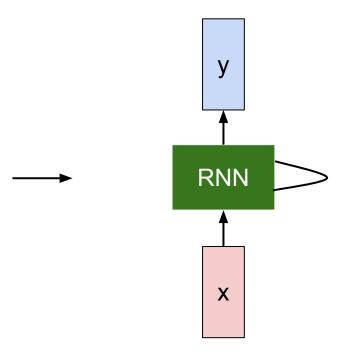
#### THE SONNETS

#### by William Shakespeare

From fairest creatures we desire increase,
That thereby beauty's rose might never die,
But as the riper should by time decease,
His tender heir might bear his memory:
But thou, contracted to thine own bright eyes,
Feed'st thy light's flame with self-substantial fuel,
Making a famine where abundance lies,
Thyself thy foe, to thy sweet self too cruel:
Thou that art now the world's fresh ornament,
And only herald to the gaudy spring,
Within thine own bud buriest thy content,
And tender churl mak'st waste in niggarding:
Pity the world, or else this glutton be,
To eat the world's due, by the grave and thee.

When forty winters shall besiege thy brow,
And dig deep trenches in thy beauty's field,
Thy youth's proud livery so gazed on now,
Will be a tatter'd weed of small worth held:
Then being asked, where all thy beauty lies,
Where all the treasure of thy lusty days;
To say, within thine own deep sunken eyes,
Were an all-eating shame, and thriftless praise.
How much more praise deserv'd thy beauty's use,
If thou couldst answer This fair child of mine
Shall sum my count, and make my old excuse,'
Proving his beauty by succession thine!
This were to be new made when thou art old,

This were to be new made when thou art old, And see thy blood warm when thou feel'st it cold.



#### at first:

tyntd-iafhatawiaoihrdemot lytdws e ,tfti, astai f ogoh eoase rrranbyne 'nhthnee e plia tklrgd t o idoe ns,smtt h ne etie h,hregtrs nigtike,aoaenns lng

#### train more

"Tmont thithey" fomesscerliund Keushey. Thom here sheulke, anmerenith ol sivh I lalterthend Bleipile shuwy fil on aseterlome coaniogennc Phe lism thond hon at. MeiDimorotion in ther thize."

#### train more

Aftair fall unsuch that the hall for Prince Velzonski's that me of her hearly, and behs to so arwage fiving were to it beloge, pavu say falling misfort how, and Gogition is so overelical and ofter.

#### train more

"Why do what that day," replied Natasha, and wishing to himself the fact the princess, Princess Mary was easier, fed in had oftened him.

Pierre aking his soul came to the packs and drove up his father-in-law women.

#### PANDARUS:

Alas, I think he shall be come approached and the day When little srain would be attain'd into being never fed, And who is but a chain and subjects of his death, I should not sleep.

#### Second Senator:

They are away this miseries, produced upon my soul, Breaking and strongly should be buried, when I perish The earth and thoughts of many states.

#### DUKE VINCENTIO:

Well, your wit is in the care of side and that.

#### Second Lord:

They would be ruled after this chamber, and my fair nues begun out of the fact, to be conveyed, Whose noble souls I'll have the heart of the wars.

#### Clown:

Come, sir, I will make did behold your worship.

#### VIOLA:

I'll drink it.

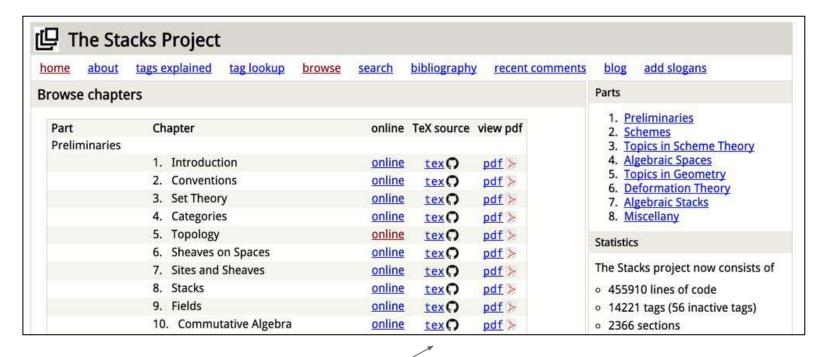
#### VIOLA:

Why, Salisbury must find his flesh and thought
That which I am not aps, not a man and in fire,
To show the reining of the raven and the wars
To grace my hand reproach within, and not a fair are hand,
That Caesar and my goodly father's world;
When I was heaven of presence and our fleets,
We spare with hours, but cut thy council I am great,
Murdered and by thy master's ready there
My power to give thee but so much as hell:
Some service in the noble bondman here,
Would show him to her wine.

#### KING LEAR:

O, if you were a feeble sight, the courtesy of your law, Your sight and several breath, will wear the gods With his heads, and my hands are wonder'd at the deeds, So drop upon your lordship's head, and your opinion Shall be against your honour.

## The Stacks Project: open source algebraic geometry textbook



Latex source

http://stacks.math.columbia.edu/

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For  $\bigoplus_{n=1,\ldots,m}$  where  $\mathcal{L}_{m_{\bullet}}=0$ , hence we can find a closed subset  $\mathcal{H}$  in  $\mathcal{H}$  and any sets  $\mathcal{F}$  on X,U is a closed immersion of S, then  $U\to T$  is a separated algebraic space.

Proof. Proof of (1). It also start we get

$$S = \operatorname{Spec}(R) = U \times_X U \times_X U$$

and the comparison in the fibre product covering we have to prove the lemma generated by  $\coprod Z \times_U U \to V$ . Consider the maps M along the set of points  $Sch_{fppf}$  and  $U \to U$  is the fibre category of S in U in Section, ?? and the fact that any U affine, see Morphisms, Lemma ??. Hence we obtain a scheme S and any open subset  $W \subset U$  in Sh(G) such that  $Spec(R') \to S$  is smooth or an

$$U = \bigcup U_i \times_{S_i} U_i$$

which has a nonzero morphism we may assume that  $f_i$  is of finite presentation over S. We claim that  $\mathcal{O}_{X,x}$  is a scheme where  $x,x',s''\in S'$  such that  $\mathcal{O}_{X,x'}\to \mathcal{O}'_{X',x'}$  is separated. By Algebra, Lemma ?? we can define a map of complexes  $\mathrm{GL}_{S'}(x'/S'')$  and we win.

To prove study we see that  $\mathcal{F}|_U$  is a covering of  $\mathcal{X}'$ , and  $\mathcal{T}_i$  is an object of  $\mathcal{F}_{X/S}$  for i>0 and  $\mathcal{F}_p$  exists and let  $\mathcal{F}_i$  be a presheaf of  $\mathcal{O}_X$ -modules on  $\mathcal{C}$  as a  $\mathcal{F}$ -module. In particular  $\mathcal{F}=U/\mathcal{F}$  we have to show that

$$\widetilde{M}^{\bullet} = \mathcal{I}^{\bullet} \otimes_{\operatorname{Spec}(k)} \mathcal{O}_{S,s} - i_X^{-1} \mathcal{F})$$

is a unique morphism of algebraic stacks. Note that

Arrows = 
$$(Sch/S)_{fppf}^{opp}$$
,  $(Sch/S)_{fppf}$ 

and

$$V = \Gamma(S, \mathcal{O}) \longrightarrow (U, \operatorname{Spec}(A))$$

is an open subset of X. Thus U is affine. This is a continuous map of X is the inverse, the groupoid scheme S.

Proof. See discussion of sheaves of sets.

The result for prove any open covering follows from the less of Example ??. It may replace S by  $X_{spaces,\acute{e}tale}$  which gives an open subspace of X and T equal to  $S_{Zar}$ , see Descent, Lemma ??. Namely, by Lemma ?? we see that R is geometrically regular over S.

Lemma 0.1. Assume (3) and (3) by the construction in the description.

Suppose  $X = \lim |X|$  (by the formal open covering X and a single map  $\underline{Proj}_X(A) = \operatorname{Spec}(B)$  over U compatible with the complex

$$Set(A) = \Gamma(X, \mathcal{O}_{X, \mathcal{O}_X}).$$

When in this case of to show that  $Q \to C_{Z/X}$  is stable under the following result in the second conditions of (1), and (3). This finishes the proof. By Definition?? (without element is when the closed subschemes are catenary. If T is surjective we may assume that T is connected with residue fields of S. Moreover there exists a closed subspace  $Z \subset X$  of X where U in X' is proper (some defining as a closed subset of the uniqueness it suffices to check the fact that the following theorem

*Proof.* This is form all sheaves of sheaves on X. But given a scheme U and a surjective étale morphism  $U \to X$ . Let  $U \cap U = \coprod_{i=1,\dots,n} U_i$  be the scheme X over S at the schemes  $X_i \to X$  and  $U = \lim_i X_i$ .

The following lemma surjective restrocomposes of this implies that  $F_{x_0} = F_{x_0} = F_{x_0,...,0}$ .

**Lemma 0.2.** Let X be a locally Noetherian scheme over S,  $E = \mathcal{F}_{X/S}$ . Set  $\mathcal{I} = \mathcal{J}_1 \subset \mathcal{I}_n^t$ . Since  $\mathcal{I}^n \subset \mathcal{I}^n$  are nonzero over  $i_0 \leq \mathfrak{p}$  is a subset of  $\mathcal{J}_{n,0} \circ \overline{A}_2$  works.

**Lemma 0.3.** In Situation ??. Hence we may assume q' = 0.

*Proof.* We will use the property we see that  $\mathfrak p$  is the mext functor (??). On the other hand, by Lemma ?? we see that

$$D(\mathcal{O}_{X'}) = \mathcal{O}_X(D)$$

where K is an F-algebra where  $\delta_{n+1}$  is a scheme over S.

Proof. Omitted.

Lemma 0.1. Let C be a set of the construction.

Let C be a gerber covering. Let F be a quasi-coherent sheaves of O-modules. We have to show that

$$\mathcal{O}_{\mathcal{O}_X} = \mathcal{O}_X(\mathcal{L})$$

.

*Proof.* This is an algebraic space with the composition of sheaves  $\mathcal{F}$  on  $X_{\acute{e}tale}$  we have

$$\mathcal{O}_X(\mathcal{F}) = \{morph_1 \times_{\mathcal{O}_X} (\mathcal{G}, \mathcal{F})\}\$$

where  $\mathcal{G}$  defines an isomorphism  $\mathcal{F} \to \mathcal{F}$  of  $\mathcal{O}$ -modules.

**Lemma 0.2.** This is an integer Z is injective.

Proof. See Spaces, Lemma ??.

**Lemma 0.3.** Let S be a scheme. Let X be a scheme and X is an affine open covering. Let  $\mathcal{U} \subset \mathcal{X}$  be a canonical and locally of finite type. Let X be a scheme. Let X be a scheme which is equal to the formal complex.

The following to the construction of the lemma follows.

Let X be a scheme. Let X be a scheme covering. Let

$$b: X \to Y' \to Y \to Y \to Y' \times_X Y \to X$$
.

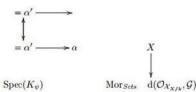
be a morphism of algebraic spaces over S and Y.

*Proof.* Let X be a nonzero scheme of X. Let X be an algebraic space. Let  $\mathcal{F}$  be a quasi-coherent sheaf of  $\mathcal{O}_X$ -modules. The following are equivalent

- F is an algebraic space over S.
- (2) If X is an affine open covering.

Consider a common structure on X and X the functor  $\mathcal{O}_X(U)$  which is locally of finite type.

This since  $\mathcal{F} \in \mathcal{F}$  and  $x \in \mathcal{G}$  the diagram  $\begin{array}{c} \mathcal{S} \\ \downarrow \\ \xi \\ \longrightarrow \mathcal{O}_{X'} \\ \downarrow \\ \text{gor}_s \end{array}$ 



is a limit. Then  $\mathcal G$  is a finite type and assume S is a flat and  $\mathcal F$  and  $\mathcal G$  is a finite type  $f_{\bullet}$ . This is of finite type diagrams, and

- the composition of G is a regular sequence,
- O<sub>X'</sub> is a sheaf of rings.

*Proof.* We have see that  $X = \operatorname{Spec}(R)$  and  $\mathcal{F}$  is a finite type representable by algebraic space. The property  $\mathcal{F}$  is a finite morphism of algebraic stacks. Then the cohomology of X is an open neighbourhood of U.

*Proof.* This is clear that G is a finite presentation, see Lemmas ??.

A reduced above we conclude that U is an open covering of  $\mathcal C$ . The functor  $\mathcal F$  is a "field

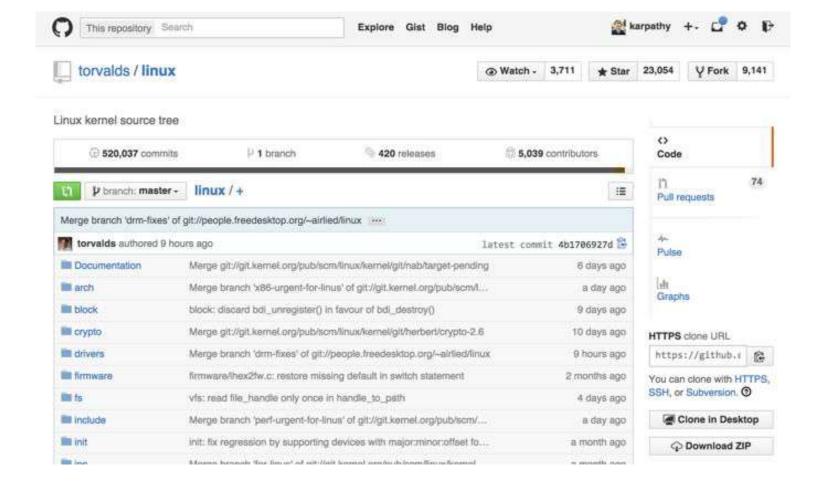
$$\mathcal{O}_{X,x} \longrightarrow \mathcal{F}_{\overline{x}} -1(\mathcal{O}_{X_{etate}}) \longrightarrow \mathcal{O}_{X_{\ell}}^{-1}\mathcal{O}_{X_{\lambda}}(\mathcal{O}_{X_{\eta}}^{\overline{v}})$$

is an isomorphism of covering of  $\mathcal{O}_{X_i}$ . If  $\mathcal{F}$  is the unique element of  $\mathcal{F}$  such that X is an isomorphism.

The property  $\mathcal{F}$  is a disjoint union of Proposition ?? and we can filtered set of presentations of a scheme  $\mathcal{O}_X$ -algebra with  $\mathcal{F}$  are opens of finite type over S.

If  $\mathcal{F}$  is a scheme theoretic image points.

If  $\mathcal{F}$  is a finite direct sum  $\mathcal{O}_{X_{\lambda}}$  is a closed immersion, see Lemma ??. This is a sequence of  $\mathcal{F}$  is a similar morphism.



```
static void do command(struct seg file *m, void *v)
 int column = 32 << (cmd[2] & 0x80);
 if (state)
   cmd = (int)(int state ^ (in 8(&ch->ch flags) & Cmd) ? 2 : 1);
 else
   seq = 1;
 for (i = 0; i < 16; i++) {
   if (k & (1 << 1))
      pipe = (in use & UMXTHREAD UNCCA) +
        ((count & 0x0000000ffffffff8) & 0x000000f) << 8;
   if (count == 0)
      sub(pid, ppc md.kexec handle, 0x20000000);
   pipe set bytes(i, 0);
 /* Free our user pages pointer to place camera if all dash */
 subsystem info = &of changes[PAGE SIZE];
 rek controls(offset, idx, &soffset);
  /* Now we want to deliberately put it to device */
 control check polarity(&context, val, 0);
 for (i = 0; i < COUNTER; i++)
   seg puts(s, "policy ");
```

## Generated C code

```
Copyright (c) 2006-2010, Intel Mobile Communications. All rights reserved.
    This program is free software; you can redistribute it and/or modify it
 * under the terms of the GNU General Public License version 2 as published by
 * the Free Software Foundation.
         This program is distributed in the hope that it will be useful,
 * but WITHOUT ANY WARRANTY; without even the implied warranty of
    MERCHANTABILITY or FITNESS FOR A PARTICULAR PURPOSE. See the
    GNU General Public License for more details.
    You should have received a copy of the GNU General Public License
     along with this program; if not, write to the Free Software Foundation,
 * Inc., 675 Mass Ave, Cambridge, MA 02139, USA.
#/
#include unx/kexec.h>
#include unx/errno.h>
#include unx/io.h>
#include inux/platform device.h>
#include inux/multi.h>
#include inux/ckevent.h>
#include <asm/io.h>
#include <asm/prom.h>
#include <asm/e820.h>
#include <asm/system info.h>
#include <asm/setew.h>
#include <asm/pgproto.h>
```

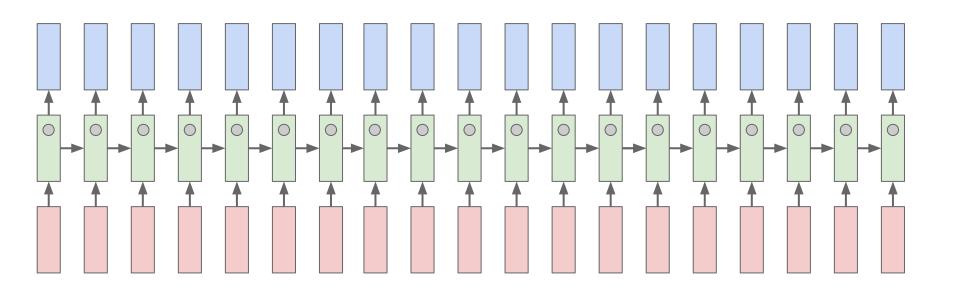
```
#include <asm/io.h>
#include <asm/prom.h>
#include <asm/e820.h>
#include <asm/system info.h>
#include <asm/setew.h>
#include <asm/pgproto.h>
#define REG PG vesa slot addr pack
#define PFM NOCOMP AFSR(0, load)
#define STACK DDR(type) (func)
#define SWAP ALLOCATE(nr)
                             (e)
#define emulate sigs() arch get unaligned child()
#define access rw(TST) asm volatile("movd %%esp, %0, %3" :: "r" (0)); \
 if ( type & DO READ)
static void stat PC SEC read mostly offsetof(struct seq argsqueue, \
         pC>[1]);
static void
os prefix(unsigned long sys)
#ifdef CONFIG PREEMPT
 PUT PARAM RAID(2, sel) = get_state state();
 set pid sum((unsigned long)state, current state str(),
           (unsigned long)-1->1r full; low;
```

**Input:** In a shocking finding, scientist discovered a herd of unicorns living in a remote, previously unexplored valley, in the Andes Mountains. Even more surprising to the researchers was the fact that the unicorns spoke perfect English.

**Output:** The scientist named the population, after their distinctive horn, Ovid's Unicorn. These four-horned, silver-white unicorns were previously unknown to science.

Now, after almost two centuries, the mystery of what sparked this odd phenomenon is finally solved.

Dr. Jorge Pérez, an evolutionary biologist from the University of La Paz, and several companions, were exploring the Andes Mountains when they found a small valley, with no other animals or humans. Pérez noticed that the valley had what appeared to be a natural fountain, surrounded by two peaks of rock and silver snow.



```
/* Unpack a filter field's string representation from user-space
    buffer. '/
char "audit_unpack_string(void "bufp, size_t "remain, size_t len)
{
    char "str;
    if (!"bufp || (len == 0) || (len > "remain))
        return ERR_PTR(-EINVAL);
    /* Of the currently implemented string fields, PATH_MAX
        defines the longest valid length.
    */
```

```
"You mean to imply that I have nothing to eat out of.... On the contrary, I can supply you with everything even if you want to give dinner parties," warmly replied Chichagov, who tried by every word he spoke to prove his own rectitude and therefore imagined Kutuzov to be animated by the same desire.

Kutuzov, shrugging his shoulders, replied with his subtle penetrating smile: "I meant merely to say what I said."
```

### quote detection cell

#### Cell sensitive to position in line:

```
The sole importance of the crossing of the Berezina lies in the fact that it plainly and indubitably proved the fallacy of all the plans for cutting off the enemy's retreat and the soundness of the only possible line of action--the one Kutuzov and the general mass of the army demanded--namely, simply to follow the enemy up. The French crowd fled at a continually increasing speed and all its energy was directed to reaching its goal. It fled like a wounded animal and it was impossible to block its path. This was shown not so much by the arrangements it made for crossing as by what took place at the bridges. When the bridges broke down, unarmed soldiers, people from Moscow and women with children who were with the French transport, all--carried on by vis inertiae--pressed forward into boats and into the ice-covered water and did not, surrender.
```

## line length tracking cell

#### if statement cell

```
Cell that turns on inside comments and quotes:
                               quote/comment cell
```

```
#ifdef config_AUDITSYSCALL
static inline int audit_match_class_bits(int class, u32 *mask)

int i;
if (classes[class]) {
  for (i = 0; i < AUDIT_BITMASK_SIZE; i++)
   if (mask[i] & classes[class][i])
   return 0;
}
return 1;
}</pre>
```

### code depth cell

#### RNN tradeoffs

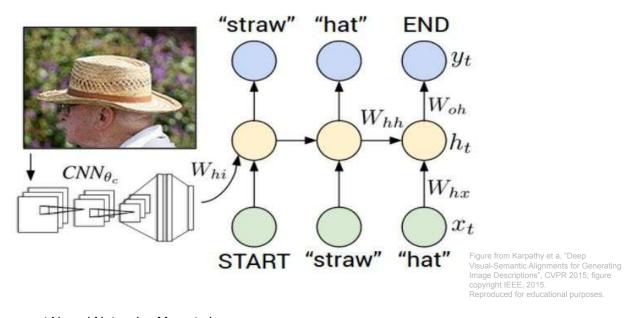
#### **RNN Advantages:**

- Can process any length input
- Computation for step t can (in theory) use information from many steps back
- Model size doesn't increase for longer input
- Same weights applied on every timestep, so there is symmetry in how inputs are processed.

#### **RNN** Disadvantages:

- Recurrent computation is slow
- In practice, difficult to access information from many steps back

# Image Captioning



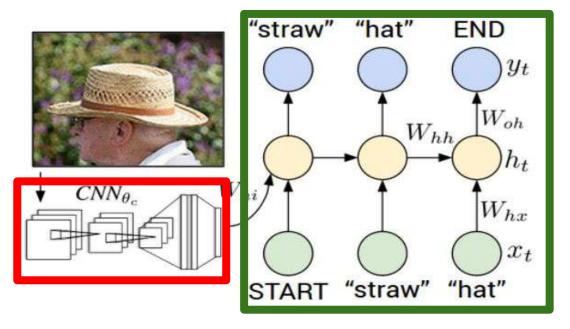
Explain Images with Multimodal Recurrent Neural Networks, Mao et al.

Deep Visual-Semantic Alignments for Generating Image Descriptions, Karpathy and Fei-Fei
Show and Tell: A Neural Image Caption Generator, Vinyals et al.

Long-term Recurrent Convolutional Networks for Visual Recognition and Description, Donahue et al.

Learning a Recurrent Visual Representation for Image Caption Generation, Chen and Zitnick

#### **Recurrent Neural Network**

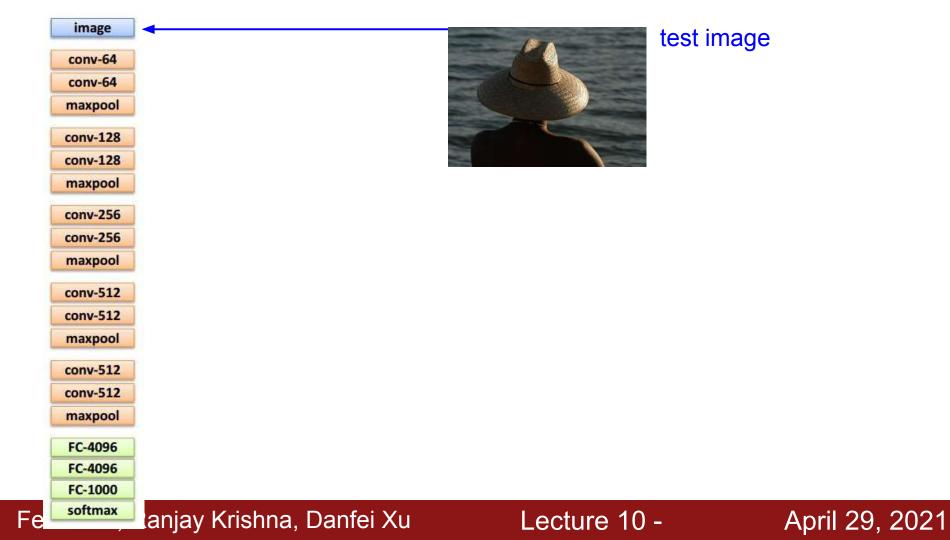


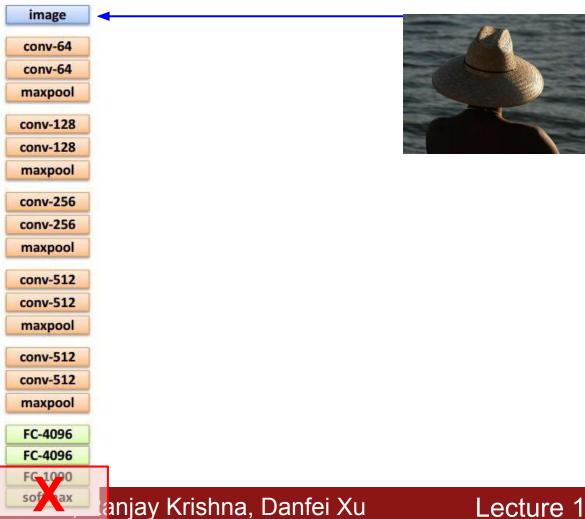
**Convolutional Neural Network** 



test image

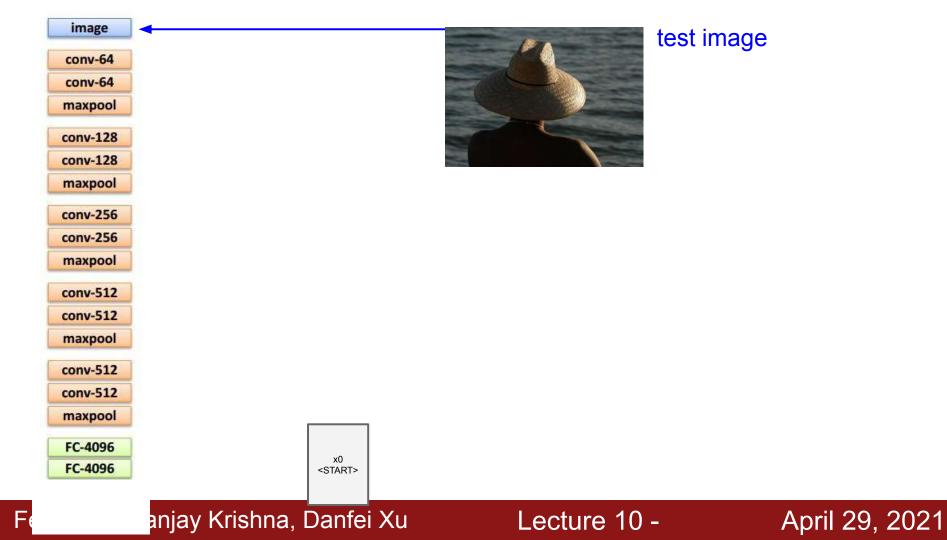
This image is CC0 public domain

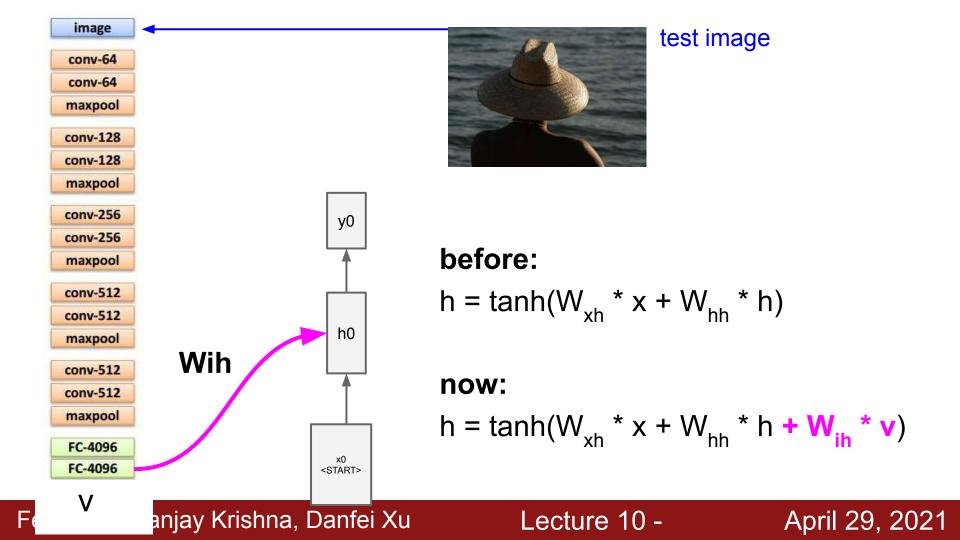


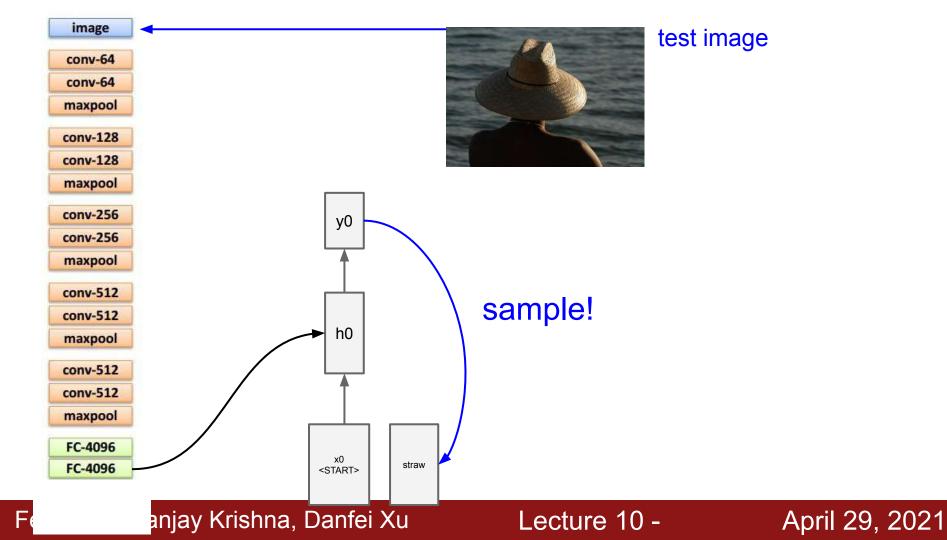


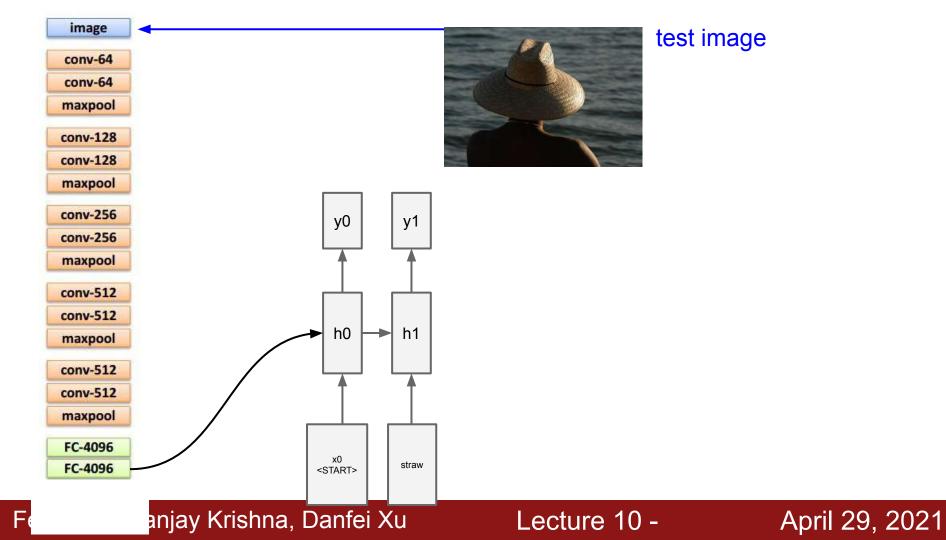
test image

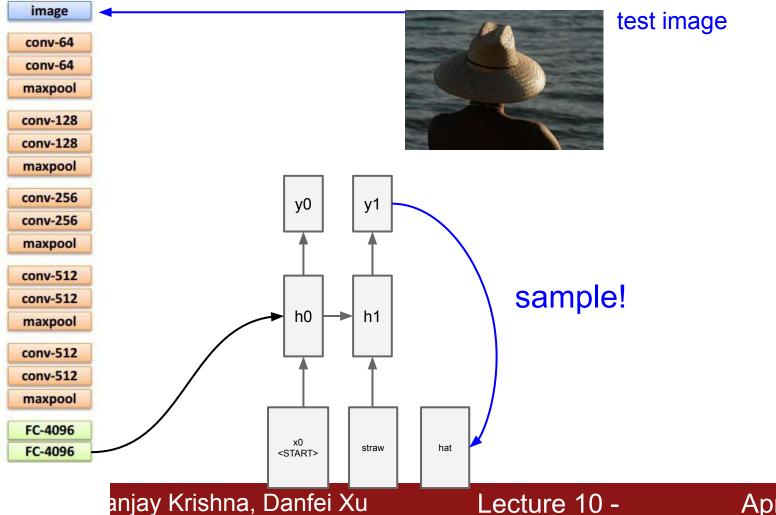
April 29, 2021



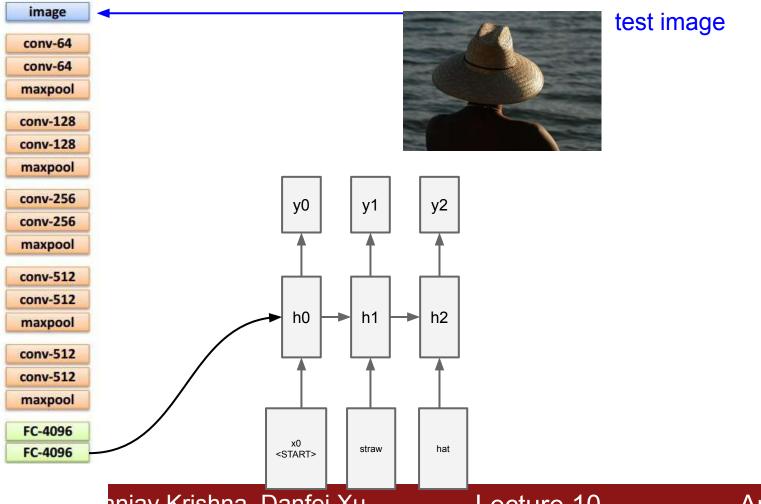




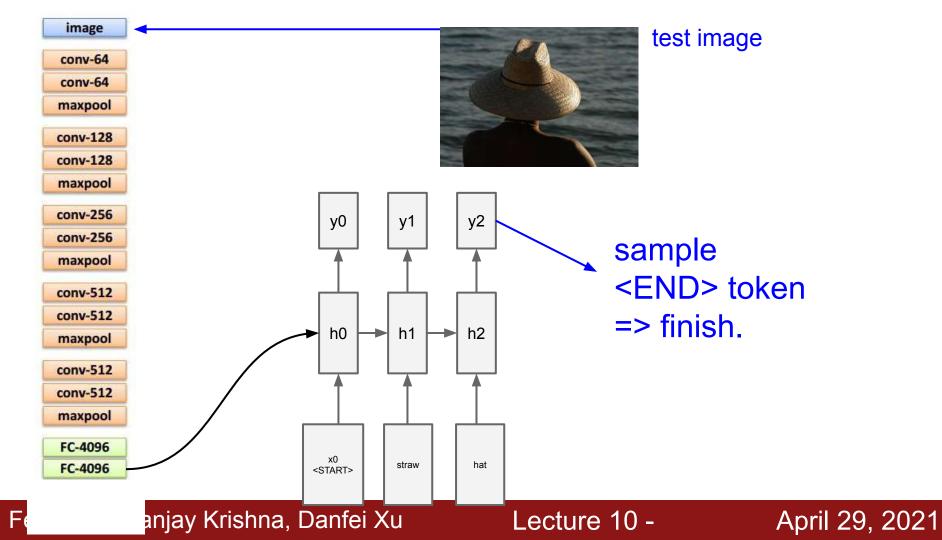




April 29, 2021



April 29, 2021



# Image Captioning: Example Results



A cat sitting on a suitcase on the floor



A cat is sitting on a tree branch



A dog is running in the grass with a frisbee



A white teddy bear sitting in the grass



Two people walking on the beach with surfboards



A tennis player in action on the court



Two giraffes standing in a grassy field



A man riding a dirt bike on a dirt track

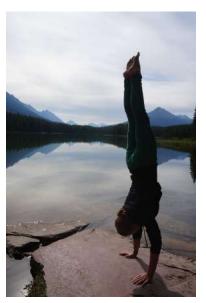
# Image Captioning: Failure Cases



A woman is holding a cat in her hand



A person holding a computer mouse on a desk



A woman standing on a beach holding a surfboard



A bird is perched on a tree branch



A man in a baseball uniform throwing a ball

# Visual Question Answering (VQA)



Q: What endangered animal is featured on the truck?

A: A bald eagle.

A: A sparrow.

A: A humming bird.

A: A raven



Q: Where will the driver go if turning right?

A: Onto 24 3/4 Rd.

A: Onto 25 3/4 Rd.

A: Onto 23 3/4 Rd.

A: Onto Main Street.



Q: When was the picture taken?

A: During a wedding.

A: During a bar mitzvah.

A: During a funeral.

A: During a Sunday church



Q: Who is under the umbrella?

A: Two women.

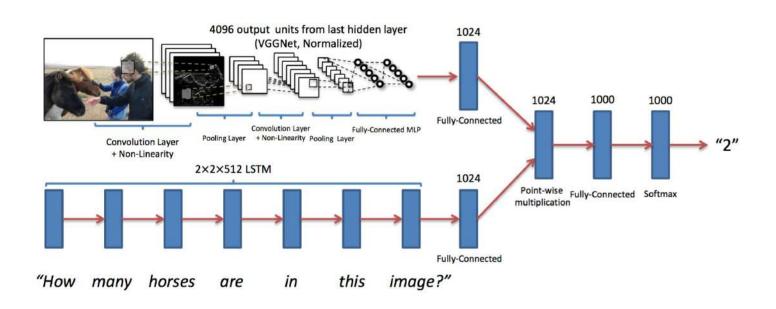
A: A child.

A: An old man.

A: A husband and a wife.

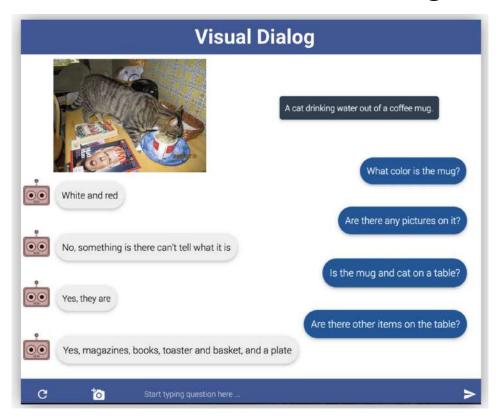
Agrawal et al, "VQA: Visual Question Answering", ICCV 2015 Zhu et al, "Visual 7W: Grounded Question Answering in Images", CVPR 2016 Figure from Zhu et al, copyright IEEE 2016. Reproduced for educational purposes.

# Visual Question Answering: RNNs with Attention



Agrawal et al, "Visual 7W: Grounded Question Answering in Images", CVPR 2015 Figures from Agrawal et al, copyright IEEE 2015. Reproduced for educational purposes.

# Visual Dialog: Conversations about images



Das et al, "Visual Dialog", CVPR 2017

Figures from Das et al, copyright IEEE 2017. Reproduced with permission.

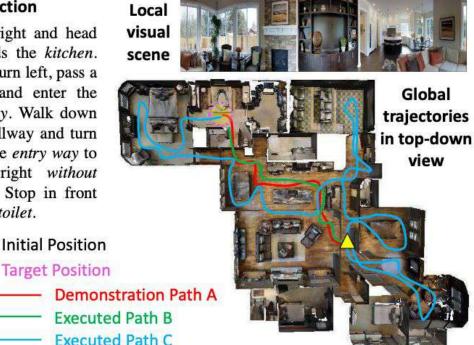
# Visual Language Navigation: Go to the living room

Agent encodes instructions in language and uses an RNN to generate a series of movements as the visual input changes after each move.

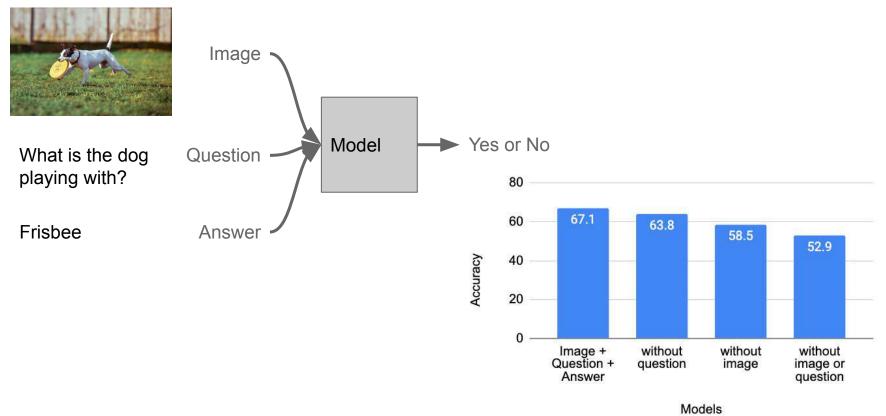
Wang et al, "Reinforced Cross-Modal Matching and Self-Supervised Imitation Learning for Vision-Language Navigation", CVPR 2018 Figures from Wang et al, copyright IEEE 2017. Reproduced with permission.

#### Instruction

Turn right and head towards the kitchen. Then turn left, pass a table and enter the hallway. Walk down the hallway and turn into the entry way to your right without doors. Stop in front of the toilet.

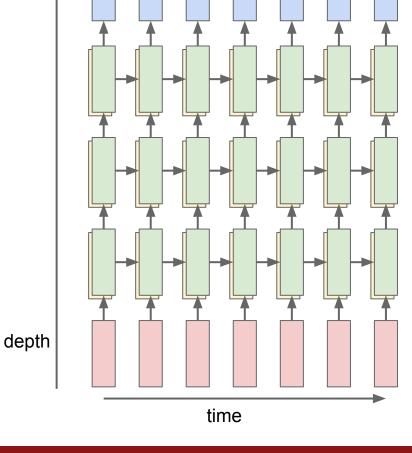


# Visual Question Answering: Dataset Bias



Jabri et al. "Revisiting Visual Question Answering Baselines" ECCV 2016

# Multilayer RNNs



# Long Short Term Memory (LSTM)

#### Vanilla RNN

$$h_t = \tanh\left(W\begin{pmatrix} h_{t-1} \\ x_t \end{pmatrix}\right)$$

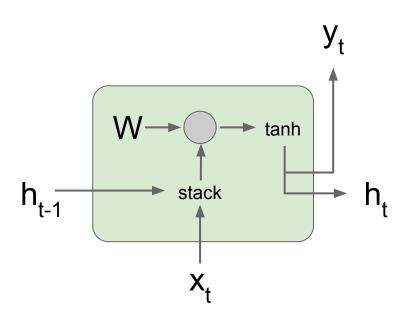
#### **LSTM**

$$\begin{pmatrix} i \\ f \\ o \\ g \end{pmatrix} = \begin{pmatrix} \sigma \\ \sigma \\ \sigma \\ \tanh \end{pmatrix} W \begin{pmatrix} h_{t-1} \\ x_t \end{pmatrix}$$

$$c_t = f \odot c_{t-1} + i \odot g$$

$$h_t = o \odot \tanh(c_t)$$

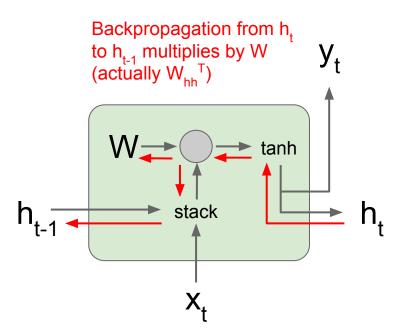
Hochreiter and Schmidhuber, "Long Short Term Memory", Neural Computation 1997



$$h_{t} = \tanh(W_{hh}h_{t-1} + W_{xh}x_{t})$$

$$= \tanh\left(\left(W_{hh} \quad W_{hx}\right) \begin{pmatrix} h_{t-1} \\ x_{t} \end{pmatrix}\right)$$

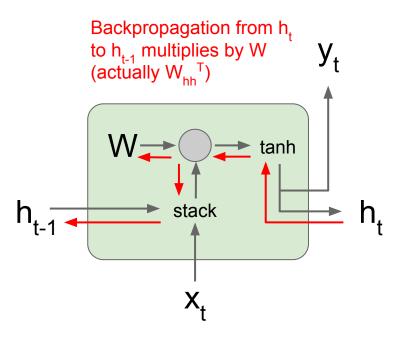
$$= \tanh\left(W \begin{pmatrix} h_{t-1} \\ x_{t} \end{pmatrix}\right)$$



$$h_{t} = \tanh(W_{hh}h_{t-1} + W_{xh}x_{t})$$

$$= \tanh\left(\left(W_{hh} \quad W_{hx}\right) \begin{pmatrix} h_{t-1} \\ x_{t} \end{pmatrix}\right)$$

$$= \tanh\left(W \begin{pmatrix} h_{t-1} \\ x_{t} \end{pmatrix}\right)$$

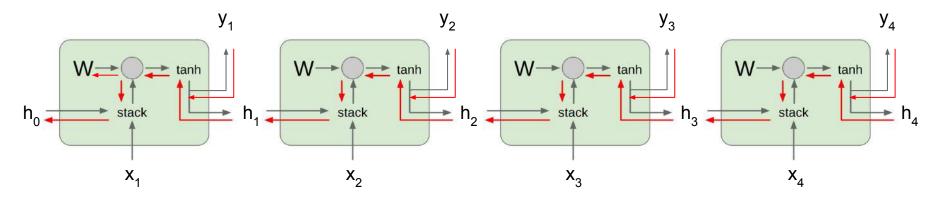


$$h_{t} = \tanh(W_{hh}h_{t-1} + W_{xh}x_{t})$$

$$= \tanh\left(\left(W_{hh} \quad W_{hx}\right) \begin{pmatrix} h_{t-1} \\ x_{t} \end{pmatrix}\right)$$

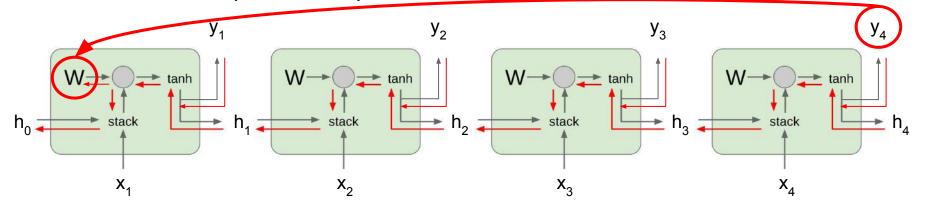
$$= \tanh\left(W \begin{pmatrix} h_{t-1} \\ x_{t} \end{pmatrix}\right)$$

$$rac{\partial h_t}{\partial h_{t-1}} = tanh'(W_{hh}h_{t-1} + W_{xh}x_t)W_{hh}$$



$$rac{\partial L}{\partial W} = \sum_{t=1}^{T} rac{\partial L_t}{\partial W}$$

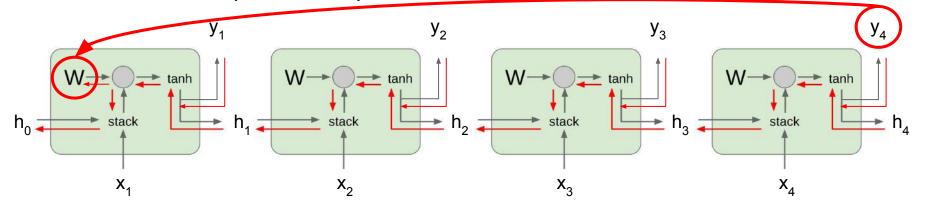
Gradients over multiple time steps:



$$\frac{\partial L}{\partial W} = \sum_{t=1}^{T} \frac{\partial L_t}{\partial W}$$

$$rac{\partial L_T}{\partial W} = rac{\partial L_T}{\partial h_T} rac{\partial h_t}{\partial h_{t-1}} \dots rac{\partial h_1}{\partial W}$$

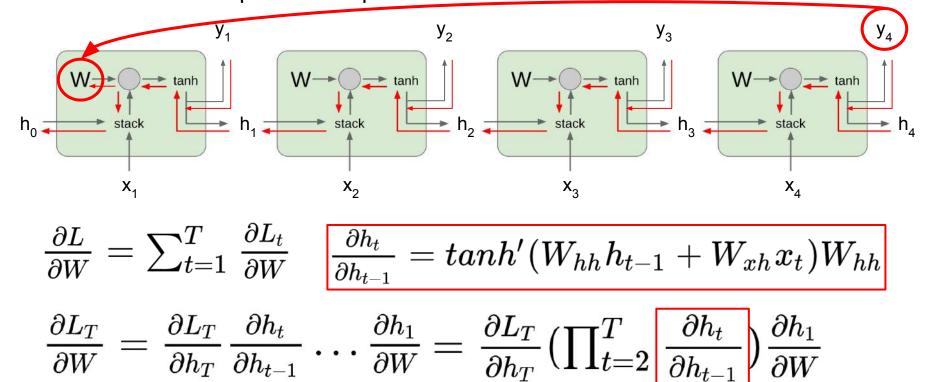
Gradients over multiple time steps:



$$rac{\partial L}{\partial W} = \sum_{t=1}^{T} rac{\partial L_t}{\partial W}$$

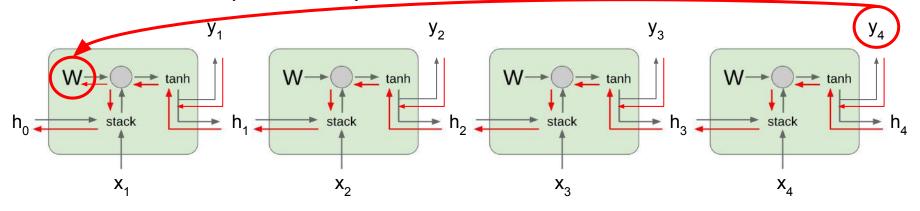
$$rac{\partial L_T}{\partial W} = rac{\partial L_T}{\partial h_T} rac{\partial h_t}{\partial h_{t-1}} \dots rac{\partial h_1}{\partial W} = rac{\partial L_T}{\partial h_T} (\prod_{t=2}^T rac{\partial h_t}{\partial h_{t-1}}) rac{\partial h_1}{\partial W}$$

Gradients over multiple time steps:



Gradients over multiple time steps:

Bengio et al, "Learning long-term dependencies with gradient descent is difficult", IEEE Transactions on Neural Networks, 1994
Pascanu et al, "On the difficulty of training recurrent neural networks", ICML 2013



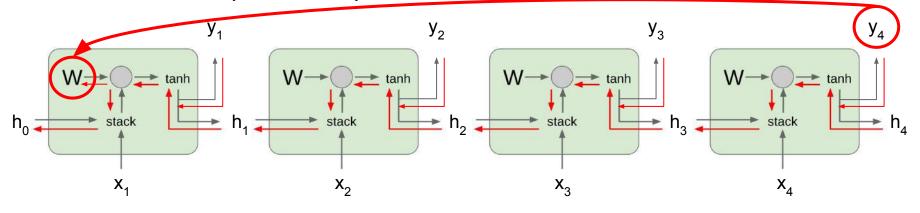
$$rac{\partial L}{\partial W} = \sum_{t=1}^{T} rac{\partial L_t}{\partial W}$$

Almost always < 1 **Vanishing gradients** 

$$rac{\partial L_T}{\partial W} = rac{\partial L_T}{\partial h_T} (\prod_{t=2}^T tanh'(W_{hh}h_{t-1} + W_{xh}x_t)) W_{hh}^{T-1} rac{\partial h_1}{\partial W}$$

Gradients over multiple time steps:

Bengio et al, "Learning long-term dependencies with gradient descent is difficult", IEEE Transactions on Neural Networks, 1994
Pascanu et al, "On the difficulty of training recurrent neural networks", ICML 2013

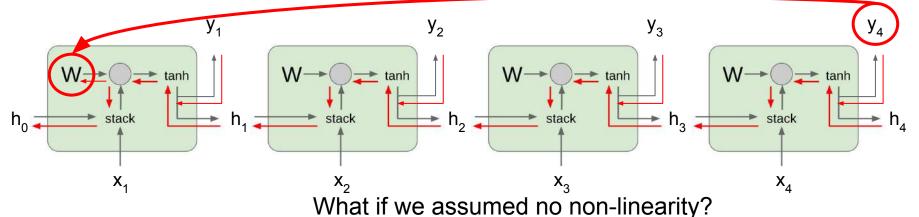


$$rac{\partial L}{\partial W} = \sum_{t=1}^{T} rac{\partial L_t}{\partial W}$$

What if we assumed no non-linearity?

Gradients over multiple time steps:

Bengio et al, "Learning long-term dependencies with gradient descent is difficult", IEEE Transactions on Neural Networks, 1994
Pascanu et al, "On the difficulty of training recurrent neural networks", ICML 2013



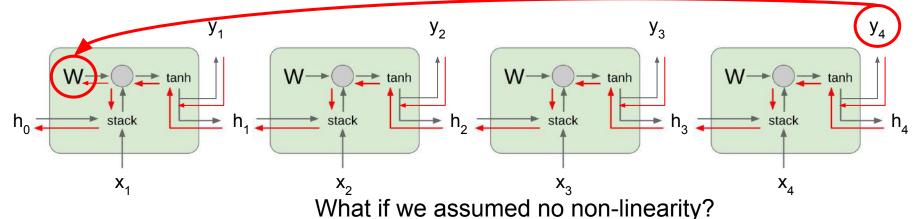
$$rac{\partial L}{\partial W} = \sum_{t=1}^{T} rac{\partial L_t}{\partial W}$$

$$rac{\partial L_T}{\partial W} = rac{\partial L_T}{\partial h_T} W_{hh}^{T-1} rac{\partial h_1}{\partial W}$$

Largest singular value < 1: Vanishing gradients

Gradients over multiple time steps:

Bengio et al, "Learning long-term dependencies with gradient descent is difficult", IEEE Transactions on Neural Networks, 1994
Pascanu et al, "On the difficulty of training recurrent neural networks", ICML 2013



$$\frac{\partial L}{\partial W} = \sum_{t=1}^{T} \frac{\partial L_t}{\partial W}$$

$$rac{\partial L_T}{\partial W} = rac{\partial L_T}{\partial h_T} W_{hh}^{T-1} rac{\partial h_1}{\partial W}$$

Largest singular value > 1: **Exploding gradients** 

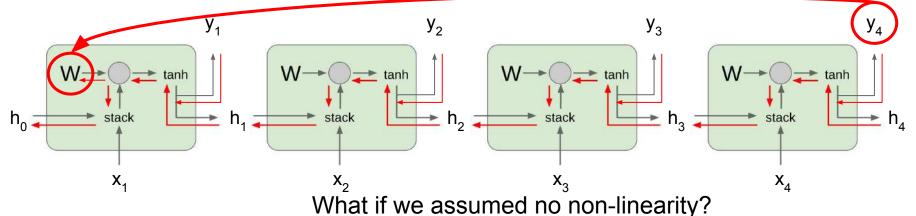
Largest singular value < 1: Vanishing gradients

→ **Gradient clipping**: Scale gradient if its norm is too big

```
grad_norm = np.sum(grad * grad)
if grad_norm > threshold:
    grad *= (threshold / grad_norm)
```

Gradients over multiple time steps:

Bengio et al, "Learning long-term dependencies with gradient descent is difficult", IEEE Transactions on Neural Networks, 1994
Pascanu et al, "On the difficulty of training recurrent neural networks", ICML 2013



$$\frac{\partial L}{\partial W} = \sum_{t=1}^{T} \frac{\partial L_t}{\partial W}$$

$$rac{\partial L_T}{\partial W} = rac{\partial L_T}{\partial h_T} W_{hh}^{T-1} rac{\partial h_1}{\partial W}$$

Largest singular value > 1: **Exploding gradients** 

Change RNN architecture

# Long Short Term Memory (LSTM)

#### Vanilla RNN

$$h_t = \tanh\left(W\begin{pmatrix} h_{t-1} \\ x_t \end{pmatrix}\right)$$

#### **LSTM**

$$\begin{pmatrix} i \\ f \\ o \\ g \end{pmatrix} = \begin{pmatrix} \sigma \\ \sigma \\ \sigma \\ \tanh \end{pmatrix} W \begin{pmatrix} h_{t-1} \\ x_t \end{pmatrix}$$

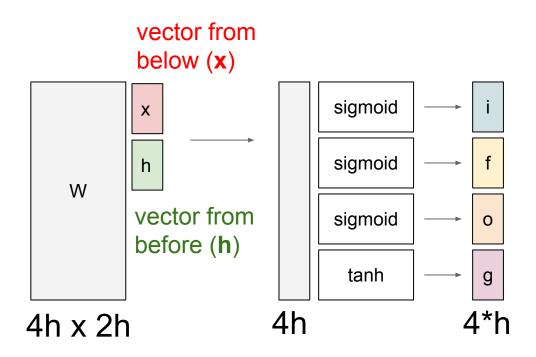
$$c_t = f \odot c_{t-1} + i \odot g$$

$$h_t = o \odot \tanh(c_t)$$

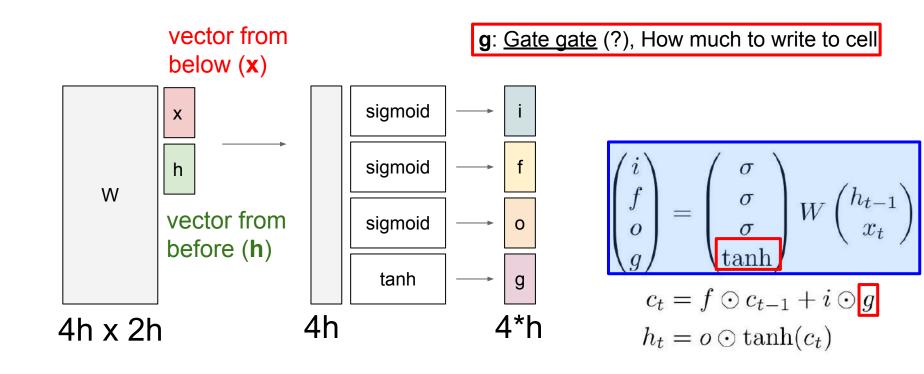
Hochreiter and Schmidhuber, "Long Short Term Memory", Neural Computation 1997

## Long Short Term Memory (LSTM)

[Hochreiter et al., 1997]

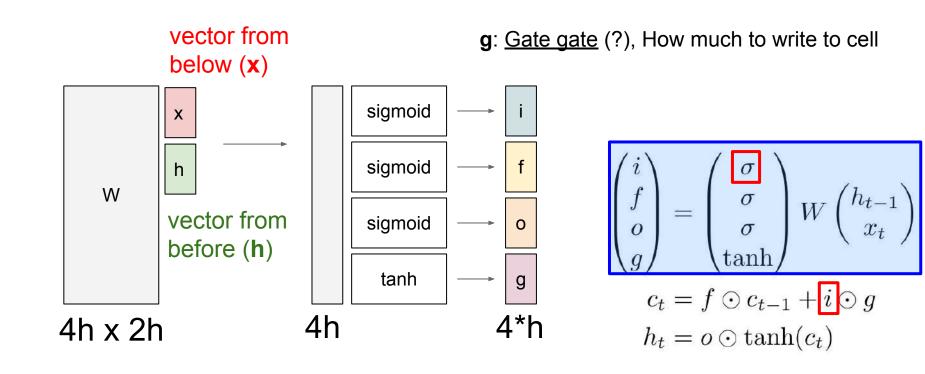


[Hochreiter et al., 1997]



[Hochreiter et al., 1997]

i: Input gate, whether to write to cell

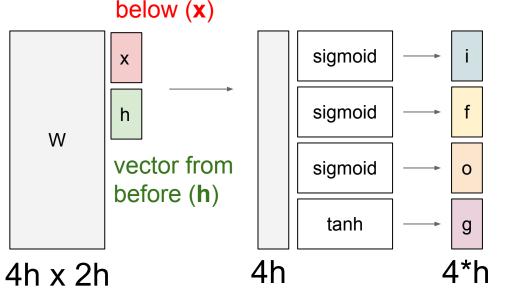


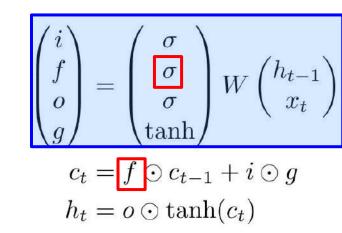
[Hochreiter et al., 1997]

i: Input gate, whether to write to cell

f: Forget gate, Whether to erase cell

vector from g: Gate gate (?), How much to write to cell





vector from

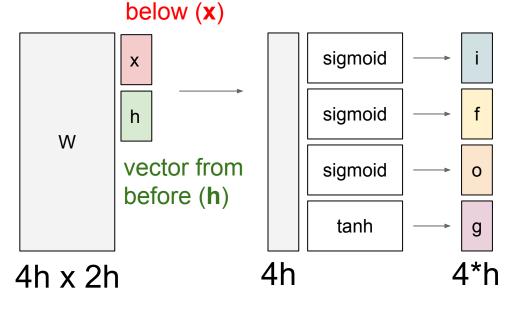
[Hochreiter et al., 1997]

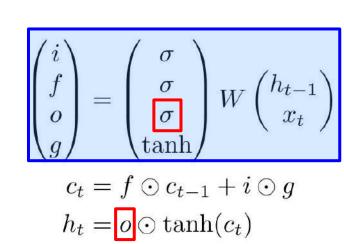
i: Input gate, whether to write to cell

f: Forget gate, Whether to erase cell

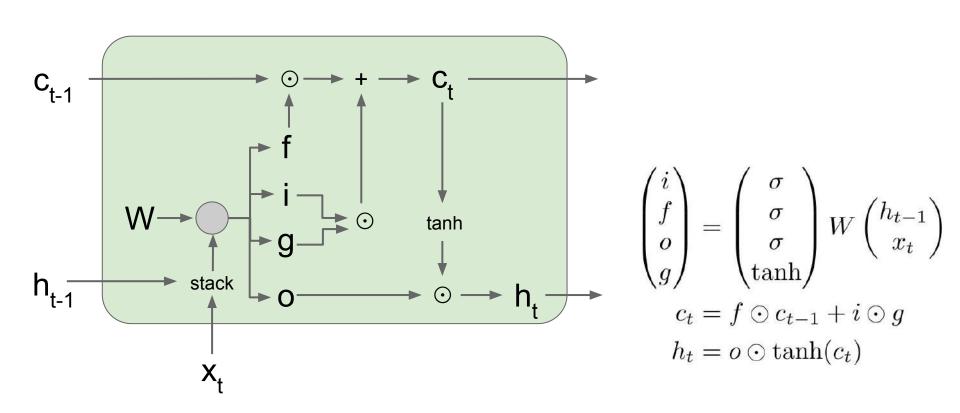
o: Output gate, How much to reveal cell

g: Gate gate (?), How much to write to cell



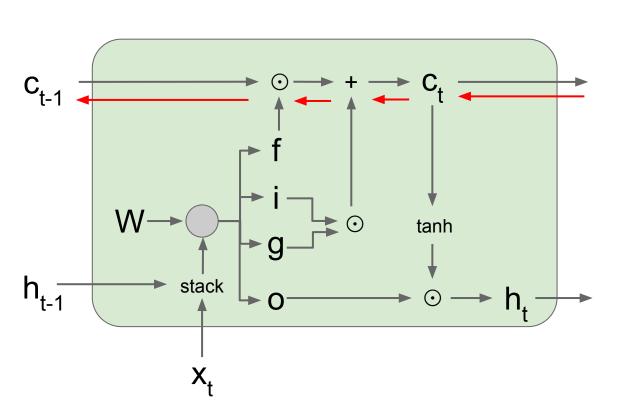


[Hochreiter et al., 1997]



#### Long Short Term Memory (LSTM): Gradient Flow

[Hochreiter et al., 1997]



Backpropagation from c<sub>t</sub> to c<sub>t-1</sub> only elementwise multiplication by f, no matrix multiply by W

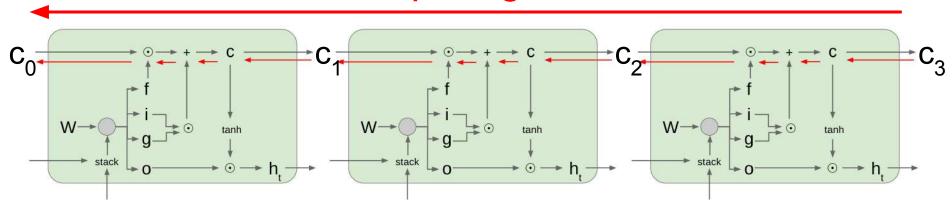
$$\begin{pmatrix} i \\ f \\ o \\ g \end{pmatrix} = \begin{pmatrix} \sigma \\ \sigma \\ \sigma \\ \tanh \end{pmatrix} W \begin{pmatrix} h_{t-1} \\ x_t \end{pmatrix}$$

$$c_t = f \odot c_{t-1} + i \odot g$$

$$h_t = o \odot \tanh(c_t)$$

# Long Short Term Memory (LSTM): Gradient Flow [Hochreiter et al., 1997]

#### Uninterrupted gradient flow!



Notice that the gradient contains the **f** gate's vector of activations

- allows better control of gradients values, using suitable parameter updates of the forget gate.

Also notice that are added through the **f**, **i**, **g**, and **o** gates

- better balancing of gradient values

# Do LSTMs solve the vanishing gradient problem?

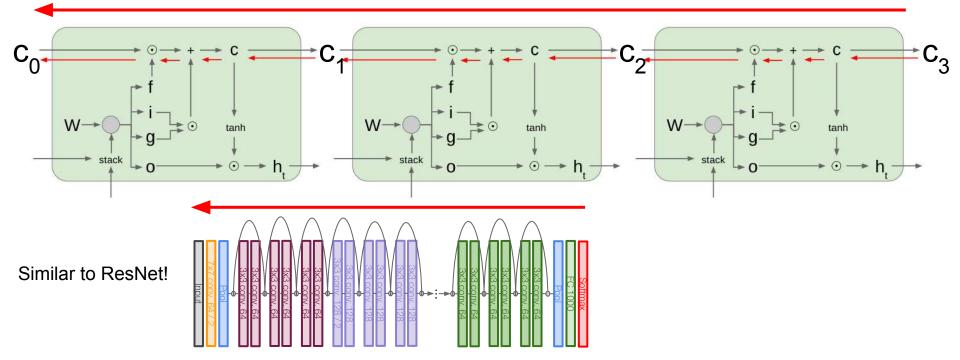
The LSTM architecture makes it easier for the RNN to preserve information over many timesteps

- e.g. **if the f = 1 and the i = 0**, then the information of that cell is preserved indefinitely.
- By contrast, it's harder for vanilla RNN to learn a recurrent weight matrix
   Wh that preserves info in hidden state

LSTM doesn't guarantee that there is no vanishing/exploding gradient, but it does provide an easier way for the model to learn long-distance dependencies

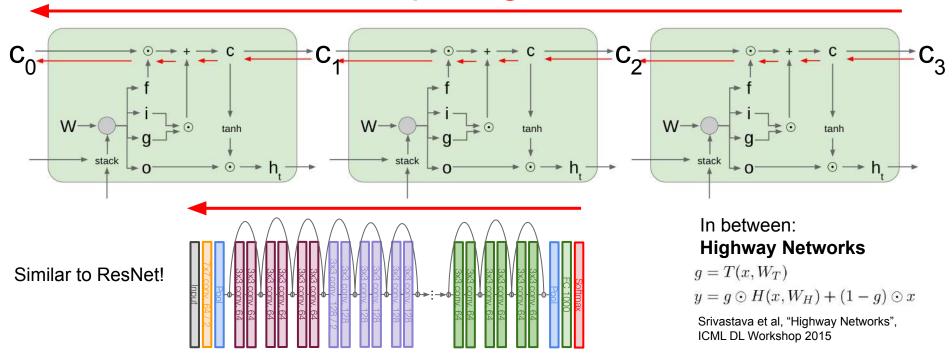
#### Long Short Term Memory (LSTM): Gradient Flow [Hochreiter et al., 1997]

### Uninterrupted gradient flow!

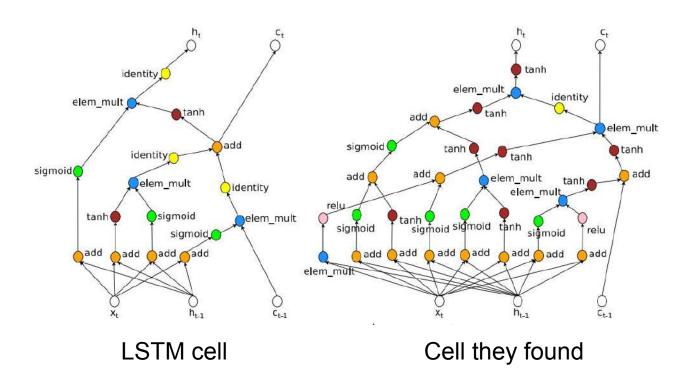


# Long Short Term Memory (LSTM): Gradient Flow [Hochreiter et al., 1997]

### Uninterrupted gradient flow!



#### Neural Architecture Search for RNN architectures



Zoph et Le, "Neural Architecture Search with Reinforcement Learning", ICLR 2017 Figures copyright Zoph et al, 2017. Reproduced with permission.

#### Other RNN Variants

**GRU** [Learning phrase representations using rnn encoder-decoder for statistical machine translation, Cho et al. 2014]

$$r_{t} = \sigma(W_{xr}x_{t} + W_{hr}h_{t-1} + b_{r})$$

$$z_{t} = \sigma(W_{xz}x_{t} + W_{hz}h_{t-1} + b_{z})$$

$$\tilde{h}_{t} = \tanh(W_{xh}x_{t} + W_{hh}(r_{t} \odot h_{t-1}) + b_{h})$$

$$h_{t} = z_{t} \odot h_{t-1} + (1 - z_{t}) \odot \tilde{h}_{t}$$

[LSTM: A Search Space Odyssey, Greff et al., 2015]

[An Empirical Exploration of Recurrent Network Architectures. Jozefowicz et al., 2015]

#### MUT1:

$$\begin{array}{rcl} z &=& \mathrm{sigm}(W_{\mathtt{xz}}x_t + b_x) \\ r &=& \mathrm{sigm}(W_{\mathtt{xr}}x_t + W_{\mathtt{hr}}h_t + b_r) \\ h_{t+1} &=& \mathrm{tanh}(W_{\mathtt{hh}}(r\odot h_t) + \mathrm{tanh}(x_t) + b_{\mathtt{h}})\odot z \\ &+& h_t\odot (1-z) \end{array}$$

#### MUT2:

$$\begin{array}{rcl} z &=& \mathrm{sigm}(W_{\mathtt{xz}}x_t + W_{\mathtt{hz}}h_t + b_{\mathtt{z}}) \\ r &=& \mathrm{sigm}(x_t + W_{\mathtt{hr}}h_t + b_{\mathtt{r}}) \\ h_{t+1} &=& \mathrm{tanh}(W_{\mathtt{hh}}(r\odot h_t) + W_{\mathtt{xh}}x_t + b_{\mathtt{h}})\odot z \\ &+& h_t\odot (1-z) \end{array}$$

#### MUT3:

$$z = \operatorname{sigm}(W_{\mathsf{xz}}x_t + W_{\mathsf{hz}} \tanh(h_t) + b_{\mathsf{z}})$$

$$r = \operatorname{sigm}(W_{\mathsf{xr}}x_t + W_{\mathsf{hr}}h_t + b_{\mathsf{r}})$$

$$h_{t+1} = \tanh(W_{\mathsf{hh}}(r \odot h_t) + W_{xh}x_t + b_{\mathsf{h}}) \odot z$$

$$+ h_t \odot (1-z)$$

#### Recurrence for Vision

- LSTM wer a good default choice until this year
- Use variants like GRU if you want faster compute and less parameters
- Use transformers (next lecture) as they are dominating NLP models
  - almost everyday there is a new vision transformer model

Su et al. "VI-bert: Pre-training of generic visual-linguistic representations." ICLR 2020 Lu et al. "Vilbert: Pretraining task-agnostic visiolinguistic representations for vision-and-language tasks." NeurIPS 2019 Li et al. "Visualbert: A simple and performant baseline for vision and language." *arXiv* 2019

### Summary

- RNNs allow a lot of flexibility in architecture design
- Vanilla RNNs are simple but don't work very well
- Common to use LSTM or GRU: their additive interactions improve gradient flow
- Backward flow of gradients in RNN can explode or vanish. Exploding is controlled with gradient clipping. Vanishing is controlled with additive interactions (LSTM)
- Better/simpler architectures are a hot topic of current research, as well as new paradigms for reasoning over sequences
- Better understanding (both theoretical and empirical) is needed.

Next time: Midterm!