Lecture 12: Generative Models

Administrative

- A3 is out. Due May 25.
- Milestone was due May 10th
 - Read website page for milestone requirements.
 - Need to Finish data preprocessing and initial results by then.
- Midterm and A2 grades will be out this week

Supervised Learning

Data: (x, y)

x is data, y is label

Goal: Learn a *function* to map x -> y

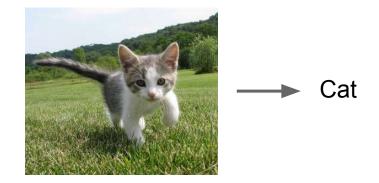
Examples: Classification, regression, object detection, semantic segmentation, image captioning, etc.

Supervised Learning

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Classification

This image is CC0 public domain

Supervised Learning

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Examples: Classification, regression, object detection, semantic segmentation, image captioning, etc.



A cat sitting on a suitcase on the floor

Image captioning

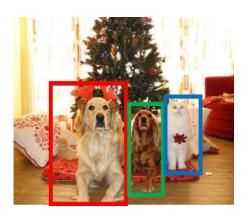
Supervised Learning

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DOG, DOG, CAT

Object Detection

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Supervised Learning

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Goal: Learn a *function* to map x -> y

Examples: Classification, regression, object detection, semantic segmentation, image captioning, etc.



Semantic Segmentation

Unsupervised Learning

Data: x Just data, no labels!

Goal: Learn some underlying hidden structure of the data

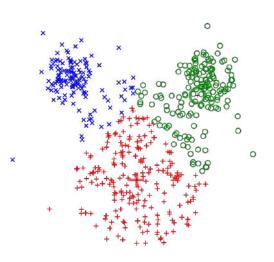
Examples: Clustering, dimensionality reduction, feature learning, density estimation, etc.

Unsupervised Learning

Data: x Just data, no labels!

Goal: Learn some underlying hidden structure of the data

Examples: Clustering, dimensionality reduction, density estimation, etc.



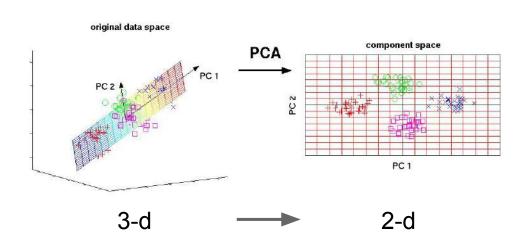
K-means clustering

Unsupervised Learning

Data: x Just data, no labels!

Goal: Learn some underlying hidden structure of the data

Examples: Clustering, dimensionality reduction, density estimation, etc.



Principal Component Analysis (Dimensionality reduction)

Unsupervised Learning

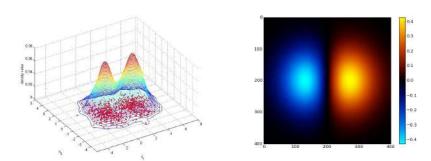
Data: x
Just data, no labels!

Goal: Learn some underlying hidden *structure* of the data

Examples: Clustering, dimensionality reduction, density estimation, etc.



1-d density estimation



2-d density estimation

Modeling p(x)

2-d density images <u>left</u> and <u>righ</u> are <u>CC0 public domain</u>

Supervised Learning

Data: (x, y)

x is data, y is label

Goal: Learn a *function* to map x -> y

Examples: Classification, regression, object detection, semantic segmentation, image captioning, etc.

Unsupervised Learning

Data: x

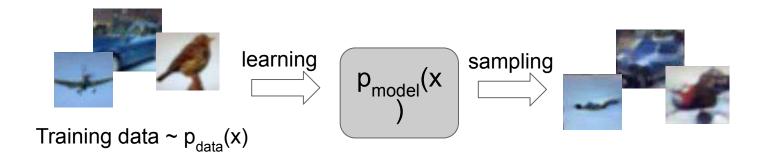
Just data, no labels!

Goal: Learn some underlying hidden *structure* of the data

Examples: Clustering, dimensionality reduction, density estimation, etc.

Generative Modeling

Given training data, generate new samples from same distribution

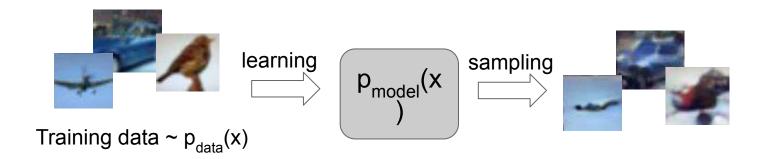


Objectives:

- Learn p_{model}(x) that approximates p_{data}(x)
 Sampling new x from p_{model}(x)

Generative Modeling

Given training data, generate new samples from same distribution



Formulate as density estimation problems:

- **Explicit density estimation**: explicitly define and solve for $p_{model}(x)$
- **Implicit density estimation**: learn model that can sample from $p_{model}(x)$ without explicitly defining it.

Why Generative Models?







- Realistic samples for artwork, super-resolution, colorization, etc.
- Learn useful features for downstream tasks such as classification.
- Getting insights from high-dimensional data (physics, medical imaging, etc.)
- Modeling physical world for simulation and planning (robotics and reinforcement learning applications)
- Many more ...

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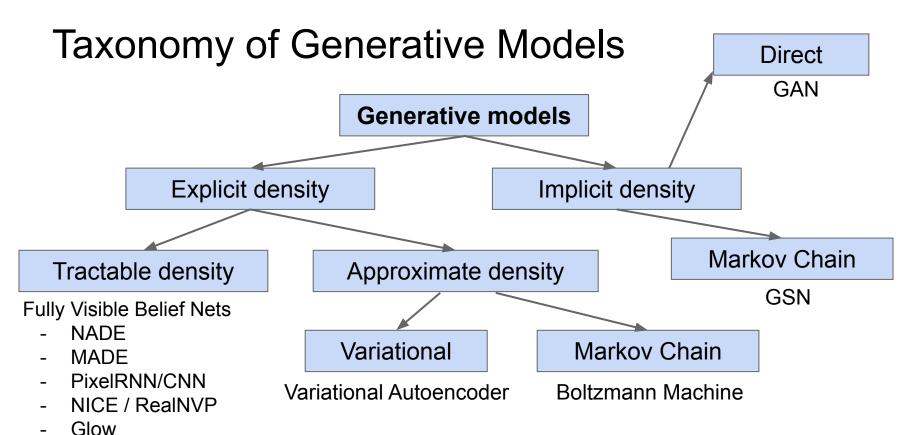


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Ffjord

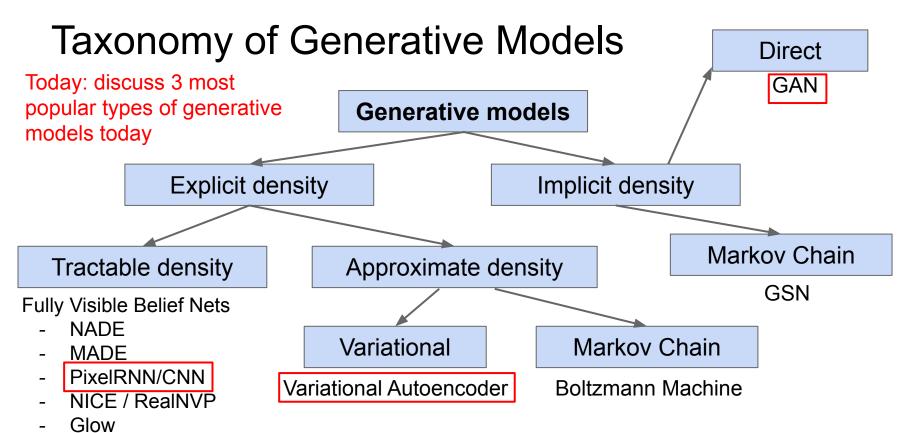


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PixelRNN and PixelCNN

(A very brief overview)

Fully visible belief network (FVBN)

Explicit density model

$$p(x) = p(x_1, x_2, \dots, x_n)$$

Likelihood of image x Joint likelihood of each pixel in the image

Fully visible belief network (FVBN)

Explicit density model

Use chain rule to decompose likelihood of an image x into product of 1-d distributions:

$$p(x) = \prod_{i=1}^n p(x_i|x_1,...,x_{i-1})$$
 \uparrow
Likelihood of image x

Probability of i'th pixel value given all previous pixels

Then maximize likelihood of training data

Fully visible belief network (FVBN)

Explicit density model

Use chain rule to decompose likelihood of an image x into product of 1-d distributions:

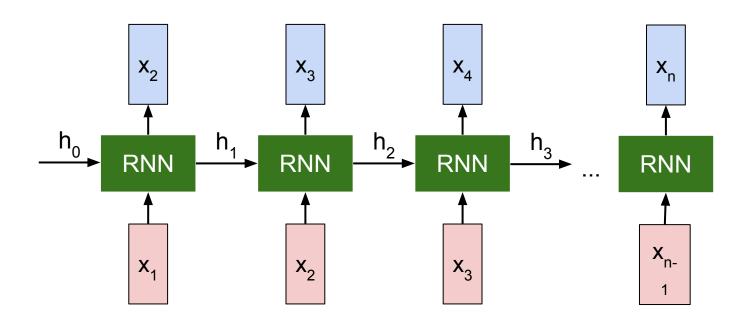
$$p(x) = \prod_{i=1}^n p(x_i|x_1,...,x_{i-1})$$
Likelihood of image x

Probability of i'th pixel value given all previous pixels

Then maximize likelihood of training data

Complex distribution over pixel values => Express using a neural network!

Recurrent Neural Network



$$p(x_i|x_1,...,x_{i-1})$$

PixelRNN [van der Oord et al. 2016]

Generate image pixels starting from corner

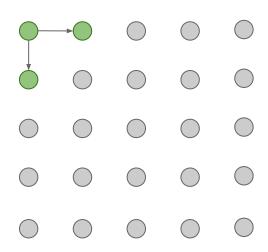
Dependency on previous pixels modeled using an RNN (LSTM)



PixeRNN [van der Oord et al. 2016]

Generate image pixels starting from corner

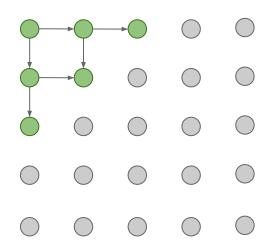
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Generate image pixels starting from corner

Dependency on previous pixels modeled using an RNN (LSTM)

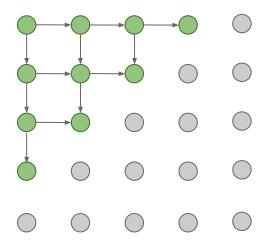


PixeIRNN [van der Oord et al. 2016]

Generate image pixels starting from corner

Dependency on previous pixels modeled using an RNN (LSTM)

Drawback: sequential generation is slow in both training and inference!



PixelCNN [van der Oord et al. 2016]

Still generate image pixels starting from corner

Dependency on previous pixels now modeled using a CNN over context region (masked convolution)

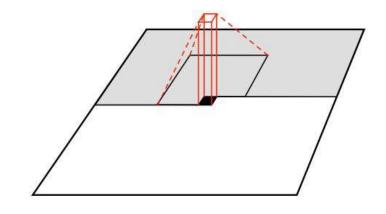


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PixelCNN [van der Oord et al. 2016]

Still generate image pixels starting from corner

Dependency on previous pixels now modeled using a CNN over context region (masked convolution)

Training is faster than PixelRNN (can parallelize convolutions since context region values known from training images)

Generation is still slow:

For a 32x32 image, we need to do forward passes of the network 1024 times for a single image

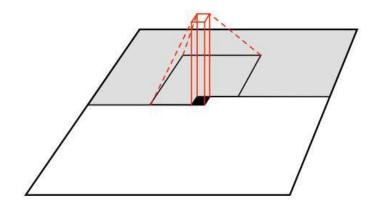


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Generation Samples



32x32 CIFAR-10



32x32 ImageNet

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PixelRNN and PixelCNN

Pros:

- Can explicitly compute likelihood p(x)
- Easy to optimize
- Good samples

Con:

Sequential generation => slow

Improving PixelCNN performance

- Gated convolutional layers
- Short-cut connections
- Discretized logistic loss
- Multi-scale
- Training tricks
- Etc...

See

- Van der Oord et al. NIPS 2016
- Salimans et al. 2017 (PixelCNN++)

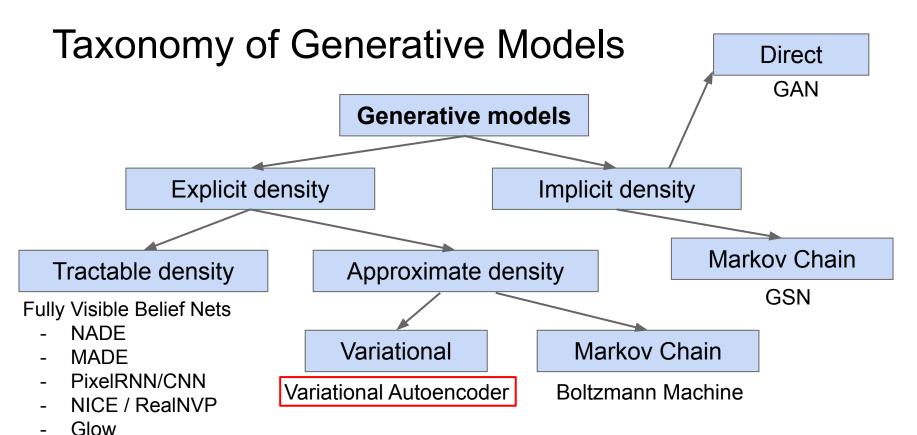


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Variational Autoencoders (VAE)

So far...

PixelRNN/CNNs define tractable density function, optimize likelihood of training data:

$$p_{\theta}(x) = \prod_{i=1}^{n} p_{\theta}(x_i|x_1, ..., x_{i-1})$$

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$$p_{\theta}(x) = \prod_{i=1}^{n} p_{\theta}(x_i|x_1, ..., x_{i-1})$$

Variational Autoencoders (VAEs) define intractable density function with latent **z**:

$$p_{ heta}(x) = \int p_{ heta}(z) p_{ heta}(x|z) dz$$

No dependencies among pixels, can generate all pixels at the same time!

Cannot optimize directly, derive and optimize lower bound on likelihood instead

So far...

PixelCNNs define tractable density function, optimize likelihood of training data:

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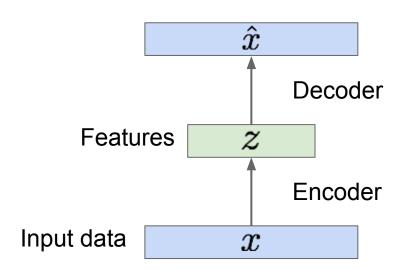
No dependencies among pixels, can generate all pixels at the same time!

Cannot optimize directly, derive and optimize lower bound on likelihood instead

Why latent z?

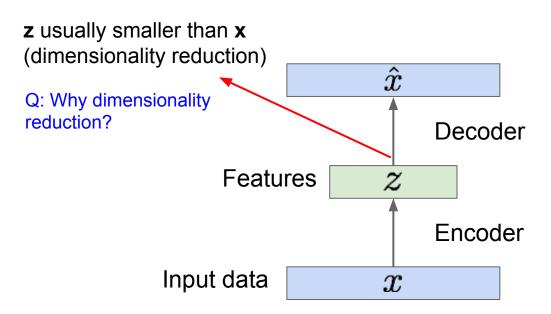
Some background first: Autoencoders

Unsupervised approach for learning a lower-dimensional feature representation from unlabeled training data



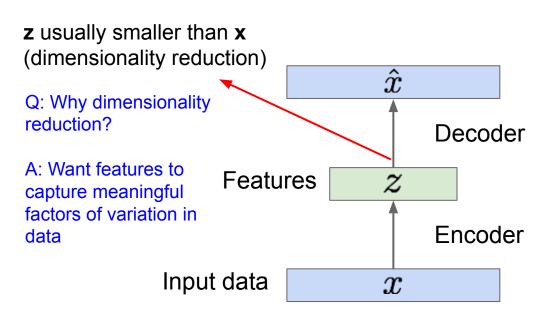


Unsupervised approach for learning a lower-dimensional feature representation from unlabeled training data



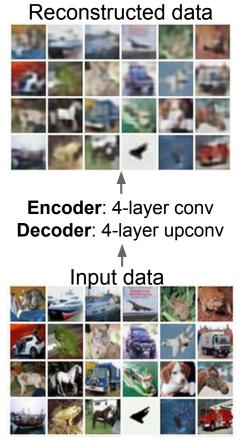


Unsupervised approach for learning a lower-dimensional feature representation from unlabeled training data



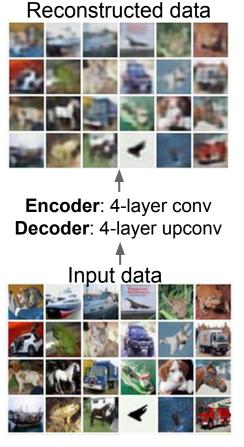


How to learn this feature Reconstructed representation? input data Train such that features \hat{x} can be used to reconstruct original data Decoder "Autoencoding" encoding input itself **Features** Encoder Input data x

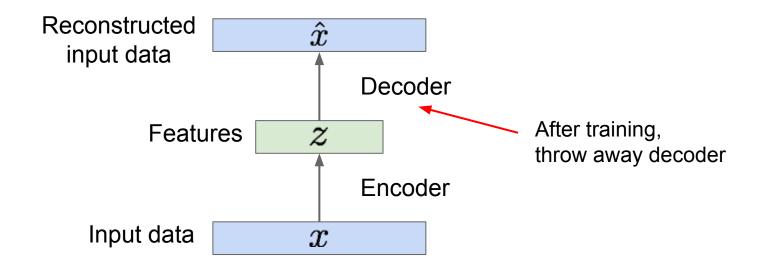


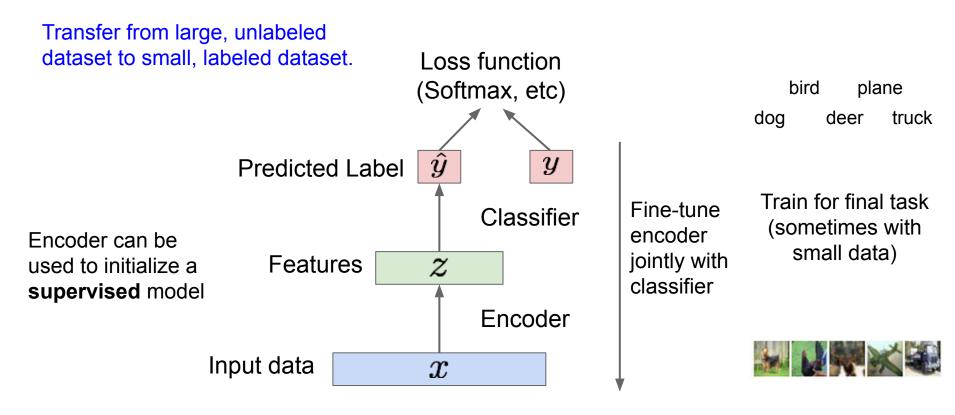
x

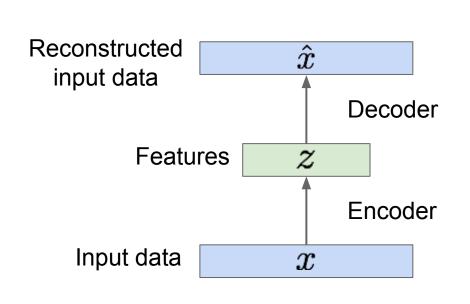
Train such that features Doesn't use labels! L2 Loss function: can be used to reconstruct original data $||x - \hat{x}||^2$ Decoder **Features** Encoder



Input data







Autoencoders can reconstruct data, and can learn features to initialize a supervised model

Features capture factors of variation in training data.

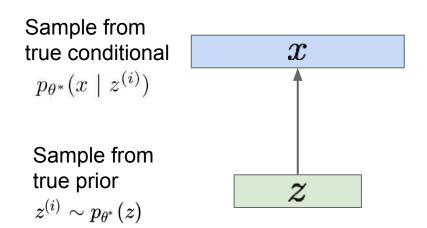
But we can't generate new images from an autoencoder because we don't know the space of z.

How do we make autoencoder a generative model?

Probabilistic spin on autoencoders - will let us sample from the model to generate data!

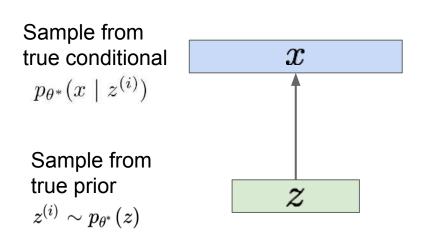
Probabilistic spin on autoencoders - will let us sample from the model to generate data!

Assume training data $\{x^{(i)}\}_{i=1}^{N}$ is generated from the distribution of unobserved (latent) representation **z**



Probabilistic spin on autoencoders - will let us sample from the model to generate data!

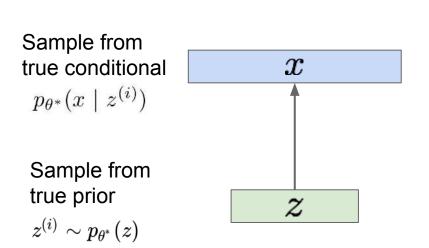
Assume training data $\{x^{(i)}\}_{i=1}^N$ is generated from the distribution of unobserved (latent) representation ${\bf z}$



Intuition (remember from autoencoders!): **x** is an image, **z** is latent factors used to generate **x**: attributes, orientation, etc.

Sample from xtrue conditional $p_{\theta^*}(x \mid z^{(i)})$ Sample from true prior $z^{(i)} \sim p_{ heta^*}(z)$

We want to estimate the true parameters θ^* of this generative model given training data x.



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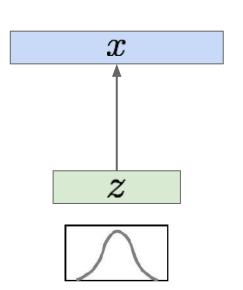
How should we represent this model?

Sample from true conditional

$$p_{\theta^*}(x \mid z^{(i)})$$

Sample from true prior

$$z^{(i)} \sim p_{ heta^*}(z)$$



We want to estimate the true parameters θ^* of this generative model given training data x.

How should we represent this model?

Choose prior p(z) to be simple, e.g. Gaussian. Reasonable for latent attributes, e.g. pose, how much smile.

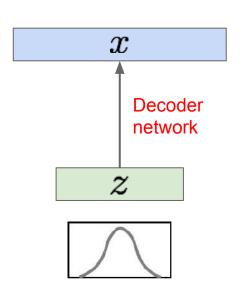


Sample from true conditional

$$p_{\theta^*}(x \mid z^{(i)})$$

Sample from true prior

$$z^{(i)} \sim p_{ heta^*}(z)$$

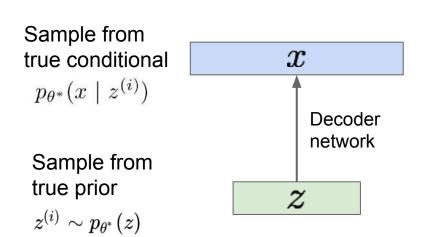


We want to estimate the true parameters θ^* of this generative model given training data x.

How should we represent this model?

Choose prior p(z) to be simple, e.g. Gaussian. Reasonable for latent attributes, e.g. pose, how much smile.

Conditional p(x|z) is complex (generates image) => represent with neural network



We want to estimate the true parameters θ^* of this generative model given training data x.

How to train the model?

Sample from true conditional $m{x}$ Decoder network Sample from true prior $m{z}^{(i)} \sim p_{ heta^*}(z)$

We want to estimate the true parameters θ^* of this generative model given training data x.

How to train the model?

Learn model parameters to maximize likelihood of training data

$$p_{\theta}(x) = \int p_{\theta}(z) p_{\theta}(x|z) dz$$

Sample from xtrue conditional $p_{\theta^*}(x \mid z^{(i)})$ Decoder network Sample from true prior $z^{(i)} \sim p_{ heta^*}(z)$

We want to estimate the true parameters θ^* of this generative model given training data x.

How to train the model?

Learn model parameters to maximize likelihood of training data

$$p_{\theta}(x) = \int p_{\theta}(z) p_{\theta}(x|z) dz$$

Q: What is the problem with this?

Intractable!

Data likelihood: $p_{\theta}(x) = \int p_{\theta}(z) p_{\theta}(x|z) dz$

Data likelihood:
$$p_{ heta}(x) = \int p_{ heta}(z) p_{ heta}(x|z) dz$$
Simple Gaussian prior

Data likelihood:
$$p_{ heta}(x) = \int p_{ heta}(z) p_{ heta}(x|z) dz$$

Data likelihood:
$$p_{\theta}(x) = \int p_{\theta}(z) p_{\theta}(x|z) dz$$

Intractable to compute p(x|z) for every z!

Data likelihood:
$$p_{\theta}(x) = \int p_{\theta}(z) p_{\theta}(x|z) dz$$

Intractable to compute p(x|z) for every z!

$$\log p(x) pprox \log rac{1}{k} \sum_{i=1}^k p(x|z^{(i)}), ext{ where } z^{(i)} \sim p(z)$$

Monte Carlo estimation is too high variance

Data likelihood:
$$p_{ heta}(x) = \int p_{ heta}(z) p_{ heta}(x|z) dz$$

Posterior density:
$$p_{ heta}(z|x) = p_{ heta}(x|z)p_{ heta}(z)/p_{ heta}(x)$$



Intractable data likelihood

Data likelihood: $p_{\theta}(x) = \int p_{\theta}(z) p_{\theta}(x|z) dz$

Posterior density also intractable: $p_{\theta}(z|x) = p_{\theta}(x|z)p_{\theta}(z)/p_{\theta}(x)$

Solution: In addition to modeling $p_{\theta}(x|z)$, learn $q_{\phi}(z|x)$ that approximates the true posterior $p_{\theta}(z|x)$.

Will see that the approximate posterior allows us to derive a lower bound on the data likelihood that is tractable, which we can optimize.

Variational inference is to approximate the unknown posterior distribution from only the observed data x

$$\log p_{\theta}(x^{(i)}) = \mathbf{E}_{z \sim q_{\phi}(z|x^{(i)})} \left[\log p_{\theta}(x^{(i)}) \right] \quad (p_{\theta}(x^{(i)}) \text{ Does not depend on } z)$$

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Taking expectation wrt. z (using encoder network) will come in handy later

$$\log p_{\theta}(x^{(i)}) = \mathbf{E}_{z \sim q_{\phi}(z|x^{(i)})} \left[\log p_{\theta}(x^{(i)}) \right] \qquad (p_{\theta}(x^{(i)}) \text{ Does not depend on } z)$$
$$= \mathbf{E}_{z} \left[\log \frac{p_{\theta}(x^{(i)} \mid z) p_{\theta}(z)}{p_{\theta}(z \mid x^{(i)})} \right] \qquad (\text{Bayes' Rule})$$

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$$= \mathbf{E}_{z} \left[\log \frac{p_{\theta}(x^{(i)} \mid z) p_{\theta}(z)}{p_{\theta}(z \mid x^{(i)})} \right] \quad \text{(Bayes' Rule)}$$

$$= \mathbf{E}_{z} \left[\log \frac{p_{\theta}(x^{(i)} \mid z) p_{\theta}(z)}{p_{\theta}(z \mid x^{(i)})} \frac{q_{\phi}(z \mid x^{(i)})}{q_{\phi}(z \mid x^{(i)})} \right] \quad \text{(Multiply by constant)}$$

$$= \mathbf{E}_{z} \left[\log p_{\theta}(x^{(i)} \mid z) \right] - \mathbf{E}_{z} \left[\log \frac{q_{\phi}(z \mid x^{(i)})}{p_{\theta}(z)} \right] + \mathbf{E}_{z} \left[\log \frac{q_{\phi}(z \mid x^{(i)})}{p_{\theta}(z \mid x^{(i)})} \right] \quad \text{(Logarithms)}$$

$$\begin{split} \log p_{\theta}(x^{(i)}) &= \mathbf{E}_{z \sim q_{\phi}(z|x^{(i)})} \left[\log p_{\theta}(x^{(i)}) \right] \quad (p_{\theta}(x^{(i)}) \text{ Does not depend on } z) \\ &= \mathbf{E}_{z} \left[\log \frac{p_{\theta}(x^{(i)} \mid z) p_{\theta}(z)}{p_{\theta}(z \mid x^{(i)})} \right] \quad \text{(Bayes' Rule)} \\ &= \mathbf{E}_{z} \left[\log \frac{p_{\theta}(x^{(i)} \mid z) p_{\theta}(z)}{p_{\theta}(z \mid x^{(i)})} \frac{q_{\phi}(z \mid x^{(i)})}{q_{\phi}(z \mid x^{(i)})} \right] \quad \text{(Multiply by constant)} \\ &= \mathbf{E}_{z} \left[\log p_{\theta}(x^{(i)} \mid z) \right] - \mathbf{E}_{z} \left[\log \frac{q_{\phi}(z \mid x^{(i)})}{p_{\theta}(z)} \right] + \mathbf{E}_{z} \left[\log \frac{q_{\phi}(z \mid x^{(i)})}{p_{\theta}(z \mid x^{(i)})} \right] \quad \text{(Logarithms)} \\ &= \mathbf{E}_{z} \left[\log p_{\theta}(x^{(i)} \mid z) \right] - D_{KL}(q_{\phi}(z \mid x^{(i)}) || p_{\theta}(z)) + D_{KL}(q_{\phi}(z \mid x^{(i)}) || p_{\theta}(z \mid x^{(i)})) \right] \end{split}$$

$$\text{The expectation wrt. z (using encoder network) let us write}$$

nice KL terms

$$\log p_{\theta}(x^{(i)}) = \mathbf{E}_{z \sim q_{\phi}(z|x^{(i)})} \left[\log p_{\theta}(x^{(i)}) \right] \quad (p_{\theta}(x^{(i)}) \text{ Does not depend on } z)$$

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$$= \mathbf{E}_{z} \left[\log p_{\theta}(x^{(i)} \mid z) \right] - D_{KL}(q_{\phi}(z \mid x^{(i)}) || p_{\theta}(z)) + D_{KL}(q_{\phi}(z \mid x^{(i)}) || p_{\theta}(z \mid x^{(i)}))$$

Decoder network gives $p_{\theta}(x|z)$, can compute estimate of this term through sampling (need some trick to differentiate through sampling).

This KL term (between Gaussians for encoder and z prior) has nice closed-form solution!

 $p_{o}(z|x)$ intractable (saw earlier), can't compute this KL term: (But we know KL divergence always >= 0.

$$\log p_{\theta}(x^{(i)}) = \mathbf{E}_{z \sim q_{\phi}(z|x^{(i)})} \left[\log p_{\theta}(x^{(i)}) \right] \quad (p_{\theta}(x^{(i)}) \text{ Does not depend on } z)$$

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$$= \mathbf{E}_{z} \left[\log \frac{p_{\theta}(x^{(i)} \mid z)p_{\theta}(z)}{p_{\theta}(z \mid x^{(i)})} \frac{q_{\phi}(z \mid x^{(i)})}{q_{\phi}(z \mid x^{(i)})} \right] \quad (\text{Multiply by constant})$$

$$= \mathbf{E}_{z} \left[\log p_{\theta}(x^{(i)} \mid z) \right] - \mathbf{E}_{z} \left[\log \frac{q_{\phi}(z \mid x^{(i)})}{p_{\theta}(z)} \right] + \mathbf{E}_{z} \left[\log \frac{q_{\phi}(z \mid x^{(i)})}{p_{\theta}(z \mid x^{(i)})} \right] \quad (\text{Logarithms})$$

$$= \mathbf{E}_{z} \left[\log p_{\theta}(x^{(i)} \mid z) \right] - D_{KL}(q_{\phi}(z \mid x^{(i)}) || p_{\theta}(z)) + D_{KL}(q_{\phi}(z \mid x^{(i)}) || p_{\theta}(z \mid x^{(i)}))$$

Decoder network gives $p_{\theta}(x|z)$, can compute estimate of this term through sampling.

This KL term (between Gaussians for encoder and z prior) has nice closed-form solution!

 $p_{\theta}(z|x)$ intractable (saw earlier), can't compute this KL term :(But we know KL divergence always ≥ 0 .

$$\log p_{\theta}(x^{(i)}) = \mathbf{E}_{z \sim q_{\phi}(z|x^{(i)})} \left[\log p_{\theta}(x^{(i)}) \right] \quad (p_{\theta}(x^{(i)}) \text{ Does not depend on } z)$$

$$= \mathbf{E}_{z} \left[\log \frac{p_{\theta}(x^{(i)} \mid z)p_{\theta}(z)}{p_{\theta}(z \mid x^{(i)})} \right] \quad (\text{Bayes' Rule})$$

$$= \mathbf{E}_{z} \left[\log \frac{p_{\theta}(x^{(i)} \mid z)p_{\theta}(z)}{p_{\theta}(z \mid x^{(i)})} \frac{q_{\phi}(z \mid x^{(i)})}{q_{\phi}(z \mid x^{(i)})} \right] \quad (\text{Multiply by constant})$$

$$= \mathbf{E}_{z} \left[\log p_{\theta}(x^{(i)} \mid z) \right] - \mathbf{E}_{z} \left[\log \frac{q_{\phi}(z \mid x^{(i)})}{p_{\theta}(z)} \right] + \mathbf{E}_{z} \left[\log \frac{q_{\phi}(z \mid x^{(i)})}{p_{\theta}(z \mid x^{(i)})} \right] \quad (\text{Logarithms})$$

$$= \underbrace{\mathbf{E}_{z} \left[\log p_{\theta}(x^{(i)} \mid z) \right] - D_{KL}(q_{\phi}(z \mid x^{(i)}) || p_{\theta}(z))}_{\mathcal{L}(x^{(i)}, \theta, \phi)} + \underbrace{D_{KL}(q_{\phi}(z \mid x^{(i)}) || p_{\theta}(z \mid x^{(i)}))}_{\geq 0} \right]}_{\geq 0}$$

Tractable lower bound which we can take gradient of and optimize! ($p_{\theta}(x|z)$ differentiable, KL term differentiable)

$$\log p_{\theta}(x^{(i)}) = \mathbf{E}_{z \sim q_{\phi}(z|x^{(i)})} \left[\log p_{\theta}(x^{(i)})\right] \quad (p_{\theta}(x^{(i)}) \text{ Does not depend on } z)$$

$$= \mathbf{E}_{z} \left[\log \frac{p_{\theta}(x^{(i)} \mid z)p_{\theta}(z)}{p_{\theta}(z \mid x^{(i)})}\right] \quad (\text{Bayes' Rule}) \qquad \qquad \text{Encoder:}$$

$$\text{reconstruct} \qquad = \mathbf{E}_{z} \left[\log \frac{p_{\theta}(x^{(i)} \mid z)p_{\theta}(z)}{p_{\theta}(z \mid x^{(i)})} \frac{q_{\phi}(z \mid x^{(i)})}{q_{\phi}(z \mid x^{(i)})}\right] \quad (\text{Multiply by constant}) \quad \text{close to prior}$$

$$= \mathbf{E}_{z} \left[\log p_{\theta}(x^{(i)} \mid z)\right] - \mathbf{E}_{z} \left[\log \frac{q_{\phi}(z \mid x^{(i)})}{p_{\theta}(z)}\right] + \mathbf{E}_{z} \left[\log \frac{q_{\phi}(z \mid x^{(i)})}{p_{\theta}(z \mid x^{(i)})}\right] \quad (\text{Logarithms})$$

$$= \mathbf{E}_{z} \left[\log p_{\theta}(x^{(i)} \mid z)\right] - D_{KL}(q_{\phi}(z \mid x^{(i)}) \mid p_{\theta}(z)) + D_{KL}(q_{\phi}(z \mid x^{(i)}) \mid p_{\theta}(z \mid x^{(i)})) \right]$$

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Tractable lower bound which we can take gradient of and optimize! ($p_{\theta}(x|z)$ differentiable, KL term differentiable)

Putting it all together: maximizing the likelihood lower bound

$$\underbrace{\mathbf{E}_{z} \left[\log p_{\theta}(x^{(i)} \mid z) \right] - D_{KL}(q_{\phi}(z \mid x^{(i)}) \mid\mid p_{\theta}(z))}_{\mathcal{L}(x^{(i)}, \theta, \phi)}$$

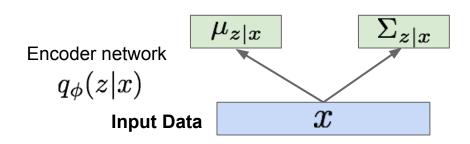
Putting it all together: maximizing the likelihood lower bound

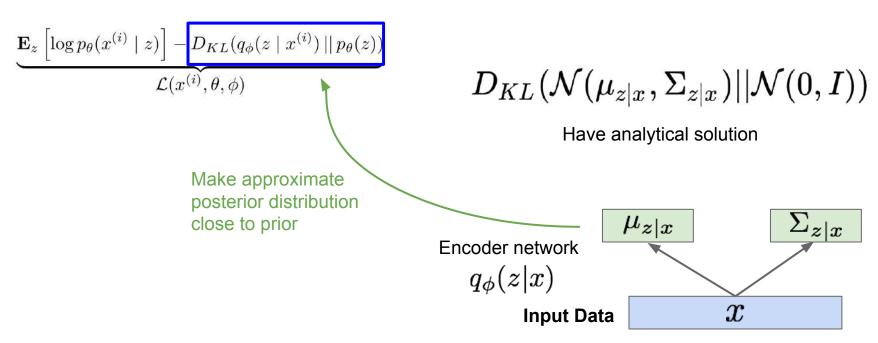
$$\underbrace{\mathbf{E}_{z} \left[\log p_{\theta}(x^{(i)} \mid z) \right] - D_{KL}(q_{\phi}(z \mid x^{(i)}) \mid\mid p_{\theta}(z))}_{\mathcal{L}(x^{(i)}, \theta, \phi)}$$

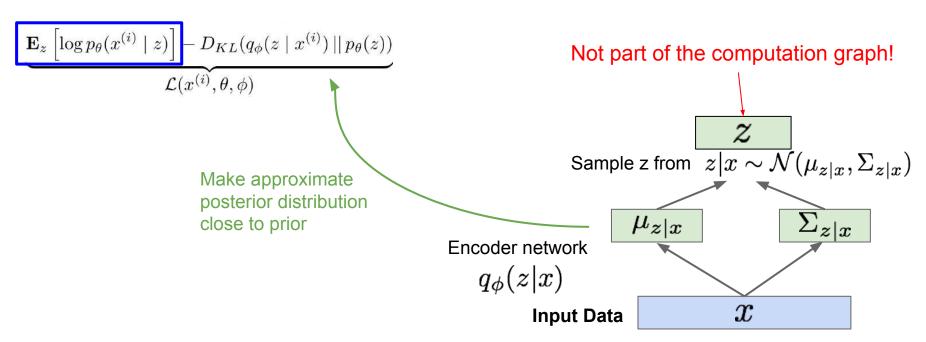
Let's look at computing the KL divergence between the estimated posterior and the prior given some data

Input Data x

$$\underbrace{\mathbf{E}_{z} \left[\log p_{\theta}(x^{(i)} \mid z) \right] - D_{KL}(q_{\phi}(z \mid x^{(i)}) \mid\mid p_{\theta}(z))}_{\mathcal{L}(x^{(i)}, \theta, \phi)}$$





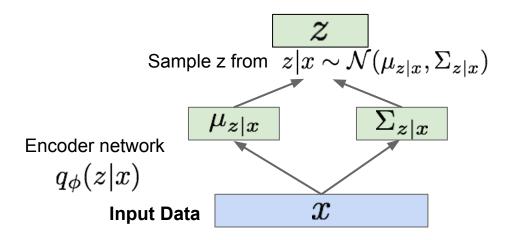


Putting it all together: maximizing the likelihood lower bound

$$\underbrace{\mathbf{E}_{z} \left[\log p_{\theta}(x^{(i)} \mid z) \right] - D_{KL}(q_{\phi}(z \mid x^{(i)}) \mid\mid p_{\theta}(z))}_{\mathcal{L}(x^{(i)}, \theta, \phi)}$$

Reparameterization trick to make sampling differentiable:

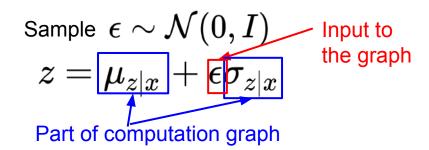
Sample
$$\epsilon \sim \mathcal{N}(0,I)$$
 $z = \mu_{z|x} + \epsilon \sigma_{z|x}$

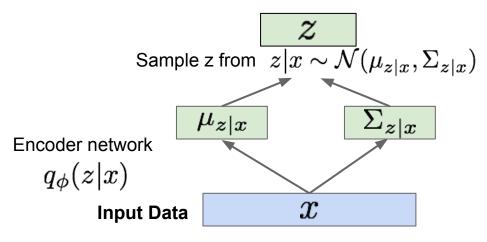


Putting it all together: maximizing the likelihood lower bound

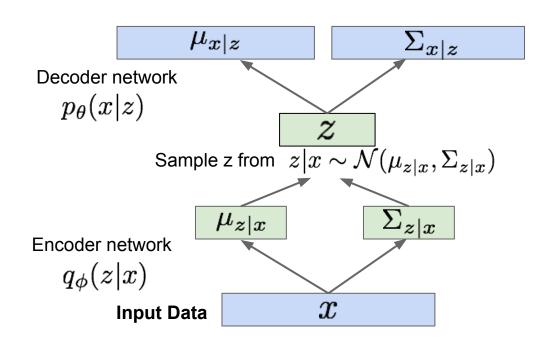
$$\underbrace{\mathbf{E}_{z} \left[\log p_{\theta}(x^{(i)} \mid z) \right] - D_{KL}(q_{\phi}(z \mid x^{(i)}) \mid\mid p_{\theta}(z))}_{\mathcal{L}(x^{(i)}, \theta, \phi)}$$

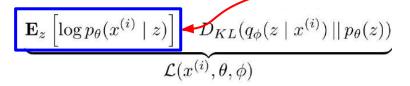
Reparameterization trick to make sampling differentiable:

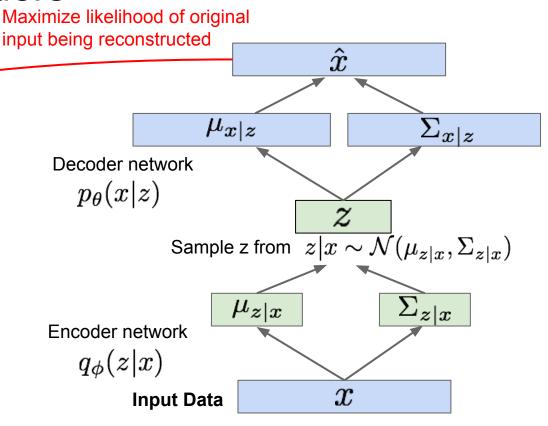




$$\underbrace{\mathbf{E}_{z} \left[\log p_{\theta}(x^{(i)} \mid z) \right] - D_{KL}(q_{\phi}(z \mid x^{(i)}) \mid\mid p_{\theta}(z))}_{\mathcal{L}(x^{(i)}, \theta, \phi)}$$



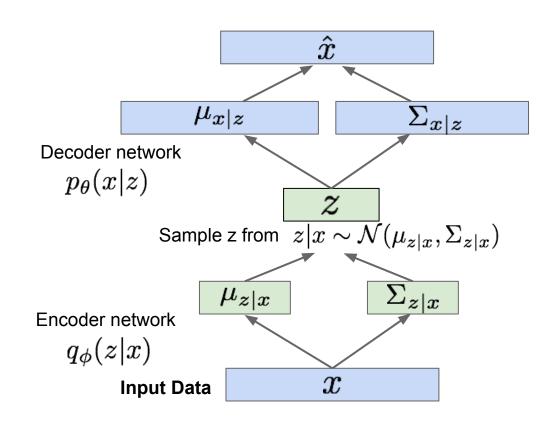




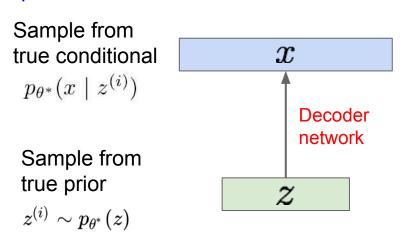
Putting it all together: maximizing the likelihood lower bound

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For every minibatch of input data: compute this forward pass, and then backprop!

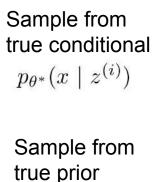


Our assumption about data generation process

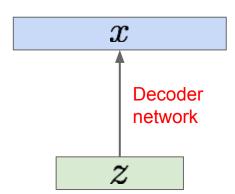


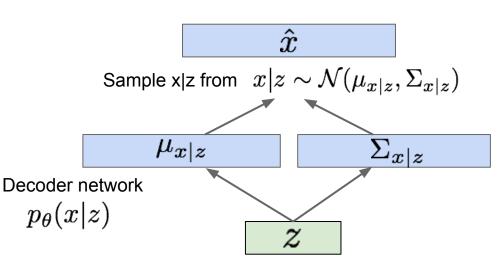
Our assumption about data generation process

Now given a trained VAE: use decoder network & sample z from prior!



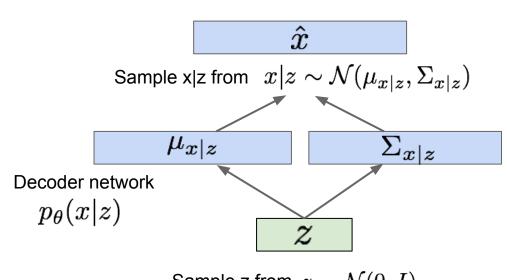
 $z^{(i)} \sim p_{ heta^*}(z)$



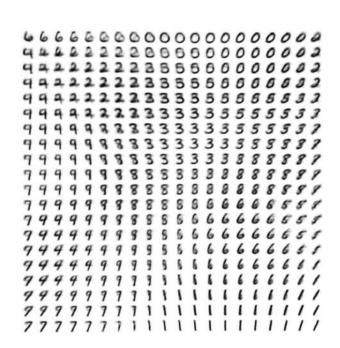


Sample z from $z \sim \mathcal{N}(0, I)$

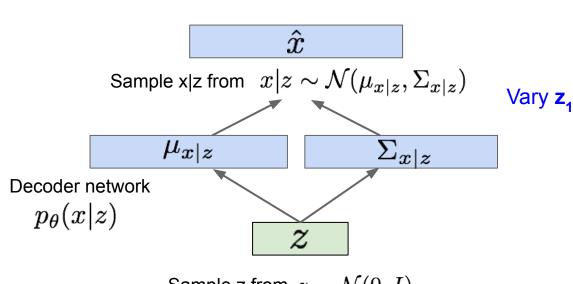
Use decoder network. Now sample z from prior!



Sample z from $\,z \sim \mathcal{N}(0,I)\,$



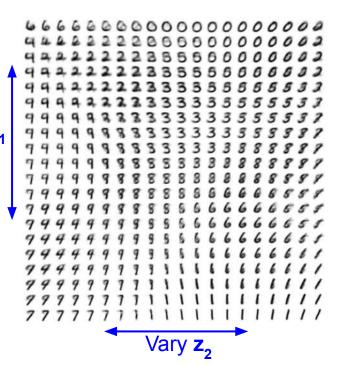
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Sample z from $\,z \sim \mathcal{N}(0,I)\,$

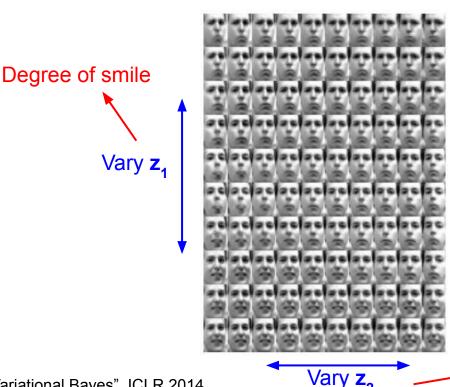
Kingma and Welling, "Auto-Encoding Variational Bayes", ICLR 2014

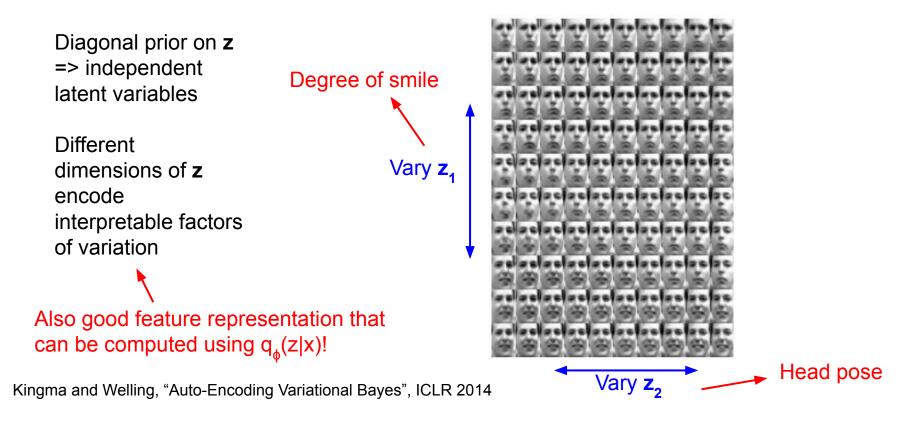
Data manifold for 2-d z



Diagonal prior on **z** => independent latent variables

Different dimensions of **z** encode interpretable factors of variation







32x32 CIFAR-10



Labeled Faces in the Wild

Figures copyright (L) Dirk Kingma et al. 2016; (R) Anders Larsen et al. 2017. Reproduced with permission.

Probabilistic spin to traditional autoencoders => allows generating data

Defines an intractable density => derive and optimize a (variational) lower bound

Pros:

- Principled approach to generative models
- Interpretable latent space.
- Allows inference of q(z|x), can be useful feature representation for other tasks

Cons:

- Maximizes lower bound of likelihood: okay, but not as good evaluation as PixelRNN/PixelCNN
- Samples blurrier and lower quality compared to state-of-the-art (GANs)

Active areas of research:

- More flexible approximations, e.g. richer approximate posterior instead of diagonal Gaussian, e.g., Gaussian Mixture Models (GMMs), Categorical Distributions.
- Learning disentangled representations.

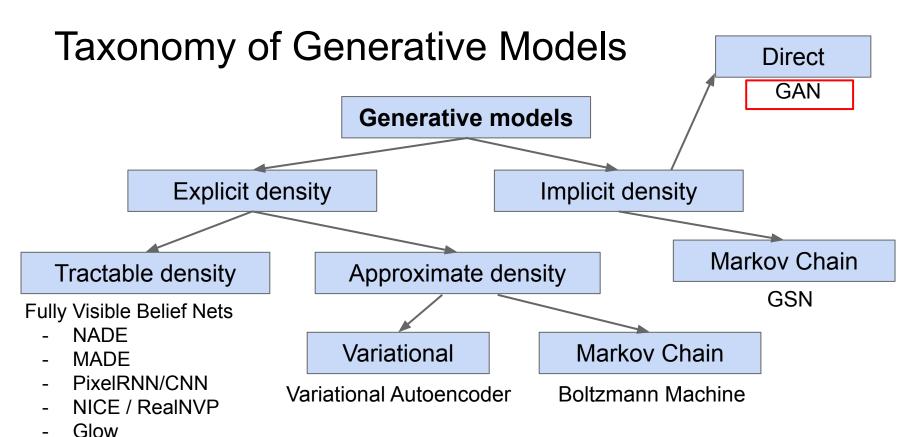


Figure copyright and adapted from Ian Goodfellow, Tutorial on Generative Adversarial Networks, 2017.

Ffjord

Generative Adversarial Networks (GANs)

So far...

PixelCNNs define tractable density function, optimize likelihood of training data:

$$p_{\theta}(x) = \prod_{i=1} p_{\theta}(x_i|x_1, ..., x_{i-1})$$

VAEs define intractable density function with latent **z**:

$$p_{\theta}(x) = \int p_{\theta}(z) p_{\theta}(x|z) dz$$

Cannot optimize directly, derive and optimize lower bound on likelihood instead

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PixelCNNs define tractable density function, optimize likelihood of training data:

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What if we give up on explicitly modeling density, and just want ability to sample?

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$$p_{ heta}(x) = \int p_{ heta}(z) p_{ heta}(x|z) dz$$

Cannot optimize directly, derive and optimize lower bound on likelihood instead

What if we give up on explicitly modeling density, and just want ability to sample?

GANs: not modeling any explicit density function!

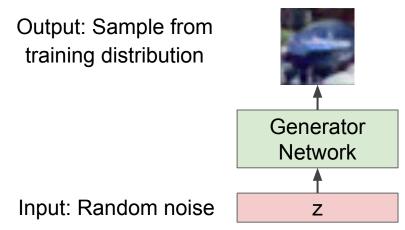
Problem: Want to sample from complex, high-dimensional training distribution. No direct way to do this!

Solution: Sample from a simple distribution we can easily sample from, e.g. random noise. Learn transformation to training distribution.

Generative Adversarial Networks

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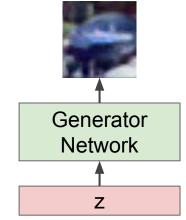
Generative Adversarial Networks

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But we don't know which sample z maps to which training image -> can't learn by reconstructing training images

Output: Sample from training distribution



Input: Random noise

Ian Goodfellow et al., "Generative Adversarial Nets", NIPS 2014

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Objective: generated images should look "real" Generator Network

Input: Random noise

Generative Adversarial Networks

Problem: Want to sample from complex, high-dimensional training distribution. No direct way to do this!

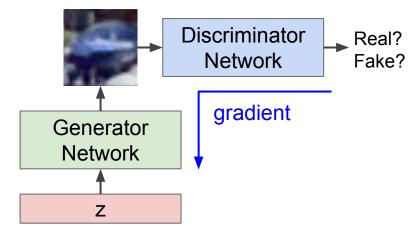
Solution: Sample from a simple distribution we can easily sample from, e.g. random noise. Learn transformation to training distribution.

But we don't know which sample z maps to which training image -> can't learn by reconstructing training images

Solution: Use a discriminator network to tell whether the generate image is within data distribution ("real") or not

Output: Sample from training distribution

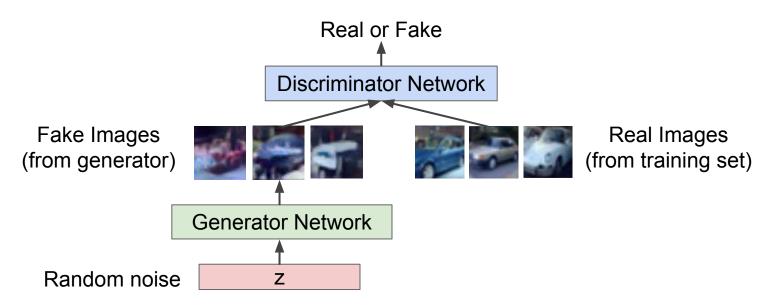
Input: Random noise



lan Goodfellow et al., "Generative Adversarial Nets", NIPS 2014

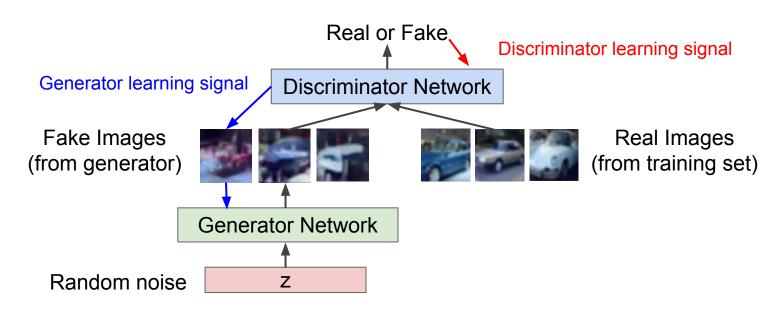
Discriminator network: try to distinguish between real and fake images **Generator network**: try to fool the discriminator by generating real-looking images

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Fake and real images copyright Emily Denton et al. 2015. Reproduced with permission.

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Discriminator network: try to distinguish between real and fake images **Generator network**: try to fool the discriminator by generating real-looking images

Train jointly in minimax game

```
\min_{\theta_g} \max_{\theta_d} \left[ \mathbb{E}_{x \sim p_{data}} \log D_{\theta_d}(x) + \mathbb{E}_{z \sim p(z)} \log (1 - D_{\theta_d}(G_{\theta_g}(z))) \right]
                      Discriminator
objective
                      objective
```

Discriminator network: try to distinguish between real and fake images **Generator network**: try to fool the discriminator by generating real-looking images

Train jointly in **minimax game**

Discriminator outputs likelihood in (0,1) of real image

$$\min_{\theta_g} \max_{\theta_d} \left[\mathbb{E}_{x \sim p_{data}} \log D_{\theta_d}(x) + \mathbb{E}_{z \sim p(z)} \log (1 - D_{\theta_d}(G_{\theta_g}(z))) \right]$$

$$\text{Discriminator output for generated fake data G(z)}$$



Discriminator network: try to distinguish between real and fake images **Generator network**: try to fool the discriminator by generating real-looking images

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 Discriminator output for for real data x generated fake data G(z)



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Discriminator outputs likelihood in (0,1) of real image

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Discriminator output for for real data x
$$\min_{\theta_d} \max_{\theta_d} \left[\mathbb{E}_{x \sim p_{data}} \log D_{\theta_d}(x) + \mathbb{E}_{z \sim p(z)} \log (1 - D_{\theta_d}(G_{\theta_g}(z))) \right]$$
Discriminator output for generated fake data G(z)

- Discriminator (θ_d) wants to **maximize objective** such that D(x) is close to 1 (real) and D(G(z)) is close to 0 (fake)
- Generator (θ_g) wants to **minimize objective** such that D(G(z)) is close to 1 (discriminator is fooled into thinking generated G(z) is real)

Minimax objective function:

$$\min_{\theta_g} \max_{\theta_d} \left[\mathbb{E}_{x \sim p_{data}} \log D_{\theta_d}(x) + \mathbb{E}_{z \sim p(z)} \log (1 - D_{\theta_d}(G_{\theta_g}(z))) \right]$$

Alternate between:

Gradient ascent on discriminator

$$\max_{\theta_d} \left[\mathbb{E}_{x \sim p_{data}} \log D_{\theta_d}(x) + \mathbb{E}_{z \sim p(z)} \log (1 - D_{\theta_d}(G_{\theta_g}(z))) \right]$$

Gradient descent on generator

$$\min_{\theta_g} \mathbb{E}_{z \sim p(z)} \log(1 - D_{\theta_d}(G_{\theta_g}(z)))$$

Minimax objective function:

$$\min_{\theta_g} \max_{\theta_d} \left[\mathbb{E}_{x \sim p_{data}} \log D_{\theta_d}(x) + \mathbb{E}_{z \sim p(z)} \log (1 - D_{\theta_d}(G_{\theta_g}(z))) \right]$$

Alternate between:

Gradient ascent on discriminator

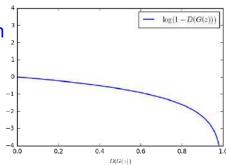
$$\max_{\theta_d} \left[\mathbb{E}_{x \sim p_{data}} \log D_{\theta_d}(x) + \mathbb{E}_{z \sim p(z)} \log (1 - D_{\theta_d}(G_{\theta_g}(z))) \right]$$

Gradient descent on generator

$$\min_{ heta_g} \mathbb{E}_{z \sim p(z)} \log (1 - D_{ heta_d}(G_{ heta_g}(z)))$$
 fake, want to learn from it to improve generator.

In practice, optimizing this generator objective does not work well!

When sample is likely fake, want to learn from it to improve generator (move to the right on X axis).



lan Goodfellow et al., "Generative Adversarial Nets", NIPS 2014

Minimax objective function:

$$\min_{\theta_g} \max_{\theta_d} \left[\mathbb{E}_{x \sim p_{data}} \log D_{\theta_d}(x) + \mathbb{E}_{z \sim p(z)} \log (1 - D_{\theta_d}(G_{\theta_g}(z))) \right]$$

Alternate between:

1. Gradient ascent on discriminator

$$\max_{\theta_d} \left[\mathbb{E}_{x \sim p_{data}} \log D_{\theta_d}(x) + \mathbb{E}_{z \sim p(z)} \log(1 - D_{\theta_d}(G_{\theta_g}(z))) \right]$$

2. Gradient descent on generator

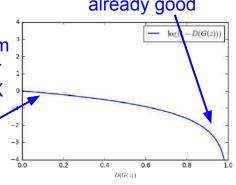
$$\min_{ heta_g} \mathbb{E}_{z \sim p(z)} \log (1 - D_{ heta_d}(G_{ heta_g}(z)))$$
 fake, want to learn from

In practice, optimizing this generator objective does not work well!

When sample is likely fake, want to learn from it to improve generator (move to the right on X axis).

But gradient in this region is relatively flat!

Gradient signal dominated by region where sample is already good



Training GANs: Two-player game

Minimax objective function:

$$\min_{\theta_g} \max_{\theta_d} \left[\mathbb{E}_{x \sim p_{data}} \log D_{\theta_d}(x) + \mathbb{E}_{z \sim p(z)} \log (1 - D_{\theta_d}(G_{\theta_g}(z))) \right]$$

Alternate between:

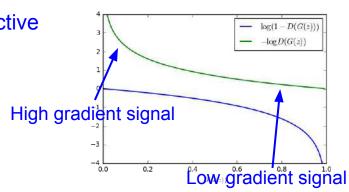
Gradient ascent on discriminator

$$\max_{\theta_d} \left[\mathbb{E}_{x \sim p_{data}} \log D_{\theta_d}(x) + \mathbb{E}_{z \sim p(z)} \log(1 - D_{\theta_d}(G_{\theta_g}(z))) \right]$$

Instead: Gradient ascent on generator, different objective

$$\max_{\theta_g} \mathbb{E}_{z \sim p(z)} \log(D_{\theta_d}(G_{\theta_g}(z)))$$

Instead of minimizing likelihood of discriminator being correct, now maximize likelihood of discriminator being wrong. Same objective of fooling discriminator, but now higher gradient signal for bad samples => works much better! Standard in practice.



Training GANs: Two-player game

Putting it together: GAN training algorithm

for number of training iterations do

for k steps do

- Sample minibatch of m noise samples $\{z^{(1)}, \ldots, z^{(m)}\}$ from noise prior $p_q(z)$.
- ullet Sample minibatch of m examples $\{oldsymbol{x}^{(1)},\ldots,oldsymbol{x}^{(m)}\}$ from data generating distribution $p_{\text{data}}(\boldsymbol{x})$.
- Update the discriminator by ascending its stochastic gradient:

$$\nabla_{\theta_d} \frac{1}{m} \sum_{i=1}^{m} \left[\log D_{\theta_d}(x^{(i)}) + \log(1 - D_{\theta_d}(G_{\theta_g}(z^{(i)}))) \right]$$

end for

- Sample minibatch of m noise samples $\{z^{(1)}, \dots, z^{(m)}\}$ from noise prior $p_q(z)$.
- Update the generator by ascending its stochastic gradient (improved objective):

$$\nabla_{\theta_g} \frac{1}{m} \sum_{i=1}^m \log(D_{\theta_d}(G_{\theta_g}(z^{(i)})))$$

end for

Putting it together: GAN training algorithm

for number of training iterations do

for k steps do

- Sample minibatch of m noise samples $\{z^{(1)}, \ldots, z^{(m)}\}$ from noise prior $p_q(z)$.
- Sample minibatch of m examples $\{x^{(1)}, \ldots, x^{(m)}\}$ from data generating distribution $p_{\text{data}}(x)$.
- Update the discriminator by ascending its stochastic gradient:

$$\nabla_{\theta_d} \frac{1}{m} \sum_{i=1}^m \left[\log D_{\theta_d}(x^{(i)}) + \log(1 - D_{\theta_d}(G_{\theta_g}(z^{(i)}))) \right]$$

Followup work (e.g. Wasserstein GAN, BEGAN) alleviates this problem, better stability!

Some find k=1

others use k > 1,

more stable.

no best rule.

end for

- Sample minibatch of m noise samples $\{z^{(1)}, \ldots, z^{(m)}\}$ from noise prior $p_q(z)$.
- Update the generator by ascending its stochastic gradient (improved objective):

$$\nabla_{\theta_g} \frac{1}{m} \sum_{i=1}^m \log(D_{\theta_d}(G_{\theta_g}(z^{(i)})))$$

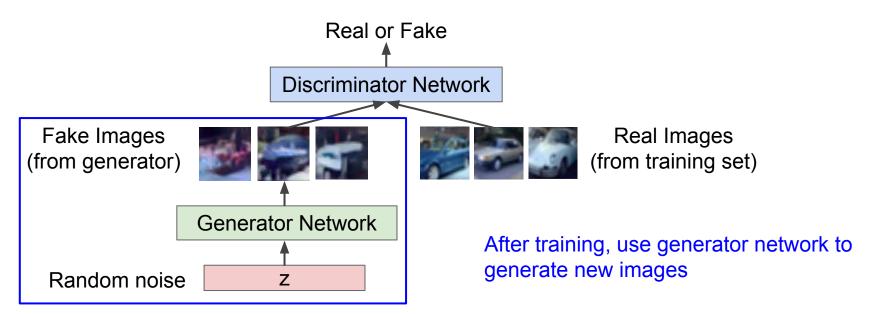
end for

Arjovsky et al. "Wasserstein gan." arXiv preprint arXiv:1701.07875 (2017)

Berthelot, et al. "Began: Boundary equilibrium generative adversarial networks." arXiv preprint arXiv:1703.10717 (2017)

Training GANs: Two-player game

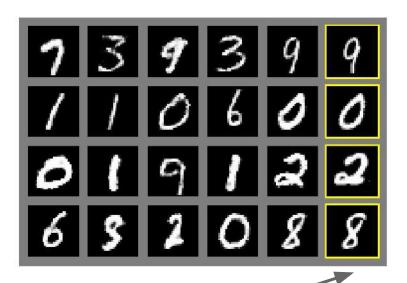
Generator network: try to fool the discriminator by generating real-looking images **Discriminator network**: try to distinguish between real and fake images



Fake and real images copyright Emily Denton et al. 2015. Reproduced with permission.

Generative Adversarial Nets

Generated samples





Nearest neighbor from training set

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Generative Adversarial Nets

Generated samples (CIFAR-10)





Nearest neighbor from training set

Figures copyright Ian Goodfellow et al., 2014. Reproduced with permission.

Generative Adversarial Nets: Convolutional Architectures

Generator is an upsampling network with fractionally-strided convolutions Discriminator is a convolutional network

Architecture guidelines for stable Deep Convolutional GANs

- Replace any pooling layers with strided convolutions (discriminator) and fractional-strided convolutions (generator).
- Use batchnorm in both the generator and the discriminator.
- Remove fully connected hidden layers for deeper architectures.
- Use ReLU activation in generator for all layers except for the output, which uses Tanh.
- Use LeakyReLU activation in the discriminator for all layers.

Radford et al, "Unsupervised Representation Learning with Deep Convolutional Generative Adversarial Networks", ICLR 2016

Generative Adversarial Nets: Convolutional Architectures

Samples from the model look much better!



Radford et al, ICLR 2016

Generative Adversarial Nets: Convolutional Architectures

Interpolating between random points in laten space

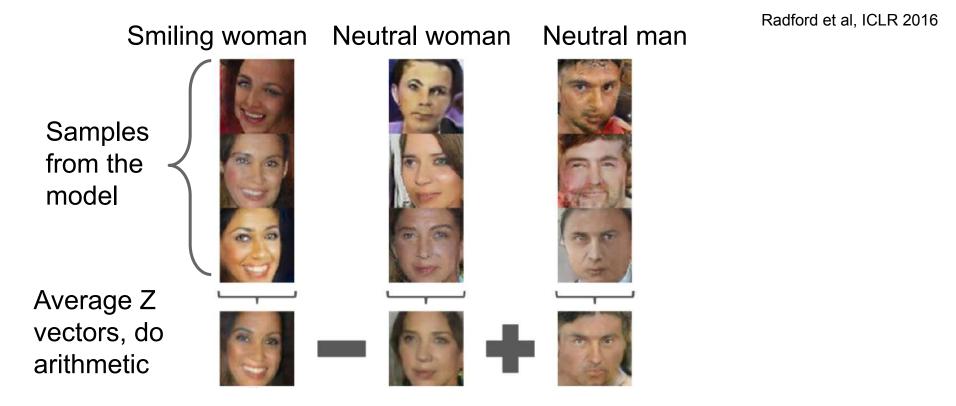


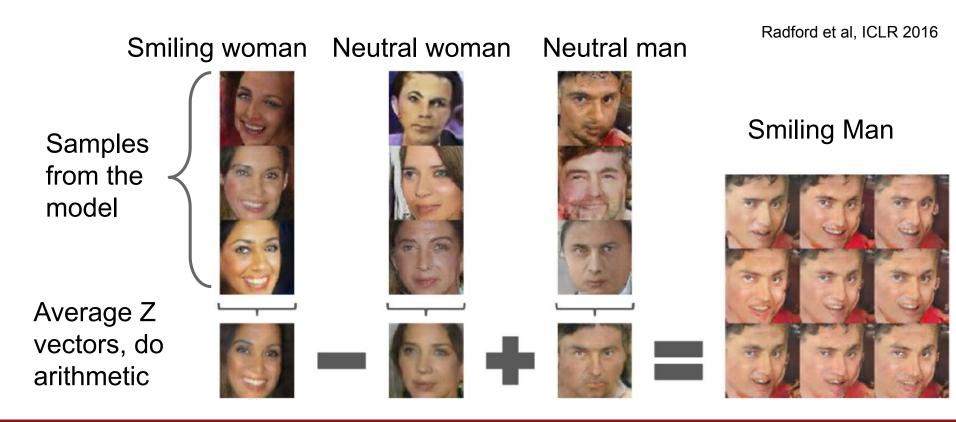
Radford et al, ICLR 2016

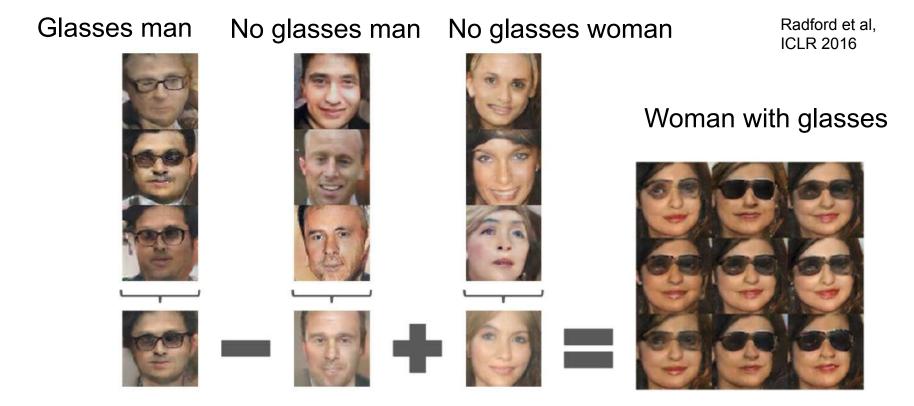
Samples from the model

Smiling woman Neutral woman Neutral man Ne

Radford et al, ICLR 2016







2017: Explosion of GANs

See also: https://github.com/soumith/ganhacks for tips and tricks for trainings GANs

"The GAN Zoo"

- GAN Generative Adversarial Networks
- . 3D-GAN Learning a Probabilistic Latent Space of Object Shapes via 3D Generative-Adversarial Modeling
- acGAN Face Aging With Conditional Generative Adversarial Networks
- AC-GAN Conditional Image Synthesis With Auxiliary Classifier GANs
- AdaGAN AdaGAN: Boosting Generative Models
- · AEGAN Learning Inverse Mapping by Autoencoder based Generative Adversarial Nets
- AffGAN Amortised MAP Inference for Image Super-resolution
- · AL-CGAN Learning to Generate Images of Outdoor Scenes from Attributes and Semantic Layouts
- · ALI Adversarially Learned Inference
- . AM-GAN Generative Adversarial Nets with Labeled Data by Activation Maximization
- AnoGAN Unsupervised Anomaly Detection with Generative Adversarial Networks to Guide Marker Discovery
- ArtGAN ArtGAN: Artwork Synthesis with Conditional Categorial GANs
- b-GAN b-GAN: Unified Framework of Generative Adversarial Networks
- . Bayesian GAN Deep and Hierarchical Implicit Models
- . BEGAN BEGAN: Boundary Equilibrium Generative Adversarial Networks
- . BiGAN Adversarial Feature Learning
- BS-GAN Boundary-Seeking Generative Adversarial Networks
- . CGAN Conditional Generative Adversarial Nets
- CaloGAN CaloGAN: Simulating 3D High Energy Particle Showers in Multi-Layer Electromagnetic Calorimeters
 with Generative Adversarial Networks
- · CCGAN Semi-Supervised Learning with Context-Conditional Generative Adversarial Networks
- CatGAN Unsupervised and Semi-supervised Learning with Categorical Generative Adversarial Networks
- CoGAN Coupled Generative Adversarial Networks

- Context-RNN-GAN Contextual RNN-GANs for Abstract Reasoning Diagram Generation
- C-RNN-GAN C-RNN-GAN: Continuous recurrent neural networks with adversarial training
- · CS-GAN Improving Neural Machine Translation with Conditional Sequence Generative Adversarial Nets
- CVAE-GAN CVAE-GAN: Fine-Grained Image Generation through Asymmetric Training
- CycleGAN Unpaired Image-to-Image Translation using Cycle-Consistent Adversarial Networks
- . DTN Unsupervised Cross-Domain Image Generation
- . DCGAN Unsupervised Representation Learning with Deep Convolutional Generative Adversarial Networks
- . DiscoGAN Learning to Discover Cross-Domain Relations with Generative Adversarial Networks
- . DR-GAN Disentangled Representation Learning GAN for Pose-Invariant Face Recognition
- DualGAN DualGAN: Unsupervised Dual Learning for Image-to-Image Translation
- . EBGAN Energy-based Generative Adversarial Network
- f-GAN f-GAN: Training Generative Neural Samplers using Variational Divergence Minimization
- . FF-GAN Towards Large-Pose Face Frontalization in the Wild
- . GAWWN Learning What and Where to Draw
- · GeneGAN GeneGAN: Learning Object Transfiguration and Attribute Subspace from Unpaired Data
- Geometric GAN Geometric GAN
- GoGAN Gang of GANs: Generative Adversarial Networks with Maximum Margin Ranking
- GP-GAN GP-GAN: Towards Realistic High-Resolution Image Blending
- IAN Neural Photo Editing with Introspective Adversarial Networks
- iGAN Generative Visual Manipulation on the Natural Image Manifold
- IcGAN Invertible Conditional GANs for image editing
- ID-CGAN Image De-raining Using a Conditional Generative Adversarial Network
- . Improved GAN Improved Techniques for Training GANs
- . InfoGAN InfoGAN: Interpretable Representation Learning by Information Maximizing Generative Adversarial Nets
- LAGAN Learning Particle Physics by Example: Location-Aware Generative Adversarial Networks for Physics Synthesis
- LAPGAN Deep Generative Image Models using a Laplacian Pyramid of Adversarial Networks

https://github.com/hindupuravinash/the-gan-zoo

2017: Explosion of GANs

Better training and generation



LSGAN, Zhu 2017.



Wasserstein GAN, Arjovsky 2017. Improved Wasserstein GAN, Gulrajani 2017.

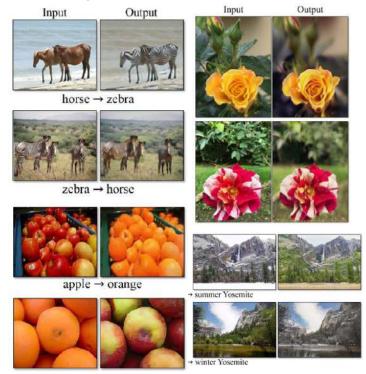




Progressive GAN, Karras 2018.

2017: Explosion of GANs

Source->Target domain transfer



CycleGAN. Zhu et al. 2017.

Text -> Image Synthesis

this small bird has a pink breast and crown, and black almost all black with a red primaries and secondaries.

this magnificent fellow is crest, and white cheek patch.





Reed et al. 2017. Many GAN applications



Pix2pix. Isola 2017. Many examples at https://phillipi.github.io/pix2pix/

2019: BigGAN

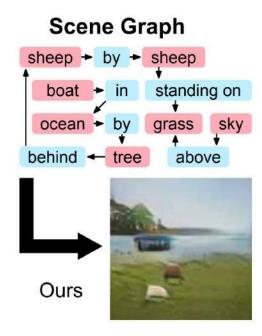


Brock et al., 2019

Scene graphs to GANs

Specifying exactly what kind of image you want to generate.

The explicit structure in scene graphs provides better image generation for complex scenes.

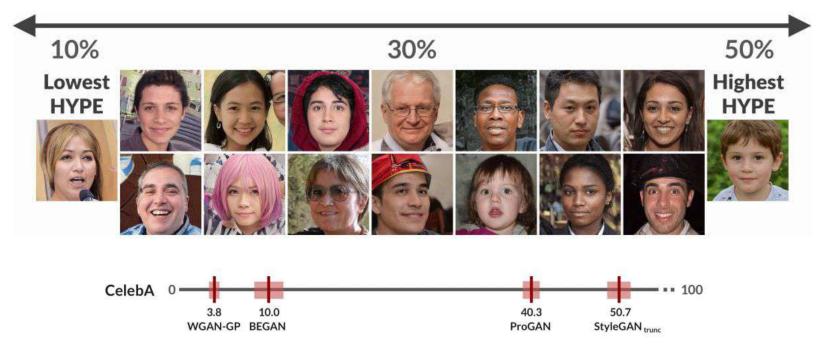


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Johnson et al. Image Generation from Scene Graphs, CVPR 2019

HYPE: Human eYe Perceptual Evaluations

hype.stanford.edu



Zhou, Gordon, Krishna et al. HYPE: Human eYe Perceptual Evaluations, NeurIPS 2019

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Summary: GANs

Don't work with an explicit density function Take game-theoretic approach: learn to generate from training distribution through 2-player game

Pros:

Beautiful, state-of-the-art samples!

Cons:

- Trickier / more unstable to train
- Can't solve inference queries such as p(x), p(z|x)

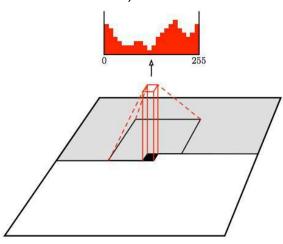
Active areas of research:

- Better loss functions, more stable training (Wasserstein GAN, LSGAN, many others)
- Conditional GANs, GANs for all kinds of applications

Summary

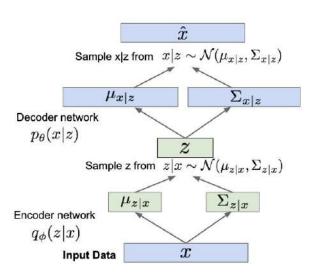
Autoregressive models:

PixelRNN, PixelCNN



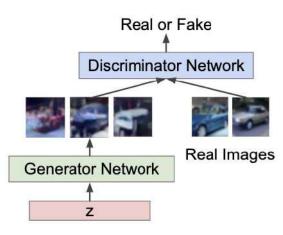
Van der Oord et al, "Conditional image generation with pixelCNN decoders". NIPS 2016

Variational Autoencoders



Kingma and Welling, "Auto-encoding variational bayes", ICLR 2013

Generative Adversarial Networks (GANs)



Goodfellow et al, "Generative Adversarial Nets", NIPS 2014

Useful Resources on Generative Models

CS 236: <u>Deep Generative Models</u> (Stanford)

CS 294-158 <u>Deep Unsupervised Learning</u> (Berkeley)

Next: Self-Supervised Learning