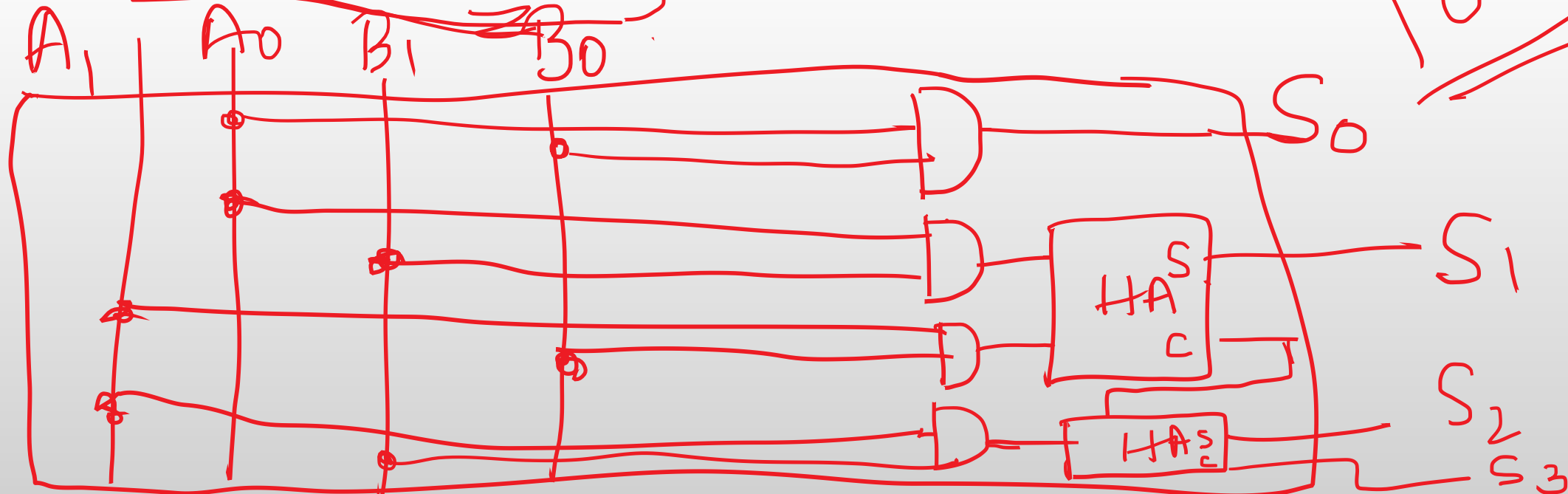
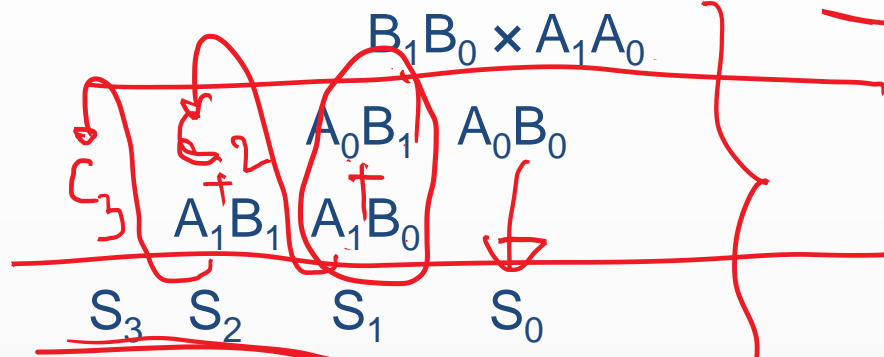




# MULTIPLIERS AND MAGNITUDE COMPARATORS

# Binary Multiplier

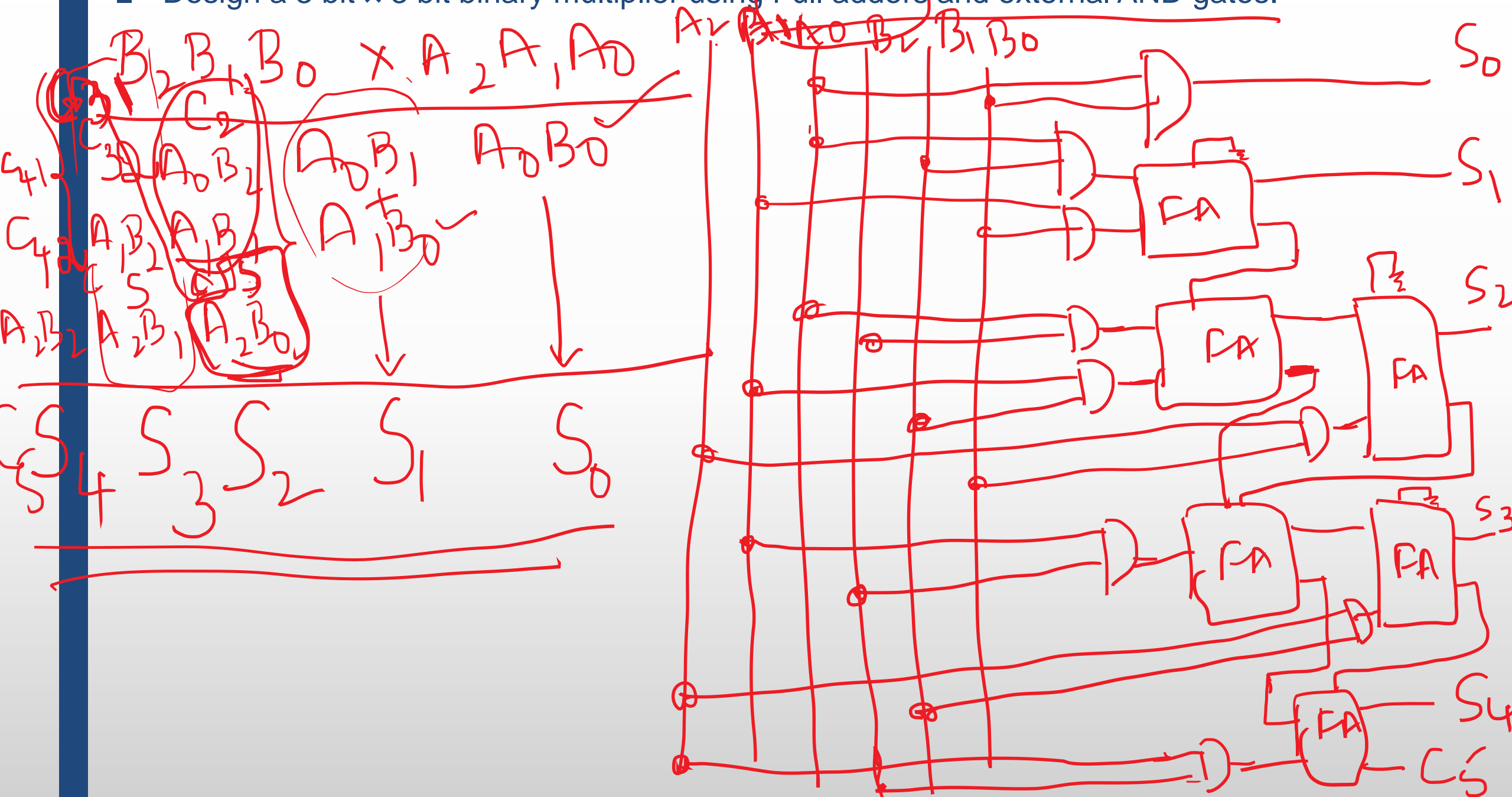
- 2 bit  $\times$  2 bit binary multiplier using adders and external gates.



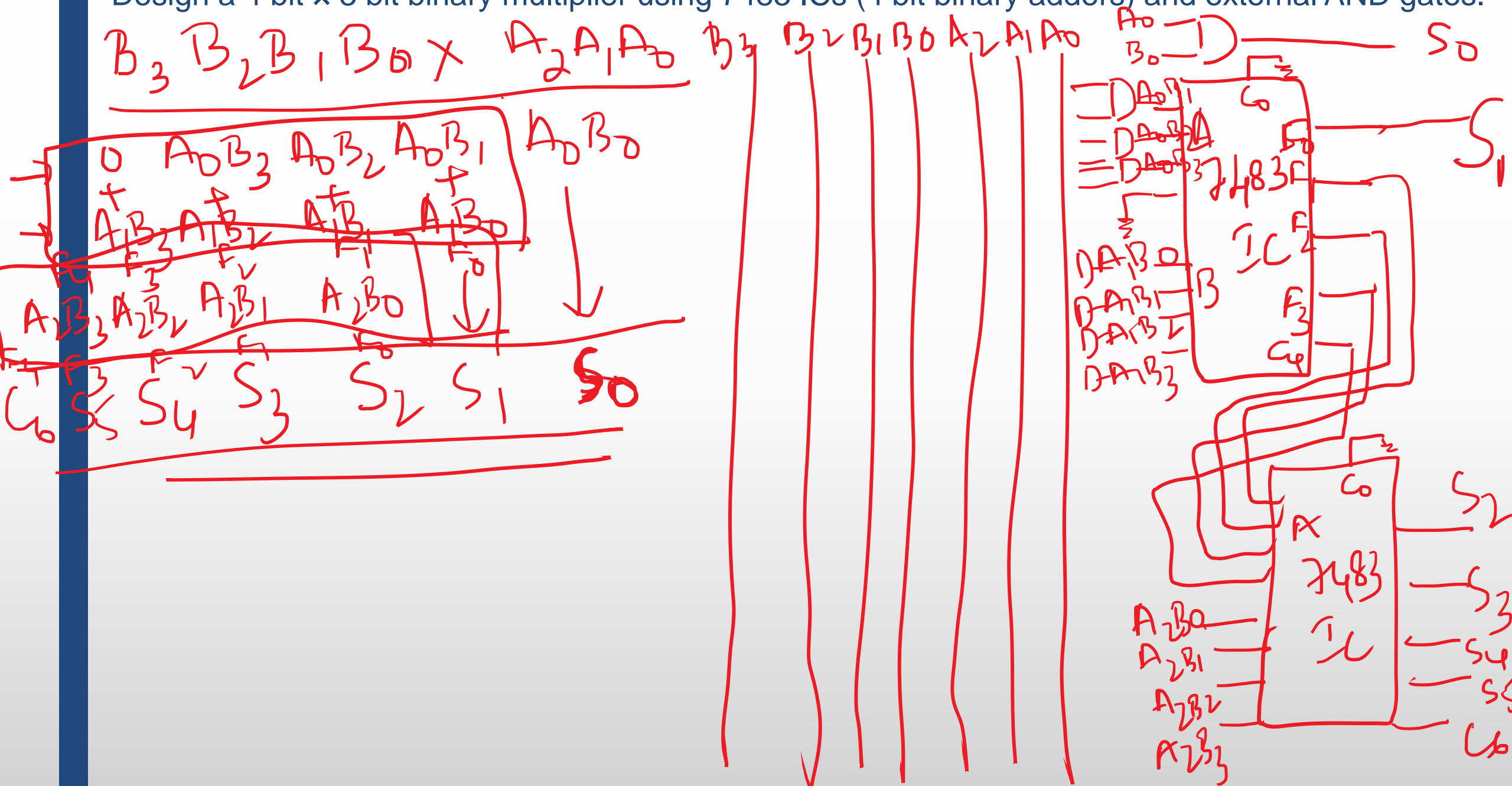
AND



- Design a 3 bit x 3 bit binary multiplier using Full adders and external AND gates.



Design a 4 bit  $\times$  3 bit binary multiplier using 7483 ICs (4 bit binary adders) and external AND gates.



# Magnitude Comparator

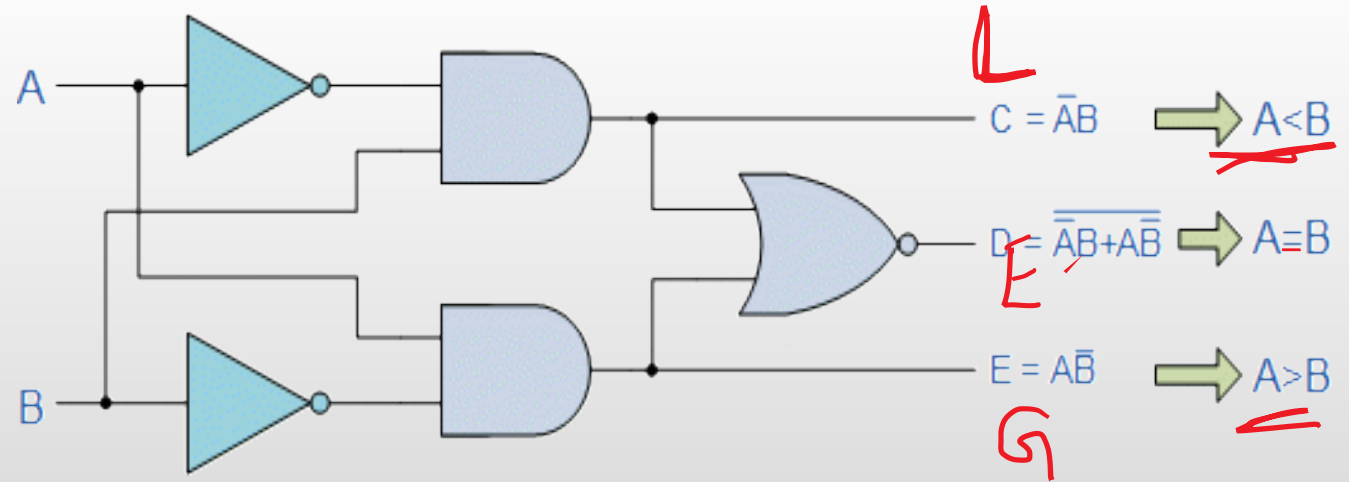
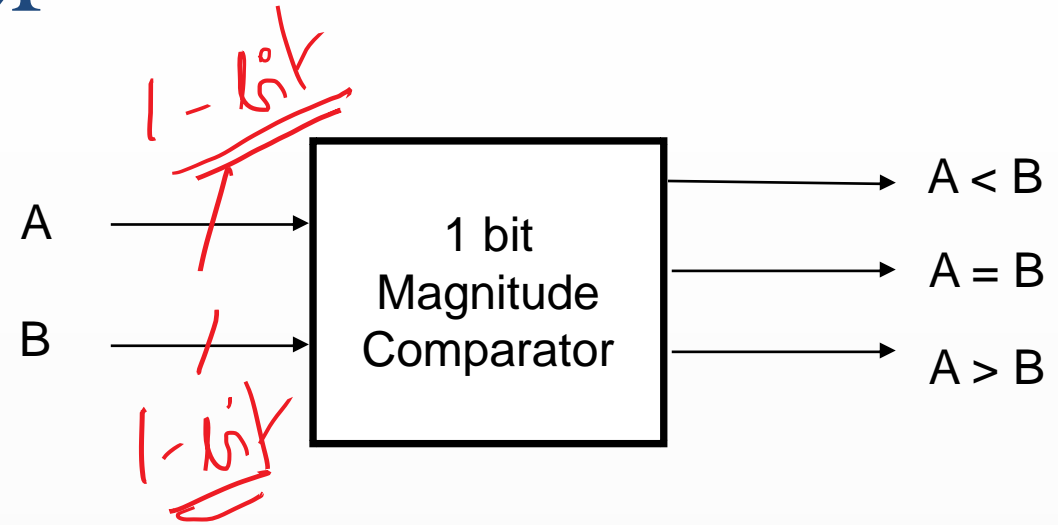
## 1 bit Magnitude comparator

A	B	L	E	G
		$A < B$	$A = B$	$A > B$
0	0	0	1	0
0	1	1	0	0
1	0	0	0	1
1	1	0	1	0

$$L = \bar{A} B$$

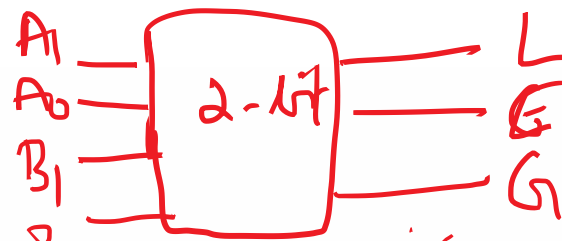
$$E = \bar{A} \bar{B} + A B$$

$$G = A \bar{B} = L + G$$



## ■ 2 bit magnitude comparator

Inputs				Outputs		
A <sub>1</sub>	A <sub>0</sub>	B <sub>1</sub>	B <sub>0</sub>	A>B	A=B	A<B
0	0	0	0	0	1	0
0	0	0	1	0	0	1
0	0	1	0	0	0	1
0	0	1	1	0	0	1
0	1	0	0	1	0	0
0	1	0	1	0	1	0
0	1	1	0	0	0	1
0	1	1	1	0	0	1
1	0	0	0	1	0	0
1	0	0	1	1	0	0
1	0	1	0	0	1	0
1	0	1	1	0	0	1
1	1	0	0	1	0	0
1	1	0	1	1	0	0
1	1	1	0	1	0	0
1	1	1	1	0	1	0



Greater than  
G<sub>1</sub> = A<sub>1</sub> B<sub>1</sub>  
G<sub>0</sub> = A<sub>0</sub> B<sub>0</sub>

Equal to :-  
E<sub>1</sub> = G<sub>1</sub> + L<sub>1</sub>  
E<sub>0</sub> = G<sub>0</sub> + L<sub>0</sub>

Less than :-  
L<sub>1</sub> = A<sub>1</sub> B<sub>1</sub>  
L<sub>0</sub> = A<sub>0</sub> B<sub>0</sub>

$$\begin{aligned}
\overline{E} &= \overline{A}_1 \overline{A}_0 \overline{B}_1 \overline{B}_0 + \overline{A}_1 \overline{A}_0 \overline{B}_1 B_0 + \overline{A}_1 \overline{A}_0 B_1 \overline{B}_0 \\
&\quad + \overline{A}_1 \overline{A}_0 B_1 B_0 \\
&= \overline{A}_1 \overline{B}_1 \left[ \overline{A}_0 \overline{B}_0 + A_0 B_0 \right] + A_1 B_1 \left[ \overline{A}_0 \overline{B}_0 + A_0 B_0 \right] \\
&= \left[ \overline{A}_1 \overline{B}_1 + A_1 B_1 \right] \left[ \overline{A}_0 \overline{B}_0 + A_0 B_0 \right] \\
&= \left[ \overline{A}_1 B_1 + A_1 \overline{B}_1 \right] \left[ \overline{A}_0 B_0 + A_0 \overline{B}_0 \right] \\
&= E_1 \cdot E_0
\end{aligned}$$

$$L = \overline{A_1} \overline{A_0} B_1 B_0 + \overline{A_1} \overline{A_0} B_1 \overline{B_0} + \overline{A_1} \overline{A_0} B_1 B_0 \\ + \overline{A_1} A_0 B_1 B_0 + \overline{A_1} A_0 B_1 \overline{B_0}$$

$$= \overline{A_1} B_1 \left[ \overline{A_0} \overline{B_0} + \overline{A_0} B_0 + A_0 \overline{B_0} + A_0 B_0 \right] \\ + A_1 \overline{A_0} B_1 B_0$$


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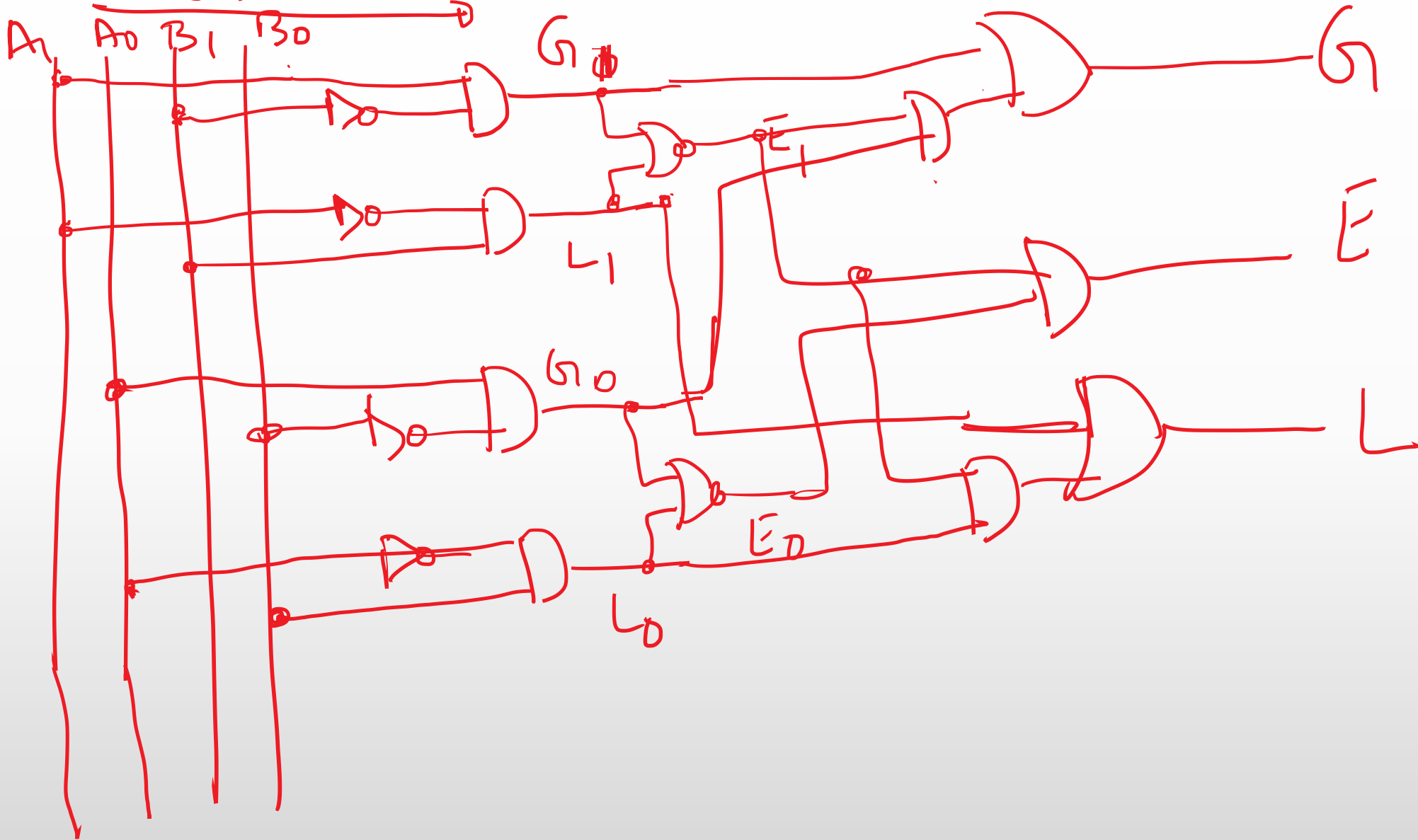

$$= \overline{A_1} B_1 + \overline{A_1} \overline{A_0} B_1 B_0 + A_1 \overline{A_0} B_1 B_0$$

$$= \overline{A_1} B_1 + \overline{A_0} B_0 \left[ \overline{A_1} B_1 + A_1 B_1 \right]$$

$$= \overline{A_1} B_1 + \overline{A_0} B_0 \cdot E_1 \quad L = L_1 + L_0 E_1$$



$$G = G_1 + \bar{E}_1 G_0$$



- 3 bit magnitude comparator

$$L = L_2 + \bar{E}_2 L_1 + \bar{E}_2 \bar{E}_1 L_0$$

$$E = E_2 \bar{E}_1 \bar{E}_0$$

$$G = G_2 + \bar{E}_2 G_1 + \bar{E}_2 \bar{E}_1 G_0$$

■ 4 bit magnitude comparator

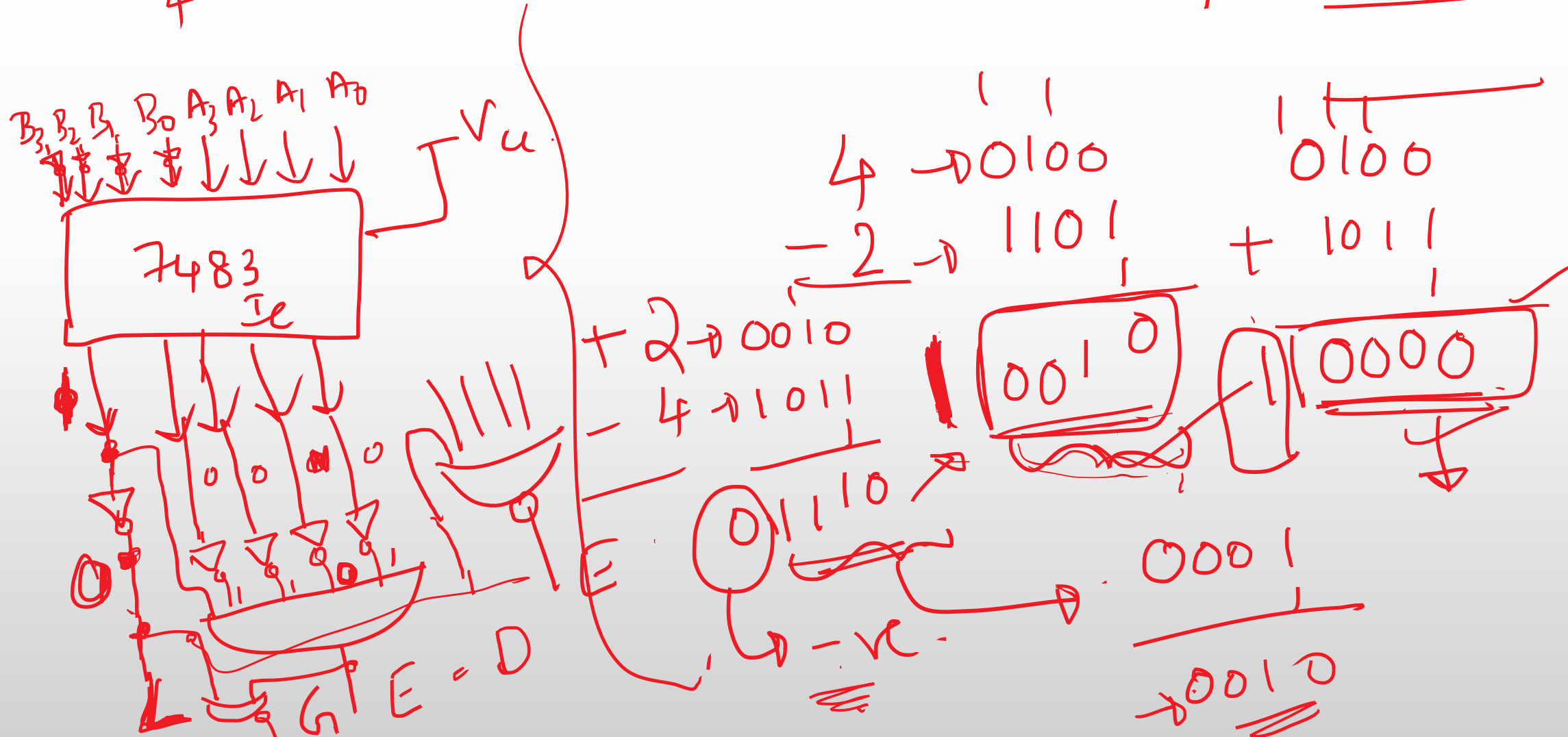
$$L = L_3 + E_3 L_2 + E_3 E_2 L_1 + E_3 E_2 E_1 L_0$$

$$E = E_3 E_2 E_1 E_0$$

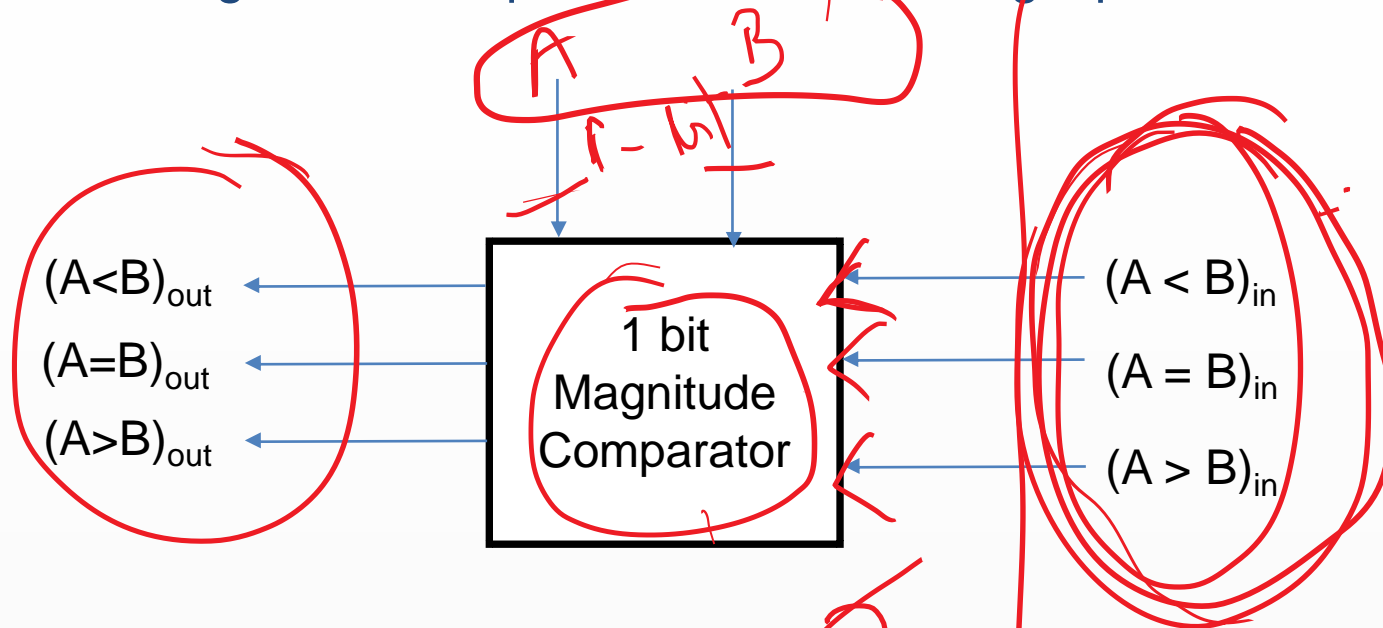
$$G = G_3 + E_3 G_2 + E_3 E_2 G_1 + E_3 E_2 E_1 G_0$$

## Design 4 bit magnitude comparator using 7483 IC and external gates.

A B  $\rightarrow$  4-bit

$$\begin{array}{rcl} 4 & \rightarrow & 0100 \\ -4 & \rightarrow & -0100 \end{array} \}$$


■ 1 bit magnitude comparator with cascading input:



$$(A > B)_{out} = (A > B) + (A = B)(A > B)_{in}$$

$$(A < B)_{out} = (A < B) + (A = B)(A < B)_{in}$$

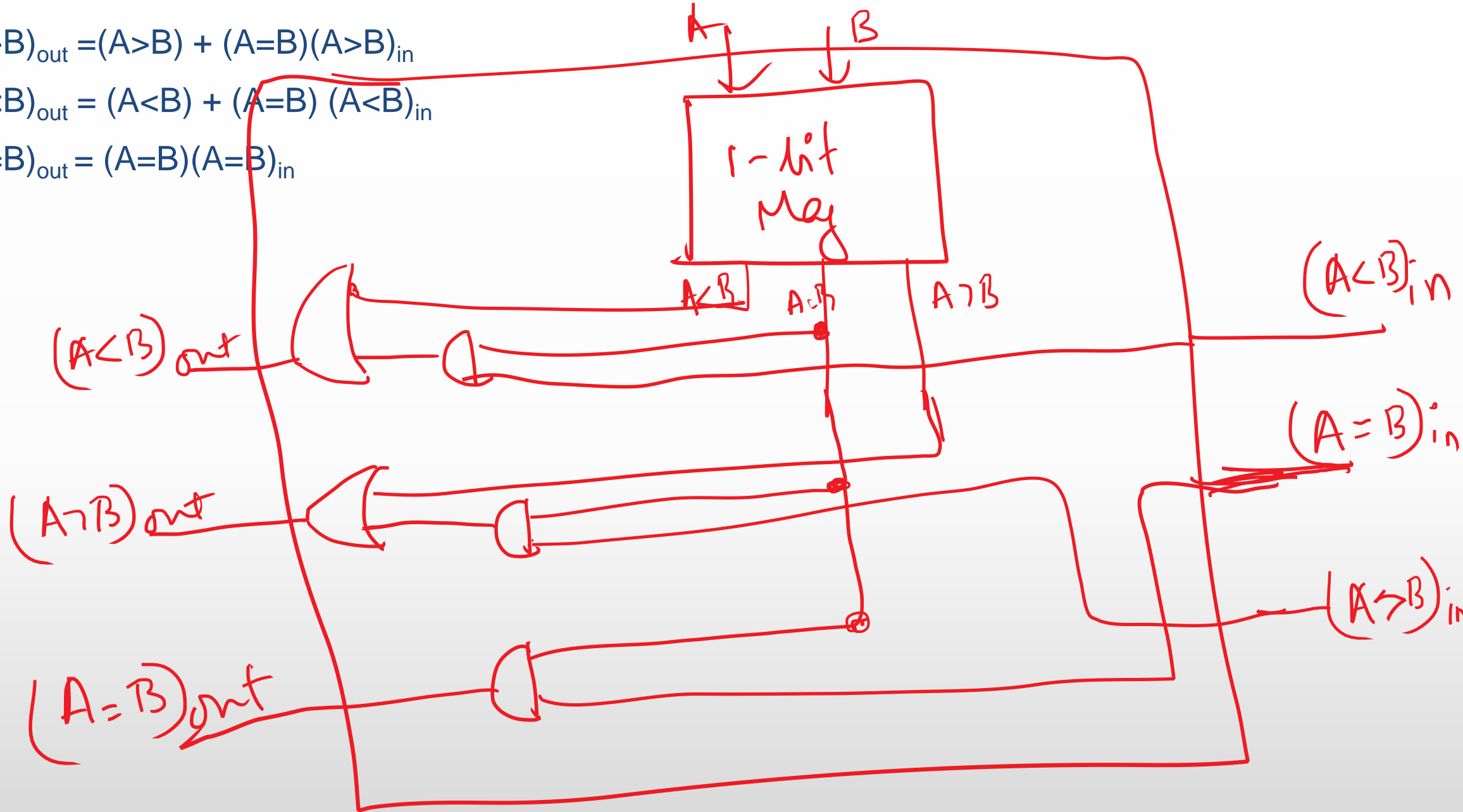
$$(A = B)_{out} = (A = B)(A = B)_{in}$$



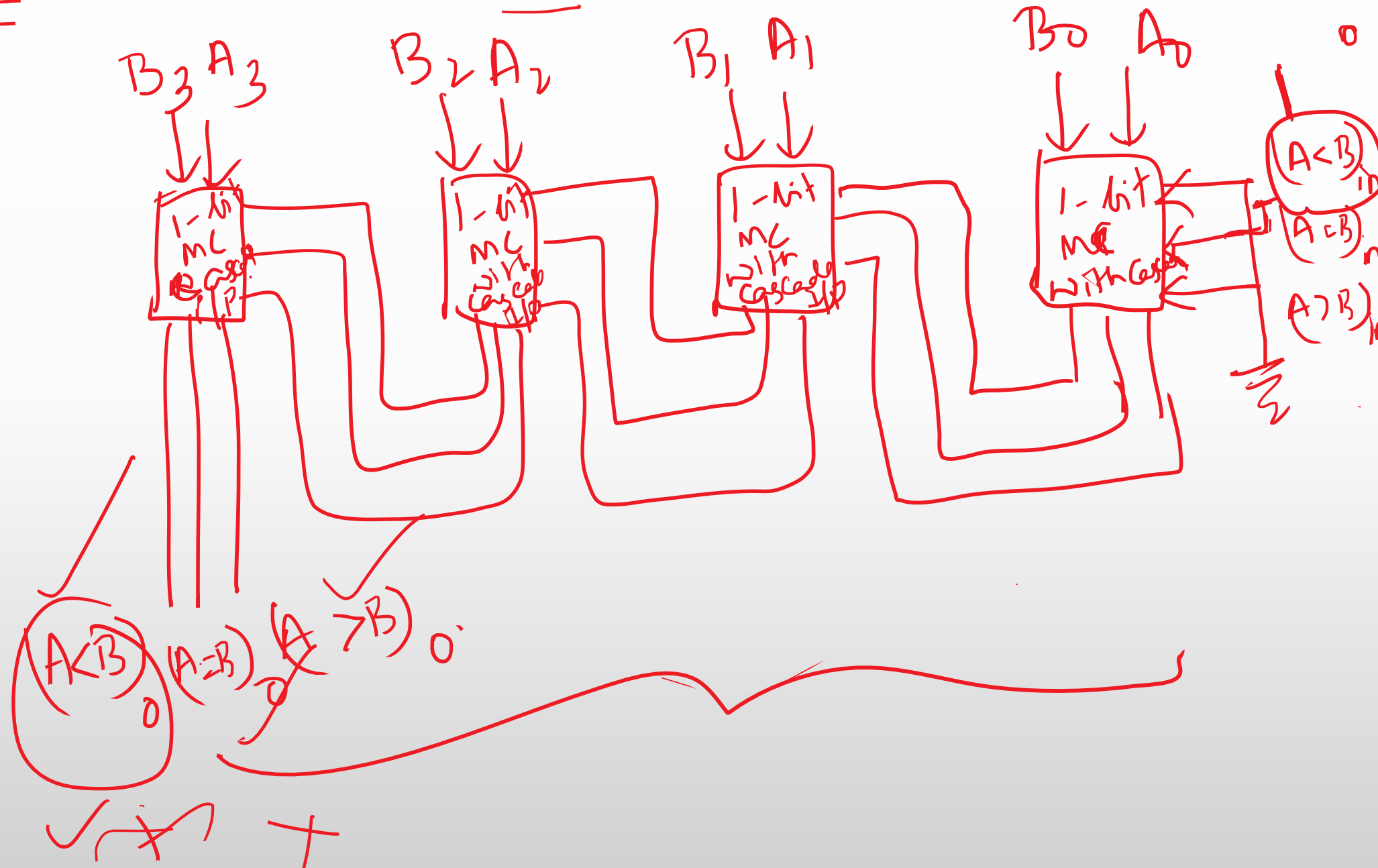
$$(A > B)_{out} = (A > B) + (A = B)(A > B)_{in}$$

$$(A < B)_{out} = (A < B) + (A = B)(A < B)_{in}$$

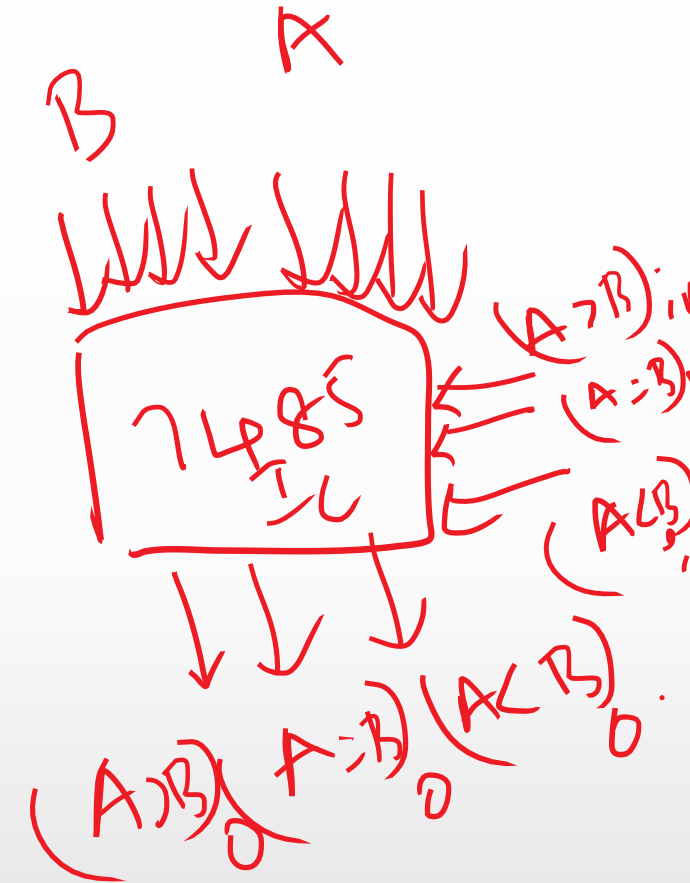
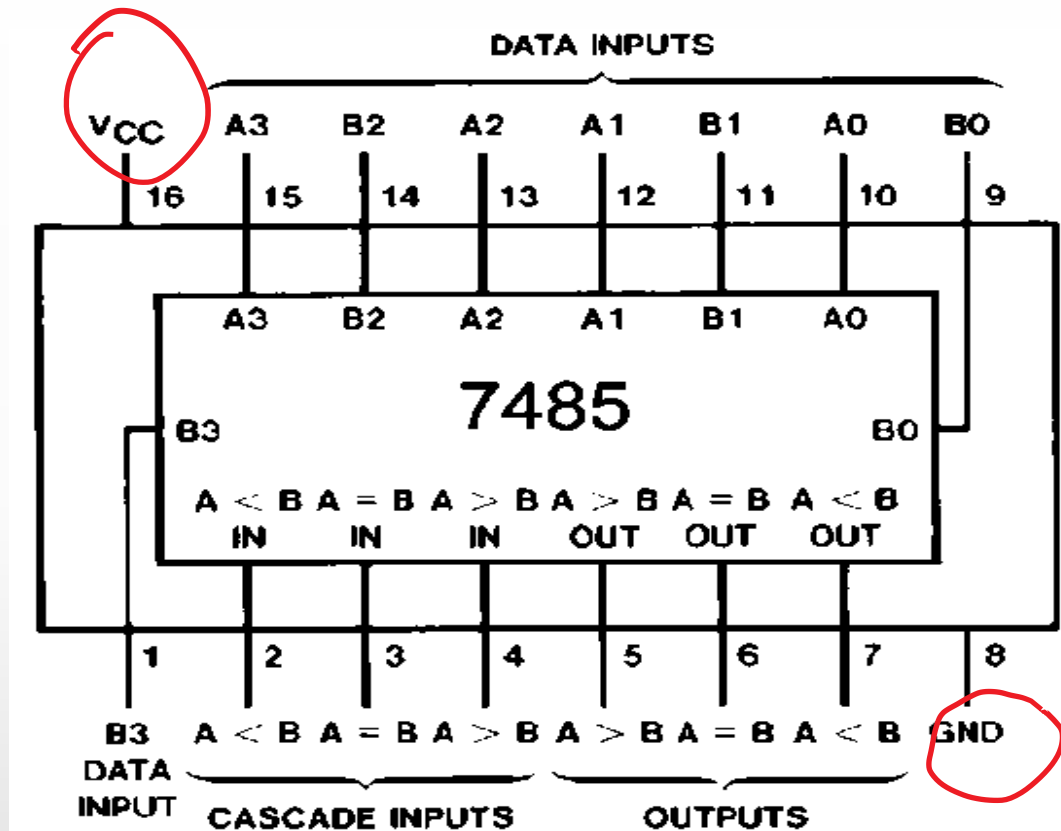
$$(A = B)_{out} = (A = B)(A = B)_{in}$$



Design a 4 bit magnitude comparator using 1 bit magnitude comparator with cascading inputs.

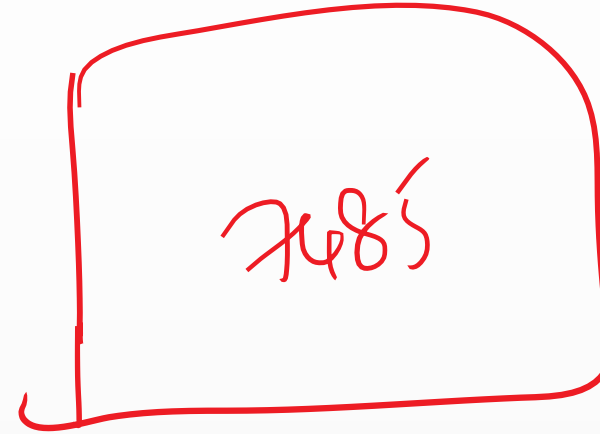


## 7485 IC ( 4 bit magnitude comparator with cascading inputs)





## Design 8 bit magnitude comparator using 7485 ICs



Design a combinational circuit using multipliers, 7483 IC and external gate to perform

$F = 2X + Y$  when  $m=0$ ,

$F = X + 2Y$  when  $m=1$

Where  $X$ ,  $Y$  are two bit numbers and output  $F$  is a 4 bit number.

$m=0 \quad F = A + B$   
 $m=1 \quad F = A - B$

