



- 3C. Trace the following curve with explanation  
 $y(1-x^2)=x^2$  (3+ 4+ 3)
- 4A. State Cauchy's mean value theorem and verify it for  
 $f(x)=\sqrt{x}$  and  $g(x)=\frac{1}{\sqrt{x}}$  in  $[a,b]$
- 4B. Find the magnitude and equations of the line of shortest distance between the lines  $\frac{x-3}{1}=\frac{y-5}{-5}=\frac{z-7}{1}$  and  $\frac{x+1}{7}=\frac{y+1}{-6}=\frac{z+1}{1}$   
 Also find the points where it intersects the lines.
- 4C. Obtain the first three nonzero terms in the Maclaurin's series expansion of  
 $f(x)=\frac{\sin^{-1}x}{\sqrt{1-x^2}}$ . (3+ 4+ 3)
- 5A. If  $u = f(x^2+y^2+z^2)$  where  $x = r\cos\theta\cos\phi$ ,  $y = r\cos\theta\sin\phi$ ,  $z = r\sin\theta$  find  $\frac{\partial u}{\partial \theta}$  and  $\frac{\partial u}{\partial \phi}$ .
- 5B. Evaluate the following limits  
 (i)  $\lim_{x \rightarrow a} \frac{a^x - x^a}{x^x - a^x}$  (ii)  $\lim_{x \rightarrow 0} \left( \frac{\tan x}{x} \right)^{\frac{1}{x^2}}$
- 5C. A plane passes through a fixed point  $(a, b, c)$ . Show that the locus of the foot of the perpendicular from the origin on to the plane is the sphere,  
 $x^2+y^2+z^2-ax-by-cz=0$ . (3 + 4+ 3)
- 6A. Find the region of convergence of the following power series.  
 (i)  $1+\frac{3}{7}x+\frac{3.6}{7.10}x^2+\frac{3.6.9}{7.10.13}x^3+....$   
 (ii)  $\frac{1}{2}+\frac{2}{3}x+\left(\frac{3}{4}\right)^2x^2+\left(\frac{4}{5}\right)^3x^3+...$
- 6B. Find the volume of the solid obtained by revolving the curve  $y^2(2a-x)=x^3$  about its asymptote.
- 6C. If the sides of a plane triangle ABC vary in such a way that its circum – radius remains a constant, then prove that  
 $\frac{\delta a}{\cos A} + \frac{\delta b}{\cos B} + \frac{\delta c}{\cos C} = 0$  (4 + 3+ 3)

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