

# Multiple Stacks and Queues

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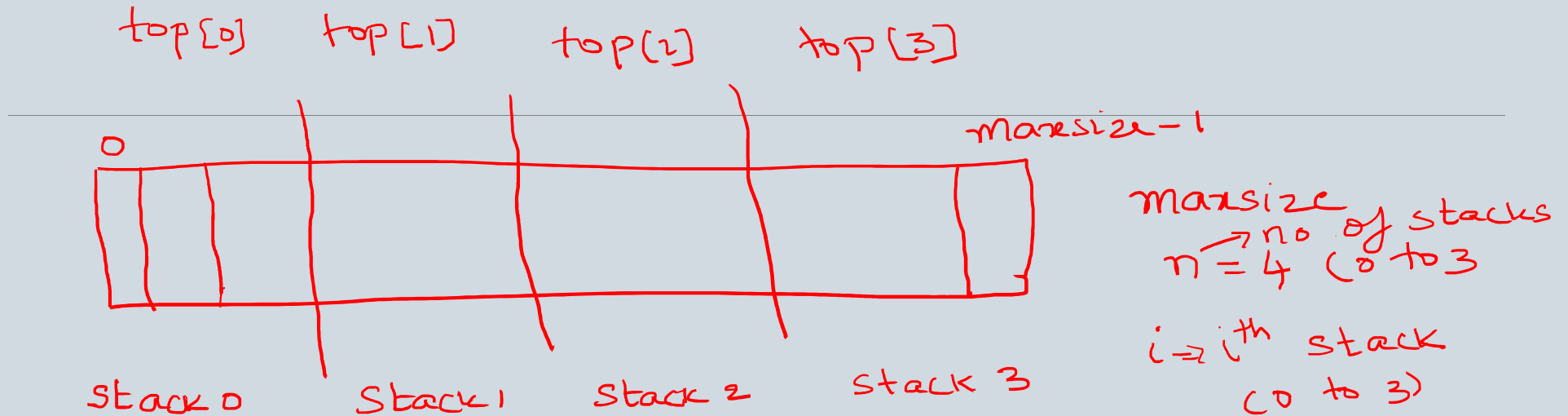
BY

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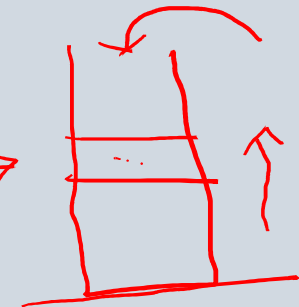
# Multiple stacks



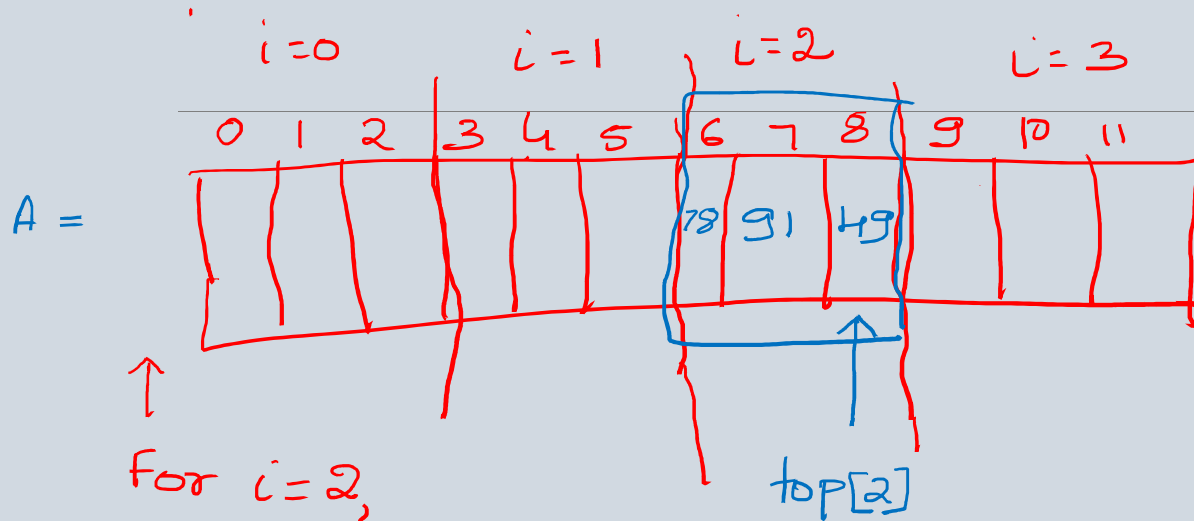
int  $top[10]$ ;  
           $\uparrow$   
           $n$

$top[i] \Rightarrow$  index of top element of the  $i^{th}$  stack  $\rightarrow$  top

$maxsize \text{ of each stack} = maxsize / n$



# Multiple stacks



$$\text{maxsize} = 12$$

$$n = 4$$

$$i^{\text{th}} \text{ stack size} = \frac{12}{4} = 3$$

for  $i=2$ ,  
 $\text{top}[2] = 8$

if  $(\text{top}[2] == 8)$  stack 2 is full  
 1 is full

$i=1$   $\text{top}[1] = 5$

$i=0$   $\text{top}[0] = 2$

$i=3$   $\text{top}[3] = 11$  same as maxsize - 1

if  $(\text{top}[i] == \frac{\text{maxsize} \times (i+1)}{n} - 1)$   
 $i^{\text{th}} \text{ stack is full}$

0  
1  
0  
1  
3

$$12 / 4 \times 1 = 3 - 1 = 2$$

$$3 \times 2 - 1 = 5$$

$$3 \times 3 - 1 = 8$$

$$3 \times 4 - 1 = 11$$

# Multiple stacks

Empty case

$$\text{top}[i] == \frac{\text{maxsize} - i}{n} - 1$$

i

0

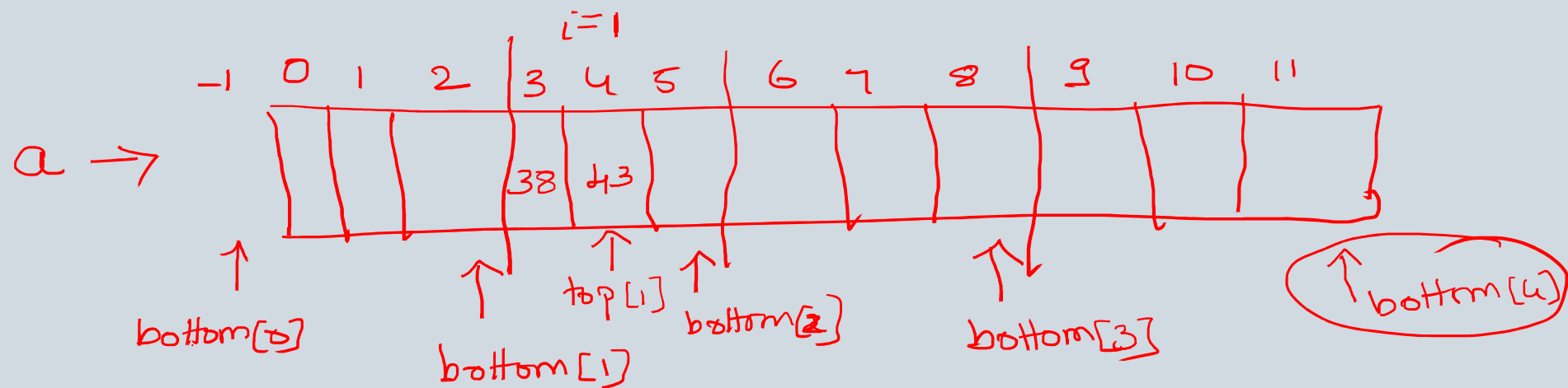
$$\text{top}[0] == -1 \quad \text{empty}$$

1

$$\left. \begin{array}{l} \text{top}[1] = 3 * 1 - 1 = 2 \\ \text{top}[1] == 2 \end{array} \right\} \begin{array}{l} \text{stack 1 is} \\ \text{empty} \end{array}$$

$$\text{top}[2] == 5$$

$$\text{top}[3] == 8$$



Maxsize = 12  
 $n = 4$   
 $top[i] = bottom[i] = \frac{maxsize}{n} * i - 1$  // initialize

Empty: if  $(top[i] == bottom[i])$ , stack is empty

Full: if  $(top[i] == bottom[i+1]) || (top[i] == maxsize - 1)$   
 $i = 0, 1, 2$       stack is full

push(int i, int ele)

{ if  $i^{th}$  stack is not full, then  $a[++top[i]] = ele;$

Pop

return(a[top[i] - 1]);

# Multiple stacks

---

```
#include<iostream>
using namespace std;
#define max_size 20 ✓
class stack
{
    int top[10];
    int a[50];
    int boundary[10];
    public:
        stack(int); // no. of stacks
        void push(int ,int);
        void pop(int);
        void display(int);
};
```

---

```
stack::stack(int n)
{
    for(int i=0;i<n;i++)
        boundary[i]=top[i]=(max_size/n)*i-1;
}
```



---

```
void stack::push(int i,int x)
```

```
{
```

```
    if((top[i]==boundary[i+1]) || (top[i]==(max_size-1)))
```

```
        cout<<"Stack is full \n";
```

```
    else
```

```
        a[++top[i]]=x;
```

```
}
```

$i = 0, 1, \dots, n-2$


→ last stack ie  $i = n-1$

---

```
void stack::pop(int i)
{
    if(top[i]==boundary[i])
        cout<<"stack is empty\n";
    else
        cout<<"deleted element is "<<(a[top[i]--]);}
```

---

```
void stack::display(int i)
{
    if(top[i]==boundary[i])
        cout<<"stack is empty\n";
    else
        for(int j=top[i];j>boundary[i];j--)
            cout<<"\nThe elements of stack are "<<"\n"<<a[j];
}
```



---

```
int main()
```

```
{
```

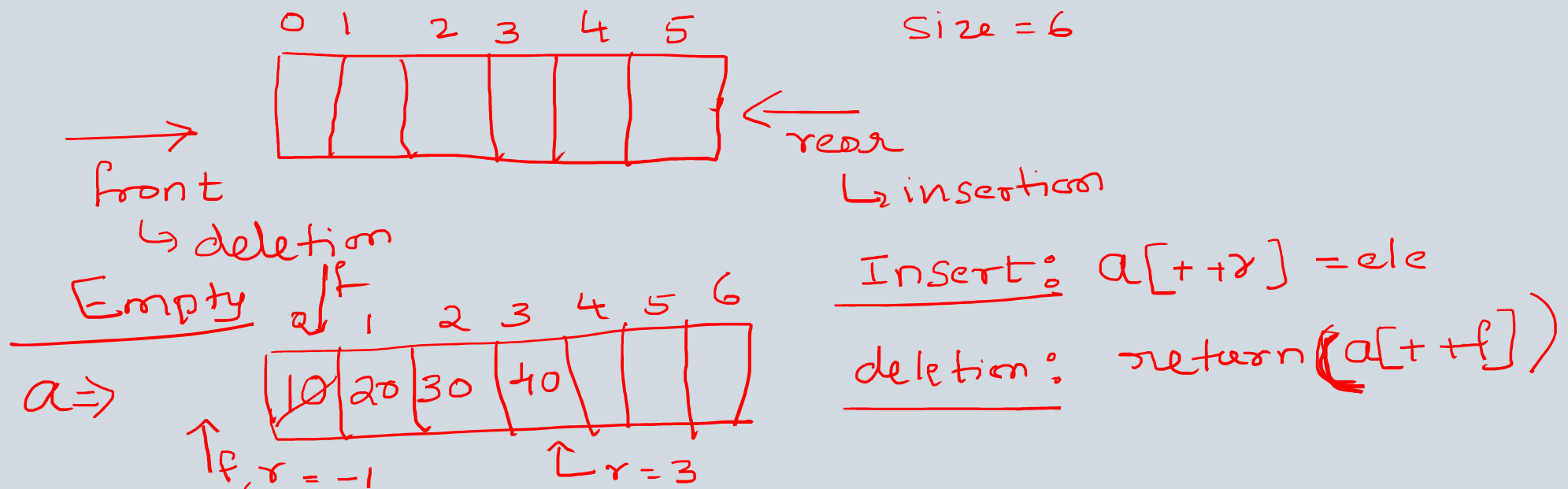
```
Write a menu driven program
```

```
return 0;
```

```
}
```

# Linear Queue

- Queue is an ordered list in which insertions and deletions happen at different ends (First in First Out)
- The elements are added at the rear end and deleted at the front end.



0	1	2	3	4	5
<del>10</del>	<del>20</del>	<del>30</del>	<del>40</del>		

$\uparrow \uparrow$   
 $f=3$     $r=3$

0	1	2	3	4	5
<del>10</del>	<del>20</del>	<del>30</del>	<del>40</del>		

$f=3$     $r=3$

Insert 50

				4	
				50	

$f \uparrow$     $\uparrow r$

Empty  $\Rightarrow$  if ( $f == r$ )

Insert 60

				5	
<del>10</del>	<del>20</del>	<del>30</del>	<del>40</del>	50	60

$\uparrow$     $\uparrow r$   
 $f$

Full  $\Rightarrow$  if ( $r == \text{maxsize} - 1$ )

				...	
--	--	--	--	-----	--

$\uparrow f$     $\uparrow r$

```

class queue{
    int front, rear;
    int a[10];
    int size;
public:
    queue(int n)
    { front=-1;rear=-1; size=n}
    void insert(int);
    void remove();
    void display();
};

void queue::insert(int ele)
{
    if (rear==size-1)
        cout<<"queue is full";
    else
        a[++rear]=ele;
}

```

```

void queue::remove()
{
    if (rear==front)
        cout<<"queue is empty";
    else
        return(a[++front]);
}

```

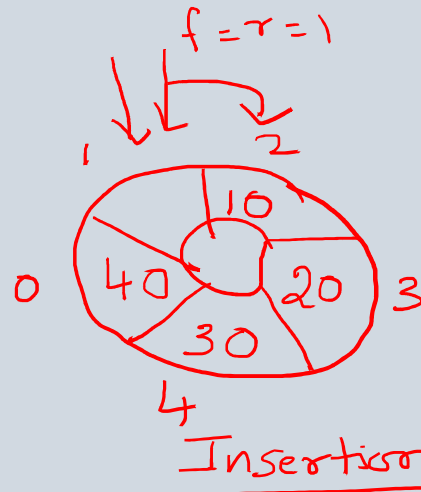
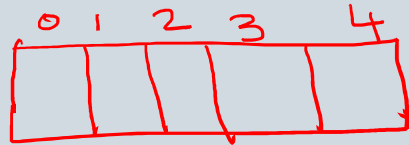
```

void display()
{
    if (rear==front)
        cout<<"queue is empty";
    else
        for(int i=rear; i>front;i--)
            cout<<a[i]<<" ";
}

```

// i = front+1  
 {  
 i <= rear  
 i++  
 }

## Circular Queue



① Insert 10,  $r=1$ ,  $f=1$

② Insert 20  $r=2$ ,  $f=1$

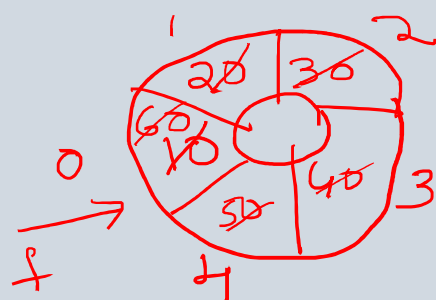
③ Insert 30  $r=3$ ,  $f=1$

④ Insert 40  $(4+1) \% 5 = 0$

$$\left. \begin{array}{l} \text{if } (r == \text{maxsize} - 1) \\ \quad r = 0; \\ \text{else} \\ \quad r = r + 1; \end{array} \right\}$$

$$\left\{ \begin{array}{l} r = (r + 1) \% \text{maxsize} \checkmark \\ a[r] = \text{ele} \end{array} \right.$$





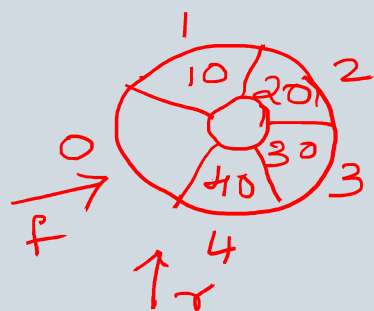
- ① Delete 10,  $f = 0$   $r = 4$
- ② Insert 60,  $r = 0$   $f = 0 \leftarrow \text{Full}$
- ③ Delete all,  $r = 0$   $f = 0 \leftarrow \text{empty}$

Remove :

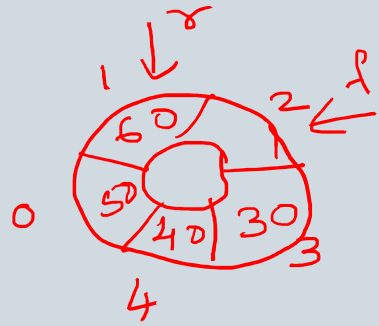
$$f = (f + 1) \% \text{maxsize}$$

return  $a[f]$

if  $\text{maxsize} = n$ , then store  $(n-1)$  elements ✓



Initialize  $f = 0, r = 0$   
 Insert 10, 20, 30, 40



Remove 10

$f = 1$        $r = 4$

Remove 20

$f = 2$        $r = 4$

Insert 50

$f = 2$        $r = 0$

Insert 60

$f = 2$        $r = 1$

if  $((r+1) \% \text{maxsize} == f)$ , Circular Q is full

Remove 30, 40, 50, 60;  $f = 1$ ,  $r = 1$

if  $(f == r)$ , circular Q is empty.

```

class CQ{
    int rear, front;
    int a[20];
    int maxsize;

public:
    CQ(int n)
    { maxsize = n; }
    void insert(int ele);
    void remove();
    void display();
}

```

```

void CQ::insert(int ele)
{
    if((rear+1)%maxsize == front)
        cout << "CQ is full\n";
    else

```

```

        { rear = (rear+1)%maxsize;
          a[rear] = ele;
        }
}

void CQ::remove()
{
    if(front == rear)
        cout << "CQ is empty\n";
    else
        { front = (front+1)%maxsize;
          cout << "deleted element is: " <<
            a[front];
        }
}

```

```

void cQueue::display()
{
    if (front == rear)
        cout << "CQ is empty\n";
    else
    {
        }
    }
}

```

