

**ASSIGNMENT – 4**  
**SUBJECT: ENGINEERING MATHEMATICS –III(MAT 2155)**

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**Instructions:**

1. Write your **Name, Roll No, Registration No** and put **signature on the top of the answer sheet.**
  2. Scan your answer sheet as **PDF file** and name the file as **Roll No. <space> Name <space> Registration No.**
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**Question Allotment**

<b>Roll numbers</b>	<b>Question number</b>
<b>Roll Numbers 1-35</b>	<b>1A and 1B</b>
<b>Roll Numbers 36 – last and re-registered</b>	<b>2A and 2B</b>

- 1A. Let  $G$  be a group and  $a \in G$ .
- (i) Define  $N(a) = \{x \in G \mid ax = xa\}$ . Show that  $N(a)$  is a subgroup of  $G$ .
- (ii) Let  $H = \bigcap N(a)$ . Show that  $H$  is a normal subgroup of  $G$ .
- 1B. Prove that the fourth root of unity forms an abelian group under multiplication.
- 2A. If every element of a group  $G$  other than the identity has order 2, prove that the group  $G$  is abelian.
- 2B. Prove that  $H$  is a normal subgroup of  $G$  iff  $H$  is a subgroup of index 2 in  $G$ .