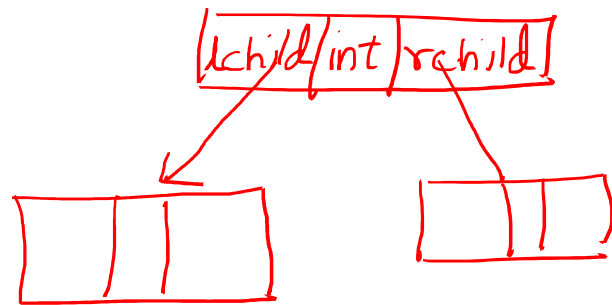


Binary Tree : Traversal Techniques

Dec. 04th, 2021

Lecture-18

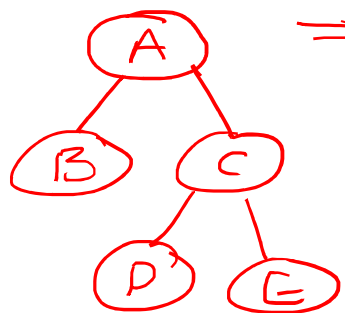
② linked list representation of BT



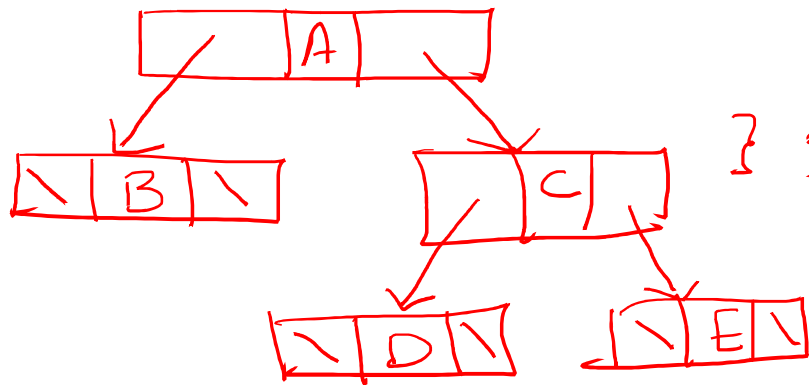
```
class btree{ int data;
```

```
btree *lchild;  
btree *rchild;
```

```
public;
```



⇒

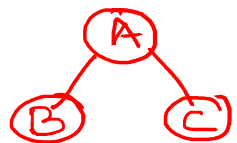


```
} ;
```

```
==
```

Traversal Techniques:

- Inorder traversal ✓ → $L \underline{V} R$
- Postorder traversal ✓ $LR \underline{V}$
- Preorder Traversal ✓ $\underline{V}LR$
- Level-order traversal ✓ — level wise display (L → R)

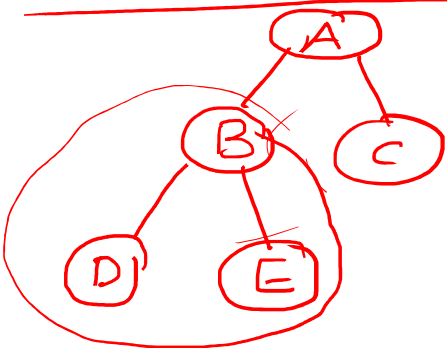


Inorder = B A C

postorder = B C A

preorder = A B C

levelorder = A B C

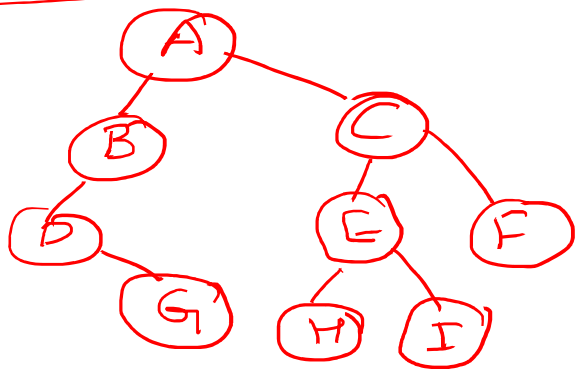


In: D B E A C

post: D E B C A

pre: A B D E C

level: A B C D E

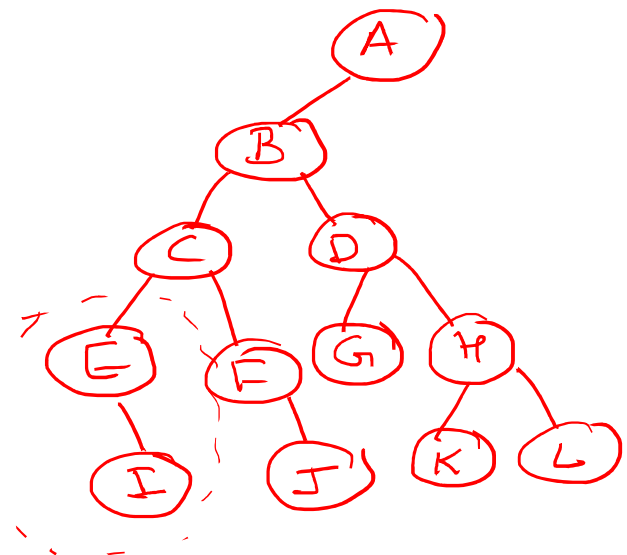


In: D G B A H E I C F

post: G D B H I E F C A

pre: A B D G C E H I F

level: A B C D E F G H I



In: E I C F J B G D K H L A

post: I E J F C G I K L H D B A

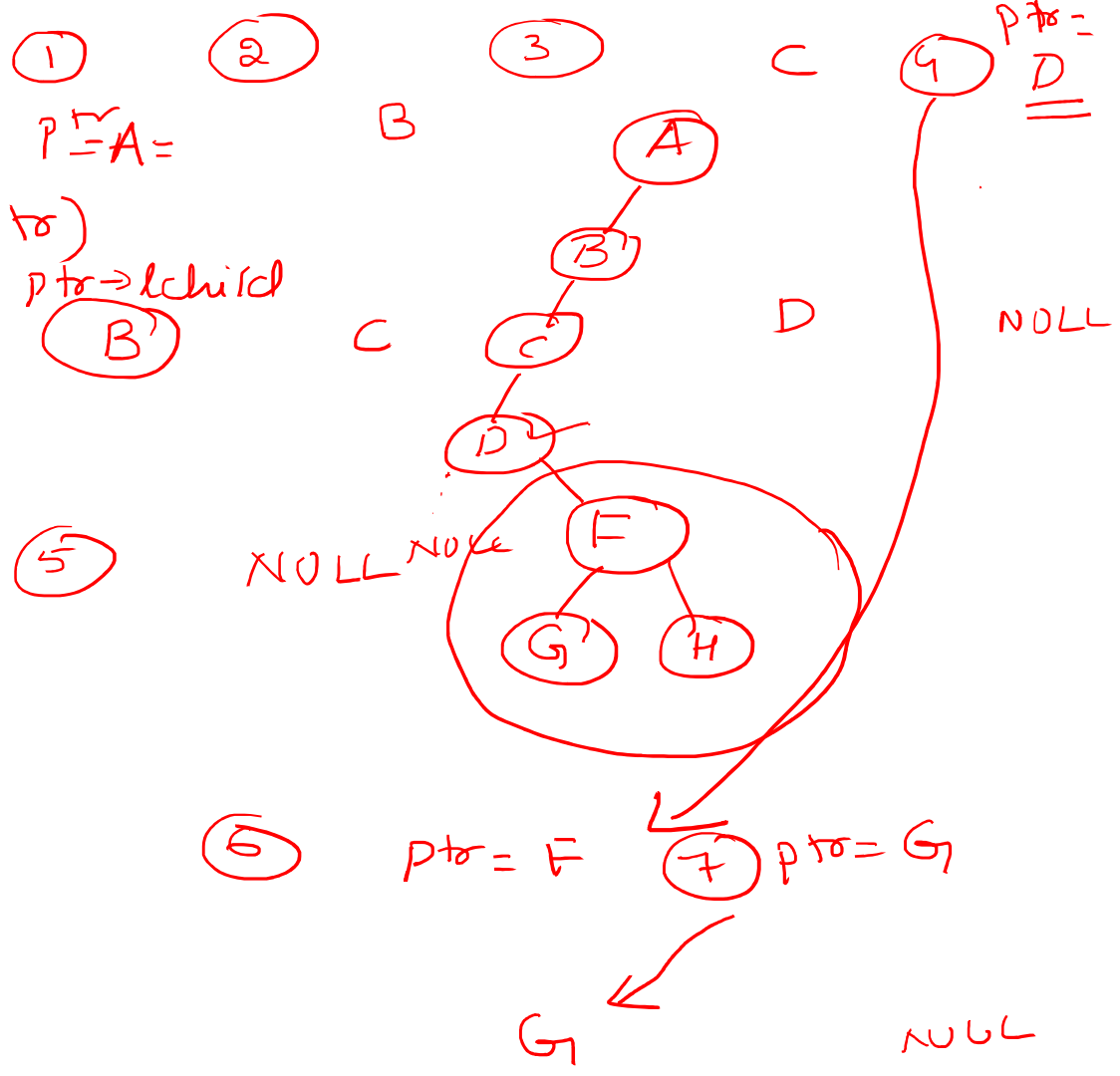
pre: A B C E I F J D G H K L

level: A B C D E F G H I J K L

```

void inorder(btree *ptr) ptr=A=
{
    if (ptr != NULL) // if (ptr)
    {
        inorder(ptr->lchild);
        cout << ptr->data;
        inorder(ptr->rchild);
    }
}

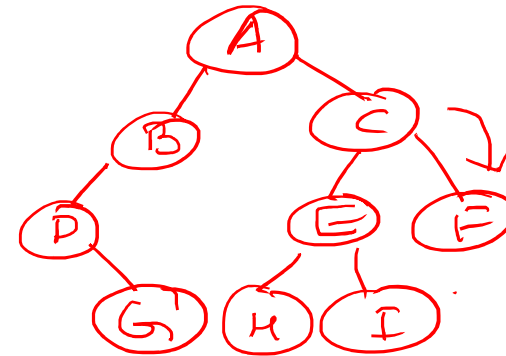
```



D G

Recursive inorder

fn call	ptr	ptr child
1	A	
2	B	
3	D	
4	NULL	count < LP
5	G	count < G
6	NULL	
7	NULL	
8	C	
9	E	
10	H	count < H
11	NULL	



Preorder

```
void preorder(btree *ptr)
```

```
{ if(ptr != NULL)
```

```
{ cout << ptr->data;
```

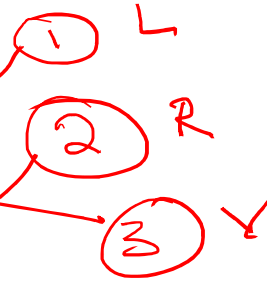
```
  preorder(ptr->lchild);
```

```
  preorder(ptr->rchild);
```

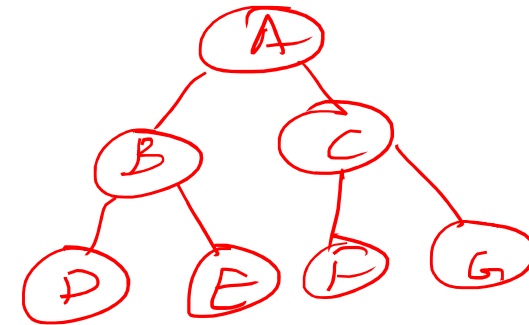
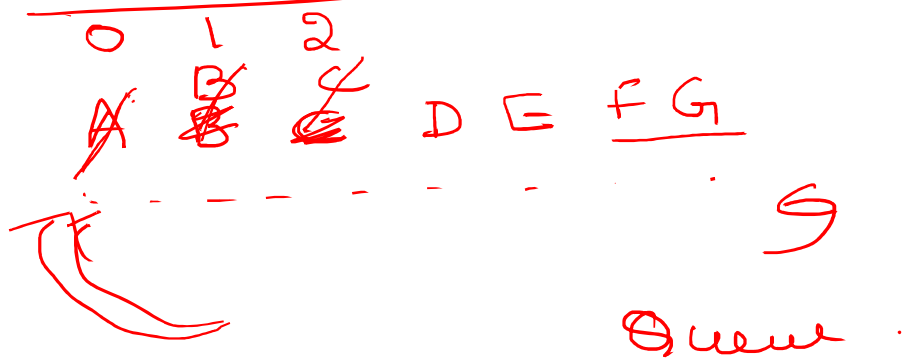
```
}
```

```
}
```

Postorder



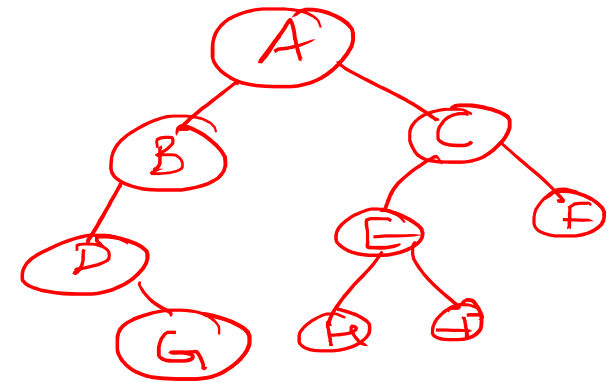
Level-order



A B C



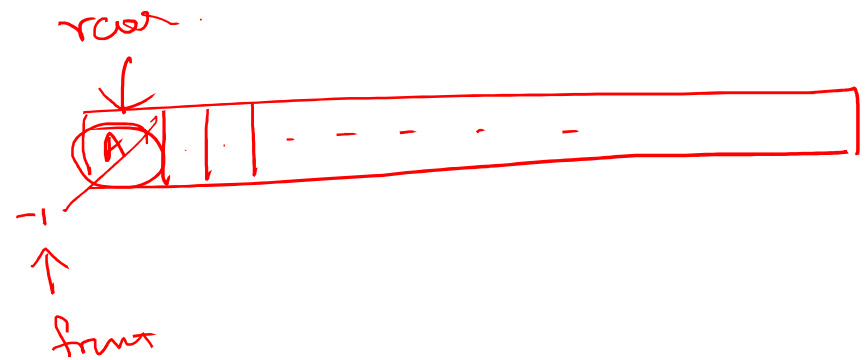
A B C D E F G H I




```

void level_order(btree *ptr)
{
    btree *q[30];
    int front = -1, rear = -1;
    if(ptr == NULL) return;

```



else

q[++rear] = ptr; // root address

while(1)

```

{
    ptr = q[++front];

```

```

    if(front == rear)
    { cout << ptr->data;

```

```

        if(ptr->lchild)

```

```

            q[++rear] = ptr->lchild;

```

```

        if(ptr->rchild)

```

```

            q[++rear] = ptr->rchild; }

```

else

break;

}

Level order traversal

```
void btree::level_order()  
{ int f=-1, rear=-1; ✓  
  btree *q[10], *ptr=root;  
  if(ptr==NULL) return;  
  q[++rear]=ptr; // f=-1, rear=0  
  cout<<"In level order:";
```

```
for(;;)  
{ if(f!=rear)  
  { ptr=q[++f];  
    cout<<ptr->data<<" ";  
    if(ptr->lchild)  
      q[++rear]=ptr->lchild;  
    if(ptr->rchild)  
      q[++rear]=ptr->rchild;  
  }  
  else // is empty  
    break;  
}
```

or

```
while(f!=rear)  
{ ptr=q[++f];  
  cout<<ptr->data<<" ";  
  if(ptr->lchild)  
    q[++rear]=ptr->lchild;  
  if(ptr->rchild)  
    q[++rear]=ptr->rchild;  
}
```

Iterative inorder traversal: logic

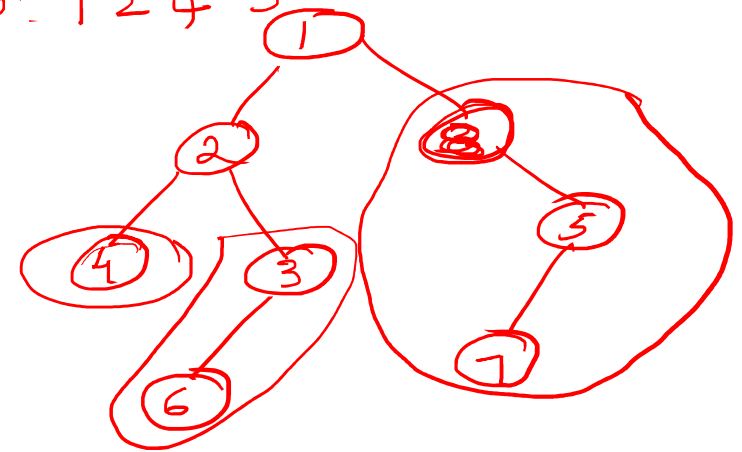
```
void inorder(ptoc *pto)
{
```

~~1 2 4 3 6 8 5 7~~

o/p: 4 2 6 3 1 8 7 5
 └──┬──┘
 left subtree root

Preorder

s: ~~1 2 4 3 6 8 5 7~~
 o/p: 1 2 4 3 6 8 5 7



Recursive

```
if (pto)
{
  inorder(pto->lchild);
  // -----
  inorder(pto->rchild);
}
```

Iterative inorder traversal

```
void btree:: inorder()
```

```
{
```

```
    int top=-1; ✓
```

```
    btree *s[20], *ptr=root;
```

```
    for (;;) 
```

```
    {
```

```
        for(; ptr; ptr=ptr->lchild) ← // inorder(ptr->lchild)
```

```
            s[++top] = ptr;
```

```
        if(top>=0)
```

```
        { ptr = s[top--]; ← else break;
```

```
            cout<<ptr->data<<" "; ←
```

```
            ptr=ptr->rchild; } ←
```

```
        }
```

```
}
```

Iterative Preorder Traversal

```
void btree:: preorder()
{
    int top=-1;
    btree *s[20], *ptr=root;
    for (;;)
    {
        for(; ptr; ptr=ptr->lchild)
            { cout<<ptr->data<<" "; s[++top] = ptr;}

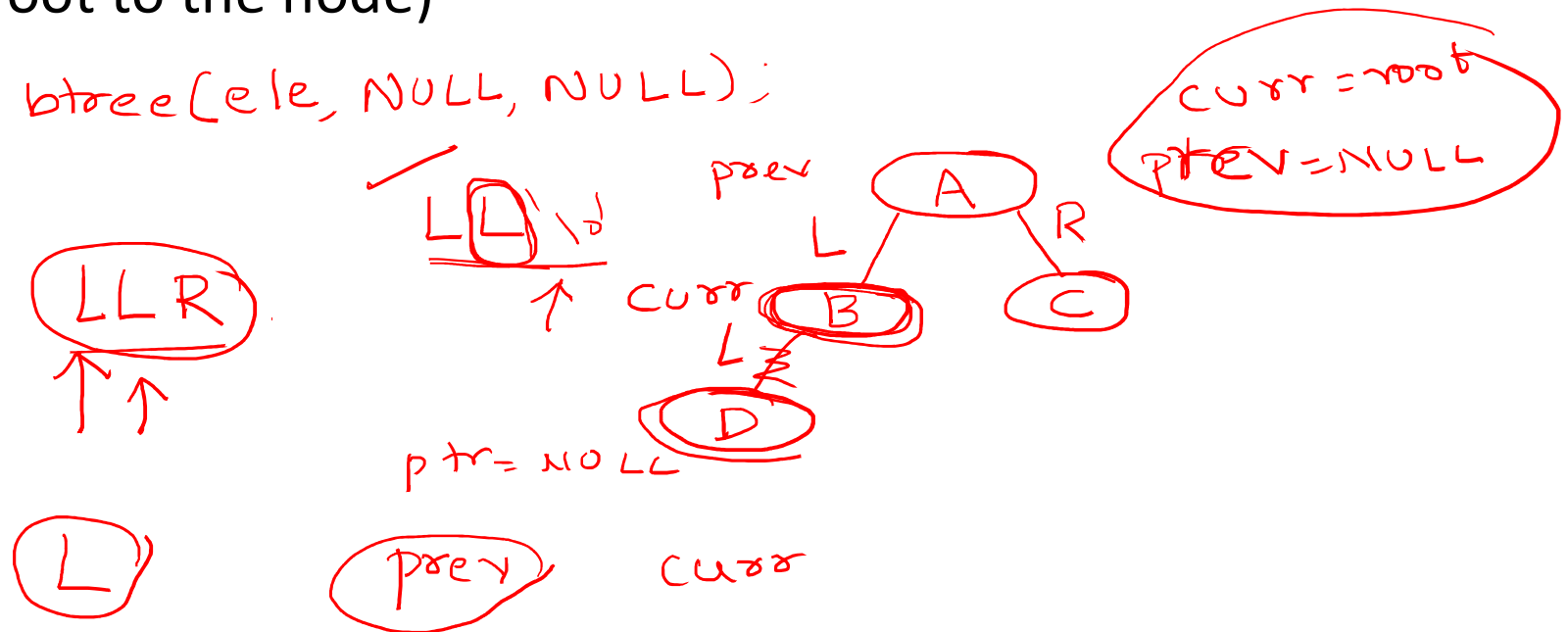
        if(top>=0)
            ptr = s[top--];
        else break;
        ptr=ptr->rchild;
    }
}
```

Try Iterative postorder traversal

Creating a Binary Tree: Logic

- Tree is created by taking the direction to the node as an input (ie the path from the root to the node)

`temp = new btree(ele, NULL, NULL);`



Creating a Binary Tree: Logic Function.

```
void btree:: create( )  
{  
    btree *prev, *curr, *temp;  
    int i=0, n; int ele; char dir[20];  
    cout<<"No. of nodes: "; cin>>n;  
    for(i=0; i<n; i++)  
    {  
        cout<<"Enter the key value: "  
        cin>>ele;  
        temp = new btree(ele, NULL, NULL);  
        if (root == NULL)  
            root = temp;  
  
        else
```

Creating a Binary Tree: function

```
{ cout << "Input the direction (uppercase) : \n";
```

$\text{cin} \gg \text{dir}; \quad //$

curr = ~~Root~~, pre = NULL

```
for(i=0; dir[i] != '\0' && curr != NULL; i++)
```

```

{ prev = curr;
  curr = curr->next;
}

```

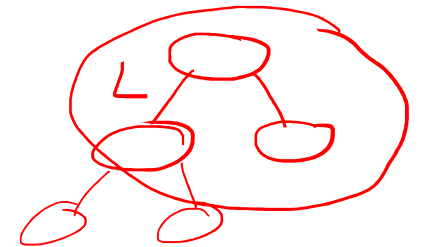
if (dir[i] == 'L')

curr = curr → lchild;

else

dir[i] curr = curr \rightarrow next id;

3

$$n = 4$$
$$1 = 0$$
$$i = 1$$


LLR^x

prex

CUTS = NO



Creating a Binary Tree: function

if (curr != NULL || dir[i] != '\0')

{ cout << "Insertion not possible: error\n";
delete temp;

}

else

{ if (dir[i] == 'L')

prev->lchild = temp;

else

prev->rchild = temp;

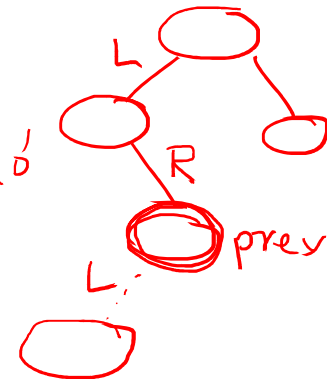
}

}

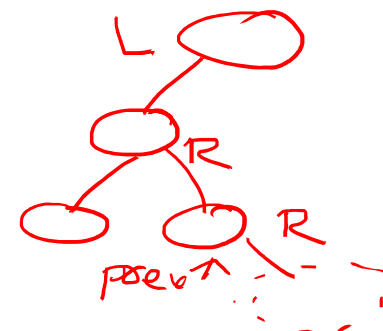
}

dir = L

LRLL '\0'



prev = root
curr = NULL



Creating a Binary Tree: recursive function

```
btree *insert(btree *ptr, char *c)  
{  
    if (ptr == NULL || *c == '\0')  
    {  
        create temp & return its address  
    }  
  
    if (*c == 'L')  
        ptr->lechild = insert(ptr->lechild, ++c)  
    else  
        ptr->rchild = insert(ptr->rchild, ++c)  
}
```

Copying a Binary Tree: function

```
btree *btree :: copy(btree *ptr)
```

```
{
```

```
    btree *temp;
```

```
    if(ptr)
```

```
    {
```

```
        temp=new btree(ptr->data, NULL, NULL);
```

```
        if(ptr->leftchild)    temp->leftchild=copy(ptr->leftchild);
```

```
        if(ptr->rightchild)   temp->rightchild=copy(ptr->rightchild);
```

```
        temp->data=ptr->data;
```

```
        return(temp);
```

```
    }
```

```
    return(NULL);
```

```
}
```



Copying a Binary Tree: Explanation

```

int btree::printAncestors(btree *root, int target)
{
    /* base cases */
    if (root == NULL)    return(0);
    if (root->data == target)    return(1);
}

```

```
if ( printAncestors(root->leftchild, target) ||
      printAncestors(root->rightchild, target) )
{
    cout << root->data << " ";
    return 1;
}
```

A target D
 ① root = A target = E ④
 ② root = B " " root = D target = E 1
 ③ root = C " " = E target = E

add of 13 B

```
graph TD; A((A)) --> B((B)); A --> F((F)); B --> C((C)); B --> D((D)); D --> E((E));
```

target

A
B
D

```

btree* btree ::parent(btree *r, int ele)
{
    //root->data==ele then root has no parent so, return NULL
    if(r==NULL||r->data==ele) -
        return(NULL); ✓

    if((r->leftchild!=NULL && r->leftchild->data==ele) ||
        (r->rightchild!=NULL && r->rightchild->data==ele))
        return(r); ✓

    btree *res=parent(r->leftchild, ele);
    if(res!=NULL) return(res);

    res=parent(r->rightchild, ele); ✓

    return(res);
}

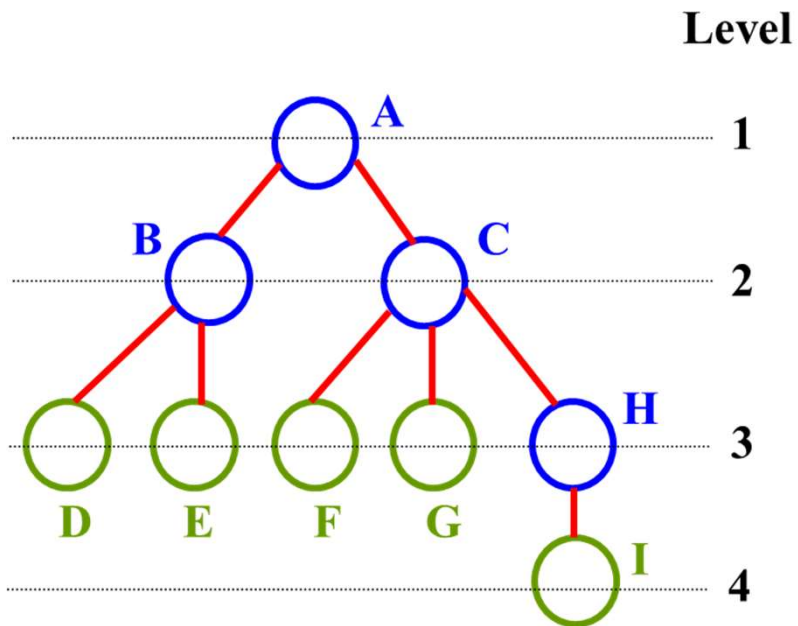
```

**return the parent
node address**

//ele is in leftchild of r
//ele is in rightchild of r



Height of a tree



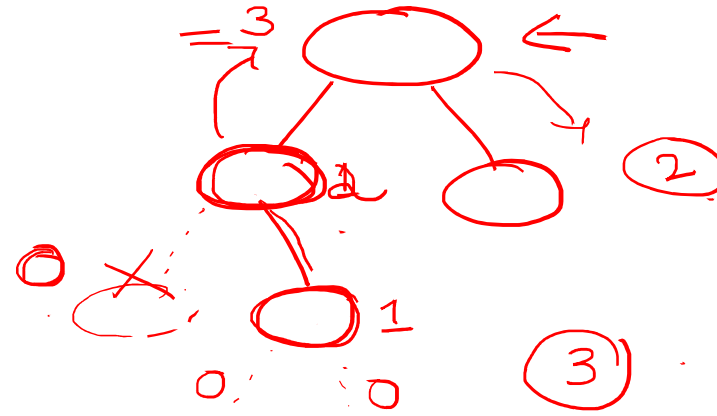
The *height (depth)* of the tree is 4

Height (or depth): the maximum level of any node in the tree

Height of a tree

```

int max(int a,int b)
{
    int m=(a>b)?a:b;
    return(m);
}
int btree::FindHeight(btree *r)
{
    if(root==NULL)    return(0);
    return( max(FindHeight(r->leftchild), FindHeight(r->rightchild)) +1);
}
    
```



- Construct a binary tree using inorder and level order traversal given below.

Inorder Traversal: 3, 4, 2, 1, 5, 8, 9
 Level Order Traversal: 1, 3, 9, 2, 5, 4, 8

LVR

