

**Criptografia i Seguretat [104355]****Activity Cryptographical Mathematical Background**

---

In these set of exercises you are required to implement the specified code described in the questions.

1. Make a program that for a given number  $n$  tells wether it is prime or not looking for factors in  $[1 : n]$ .
2. Make a program that for a given number  $n$  tells wether it is prime or not looking for factors in  $[1 : n/2]$ .
3. Make a program that for a given number  $n$  tells wether it is prime or not using Fermat's theorem.
4. Run your programs for one minute looking for primes.
5. Draw a graph (x-axis number, y-axis time) using both programs to calculate the time spent for every number.
6. Calculate  $\phi(46)$
7. Calculate  $\text{inv}(7, 46)$  using Euler's theorem.
8. Calculate  $\text{inv}(9, 27)$  using Euler's theorem.
9. Calculate  $\text{inv}(7, 25)$  using the Extended Euclides algorithm.
10. Calculate  $19^{75} \bmod 63$  using the Fast exponentiation algorithm.