

13. Use $y = \sqrt[3]{x}$; $dy = 1/(3\sqrt[3]{x^2}) \cdot dx$ with $x = 8$ and $dx = 0.5$. Thus $dy = 1/24 \approx 1/25 = 0.04$; knowing $\sqrt[3]{8} = 2$, we have $\sqrt[3]{8.5} \approx 2.04$.

15. Use $y = \cos x$; $dy = -\sin x \cdot dx$ with $x = \pi/2 \approx 1.57$ and $dx \approx -0.07$. Thus $dy = 0.07$; knowing $\cos \pi/2 = 0$, we have $\cos 1.5 \approx 0.07$.

17. $dy = (2x + 3)dx$

19. $dy = \frac{-2}{4x^3} dx$

21. $dy = (2xe^{3x} + 3x^2e^{3x})dx$

23. $dy = \frac{2(\tan x + 1) - 2x \sec^2 x}{(\tan x + 1)^2} dx$

25. $dy = (e^x \sin x + e^x \cos x)dx$

27. $dy = \frac{1}{(x+2)^2} dx$

29. $dy = (\ln x)dx$

31. (a) ± 12.8 feet

(b) ± 32 feet

33. $\pm 48 \text{ in}^2$, or $1/3 \text{ ft}^2$

35. (a) 298.8 feet

(b) ± 17.3 ft

(c) $\pm 5.8\%$

37. The isosceles triangle setup works the best with the smallest percent error.

Section 4.5

1. F

3. $x_0 = 1.5$, $x_1 = 1.5709148$, $x_2 = 1.5707963$, $x_3 = 1.5707963$, $x_4 = 1.5707963$, $x_5 = 1.5707963$

5. $x_0 = 0$, $x_1 = 2$, $x_2 = 1.2$, $x_3 = 1.0117647$, $x_4 = 1.0000458$, $x_5 = 1$

7. $x_0 = 2$, $x_1 = 0.6137056389$, $x_2 = 0.9133412072$, $x_3 = 0.9961317034$, $x_4 = 0.9999925085$, $x_5 = 1$

9. roots are: $x = -3.714$, $x = -0.857$, $x = 1$ and $x = 1.571$

11. roots are: $x = -2.165$, $x = 0$, $x = 0.525$ and $x = 1.813$

13. $x = -0.637$, $x = 1.410$

15. $x = \pm 4.493$, $x = 0$

17. The approximations alternate between $x = 1$, $x = 2$ and $x = 3$.

Chapter 5

Section 5.1

1. Answers will vary.

3. Answers will vary.

5. Answers will vary.

7. velocity

9. $1/9x^9 + C$

11. $t + C$

13. $-1/(3t) + C$

15. $2\sqrt{x} + C$

17. $-\cos \theta + C$

19. $5e^\theta + C$

21. $\frac{5t}{2 \ln 5} + C$

23. $t^6/6 + t^4/4 - 3t^2 + C$

25. $e^{\pi x} + C$

27. $\frac{x^2}{2} + 3x + \ln |x| + C$

29. (a) $x > 0$

(b) $1/x$

(c) $x < 0$

(d) $1/x$

(e) $\ln |x| + C$. Explanations will vary.

31. $-\cos x + 3$

33. $x^4 - x^3 + 7$

35. $\tan x + 4$

37. $4 \tan^{-1} x + \pi + 12$

39. $\frac{7x^3}{6} - \frac{9x}{2} + \frac{40}{3}$

41. $\theta - \sin(\theta) - \pi + 4$

43. $3x - 2$

45. $dy = (2xe^x \cos x + x^2 e^x \cos x - x^2 e^x \sin x)dx$

Section 5.2

1. Answers will vary.

3. 0

5. (a) 3

(b) 4

(c) 3

(d) 0

(e) -4

(f) 9

7. (a) 4

(b) 2

(c) 4

(d) 2

(e) 1

(f) 2

9. (a) π

(b) π

(c) 2π

(d) 10π

11. (a) $4/\pi$

(b) $-4/\pi$

(c) 0

(d) $2/\pi$

13. (a) $40/3$

(b) $26/3$

(c) $8/3$

(d) $38/3$

15. (a) 3ft/s

(b) 9.5ft

(c) 9.5ft

17. (a) 96ft/s

(b) 6 seconds

(c) 6 seconds

(d) Never; the maximum height is 208ft.

19. 5
 21. Answers can vary; one solution is $a = -2, b = 7$
 23. -7
 25. Answers can vary; one solution is $a = -11, b = 18$
 27. $-\cos x - \sin x + \tan x + C$
 29. $\ln|x| + \csc x + C$

Section 5.3

1. limits
 3. Rectangles.
 5. $2^2 + 3^2 + 4^2 = 29$
 7. $0 - 1 + 0 + 1 + 0 = 0$
 9. $-1 + 2 - 3 + 4 - 5 + 6 = 3$
 11. $1 + 1 + 1 + 1 + 1 + 1 = 6$
 13. Answers may vary; $\sum_{i=0}^8 (i^2 - 1)$
 15. Answers may vary; $\sum_{i=0}^4 (-1)^i e^i$
 17. 1045
 19. -8525
 21. 5050
 23. 155
 25. 24
 27. 19
 29. $\pi/3 + \pi/(2\sqrt{3}) \approx 1.954$
 31. 0.388584
 33. (a) Exact expressions will vary; $\frac{(1+n)^2}{4n^2}$.
 (b) 121/400, 10201/40000, 1002001/4000000
 (c) $1/4$
 35. (a) 8.
 (b) 8, 8, 8
 (c) 8
 37. (a) Exact expressions will vary; $100 - 200/n$.
 (b) 80, 98, 499/5
 (c) 100
 39. $F(x) = 5 \tan x + 4$
 41. $G(t) = 4/6t^6 - 5/4t^4 + 8t + 9$
 43. $G(t) = \sin t - \cos t - 78$

Section 5.4

1. Answers will vary.
 3. T
 5. 20
 7. 0
 9. 1
 11. $(5 - 1/5)/\ln 5$
 13. -4
 15. $16/3$
 17. $45/4$
 19. $1/2$

21. $1/2$
 23. $1/4$
 25. 8
 27. 0
 29. Explanations will vary. A sketch will help.
 31. $c = \pm 2/\sqrt{3}$
 33. $c = 64/9 \approx 7.1$
 35. $2/\pi i$
 37. $16/3$
 39. $\pi/4$
 41. -300ft
 43. $1.5/\ln(2) \approx 2.164\text{miles}$
 45. $128/5\text{ft}$
 47. 50ft/s
 49. 0ft/s
 51. 21
 53. $343/6$
 55. $F'(x) = 3x^{11}$
 57. $F'(x) = e^x \sin(e^x) - \frac{1}{x} \sin(\ln x)$
 59. $F'(x) = \ln(1 - e^x) + \frac{\ln x}{1 - x}$

Section 5.5

1. Chain Rule.
 3. $\frac{1}{8}(x^3 - 5)^8 + C$
 5. $\frac{1}{18}(x^2 + 1)^9 + C$
 7. $\frac{1}{2} \ln|2x + 7| + C$
 9. $\frac{2}{3}(x + 3)^{3/2} - 6(x + 3)^{1/2} + C = \frac{2}{3}(x - 6)\sqrt{x + 3} + C$
 11. $2e^{\sqrt{x}} + C$
 13. $-\frac{1}{2x^2} - \frac{1}{x} + C$
 15. $\frac{1}{3}(2x + 1)^{3/2} - \sqrt{2x + 1} + C$
 17. $-\frac{1}{6} \sin(3 - 6x) + C$
 19. $\frac{1}{2} \ln|\sec(2x) + \tan(2x)| + C$
 21. $\frac{\sin(x^2)}{2} + C$
 23. The key is to multiply $\csc x$ by 1 in the form $(\csc x + \cot x)/(\csc x + \cot x)$.
 25. $\sin(e^x) + C$
 27. $\frac{1}{3}e^{3x-1} + C$
 29. $\frac{1}{2}e^{(x-1)^2} + C$
 31. $\frac{e^{-3x}}{3} - e^{-x} + C$
 33. $\frac{16^x}{\ln(16)} + C$
 35. $\frac{(\ln x)^3}{3} + C$
 37. $\frac{1}{2} \ln(\ln(x^2)) + C$
 39. $\frac{1}{2}(x^2 + 10x + 20 \ln|x - 3|) + C$
 41. $\frac{1}{3} \ln|x^2 + 3x + 3| + \frac{\ln|x|}{3} + C$
 43. $3 \sin^{-1}\left(\frac{x}{3}\right) + C$

45. $\frac{2}{3} \sec^{-1}(|x|/3) + C$
47. $\frac{1}{2} \sin^{-1}(x^2) + C$
49. $2 \sin^{-1}\left(\frac{x-3}{4}\right) + C$
51. $\frac{1}{2} \tan^{-1}(x^2) + C$
53. $-\frac{1}{3(x^3+3)} + C$
55. $-\sqrt{1-x^2} + C$
57. $-\frac{2}{3} \cos^{\frac{3}{2}}(x) + C$
59. $\frac{7}{3} \ln|3x+2| + C$
61. $\ln|x^2+7x+3| + C$
63. $-\frac{x^2}{2} + 2 \ln|x^2-7x+1| + 7x + C$
65. $\tan^{-1}(2x) + C$
67. $\frac{1}{3} \sin^{-1}\left(\frac{3x}{4}\right) + C$
69. $\frac{3}{2} \ln|x^2-2x+10| + \frac{1}{3} \tan^{-1}\left(\frac{x-1}{3}\right) + C$
71. $\frac{15}{2} \ln|x^2-10x+32| + x + \frac{41 \tan^{-1}\left(\frac{x-5}{\sqrt{7}}\right)}{\sqrt{7}} + C$
73. $\frac{x^2}{2} + 3 \ln|x^2+4x+9| - 4x + \frac{24 \tan^{-1}\left(\frac{x+2}{\sqrt{5}}\right)}{\sqrt{5}} + C$
75. $\tan^{-1}(\sin(x)) + C$
77. $3\sqrt{x^2-2x-6} + C$
79. $-\ln 2$
81. $2/3$
83. $(1-e)/2$
85. $\pi/2$
87. $e^{\pi/3} - 1$
89. 1
91. 2
93. $-\frac{1}{2} \cos(2x + \pi) + \frac{91}{2}$
95. $-\ln|\cos x| + 3x + 5$

Section 5.6

1. F
3. They are superseded by the Trapezoidal Rule; it takes an equal amount of work and is generally more accurate.
5. (a) 250
(b) 250
(c) 250
7. (a) $2 + \sqrt{2} + \sqrt{3} \approx 5.15$
(b) $2/3(3 + \sqrt{2} + 2\sqrt{3}) \approx 5.25$
(c) $16/3 \approx 5.33$
9. (a) 0.2207
(b) 0.2005
(c) 1/5
11. (a) $9/2(1 + \sqrt{3}) \approx 12.294$
(b) $3 + 6\sqrt{3} \approx 13.392$
(c) $9\pi/2 \approx 14.137$
13. Trapezoidal Rule: 3.0241
Simpson's Rule: 2.9315

15. Trapezoidal Rule: 3.0695
Simpson's Rule: 3.14295
17. Trapezoidal Rule: 2.52971
Simpson's Rule: 2.5447
19. Trapezoidal Rule: 3.5472
Simpson's Rule: 3.6133
21. (a) $n = 150$ (using $\max(f''(x)) = 1$)
(b) $n = 18$ (using $\max(f^{(4)}(x)) = 7$)
23. (a) $n = 5591$ (using $\max(f''(x)) = 300$)
(b) $n = 46$ (using $\max(f^{(4)}(x)) = 24$)
25. (a) Area is 25.0667 cm²
(b) Area is 250,667 yd²

Chapter 6

Section 6.1

1. T
3. Determining which functions in the integrand to set equal to "u" and which to set equal to "dv".
5. $-e^{-x} - xe^{-x} + C$
7. $-x^3 \cos x + 3x^2 \sin x + 6x \cos x - 6 \sin x + C$
9. $x^3 e^x - 3x^2 e^x + 6x e^x - 6e^x + C$
11. $-\frac{1}{2} x e^{-2x} - \frac{e^{-2x}}{4} + C$
13. $\frac{1}{5} e^{2x} (\sin x + 2 \cos x) + C$
15. $\frac{1}{13} e^{2x} (2 \sin(3x) - 3 \cos(3x)) + C$
17. $-\frac{1}{2} \cos^2 x + C$
19. $x \tan^{-1}(2x) - \frac{1}{4} \ln(4x^2 + 1) + C$
21. $x \cos^{-1} x - \sqrt{1-x^2} + C$
23. $-\frac{x^2}{4} + \frac{1}{2} x^2 \ln x + 2x - 2x \ln x + C$
25. $\frac{1}{2} x^2 \ln(x^2) - \frac{x^2}{2} + C$
27. $2\sqrt{x} \ln x - 4\sqrt{x} + C$
29. $2x + (x+1)(\ln(x+1))^2 - (2x+2)\ln(x+1) + C$
31. $\ln|\sin(x)| - x \cot(x) + C$
33. $\frac{1}{3}(x^2 - 2)^{3/2} + C$
35. $x \sec x - \ln|\sec x + \tan x| + C$
37. $\frac{x^{n+1} \ln x}{n+1} - \frac{x^{n+1}}{(n+1)^2} + C$
39. $2 \sin(\sqrt{x}) - 2\sqrt{x} \cos(\sqrt{x}) + C$
41. $2\sqrt{x} e^{\sqrt{x}} - 2e^{\sqrt{x}} + C$
43. π
45. 0
47. $1/2$
49. $\frac{98}{\ln 7} - \frac{48}{(\ln 7)^2}$
51. $\frac{1}{2} + \frac{e^{\pi}}{2}$
53. $xe^x \ln x - e^x + C$
55. $\sin x - x \cos x + 9$
57. $\frac{1}{3} x^3 \ln x - \frac{x^3}{9} + \frac{7e^3}{9}$

Section 6.2