

45. $\frac{2}{3} \sec^{-1}(|x|/3) + C$
47. $\frac{1}{2} \sin^{-1}(x^2) + C$
49. $2 \sin^{-1}\left(\frac{x-3}{4}\right) + C$
51. $\frac{1}{2} \tan^{-1}(x^2) + C$
53. $-\frac{1}{3(x^3+3)} + C$
55. $-\sqrt{1-x^2} + C$
57. $-\frac{2}{3} \cos^{\frac{3}{2}}(x) + C$
59. $\frac{7}{3} \ln|3x+2| + C$
61. $\ln|x^2+7x+3| + C$
63. $-\frac{x^2}{2} + 2 \ln|x^2-7x+1| + 7x + C$
65. $\tan^{-1}(2x) + C$
67. $\frac{1}{3} \sin^{-1}\left(\frac{3x}{4}\right) + C$
69. $\frac{3}{2} \ln|x^2-2x+10| + \frac{1}{3} \tan^{-1}\left(\frac{x-1}{3}\right) + C$
71. $\frac{15}{2} \ln|x^2-10x+32| + x + \frac{41 \tan^{-1}\left(\frac{x-5}{\sqrt{7}}\right)}{\sqrt{7}} + C$
73. $\frac{x^2}{2} + 3 \ln|x^2+4x+9| - 4x + \frac{24 \tan^{-1}\left(\frac{x+2}{\sqrt{5}}\right)}{\sqrt{5}} + C$
75. $\tan^{-1}(\sin(x)) + C$
77. $3\sqrt{x^2-2x-6} + C$
79. $-\ln 2$
81. $2/3$
83. $(1-e)/2$
85. $\pi/2$
87. $e^{\pi/3} - 1$
89. 1
91. 2
93. $-\frac{1}{2} \cos(2x + \pi) + \frac{91}{2}$
95. $-\ln|\cos x| + 3x + 5$

Section 5.6

1. F
3. They are superseded by the Trapezoidal Rule; it takes an equal amount of work and is generally more accurate.
5. (a) 250
(b) 250
(c) 250
7. (a) $2 + \sqrt{2} + \sqrt{3} \approx 5.15$
(b) $2/3(3 + \sqrt{2} + 2\sqrt{3}) \approx 5.25$
(c) $16/3 \approx 5.33$
9. (a) 0.2207
(b) 0.2005
(c) 1/5
11. (a) $9/2(1 + \sqrt{3}) \approx 12.294$
(b) $3 + 6\sqrt{3} \approx 13.392$
(c) $9\pi/2 \approx 14.137$
13. Trapezoidal Rule: 3.0241
Simpson's Rule: 2.9315

15. Trapezoidal Rule: 3.0695
Simpson's Rule: 3.14295
17. Trapezoidal Rule: 2.52971
Simpson's Rule: 2.5447
19. Trapezoidal Rule: 3.5472
Simpson's Rule: 3.6133
21. (a) $n = 150$ (using $\max(f''(x)) = 1$)
(b) $n = 18$ (using $\max(f^{(4)}(x)) = 7$)
23. (a) $n = 5591$ (using $\max(f''(x)) = 300$)
(b) $n = 46$ (using $\max(f^{(4)}(x)) = 24$)
25. (a) Area is 25.0667 cm²
(b) Area is 250,667 yd²

Chapter 6

Section 6.1

1. T
3. Determining which functions in the integrand to set equal to "u" and which to set equal to "dv".
5. $-e^{-x} - xe^{-x} + C$
7. $-x^3 \cos x + 3x^2 \sin x + 6x \cos x - 6 \sin x + C$
9. $x^3 e^x - 3x^2 e^x + 6x e^x - 6e^x + C$
11. $-\frac{1}{2} x e^{-2x} - \frac{e^{-2x}}{4} + C$
13. $\frac{1}{5} e^{2x} (\sin x + 2 \cos x) + C$
15. $\frac{1}{13} e^{2x} (2 \sin(3x) - 3 \cos(3x)) + C$
17. $-\frac{1}{2} \cos^2 x + C$
19. $x \tan^{-1}(2x) - \frac{1}{4} \ln(4x^2 + 1) + C$
21. $x \cos^{-1} x - \sqrt{1-x^2} + C$
23. $-\frac{x^2}{4} + \frac{1}{2} x^2 \ln x + 2x - 2x \ln x + C$
25. $\frac{1}{2} x^2 \ln(x^2) - \frac{x^2}{2} + C$
27. $2\sqrt{x} \ln x - 4\sqrt{x} + C$
29. $2x + (x+1)(\ln(x+1))^2 - (2x+2)\ln(x+1) + C$
31. $\ln|\sin(x)| - x \cot(x) + C$
33. $\frac{1}{3}(x^2 - 2)^{3/2} + C$
35. $x \sec x - \ln|\sec x + \tan x| + C$
37. $\frac{x^{n+1} \ln x}{n+1} - \frac{x^{n+1}}{(n+1)^2} + C$
39. $2 \sin(\sqrt{x}) - 2\sqrt{x} \cos(\sqrt{x}) + C$
41. $2\sqrt{x} e^{\sqrt{x}} - 2e^{\sqrt{x}} + C$
43. π
45. 0
47. $1/2$
49. $\frac{98}{\ln 7} - \frac{48}{(\ln 7)^2}$
51. $\frac{1}{2} + \frac{e^{\pi}}{2}$
53. $x e^x \ln x - e^x + C$
55. $\sin x - x \cos x + 9$
57. $\frac{1}{3} x^3 \ln x - \frac{x^3}{9} + \frac{7e^3}{9}$

Section 6.2

1. F
3. F
5. $\frac{1}{4} \sin^4(x) + C$
7. $\frac{3}{8}x - \frac{1}{4} \sin(2x) + \frac{1}{32} \sin(4x) + C$
9. $\frac{3}{8}x + \frac{1}{4} \sin(2x) + \frac{1}{32} \sin(4x) + C$
11. $\frac{1}{6} \cos^6 x - \frac{1}{4} \cos^4 x + C$
13. $-\frac{1}{9} \sin^9(x) + \frac{3 \sin^7(x)}{7} - \frac{3 \sin^5(x)}{5} + \frac{\sin^3(x)}{3} + C$
15. $\tan x - \sec x + C$
17. $\frac{1}{2} \left(-\frac{1}{3} \cos(3x) + \cos(-x) \right) + C$
19. $\frac{1}{2} \left(\frac{1}{\pi} \sin(\pi x) - \frac{1}{3\pi} \sin(3\pi x) \right) + C$
21. $\frac{1}{\pi} \sin\left(\frac{\pi}{2}x\right) + \frac{1}{3\pi} \sin(\pi x) + C$
23. $\frac{\sqrt{2}}{4}x - \frac{1}{12} \sin\left(6x + \frac{\pi}{4}\right) + C$
25. $\frac{\tan^5(x)}{5} + C$
27. $\frac{\tan^6(x)}{6} + \frac{\tan^4(x)}{4} + C$
29. $\frac{\sec^5(x)}{5} - \frac{\sec^3(x)}{3} + C$
31. $\frac{1}{3} \tan^3 x - \tan x + x + C$
33. $\frac{1}{4} \tan x \sec^3 x + \frac{3}{8} (\sec x \tan x + \ln |\sec x + \tan x|) + C$
35. $\frac{1}{4} \tan x \sec^3 x - \frac{1}{8} (\sec x \tan x + \ln |\sec x + \tan x|) + C$
37. 0
39. $3\pi/4$
41. $1/2$
43. $1/5$
45. $\frac{3}{4} + \ln 2$
47. $\frac{1}{2} \tan^2 x + \ln |\cos x| + 4$
49. $\frac{1}{2} \left(-\frac{1}{8} \cos(8x) - \frac{1}{2} \cos(2x) \right) - \frac{11}{16}$

Section 6.3

1. backwards
3. (a) $\tan^2 \theta + 1 = \sec^2 \theta$
(b) $9 \sec^2 \theta$
5. $\frac{1}{2} \left(x\sqrt{x^2+1} + \ln |\sqrt{x^2+1} + x| \right) + C$
7. $\frac{1}{2} \left(\sin^{-1} x + x\sqrt{1-x^2} \right) + C$
9. $\frac{1}{2} x\sqrt{x^2-1} - \frac{1}{2} \ln |x + \sqrt{x^2-1}| + C$
11. $x\sqrt{x^2+1/4} + \frac{1}{4} \ln |2\sqrt{x^2+1/4} + 2x| + C =$
 $\frac{1}{2} x\sqrt{4x^2+1} + \frac{1}{4} \ln |\sqrt{4x^2+1} + 2x| + C$
13. $4 \left(\frac{1}{2} x\sqrt{x^2-1/16} - \frac{1}{32} \ln |4x + 4\sqrt{x^2-1/16}| \right) + C =$
 $\frac{1}{2} x\sqrt{16x^2-1} - \frac{1}{8} \ln |4x + \sqrt{16x^2-1}| + C$
15. $\frac{1}{2} a^2 \ln \left(\sqrt{x^2+a^2} + x \right) + \frac{1}{2} x\sqrt{x^2+a^2} + C$
17. $3 \sin^{-1} \left(\frac{x}{\sqrt{7}} \right) + C$ (Trig. Subst. is not needed)
19. $\sqrt{x^2-11} - \sqrt{11} \sec^{-1}(x/\sqrt{11}) + C$
21. $\sqrt{x^2-3} + C$ (Trig. Subst. is not needed)
23. $-\frac{1}{\sqrt{x^2+9}} + C$ (Trig. Subst. is not needed)

25. $\frac{1}{18} \frac{x+2}{x^2+4x+13} + \frac{1}{54} \tan^{-1} \left(\frac{x+2}{2} \right) + C$
27. $\frac{1}{7} \left(-\frac{\sqrt{5-x^2}}{x} - \sin^{-1}(x/\sqrt{5}) \right) + C$
29. $\frac{1}{2} e^{\sin^{-1} x} \left(x + \sqrt{1-x^2} \right) + C$
31. $\pi/2$
33. $2\sqrt{2} + 2 \ln(1 + \sqrt{2})$
35. $9 \sin^{-1}(1/3) + \sqrt{8}$ Note: the new lower bound is $\theta = \sin^{-1}(-1/3)$ and the new upper bound is $\theta = \sin^{-1}(1/3)$. The final answer comes with recognizing that $\sin^{-1}(-1/3) = -\sin^{-1}(1/3)$ and that $\cos(\sin^{-1}(1/3)) = \cos(\sin^{-1}(-1/3)) = \sqrt{8}/3$.
37. $\frac{1}{2} \left(x\sqrt{x^2+1} + \ln |\sqrt{x^2+1} + x| \right) + 6$
39. $5 \ln \left| \frac{x}{\sqrt{8}} + \frac{\sqrt{x^2-8}}{\sqrt{8}} \right| + 4$

Section 6.4

1. rational
3. $\frac{A}{x} + \frac{B}{x-3}$
5. $\frac{A}{x-\sqrt{7}} + \frac{B}{x+\sqrt{7}}$
7. $3 \ln |x-2| + 4 \ln |x+5| + C$
9. $\frac{1}{3} (\ln |x+2| - \ln |x-2|) + C$
11. $-\frac{4}{x+8} - 3 \ln |x+8| + C$
13. $-\ln |2x-3| + 5 \ln |x-1| + 2 \ln |x+3| + C$
15. $x + \ln |x-1| - \ln |x+2| + C$
17. $-\ln |x+5| + \frac{1}{2} \ln (x^2+4) + \frac{1}{2} \tan^{-1} \left(\frac{x}{2} \right) + C$
19. $\frac{x^2}{2} + x + \frac{125}{9} \ln |x-5| + \frac{64}{9} \ln |x+4| - \frac{35}{2} + C$
21. $\frac{1}{6} \left(-\ln |x^2+2x+3| + 2 \ln |x| - \sqrt{2} \tan^{-1} \left(\frac{x+1}{\sqrt{2}} \right) \right) + C$
23. $\ln |3x^2+5x-1| + 2 \ln |x+1| + C$
25. $\frac{9}{10} \ln |x^2+9| + \frac{1}{5} \ln |x+1| - \frac{4}{15} \tan^{-1} \left(\frac{x}{3} \right) + C$
27. $-\ln |x| - \frac{1}{2x^2} + \frac{1}{2} \ln (x^2+1) + C$
29. $\frac{1}{2} \ln |x^2+10x+27| + 5 \ln |x+2| - 6\sqrt{2} \tan^{-1} \left(\frac{x+5}{\sqrt{2}} \right) + C$
31. $\frac{1}{3} (\ln |\cos x+2| - \ln |\cos x-2|) + C$
33. $\ln(2000/243) \approx 2.108$
35. $\ln(9/5)$
37. $1/8$

Section 6.5

1. Because $\cosh x$ is always positive.

$$\begin{aligned}
 3. \quad \coth^2 x - \operatorname{csch}^2 x &= \left(\frac{e^x + e^{-x}}{e^x - e^{-x}} \right)^2 - \left(\frac{2}{e^x - e^{-x}} \right)^2 \\
 &= \frac{(e^{2x} + 2 + e^{-2x}) - (4)}{e^{2x} - 2 + e^{-2x}} \\
 &= \frac{e^{2x} - 2 + e^{-2x}}{e^{2x} - 2 + e^{-2x}} \\
 &= 1
 \end{aligned}$$

$$\begin{aligned}
 5. \quad \cosh^2 x &= \left(\frac{e^x + e^{-x}}{2} \right)^2 \\
 &= \frac{e^{2x} + 2 + e^{-2x}}{4} \\
 &= \frac{1}{2} \frac{(e^{2x} + e^{-2x}) + 2}{2} \\
 &= \frac{1}{2} \left(\frac{e^{2x} + e^{-2x}}{2} + 1 \right) \\
 &= \frac{\cosh 2x + 1}{2}.
 \end{aligned}$$

$$\begin{aligned}
 7. \quad \frac{d}{dx} [\operatorname{sech} x] &= \frac{d}{dx} \left[\frac{2}{e^x + e^{-x}} \right] \\
 &= \frac{-2(e^x - e^{-x})}{(e^x + e^{-x})^2} \\
 &= -\frac{2(e^x - e^{-x})}{(e^x + e^{-x})(e^x + e^{-x})} \\
 &= -\frac{2}{e^x + e^{-x}} \cdot \frac{e^x - e^{-x}}{e^x + e^{-x}} \\
 &= -\operatorname{sech} x \tanh x
 \end{aligned}$$

$$\begin{aligned}
 9. \quad \int \tanh x \, dx &= \int \frac{\sinh x}{\cosh x} \, dx \\
 \text{Let } u &= \cosh x; \, du = (\sinh x) \, dx \\
 &= \int \frac{1}{u} \, du \\
 &= \ln |u| + C \\
 &= \ln(\cosh x) + C.
 \end{aligned}$$

11. $2 \sinh 2x$

13. $\coth x$

15. $x \cosh x$

17. $\frac{3}{\sqrt{9x^2+1}}$

19. $\frac{1}{1-(x+5)^2}$

21. $\sec x$

23. $y = 3/4(x - \ln 2) + 5/4$

25. $y = x$

27. $1/2 \ln(\cosh(2x)) + C$

29. $1/2 \sinh^2 x + C$ or $1/2 \cosh^2 x + C$

31. $x \cosh(x) - \sinh(x) + C$

33. $\cosh^{-1}(x^2/2) + C = \ln(x^2 + \sqrt{x^4 - 4}) + C$

35. $\frac{1}{16} \tan^{-1}(x/2) + \frac{1}{32} \ln|x-2| + \frac{1}{32} \ln|x+2| + C$

37. $\tan^{-1}(e^x) + C$

39. $x \tanh^{-1} x + 1/2 \ln|x^2 - 1| + C$

41. 0

43. 2

Section 6.6

1. The interval of integration is finite, and the integrand is continuous on that interval.

3. converges; could also state < 10 .

5. $p > 1$

7. $e^5/2$

9. $1/3$

11. $1/\ln 2$

13. diverges

15. 1

17. diverges

19. diverges

21. diverges

23. 1

25. 0

27. $-1/4$

29. -1

31. diverges

33. $1/2$

35. converges; Limit Comparison Test with $1/x^{3/2}$.

37. converges; Direct Comparison Test with xe^{-x} .

39. converges; Direct Comparison Test with xe^{-x} .

41. diverges; Direct Comparison Test with $x/(x^2 + \cos x)$.

43. converges; Limit Comparison Test with $1/e^x$.

Section 6.7

1. F

3. $f'(x) = \frac{e^{x^2}}{\sqrt{\pi} \operatorname{erfi} x}$

5. $f'(x) = \frac{4}{\sqrt{\pi}} e^{-(2x+3)^2}$

7. $f'(x) = 2x \operatorname{erfi} x + \frac{6}{\sqrt{\pi}} x^2 e^{9x^2}$

9. $h'(x) = \frac{2}{\sqrt{\pi}} (e^{-x^2} \operatorname{erfi} x + e^{x^2} \operatorname{erf} x)$

11. $k'(x) = 2\sqrt{\pi} e^{\operatorname{erf}^{-1}(4x)^2} + 5$

13. $\frac{\sqrt{\pi}}{4} \operatorname{erf}(2x) + C$

15. $\frac{\sqrt{\pi}}{2\sqrt{a}} \operatorname{erf}(\sqrt{ax}) + C$

17. $x \operatorname{erfi} x - \frac{1}{\sqrt{\pi}} e^{x^2} + C$

19. $\frac{\sqrt{\pi}}{4} \operatorname{erf}(2x+5) + C$

21. $\frac{\sqrt{\pi}}{2e^9} \operatorname{erfi}(x+3) + C$

23. $\frac{1}{2} x e^{x^2} - \frac{\sqrt{\pi}}{4} \operatorname{erfi} x + C$

25. $\frac{\sqrt{\pi}}{2} \ln |\operatorname{erfi} x| + C$

27. $e^4 \sqrt{\pi} \operatorname{erf}(x-2) - \frac{1}{2} e^{-x^2+4x} + C$

29. $\frac{\sqrt{\pi}}{2e^{1/4}} \operatorname{erfi}(\ln x + \frac{1}{2}) + C$

31. $\frac{\sqrt{\pi}}{3} \operatorname{erf}(x^{3/2}) + C$

33. $\frac{\sqrt{\pi}}{6} (\operatorname{erf} 1000 - \operatorname{erf} 1)$

35. $\frac{\sqrt{\pi}}{2} \operatorname{erf} 1$

37. $\sqrt{\pi} (\operatorname{erfi} 6 - \operatorname{erf} 6)$

39. $2/\sqrt{\pi}$

41. 0

43. ∞

45. $1/\sqrt{\pi}$

47. $\operatorname{Si}(7x) + C$

49. $x \operatorname{Si}(x) + \cos x + C$

51. $\operatorname{Si}(a)$