# Prueba métodos de segunda entrega

LU con gaussiana simple:

Stage # 1

L:

U:

```
Stage # 2
```

[[4. -1. 0. 3. ]
[0. 15.75 3. 7.25 ]
[0. 0. -3.75238095 1.6984127]
[0. 0. -3.61904762 15.58730159]]
L:

[ 0. -0.08253968 1. 0.

[3.5 0.53968254 0. 1. ]]

]

U:

[[ 4. -1. 0. 3. ]

[0. 15.75 3. 7.25]

[0. 0. -3.75238095 1.6984127]

[0. 0. 15.58730159]]

Stage # 3

[[ 4. -1. 0. 3. ]

```
[0. 15.75 3. 7.25]
```

U:

**Solution reg:** 

#### LU con pivoteo parcial:

## Stage # 1

[[14. 5. -2. 30. ]

[0. 15.14285714 3.14285714 5.85714286]

[0. -1.3 -4. 1.1]

[0. -2.42857143 0.57142857 -5.57142857]]

L:

[[1. 0. 0. 0. ]

[0.07142857 1. 0. 0. ]

[0. 0. 1. 0. ]

[0.28571429 0. 0. 1. ]]

U:

[[14. 5. -2. 30. ]

[0. 15.14285714 3.14285714 5.85714286]

[0. 0. 0. 0.]

[0. 0. 0. 0. ]]

Stage # 2

```
[[14. 5. -2.
              30. ]
[ 0.
    15.14285714 3.14285714 5.85714286]
[0. 0. 1.0754717 -4.63207547]]
L:
[ 0.07142857 1. 0.
                0.
[0. -0.08584906 1. 0.
[ 0.28571429 -0.16037736 0.
                     ]]
                   1.
U:
[[14. 5. -2.
              30.
[0. 15.14285714 3.14285714 5.85714286]
[ 0.
     0. 0.
             0. ]]
Stage # 3
[[14.
     5.
              30. ]
         -2.
[0. 15.14285714 3.14285714 5.85714286]
```

```
[0. 0. -3.73018868 1.60283019]
```

[[ 1. 0. 0. 0. ]

[0.07142857 1. 0. 0. ]

[0. -0.08584906 1. 0. ]

[ 0.28571429 -0.16037736 -0.28831563 1. ]]

U:

[[14. 5. -2. 30. ]

[0. 15.14285714 3.14285714 5.85714286]

[0. 0. -3.73018868 1.60283019]

[0. 0. -4.16995448]]

**Solution reg:** 

```
Doolittle:
Stage # 1
L:
[[1. 0. 0. 0. ]
[0.25 1. 0. 0.]
[0. 0. 1. 0.]
[3.5 0. 0. 1.]]
U:
[[ 4. -1. 0. 3.]
[0. 1. 0. 0.]
[0. 0. 1. 0.]
[0. 0. 0. 1.]]
Stage # 2
L:
[[ 1.
                      0. ]
         0.
               0.
[ 0.25
                0.
                     0.
         1.
                          ]
       -0.08253968 1.
[ 0.
                               ]
                          0.
```

```
[ 3.5  0.53968254 0.
                     1. ]]
U:
[[ 4. -1. 0. 3. ]
[ 0. 15.75 3. 7.25]
[0. 0. 1. 0.]
[0. 0. 0. 1.]]
Stage # 3
L:
[[ 1. 0.
            0. 0. ]
[ 0.25 1. 0.
               0. ]
[0. -0.08253968 1. 0. ]
[3.5 0.53968254 0.96446701 1.
                             ]]
U:
     -1. 0. 3. ]
[[ 4.
[ 0.
      15.75 3. 7.25 ]
[ 0.
           -3.75238095 1.6984127]
      0.
[ 0.
      0. 0.
                 1. ]]
```

```
Stage # 4
```

```
[[ 1. 0. 0. 0. ]
```

U:

**Solution reg:** 

```
Crout:
Stage # 1
L:
[[ 4. 0. 0. 0.]
[1. 1. 0. 0.]
[0. 0. 1. 0.]
[14. 0. 0. 1.]]
U:
[[ 1. -0.25 0. 0.75]
[0. 1. 0. 0.]
[0. 0. 1. 0.]
[0. 0. 0. 1.]]
Stage # 2
L:
[[ 4. 0. 0. 0. ]
[1. 15.75 0. 0.]
[0. -1.3 1. 0.]
```

```
[14. 8.5 0. 1.]]
U:
                     0.75 ]
[[ 1.
       -0.25 0.
[ 0.
             0.19047619 0.46031746]
       1.
[ 0.
       0.
             1.
                   0.
                       ]
[ 0.
       0.
             0.
                   1.
                        ]]
Stage # 3
L:
[[ 4.
      0.
              0.
                    0. ]
[ 1.
       15.75
             0.
                  0. ]
[ 0.
      -1.3
             -3.75238095 0.
                             ]
[14.
       8.5 -3.61904762 1.
                              ]]
U:
[[ 1.
                     0.75 ]
       -0.25
               0.
```

0.19047619 0.46031746]

-0.45262267]

]]

1.

[ 0.

[ 0.

[ 0.

1.

0.

0.

1.

0.

```
Stage # 4
```

```
[[ 4.  0.  0.  0. ]
```

U:

**Solution reg:** 

**Cholesky:** 

Stage # 1

L:

U:

$$[0.+0.j 1.+0.j 0.+0.j 0.+0.j]$$

Stage # 2

L:

U:

$$[[2. +0.j-0.5 +0.j 0. +0.j 1.5 +0.j]$$

$$[0. +0.j 0. +0.j 1. +0.j 0. +0.j]$$

$$[0. +0.j 0. +0.j 0. +0.j 1. +0.j]$$

Stage # 3

L:

U:

1. +0.j ]]

Stage # 4

L:

U:

[[ 2. +0.j -0.5 +0.j 0. +0.j

1.5 +0.j ]

[ 0. +0.j 3.96862697+0.j 0.75592895+0.j

1.82682829+0.j ]

[ 0. +0.j 0. +0.j 0. +1.93710633j

0. -0.87677825j]

[ 0. +0.j 0. +0.j 0. +0.j

3.73486795+0.j ]]

#### **Solution reg:**

#### Jacobi:

```
T:
[[ 0.
       0.25
              0.
                   -0.75
[-0.06451613 0.
                -0.19354839 -0.51612903]
[ 0.
      -0.325
              0.
                    0.275 ]
[-0.46666667 -0.16666667 0.06666667 0.
                                    ]]
C:
[[ 0.25 ]
[ 0.06451613]
[-0.25]
[ 0.03333333]]
radio espectral:
0.7535169428701507
| 1 | 0.3609341242060913 | [[ 0.25
                                0.06451613 -0.25
                                                 0.03333333]]
2 | 0.14562059206430902 | [[ 0.24112903 0.07956989 -0.26180108 -0.11075269]]
| 3 | 0.14300818286037656 | [[ 0.35295699 0.15679327 -0.3063172 -0.1099086 ]]
| 5 | 0.06781846767106765 | [[ 0.4228897 | 0.19647642 -0.35020331 -0.18846589]]
| 7 | 0.034373218837995455 | [[ 0.46565284 0.22048036 -0.37627299 -0.230312 ]]
| 8 | 0.022299115905640772 | [[ 0.47785409 0.22617175 -0.38499192 -0.24580292]]
9 | 0.018404146842246727 | [[ 0.49089513 0.23506742 -0.39110162 -0.25302666]]
| 10 | 0.01274208943260705 | [[ 0.49853685 0.23913697 -0.39597924 -0.2610024 ]]
| 11 | 0.010153523789418853 | [[ 0.50553605 0.24370452 -0.39949518 -0.26557197]]
| 12 | 0.007297184431054095 | [[ 0.51010511 0.24629195 -0.40223626 -0.26983392]]
| 13 | 0.005682976184690885 | [[ 0.51394843 0.24872742 -0.40424921 -0.27258013]]
```

```
| 14 | 0.004170129100507794 | [[ 0.51661695 0.25028647 -0.40579595 -0.27491378]]
| 15 | 0.003202876242866248 | [[ 0.51875696 0.25161814 -0.40694439 -0.27652205]]
| 16 | 0.002377650044978286 | [[ 0.52029607 0.25253243 -0.40781946 -0.27781923]]
| 17 | 0.0018113554695020299 | [[ 0.52149753 0.25327201 -0.40847333 -0.2787482 ]]
| 18 | 0.0013534193250926492 | [[ 0.52237915 0.25380052 -0.40896916 -0.27947574]]
| 19 | 0.0010262349782541843 | [[ 0.52305693 0.25421511 -0.409341 -0.2800083 ]]
| 21 | 0.0005819809551116511 | [[ 0.52394342  0.2547519  -0.40983351 -0.28072252]]
| 22 | 0.0004373454493213835 | [[ 0.52422986 0.25492498 -0.40999306 -0.28095448]]
| 23 | 0.0003302180435300071 | [[ 0.52444711  0.25505711 -0.4101131 -0.28112764]]
| 24 | 0.00024844229604978866 | [[ 0.52461001 0.2551557 -0.41020366 -0.28125904]]
| 25 | 0.0001874221799343558 | [[ 0.52473321 0.25523054 -0.41027184 -0.28135753]]
27 | 0.00010639302687024356 | [[ 0.52489568 0.25532905 -0.41036196 -0.28148802]]
| 28 | 8.012914855822946e-05 | [[ 0.52494828 0.25536092 -0.41039115 -0.28153029]]
| 29 | 6.040125884579987e-05 | [[ 0.52498795 0.255385 -0.41041313 -0.28156209]]
| 30 | 4.5500530962233675e-05 | [[ 0.52501782 0.25540311 -0.4104297 -0.28158609]]
31 | 3.4292711698199305e-05 | [[0.52504034 0.25541677 -0.41044218 -0.28160415]]
33 | 1.9470213684017856e-05 | [[ 0.52507009 0.25543481 -0.41045868 -0.28162802]]
| 34 | 1.4669798856319548e-05 | [[ 0.52507972 0.25544065 -0.41046402 -0.28163576]]
| 35 | 1.1054701396074889e-05 | [[ 0.52508698 0.25544506 -0.41046805 -0.28164158]]
| 36 | 8.329473337992045e-06 | [[ 0.52509245 0.25544837 -0.41047108 -0.28164597]]
37 | 6.276644365854363e-06 | [[ 0.52509657 0.25545087 -0.41047336 -0.28164928]]
38 | 4.72941863820054e-06 | [[ 0.52509968 0.25545276 -0.41047509 -0.28165177]]
39 | 3.5637761663255912e-06 | [[ 0.52510202 0.25545418 -0.41047638 -0.28165365]]
40 | 2.6853207891975457e-06 | [[ 0.52510378 0.25545525 -0.41047736 -0.28165506]]
| 41 | 2.0234602362765088e-06 | [[ 0.52510511 0.25545605 -0.4104781 -0.28165613]]
| 42 | 1.524697070927425e-06 | [[ 0.52510611 0.25545666 -0.41047865 -0.28165693]]
| 43 | 1.1488933128741926e-06 | [[ 0.52510686 0.25545712 -0.41047907 -0.28165754]]
44 | 8.657058973397584e-07 | [[ 0.52510743 0.25545746 -0.41047939 -0.28165799]]
```

```
| 45 | 6.523267194297135e-07 | [[ 0.52510786 0.25545772 -0.41047962 -0.28165834]]
| 46 | 4.915377253677003e-07 | [[ 0.52510818 0.25545792 -0.4104798 -0.2816586 ]]
47 | 3.7038286194962125e-07 | [[ 0.52510843 0.25545806 -0.41047994 -0.28165879]]
| 48 | 2.790892744563103e-07 | [[ 0.52510861 0.25545818 -0.41048004 -0.28165894]]
49 | 2.1029877372291008e-07 | [[ 0.52510875 0.25545826 -0.41048012 -0.28165905]]
| 50 | 1.5846353178159807e-07 | [[ 0.52510885 0.25545832 -0.41048017 -0.28165913]]
| 51 | 1.1940504540415286e-07 | [[ 0.52510893 0.25545837 -0.41048022 -0.2816592 ]]
| 52 | 8.997367396720935e-08 | [[ 0.52510899 0.25545841 -0.41048025 -0.28165924]]
Gauss-Seidel:
T:
[[ 0.
        0.25
                     -0.75 ]
               0.
[ 0.
       -0.01612903 -0.19354839 -0.46774194]
       0.00524194 0.06290323 0.42701613]
[ 0.
[ 0.
       -0.11362903 0.03645161 0.45642473]]
C:
[[ 0.25 ]
[ 0.0483871 ]
[-0.26572581]
[-0.1091129]]
radio espectral:
0.5994876461601171
| Iter | E |
| 2 | 0.16541590217059002 | [[ 0.34393145 0.15007414 -0.32878014 -0.17409904]]
| 3 | 0.10021770191219365 | [[ 0.41809282 0.19103484 -0.35996356 -0.21761336]]
```

| 4 | 0.059762438191934164 | [[ 0.46096873 0.21676315 -0.3802917 -0.24326538]]

```
7 | 0.012872489375017275 | [[ 0.51128483 0.24712813 -0.40397782 -0.27338613]]
| 8 | 0.007716879024174241 | [[ 0.51682163 0.25046457 -0.40658217 -0.27669967]]
9 | 0.004626178059659651 | [[ 0.52014089 0.25246471 -0.40814344 -0.2786861 ]]
| 10 | 0.002773336370545754 | [[ 0.52213075 0.25366376 -0.4090794 -0.27987694]]
| 11 | 0.0016625808687072675 | [[ 0.52332364 0.25438258 -0.4096405 -0.28059083]]
| 13 | 0.0005975073561320842 | [[ 0.52446748 0.25507184 -0.41017852 -0.28127536]]
| 14 | 0.0003581982784618611 | [[ 0.52472448 0.25522671 -0.41029941 -0.28142917]]
| 15 | 0.00021473544281859914 | [[ 0.52487856 0.25531955 -0.41037188 -0.28152138]]
| 16 | 0.00012873124516221438 | [[ 0.52497092 0.25537521 -0.41041532 -0.28157665]]
| 17 | 7.717279114958393e-05 | [[ 0.52502629 0.25540857 -0.41044137 -0.28160979]]
| 18 | 4.626413491387999e-05 | [[ 0.52505948 0.25542858 -0.41045698 -0.28162965]]
| 19 | 2.773477734112971e-05 | [[ 0.52507938 0.25544057 -0.41046634 -0.28164156]]
| 20 | 1.6626656384995486e-05 | [[ 0.52509131 0.25544776 -0.41047195 -0.2816487 ]]
21 | 9.967475099843376e-06 | [[ 0.52509847 0.25545206 -0.41047531 -0.28165298]]
22 | 5.975378185666305e-06 | [[ 0.52510275 0.25545465 -0.41047733 -0.28165555]]
23 | 3.582165403429045e-06 | [[ 0.52510532 0.2554562 -0.41047854 -0.28165709]]
24 | 2.1474639059772973e-06 | [[0.52510686 0.25545713 -0.41047926 -0.28165801]]
| 25 | 1.2873780821539104e-06 | [[ 0.52510779 0.25545768 -0.4104797 -0.28165856]]
26 | 7.717672562045895e-07 | [[ 0.52510834 0.25545802 -0.41047996 -0.28165889]]
27 | 4.626649358021458e-07 | [[ 0.52510867 0.25545822 -0.41048012 -0.28165909]]
28 | 2.7736191328926196e-07 | [[ 0.52510887 0.25545834 -0.41048021 -0.28165921]]
29 | 1.6627504048509075e-07 | [[ 0.52510899 0.25545841 -0.41048027 -0.28165928]]
30 | 9.96798326917106e-08 | [[ 0.52510906 0.25545845 -0.4104803 -0.28165932]]
```

## SOR (relajación):

T:

```
[ 0.0483871 -0.53629032 -0.29032258 -0.66532258]
[-0.02358871 0.26144153 -0.35846774 0.73684476]
[ 0.33554435 -0.10228327 0.03673387 0.52751512]]
C:
[[ 0.375 ]
[ 0.06048387]
[-0.40448589]
[-0.26806956]]
radio espectral:
0.6312081938144991
| Iter | E |
3 | 0.14532732350431174 | [[ 0.59014422 0.23522845 -0.39033638 -0.30859371]]
| 4 | 0.10981562792867332 | [[ 0.51530648 0.28152633 -0.4443708 -0.27123634]]
| 5 | 0.0736017944866153 | [[ 0.52806002 0.24390875 -0.38360511 -0.28336154]]
| 6 | 0.04309603460965154 | [[ 0.52121751 0.25512531 -0.42445767 -0.27939858]]
7 | 0.021289186893738724 | [[ 0.52438664 0.25800267 -0.40379938 -0.28225196]]
| 8 | 0.01074325590162919 | [[ 0.52709114 0.25251377 -0.41262971 -0.28222923]]
9 | 0.006899037365800104 | [[ 0.52365497 0.25813679 -0.41094639 -0.2810727 ]]
| 11 | 0.004227797073687221 | [[ 0.52444102 0.25638029 -0.41179033 -0.28131836]]
| 12 | 0.0028492851107941534 | [[ 0.52540526 0.25508527 -0.40950273 -0.28184609]]
| 13 | 0.0016903257881472752 | [[ 0.5250312  0.2555134  -0.41107293  -0.28158444]]
| 15 | 0.00043631641904563805 | [[ 0.52517067 0.25533652 -0.41056857 -0.28167376]]
| 16 | 0.000269869947242065 | [[ 0.52504884 0.25556209 -0.41049266 -0.2816371 ]]
```

```
| 18 | 0.00016665347467758126 | [[ 0.52508303 0.2554967 -0.41053169 -0.28164601]]
| 19 | 0.00011384964936981007 | [[ 0.52512151 0.25544277 -0.41044149 -0.28166689]]
| 20 | 6.816800086131088e-05 | [[ 0.52510554 0.25546126 -0.41050422 -0.28165617]]
21 | 3.5926281401066357e-05 | [[ 0.52510839 0.25546165 -0.41046862 -0.28166007]]
22 | 1.771948170711931e-05 | [[ 0.5251115  0.25545384 -0.41048422 -0.2816599 ]]
23 | 1.0644413450872444e-05 | [[ 0.52510682 0.2554626 -0.41048062 -0.28165854]]
24 | 8.426539811643612e-06 | [[0.52511092 0.25545573 -0.41047851 -0.28166015]]
| 25 | 6.571070997423744e-06 | [[ 0.52510811 0.25546007 -0.41048235 -0.28165885]]
| 26 | 4.5378254339767775e-06 | [[ 0.52510968 0.25545785 -0.41047881 -0.28165969]]
27 | 2.7470507661039295e-06 | [[ 0.52510901 0.25545865 -0.41048131 -0.28165925]]
28 | 1.4620350791622568e-06 | [[0.52510915 0.25545862 -0.41047987 -0.28165942]]
| 29 | 7.20197106090464e-07 | [[ 0.52510926 0.25545834 -0.41048052 -0.28165941]]
| 30 | 4.207385047981539e-07 | [[ 0.52510908 0.25545868 -0.41048035 -0.28165936]]
| 31 | 3.293454914862184e-07 | [[ 0.52510924 0.2554584 -0.41048028 -0.28165942]]
| 32 | 2.588757888007562e-07 | [[ 0.52510913 0.25545858 -0.41048043 -0.28165937]]
| 33 | 1.807148320424063e-07 | [[ 0.52510919 0.25545849 -0.41048029 -0.2816594 ]]
| 34 | 1.1059753951318346e-07 | [[ 0.52510916 0.25545852 -0.41048039 -0.28165938]]
| 35 | 5.945865338657106e-08 | [[ 0.52510917 0.25545852 -0.41048033 -0.28165939]]
```

#### Vandermonde:

Matriz de Vandermonde:

```
[[-1. 1. -1. 1.]
[ 0. 0. 0. 1.]
[27. 9. 3. 1.]
[64. 16. 4. 1.]]
```

Coeficientes del polinomio:

```
[-1.14166667 5.825 -5.53333333 3.
```

#### Polinomio:

 $-1.1416666666666666x^3 + 5.824999999999999x^2 + -5.5333333333332x^1 + 3.0x^0$ 

### **Newton:**

Tabla de diferencias divididas:

Coeficientes del polinomio de Newton:

Polinomio:

$$(15.5) + (-12.5)(x - (-1)) + (3.54166666666666666)(x - (-1))(x - (0)) + (-1.14166666666666)(x - (-1))(x - (0))(x - (3))$$

### Lagrange:

Polinomios interpolantes de Lagrange:

Polinomio

```
15.5*L0+3*L1+8*L2+1*L3
```

Polinomio extendido:

#### **Trazadores lineales:**

Coeficientes de los trazadores:

-12.5 3.0

-7.0 29.0

Trazadores:

-12.5x + 3.0

1.66666666666667x + 3.0

-7.0x + 29.0

### Trazadores cuadráticos:

Coeficientes de los trazadores:

0.0 -12.5 3.0000000000000004

4.722222222222 -12.5 3.00000000000000004

-22.83333333333335 152.83333333333 -244.9999999999999

Trazadores:

 $0.0x^2 + -12.5x + 3.00000000000000004$ 

 $4.722222222222222x^2 + -12.5x + 3.00000000000000004$ 

## **Trazadores cúbicos:**

#### Coeficientes de los trazadores:

2.53333333333333 7.6 -7.4333333333333345 3.0

-1.5222222222223 7.6 -7.4333333333333333 3.0

 $2.033333333333334 \quad -24.400000000000006 \quad 88.566666666666 \quad -93.0000000000001$ 

#### Trazadores:

 $-1.522222222222213x^3 + 7.6x^2 + -7.43333333333333345x + 3.0$ 

 $2.03333333333333334x^3 + -24.400000000000006x^2 + 88.56666666666668x + -93.00000000000001$