

$$3) B_2 = \{2, x-1\}$$

$$D_4 = \{(-1, -1), (0, 0), (1, 1), (2, 8)\}$$

$$y = f(x) = mx + b$$

$$f(-1) = -m + b = -1$$

$$f(0) = b = 0$$

$$f(1) = m + b = 1$$

$$f(2) = 2m + b = 8$$

$$\Rightarrow \underbrace{\begin{bmatrix} -1 & 1 \\ 0 & 1 \\ 1 & 1 \\ 2 & 1 \end{bmatrix}}_A \underbrace{\begin{bmatrix} m \\ b \end{bmatrix}}_x = \underbrace{\begin{bmatrix} -1 \\ 0 \\ 1 \\ 8 \end{bmatrix}}_B$$

$Ax = B$ has NO solution.

Least squares:

x^*

$$A^T A x^* = A^T B$$

$$A^T = \begin{bmatrix} -1 & 0 & 1 & 2 \\ 1 & 1 & 1 & 1 \end{bmatrix}$$

$$\begin{bmatrix} -1 & 0 & 1 & 2 \\ 1 & 1 & 1 & 1 \end{bmatrix} \cdot \begin{bmatrix} -1 \\ 0 \\ 1 \\ 2 \end{bmatrix} = \begin{bmatrix} -1 & 0 & 1 & 2 \\ 1 & 1 & 1 & 1 \end{bmatrix} \begin{bmatrix} -1 \\ 0 \\ 1 \\ 8 \end{bmatrix}$$

$$\begin{bmatrix} 6 & 2 \\ 2 & 4 \end{bmatrix} x^* = \begin{bmatrix} 18 \\ 8 \end{bmatrix}$$

$$= \begin{bmatrix} 6 & 2 \\ 2 & 4 \end{bmatrix} \begin{bmatrix} m^* \\ b^* \end{bmatrix} = \begin{bmatrix} 18 \\ 8 \end{bmatrix}$$

$$\left[\begin{array}{cc|c} 6 & 2 & 18 \\ 2 & 4 & 8 \end{array} \right] \Rightarrow \left[\begin{array}{cc|c} 1 & 0 & 14/5 \\ 0 & 1 & 3/5 \end{array} \right] \quad \begin{array}{l} m^* = 14/5 \\ b^* = 3/5 \end{array}$$

$$x^* = \begin{bmatrix} 14/5 \\ 3/5 \end{bmatrix} \Rightarrow \boxed{y = 14/5 x + 3/5}$$