COMP 6721 Applied Artificial Intelligence (Fall 2023)

Lab Exercise #4: Naïve Bayes Classification

Question 1 Assume Jim is foraging for wild mushrooms and decides to use the mobile AI app "MushDoom" to help identify his findings. After scanning a mushroom, the app categorizes them as Premium Grade, Standard Grade, or Caution Advised. The app has the following accuracy rates based on its database and algorithms: 25% of the mushrooms it scans are labeled as Premium Grade, 50% are labeled as Standard Grade, and 25% are labeled as Caution Advised.

However, based on historical data and user feedback, mushrooms labeled as *Premium Grade* by the app have a 5% chance of being poisonous, a mushroom labeled as *Standard Grade* has a 15% chance of being poisonous, and a mushroom labeled as *Caution Advised* has a 25% chance.

If Jim consumes a mushroom identified by the app and falls ill from poisoning:

- (a) What is the probability that the app had labeled the mushroom as *Premium Grade*?
- (b) What is the probability that the app had labeled the mushroom as *Standard Grade*?
- (c) What is the probability that the app had labeled the mushroom as Caution Advised?

Question 2 Assume that Cecilia receives many e-mails from her home town in Klinga, where people speak Klinish. If you do not know Klinish, don't worry. It is a simple language made up of only 1,000 words that all start with the letter "k". A Klinish document may also contain words that do not start with "k", but these are considered out-of-vocabulary words (like a proper name, for example). Jack is trying to help Cecilia sort her Inbox into 3 mail folders (Personal, Work and Promotion). However, Jack does not speak Klinish, so all he has to work from are old e-mails that Cecilia has already sorted into the right folders. The table below shows a sample of the data that Jack has gathered from Cecilia's previous e-mails. The table indicates the frequency of each Klinish word in each folder (to be complete, the table should contain 1,000 rows, corresponding to each word in Klinish). For example, the word kiki appeared 30 times in e-mails labelled Personal, 50 times in e-mails about Work, and 9 times in Promotion e-mails.

		Folder		
		Personal	Work	Promotion
Word	kami	45	12	17
	kawa	78	1	67
	keke	0	5	80
	kiki	30	50	9
	koko	6	10	10
	kotuku	5	27	20
	koula	17	56	3
Total Nb of Words		20,000	25,000	17,000

The table above corresponds to data collected from 50 e-mails labeled *Personal*, 65 e-mails labeled *Work* and 45 e-mails labeled *Promotion*.

Based on the data above, Jack is trying to classify the following two e-mails (note that upper and lower cases should not be distinguished):

Email 1:	Koko kami kawa koula keke
Email 2:	Keke kawa, koko Google koula keke!

- (a) Use a Naïve Bayes classifier without any smoothing, to classify the two e-mails above. Use the sum of logs (base 10), and show the score of each of the 3 classes (Personal, Work and Promotion) and the most likely class.
- (b) Do the same as part A above, but this time use "add 0.5 smoothing" (i.e., instead of adding the value 1 to each word frequency, add $\frac{1}{2}$ to each word

frequency). Adjust the smoothing formula accordingly, and show all your work. Again, use the sum of logs (base 10), and show the score of each of the 3 classes and the most likely class.

Question 3 Let's write a *Python* program to train and run a model using the *Multinomial Naïve Bayes Classifier*. You can use the MNB implementation provided by *scikit-learn*, a popular machine learning library for Python.¹

Let's first check if scikit-learn is already installed and if not, install it:

• Activate your desired Anaconda environment (use comp6721 for the environment created in the first lab):

```
conda activate your_environment_name
```

• Check if scikit-learn is already installed:

```
python -c "import sklearn; print(sklearn.__version__)"
```

If this command returns a version number, it means scikit-learn is already installed. If it raises an error, continue with the installation steps below.

• Install scikit-learn:

```
conda install scikit-learn
```

Here's how to get started with Naïve Bayes in scikit-learn:

```
import numpy as np
from sklearn.naive_bayes import MultinomialNB
from sklearn.feature_extraction.text import CountVectorizer
```

Start by implementing the *Email Spam Classifier* you've worked through on Worksheet #3. Create the training data:

```
corpus = np.array([
    'cheap meds for sale',
    'click here for the best meds',
    'book your trip',
    'cheap book sale, not meds',
    'here is the book for you'
])
```

To transform the text corpus into a feature vector, you can use scikit-learn's CountVectorizer:

```
vectorizer = CountVectorizer()
X = vectorizer.fit_transform(corpus)
```

You also need the target vector with the labels for the training data (here, SPAM is 0 and HAM is 1):

 $^{^1\}mathrm{See}$ <code>https://scikit-learn.org/stable/modules/generated/sklearn.naive_bayes.MultinomialNB.html</code>

 $^{^2} See \qquad \text{https://scikit-learn.org/stable/modules/generated/sklearn.feature_extraction.text.} \\ \text{CountVectorizer.html}$

```
y = np.array([0,0,0,1,1])
```

Get a classifier using the prior probabilities for each class (0.6 for SPAM, 0.4 for HAM):

```
classifier = MultinomialNB(class_prior=[0.6, 0.4])
```

Train a model using your classifier:

```
model = classifier.fit(X, y)
```

Now you can try to apply your model to classify a new email as SPAM or HAM. Here is the example email ('the cheap book') as a feature vector:

```
new_mail = [[0, 1, 1, 0, 0, 0, 0, 0, 0, 0, 1, 0, 0, 0]]
```

- (a) Create a complete, working Python program. Print out the intermediate variables to see the data you are working with. Predict the class for the new_mail using your model and print it out.
- (b) Inspect the scikit-learn documentation to understand how *smoothing* is handled for this algorithm.
- (c) Change the code to transform the new_mail automatically from a string into a feature vector.
- (d) Change the code to automatically compute the prior probabilities using the training data. Print out the priors for the model to verify that they are indeed correct.