

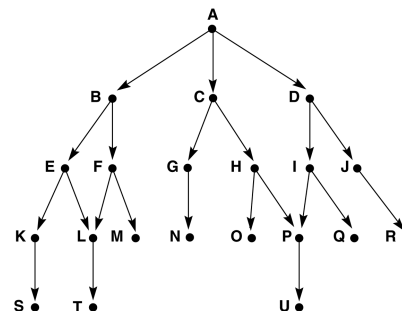
COMP 6721 Applied Artificial Intelligence (Fall 2023)

Worksheet #1: Solving Problems by Searching

This is an active learning exercise; we'll work on it during the lecture in teams of two!

Breadth-First Search. Let's apply the BFS algorithm discussed in the lecture on an example:

```
begin
  open := [Start];           % initialize
  closed := [];              % states remain
  while open ≠ [] do
    begin
      remove leftmost state from open, call it X;
      if X is a goal then return SUCCESS % goal found
      else begin
        generate children of X;
        put X on closed;
        discard children of X if already on open or closed; % loop check
        put remaining children on right end of open % queue
      end
    end
  end
  return FAIL
end.                          % no states left
```



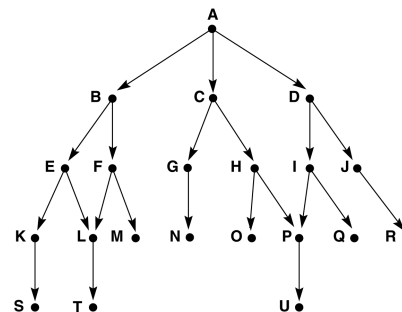
Assume **U** is the **goal state**. Note that **open** is a **queue**:

1. open = [A_{null}], closed = []
2. open = [B_A C_A D_A], closed = [A]
3. open = [C_A D_A E_B F_B], closed = [B A]
4. open = [_____], closed = [_____]
5. open = [_____], closed = [_____]
6. open = [_____], closed = [_____]
7. open = [_____], closed = [_____]

Depth-First Search. Now we do the same for the DFS algorithm:

Function depth_first_search algorithm

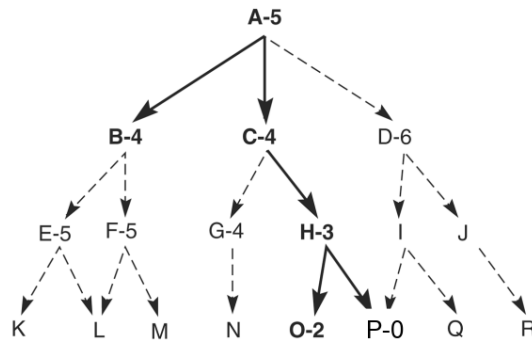
```
begin
  open := [Start];           % initialize
  closed := [];              % states remain
  while open ≠ [] do
    begin
      remove leftmost state from open, call it X;
      if X is a goal then return SUCCESS % goal found
      else begin
        generate children of X;
        put X on closed;
        discard children of X if already on open or closed; % loop check
        put remaining children on left end of open % stack
      end
    end
  end;
  return FAIL
end.                          % no states left
```



Again, assume **U** is the **goal state**. Note that **open** is a **stack**:

1. open = [A_{null}], closed = []
2. open = [B_A C_A D_A], closed = [A]
3. open = [E_B F_B C_A D_A], closed = [B A]
4. open = [K_E L_E F_B C_A D_A], closed = [E B A]
5. open = [S_K L_E F_B C_A D_A], closed = [K E B A]
6. open = [_____], closed = [_____]
7. open = [_____], closed = [_____]
8. open = [_____], closed = [_____]
9. open = [_____], closed = [_____]
10. open = [_____], closed = [_____]

Best-First Search. Next, we try a best-first (greedy) search. We have a heuristic $h(n)$ that estimates the cost for each path. The goal is **P**. At each step, expand the node with the *lowest* cost (as predicted by the heuristic), i.e., sort the open list by $h(n)$ (smallest first):



1. open = [A_{null}^5], closed = []
2. open = [B_A^4 C_A^4 D_A^6] (random choice), closed = [A]
3. open = [C_A^4 E_B^5 F_B^5 D_A^6], closed = [B A]
4. open = [.....], closed = [.....]
5. open = [.....], closed = [.....]
6. ???

Finally, extract the path to the solution from the search result:

Algorithm A. Compute the next step of the Algorithm A on the 8-puzzle:

1	2	3
8		4
7	6	5

Goal

where:

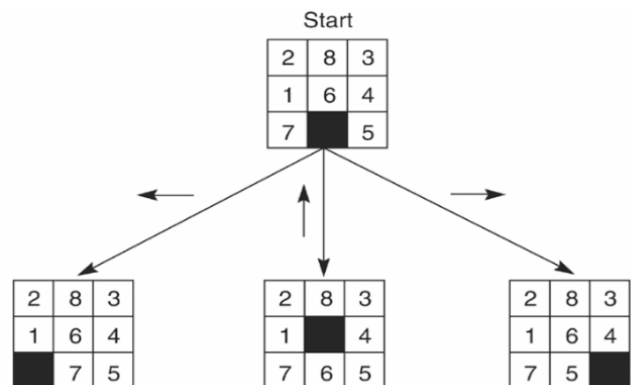
$$f(n) = g(n) + h(n),$$

$g(n)$ = actual distance from n
to the start state, and

$h(n)$ = number of tiles out of place.

$$g(n) = 0$$

$$g(n) = 1$$



Values of $f(n)$ for each state,

6

4

6

1. Pick the state with the *lowest* total cost $f(n)$
2. and compute the next possible search states, including the new values of $f(n)$, $g(n)$ and $h(n)$.