### Process Rate Estimator

A modeling side-hustle for the ETH group sustainable agroecosystems

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#### 1 Introduction

Denitrification is the natural process by which nitrate  $(NO_3^-)$  in the soil are converted by bacteria into nitrous oxide  $(N_2O)$  or pure nitrigen  $(N_2)$ . The latter is called *total denitrification* — the full process described in Equation 1 takes place.

$$NO_3^{-} \xrightarrow[\text{reductase}]{\text{NITrate}} NO_2^{-} \xrightarrow[\text{reductase}]{\text{NITrite}} NO \xrightarrow[\text{reductase}]{\text{NITrite oxide}} N_2O^{-} \xrightarrow[\text{reductase}]{\text{NITrous oxide}} N_2$$
 (1)

Denitrification occurs in conditions where oxygen is limited, such as waterlogged soils. It is part of the nitrogen cycle, where nitrogen is circulated between the atmosphere, organisms and the earth.

## 2 Formal model description

The diffusion fluxes between soil increments are described by Frick's law (Equation 2).

$$F_{\rm calc} = \frac{dC}{dZ} D_{\rm s} \rho \tag{2}$$

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Here,  $D_s$  is the gas diffusion coefficient,  $\rho$  is the gas density of N<sub>2</sub>O, and  $\frac{dC}{dZ}$  is the N<sub>2</sub>O concentration gradient from lower to upper depth.

The gas diffusion coefficient  $D_s$  was calculated according Equation 3 as established by Millington and Quirk (1961).

$$D_{\rm s} = \left(\frac{\theta_w^{\frac{10}{3}} + D_{\rm fw}}{H} + \theta_a^{\frac{10}{3}} \times D_{\rm fa}\right) \times \theta_T^{-2} \tag{3}$$

Here, H represents a dimensionless form of Henry's solubility constant (H') for  $N_2O$  in water at a given temperature. The constant H for  $N_2O$  is calculated as follows:

$$H = \frac{8.5470 \times 10^5 \times \exp{\frac{-2284}{T}}}{R \times T}$$
 (4)

Here, R is the gas constant, and T is the temperature (T = 298 K).

# References

Millington, RJ, and JP Quirk. 1961. "Permeability of Porous Solids." Transactions of the Faraday Society 57: 1200-1207.