Giving the leaves back to the forest*

A primer on the use of random forest models as chained equations for imputing missing data

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ABSTRACT Political scientists often struggle with decisions about what to do with incomplete cases for their regression analyses, and one can often make several decisions that influence one's ultimate substantive conclusions. In many areas of research outside of political science and the social sciences, scholars take advantage of an extension of multiple imputation, which offers the choice to leverage machine learning models for predicting values in missing data. This manuscript provides a summary of missing data and its consequences for our regression models along with providing an explanation of how to implement random forest models with an expanded form of the multiple imputation procedure, called multiple imputation with chained equation to handle complex causes for non-random missingness in our data. After providing a primer on standard missing data procedures in political science and random forest with multiple imputation with chained equations, I examine its performance on simulated data and data from the 2020 American National Election Study. I conclude by providing recommendations for dealing with missing data in practice.

KEYWORDS Missing data; Multiple imputation; Machine learning

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Introduction

Missing values are common in social science data. king_et-al_2001empty citation estimate that political scientists lose about one-third of their data in their complete case regression analyses due to missing data. There are many reasons why missing values arise in our data. In surveys, these are referred to as item-nonresponse and pose threats to obtaining unbiased estimates for public opinion research when researchers utilize listwise deletion (LWD) in their regression analyses (weisberg_2005); mainly when the researcher can predict the cause of the missingness with an observed cause - which scholars refer to the data as "missing at random" (king_et-al_2001).\frac{1}{2} More generally, missing values come about in other types of data due to the unit's (e.g., country, respondent, politician) attempt to obfuscate information, data collector error, or researcher error. When common and not from a stochastic data generating process (DGP), missing data pose threats to causal inference either through model identification with non-full rank matrices or through sample representativeness and the challenges that create claims about causal inference.

Unsurprisingly, several political scientists generate tools and learn from other fields to deal with these challenges due to the severity of the consequences for inference. There are four primary approaches that political scientists use in dealing with missing data: (1) listwise deletion or complete case analysis (LWD), (2) simple mean or median based imputation, (3) hot deck or regression-based imputation, or (4) multiple imputation (MI). Many of the most popular approaches to imputation carry assumptions that scholars have to satisfy. This manuscript aims to provide a primer to political scientists on the use of machine learning models in the Multiple Imputation with Chained Equations (MICE) framework - an extension of the familiar MI approach.

^{1.} Which is a common occurrence, more so than missingness caused entirely by random chance - which, if one meets this condition, gives unbiased estimates with LWD.

Machine learning with MICE is not a new approach. While a JSTOR search of Political Science journals reports a handful of articles that discuss this particular approach, it is certainly not widely used by political scientists nor has it received much accessible discussion of how it works.

As the present article discusses, MICE allows the researcher to choose various models to aid the imputation process. Selecting a model with its underlying assumptions provides many benefits for researchers in choosing a procedure that is most appropriate for their particular circumstances. Choosing models that allow for flexibility and models that do not have a number of restrictive assumptions benefit those unsure about the exact data-generating process of the missingness. The specific emphasis in this paper on using random forest models in MICE (RF-MICE) results from the strong preference of those who use machine learning models for predictive regressions to use random forest models due to their flexibility as a result of their fully non-parametric nature and for their performance under many different, and complex, circumstances. Fields like the biomedical sciences treat missing values as out-of-sample predictions that random forest models predict; they see the purpose of imputation as aligned with a task that random forest models are optimal. As other fields use this RF-MICE procedure, there are implementations in STATA, R, and Python. All of which are relatively easy in terms of knowledge to code in either of these languages (buuren goothuis-oudshoorn 2011). To be clear, this manuscript argues that we should not only consider using the MICE framework for imputation but also should consider using Random Forest models.

This manuscript compares the utility of random forest models in the MICE procedure for imputation to other common imputation tools used in political science. In doing this, the manuscript encourages political scientists to consider this procedure when faced with conditions where missing data are present, and the other common tools seem unsuitable. It is not to paint these models

as superior in absolute terms to other procedures for imputation. To do that is a waste of time given the variety of circumstances where some methodological tools are suitable in some circumstances and not for others. This manuscript provides a primer encouraging political scientists to consider this tool when faced with missing data and to give them enough background so they may be comfortable using it. Furthermore, the manuscript agrees with the common recommendation that practitioners should recognize the value of reducing one's dependence on a single procedure and contends that one must consider using multiple procedures to reduce the dependency of one's results on any given procedure. The replication code for the applied analysis accompanying this manuscript also demonstrates how to implement this procedure.

The next section reviews common approaches handling missing data that political scientists currently use. The next section describes machine learning and random forest models and links this to my claim of their utility for predicting missing data when used in the MICE procedure. I then move into applied examples where I examine the performance of these random forest models to other common approaches to dealing with missing data on simulated data and an applied example with the 2020 American National Election Study. I then discuss recommendations for when one should use the reigning popular techniques or the random forest application in the MICE procedure.

Types of missing data, imputation, and MI in Political Science MCAR, MAR, and MNAR

Missing data arise in different forms. Researchers describe missing data in three ways - often using somewhat unintuitive acronyms. The first form missing data takes is Missing Completely

At Random (MCAR). This means that the data generating process for the missingness is random - there are no observed or unobserved causes of missingness. The second form missing data takes is Missing At Random (MAR). In MAR, these data are missing due to some observed cause. Some argue that MAR is much more common given the state of how large most contemporary social science data sets are (schunk_2008). The third form that missing data take is Missing Not At Random (MNAR)². MNAR happens when observed and unobserved causes explain the missingness. What distinguishes MNAR from MAR is that the researcher does not have a clear path forward to handle the cause of missingness. This occurs either because the variable where there is missingness is, itself, a cause of the missingness, or data explaining the cause of missingness is unobserved by the researcher. Since missing data take different forms, researchers use a few different approaches to deal with these challenges.

Dealing with missingness

At the time of writing, king_et-al_2001empty citation estimated that 94% of political scientists use LWD to deal with missing data. In short, LWD does not seek to impute missing values. Instead, if the DV or any of the covariates in a regression model for a given observation are missing, the researcher does not include that observation in the analysis. Traditionally, scholars argue that LWD performs best (in terms of reducing the resulting bias in the researcher's subsequent regression models) when the data are MCAR.

If the data are MAR or MNAR, deleting observations with missing data introduces bias in one's regression estimates through a failure to account for correlation between the independent variable(s) and the error (king_et-al_2001). Furthermore, it has the potential to decrease

^{2.} Sometimes called Non-ignorable (NI).

statistical power. A meta-analysis of comparative and international political economy papers that use LWD demonstrates that political scientists have much, upwards of 50%, more Type I error - an incorrect rejection of the null hypothesis - than we would expect as a result of how we implement LWD (lall_2016). To visualize this, we can draw a directed acyclic graph; Figure 1

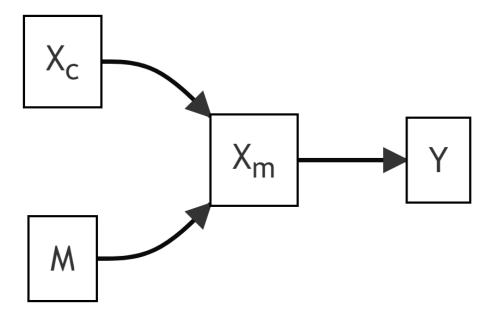


Figure 1: MAR data as confound

Others push against this claim and instead argue that LWD does not inherently generate bias for non-MCAR data but that researchers neglect to control for the cause of MAR or MNAR (arel-bundock_pelc_2018). This is still dependent on the researcher's grasp of theory and ability to identify the DGP leading to the missingness. Though the onus is on the researcher to do this, it is often a relatively high standard given the complexity to which social phenomena relate and the tendency for our datasets to be highly-dimensional. Furthermore, this also increases

the number of parameters one must include in their statistical models - which runs the risk of increasing collinearity (schrodt_2014_jorp).

Like LWD, simple imputation techniques like mean-and-median-based imputation do not reduce the chances of biased regression estimates. These approaches, called interpolation and extrapolation, are common for panel data and cross-sectional time series data. If you have missing data for an observation in one panel, you can take the same observations' responses in a previous panel and a latter panel. You then take the mean or the median of that particular observation for that variable. Other approaches seek to reduce this MAR-based bias through conditioning on other variables.

Hot Deck approaches to imputing missingness are regression-based in that they define the dependent variable as the one the researcher is attempting to impute and use variables thought to predict the cause of missingness in MAR contexts (schunk_2008). In this approach, you often use a few variables to condition on. In many cases, the precise mechanism generating missingness is often tricky to triangulate. As a result, if you fail to provide the correct model specification when the data are MAR, you often end up with biased regression estimates.

MI seeks to solve this issue by using the entire dataset for imputing missing values (rubin_1996). This approach uses the other variables in the dataset to generate a joint posterior distribution of all possible missing values for that particular observation. Many assume that most social science data sets are sufficiently large enough to condition on the mechanism generating MAR (schunk_2008). Unlike the other approaches, MI also generates uncertainty around the imputed values - via its construction of the joint posterior distribution (rubin_1996) - which enables the researcher to be more transparent about the validity of those imputed values and to include that uncertainty in the researcher's subsequent statistical analyses

(king_et-al_2001). A prevalent implementation of MI in political science is Honaker, King, and Blackwell's honaker_et-al_2011empty citation] AMELIA II software (lall_2016). This useful tool provides a computationally fast and simple process for imputation. Compared to the other approaches to missing data, AMELIA II performs quite well (honaker_et-al_2011). MI, however, often requires a set of distributional assumptions for the joint distribution - often the multivariate normal (honaker_et-al_2011).

There is a variant to MI that seeks more computational efficiency and loosens some of the distributional assumptions required. This variant is called Multiple Imputation through Chained Equations (MICE). MICE performs quite well for large imputation tasks. MI struggles to impute values when there is missingness in the other variables of the dataset (kropko_et-al_2014) - which is quite common. Though not reliant on a multivariate normal distribution, Conditional MI still relies on generalized linear models (GLM) in calculating the values. MICE tries to get around this limitation in a few steps, as described by azur_et-al_2011empty citation. Figure 2 provides a visual representation of the procedure for a form of MICE used in this manuscript. I include more details about random forest models in the following subsection.

First, MICE performs a simple imputation, or interpolation, for every missing value in the entire dataset. These are the placeholder values. The second step in the general MICE paradigm involves identifying one variable to impute. Once complete, it then removes those placeholder values. The third step then involves regressing the observed values of the variable on the other variables in the model and replacing the predicted values generated from the regression model for the missing values. The fourth step is to repeat steps two and three for each variable in the data set with missing values - this constitutes a single iteration. As a fifth step, you perform between five and

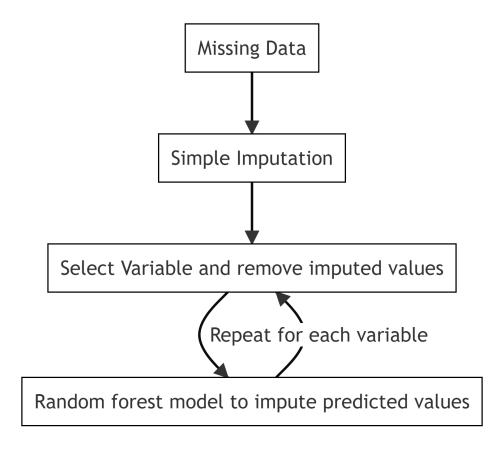


Figure 2: Steps of RF-MICE procedure

ten iterations³.

The advantage of this chained equation procedure is to estimate each variable as an outcome with its own regression model that is most appropriate for it. The regression models that one may use in MICE are as numerous as those a researcher may choose from when engaged in statistical analysis. This means that the assumptions and the performance of the model one uses for the imputation are the same as in standard statistical analyses. Though it decreases some of the requirements for modeling the MAR process, it is not entirely atheoretical. We can, however, reduce the dependence that the imputed data have on a researcher's ability to theorize about the MAR process by selecting models that are accustomed to dealing with a large number of parameters without increasing inefficiency.

One valuable model for allowing one to include a large number of parameters without losses to efficiency, is a form of ensemble machine learning model called Random Forests. As the following discussion highlights, random forest models are optimal for engaging in predictive tasks, which appears appropriate for the task of predicting missing values. These models have the additional benefit of not requiring a multivariate normal distribution, not requiring one to specify a potentially incorrect model of which variables are included in the MAR process, nor is it in the form of a Generalized Linear Model (GLM). That is, these models reduce some of the dependence of an imputation task on the researcher's beliefs about the source of the missingness. As researchers apply these random forest models within the MICE framework, they also benefit from the advantages that MI provide over the hot deck framework. These two features suggest that this procedure offers much more flexibility to the researcher.

^{3.} Though, the exact number of recommended iterations used in MICE are still up for debate (buuren_goothuis-oudshoorn_2011). The recommendation is that you elect to go with more iterations if not constrained by computational limitations.

The utility of random forest models for imputing political

science data

Random forest models are concerned with calculating a fixed out-of-sample prediction under the supervised machine learning framework. They are popular among data scientists and researchers primarily interested in providing predictions instead of engaging in causal inference. In non-imputation applications of supervised machine learning models - a broader category of machine learning models that includes random forests, these models take partial, observed information about an outcome and estimate the relationship between the units with observed outcomes and several other observed features for those units. Then for the units without an observed outcome, we generalize that relationship to predict an outcome for them.

To get an intuition of the fundamental goal of a supervised machine learning model, I will provide an example. If we are looking to sort beans into a good or bad pile before we toss them into a pot, we often want to collect information about them. Features like color, size, and plumpness can all be good indicators of whether a bean will taste good or bad. Say we have over 5,000 beans, and we are a chef at a restaurant approaching the dinner hour, and we do not have time to sort all these beans. To save time, we look at these features like color, size, and plumpness and make two piles - good or bad for a subset of our 5,000 beans; say, in this instance, about 25%. We then get one of our employees to sort the rest of the beans for us. This employee may know less than us about what features matter more and how to identify a bean that will taste good or bad. Nevertheless, they can look at the two piles we have already made and try to pick up on patterns that make good and bad beans different from one another. With this information, the employee can "learn" these patterns so that even without the same knowledge as the chef, they

can still make predictions about whether a bean will taste good or bad.

We have some units with recorded observations for a particular variable for imputation. Leveraging this, we can treat these documented observations as information so that we can "train" our computer to find a relationship between the observed information in that variable and information from other variables for that unit. We can then generalize this relationship to predict what that value would be for a missing unit. This seems like a reasonable approach to thinking about imputing missing values. We are not making naive imputations by taking the mean value. As we are using an expanded form of MI, we can also use all variables in the dataset to clarify that pattern. As a MICE procedure, we can specify a machine learning model, and we do this iteratively so that if we have more than one variable that we want to impute, we are not limited to accurate imputed values only for the units that are complete except for that particular variable to be imputed. I will elaborate more on how this works in a few paragraphs. Before we go there, however, I want to take the time to provide a few more details about how random forest models work, as they do not represent the whole of supervised machine learning.

Practitioners refer to random forests as tree-based ensemble models. As a supervised machine learning model, they start with the basic intuition described above; but in the process of "learning" or "training," these models follow a few distinct steps. Decision tree models split regions of the predictive space. For example, say we want to predict vote choice by one's partisanship. We would split the predictive space into regions. These regions could be different degrees of partisanship, like strong Republicans and weak Republicans. When we split this predictive space into regions, we essentially are subsetting our dataset of partisans into these different areas of the predictive space and trying to optimize a model to provide the best predictions in each region in our predictive space. That is, we try to find a model that maximizes the predictive performance of vote choice

for strong Republicans, weak Republicans, independents, and so on. We examine performance by comparing how well we are predicting the unobserved outcomes relative to the observed outcomes within those predictive regions. We can "bag" our trees. When we "bag" the decision trees, we bootstrap the training sample and build a tree for each bootstrapped sample and average across them. Doing this allows for a decrease in the variance of the predictions coming from the model, which helps with reducing the chances of generating a trained model that will fail to adequately generalize to our data set not included in the training step.

As this is a primer for the applied researcher, I note that this discussion simplifies decision trees and random forest models. For those interested in more details about these concepts, james_et-al_2013empty citation provide a helpful discussion of these concepts. The main point is that random forest models specialize in generating predictions by optimizing at the value and not the variable level. This characteristic suggests that these models have the potential to be powerful tools for many different applications.

We can discuss their applicability to imputation in the MICE framework with a foundation in how random forest models work. As random forest models specialize in generating fixed out-of-sample predictions, these models have a joint goal with multiple imputation in that it should not be evaluated on the model's correctness but on the model's ability to predict a fixed (true) value (rubin_1996). Here, one might think of missing data as the out-of-sample predictions intended to be estimated. With random forest models, you train the model on a training data set (often randomly generated through cross-validation), a randomly selected portion of your data that you train the model on, and then fit the model on the testing set, the remaining data not used for the training stage of your model (hastie_et-al_2009).

OLS models often perform relatively poorly on making out-of-sample predictions as they are

BLUE, assuming the data on hand are relatively representative of the population. As we have MAR data, this assumption likely fails, and any out-of-sample predictions are likely to be biased. Further, OLS may also generate out-of-bounds predictions for non-continuous data (long_1997) which is particularly troublesome in settings of prediction.

Other models provide within-bounds predictions, such as logistic models; however, as generalized linear models, they still assume a linear functional form and often produce biased interpretations of the likelihood function when presented with unobserved systematic processes [CITATION]. Though OLS and Logistic regression underlie a lot of machine learning as tools, many consider them to have limited applicability to complicated settings requiring prediction. Random forest models provide within-bounds predictions, and they are fully non-parametric (hastie_et-al_2009), meaning they do not assume a functional form and consequently a joint distribution. This means that we have more flexibility in terms of what variables we have in our datasets that we need to impute. As social scientists, we rarely have datasets that contain DGPs that fall neatly within the optimal realm for GLMs. This added flexibility by using MICE and random forests makes the researcher's job easier.

On other performance metrics, random forest models, as an ensemble method, provide much more accurate predictions than single-tree alternatives in machine learning, such as CART (montgomery_olivella_2018). As discussed above, rather than generating a single estimate from a single model, ensemble models, like random forests, calculate multiple models and learn from their performance; this is the purpose of using the bootstrapped samples.

In the context of using MICE, I argue that political scientists should *consider* using random forest models to make accurate predictions with fewer assumptions and be more lenient in terms of conditioning on the cause of MAR in the data set. Recall that within each MICE iteration,

one performs a model predicting (imputing) a missing value based on the other variables in the dataset. Explicitly, this means you are running a model per variable with missing data.

Given that random forests are non-parametric, within each MICE iteration, the relationship between the variable to be imputed and those used to make the predictions can be non-linear and can take many different multivariate distributional forms. This is a significant advancement on traditional MI, which assumes a multivariate normal distribution. Additionally, this is an advancement on other MICE models that political scientists use, which may not inherently conceptualize missing data as these unobserved values to predict from a generalized relationship of the observed variable with the other variables in the dataset. These relationships are also not assumed to be linear. Furthermore, using RF-MICE has the advantage over hot-deck procedures for those unsure about a variable's precise DGP for MAR.

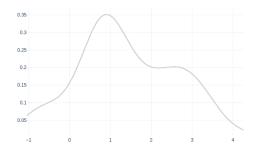
In the next section, I illustrate the use of random forest models for political scientists by demonstrating a simulated application of a random forest implementation of MICE. The following section also compares this implementation's performance to other common approaches to handling missing data in political science in terms of our ability to reduce unobserved bias in our data and in computational costs. # Application of MICE with random forests

Using the numpy library (Harris et al. 2020), I simulate a population where N = 1000000. The population has 5 variables with the DGP's presented in Equation 1.

$$\begin{split} a_i &= Gamma(2,2) \\ b_i &= Binomial(1,0.6) \\ x_i &= 0.2 \times a_i + 0.5 \times b_i + Normal(0,1) \\ z_i &= 0.9 \times a_i \times b_i + Normal(0,1) \\ y_i &= 0.6 \times x_i + 0.9 \times z_i + Normal(0,1) \end{split} \tag{1}$$

I then use the polars library (polars) to generate 1000 random samples from the population with n = 100 for each sample. To introduce missingness into my data, I use the miceforest library (miceforest) to "ampute" 40% of the data for each of these samples with a MAR process. As one of the advantages of the RF-MICE procedure is to impute data generated from more complicated MAR processes, I ampute the data by constructing a logistic regression for each variable. Where the predicted value equals one, the corresponding observation is counted as missing (miceforest). For the reader, Figure 9 presents the distributions of data for the X, Z, and Y variables for my samples before amputation as well as the distribution of data for the X, Z, and Y variables for my samples after amputation.

With these amputed datasets, I then apply some of the procedures I have discussed to impute these values. Interpolation is a quite simple procedure where I can fill in missing values by using the mean value of that particular variable for the non-missing observations. I perform this interpolation with the mice package (van Buuren and Groothuis-Oudshoorn 2011) and iterate over it to provide 10 datasets. I also use the AMELIA II package (honaker_et-al_2011) to perform standard MI and also store 10 datasets from the iterations. I use a standard Bayesian linear model in the MICE framework with the mice package (van Buuren and Groothuis-Oudshoorn 2011). Bayesian linear models with uniform distributions or a weak prior distribution are similar



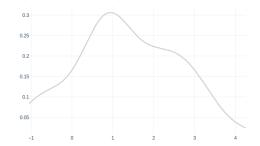
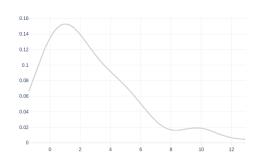


Figure 3: X

Figure 4: X - amputed



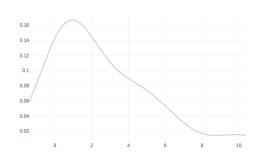


Figure 5: Z

Figure 6: Z - amputed

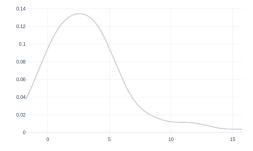




Figure 7: Y

Figure 8: Y - amputed

Figure 9: Distributions of simulated data

to the familiar Ordinary Least Squares (gelman_et-al_2021). As discussed before, the final procedure I use is a random forest in the MICE framework. I perform the RF-MICE procedure using the mice package (van Buuren and Groothuis-Oudshoorn 2011) and an alternative package miceRanger (Wilson 2021).

When producing the imputed datasets, I use the tictoc package to record the amount of time each procedure takes to complete the task on the 1000 samples as a measure of computational cost.⁴ As a number of factors may affect the absolute computational costs for these procedures (e.g., hardware, whether other applications or software are running, whether one uses parallelization, etcetera), I am primarily going to focus on the relative computational costs of each procedure.

Each imputation procedure produced m=10 datasets per simulated dataset, s=1000. I have a total of $s \times m$ datasets. For each s dataset, I took the difference of each m dataset from the complete dataset and took the average of these differences to give me a mean score of the discrepancy for each s dataset. **?@fig-discrepancy** represents these mean discrepancy scores for the three variables that were originally imputed.

Overall, we see that the procedures yield somewhat small differences between the actual and estimated values. For Y, AMELIA II has a mean discrepancy of -0.309, the Linear MICE procedure has a mean discrepancy of -0.198, the interpolation procedure has a mean discrepancy of 0.039, and RF-MICE with the mice package has a mean discrepancy of -0.188 and a mean discrepancy of -0.233. For X, we see that the RF-MICE with the mice package has a mean discrepancy of -0.030 and -0.008 with the miceRanger package, interpolation has a mean discrepancy of -0.074, Linear

^{4.} It is important to note that these benchmarks are based on a computer running Pop_OS 22.04 LTS with 32.0 GB of memory, on a Intel i7-9700K processor at 3.60GHz with 8 cores using a NVIDIA GEForce RTX 2070 graphics card.

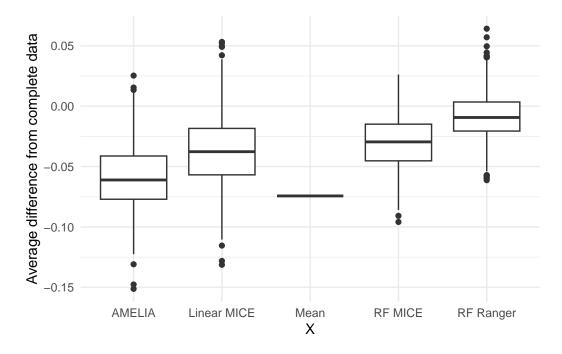


Figure 10: Discrepancies - X

MICE has a mean discrepancy of -0.038, and AMELIA has a mean discrepancy of -0.060. For Z, we also see that RF-MICE with the mice package has a mean discrepancy of -0.103 and -0.017 with the miceRanger package, interpolation has a mean discrepancy of -0.110, Linear MICE has a mean discrepancy of -0.106 and AMELIA II has a mean discrepancy of -0.199.

Though it is not a novel claim, I argue that in situations where we have missingness due to a MAR pattern, our regression models suffer from bias due to the systematic process generating that missingness. What I have argued so far is that we should consider using RF-MICE as it is, relative to other MI tools, a flexible tool that may be able to model a number of MAR processes which would help with reducing bias in our regression models.

To examine this claim, I take the amputed and imputed datasets (10) and use Rubin's rule to pool across the regression models performed on each amputed and imputed sample. In total, I fit

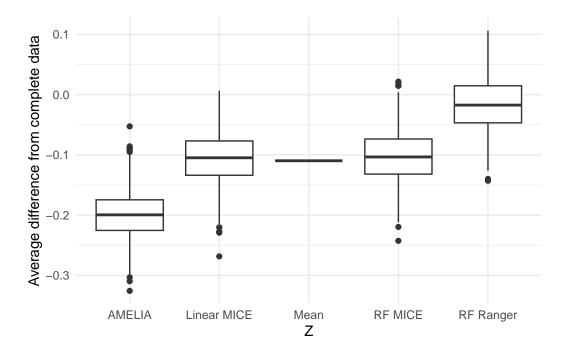


Figure 11: Discrepancies - Z

 $m \times s - 10 \times 1000$ regressions where I pool across my average posterior draws from m to produce a single set of statistics for each s. I calculate the discrepancy of the pooled average posterior draws for X and Z – the variables directly contributing to the DGP of Y – from their parameters. I then present boxplots that demonstrates the differences in levels of bias between LWD, Amelia, Linear MICE, and RF-MICE across my samples. The specification for the regression is depicted in e^{-10}

 $y_i Normal($

$$\mu_i = \alpha + \beta_1(x_i - \bar{x}) + \beta_2(z_i - \bar{z})\alpha = Uniform(-\infty, \infty)\beta_1 = Uniform(-\infty, \infty)\beta_2 = Uniform(-\infty, \infty)\sigma = Uniform(-\infty, \infty)\beta_2 =$$

For readers not familiar with this notation, ?@eq-regression essentially describes the familiar

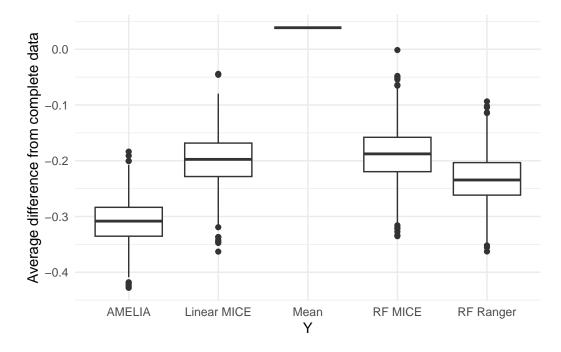


Figure 12: Discrepancies - Z

OLS regression. I fit a model where y_i is explained by my likelihood function, μ_i and I assume that my parameters in my model can take any real number value. That is, I am not imposing a constraint with my defined priors about how large or small my estimates of β_1 , β_2 , and α can be. σ depicts the variance, which I constrain to be positive.

Figure 13 and Figure 14 present the distribution of differences between my average posterior draw and of my parameter value for the β coefficient for X and for Z respectively. First looking at bias in the β estimates for X, I see that the median discrepancy caused by LWD is quite small (close to zero). However, in looking at the spread, there are a number of models that produced biased estimates. It appears that the only two procedures that had a median of no bias was Linear MICE and RF-MICE with the miceRanger package (miceranger). We see, that the spread of discrepancies is incredibly small when performing RF-MICE with the miceRanger package (miceranger).

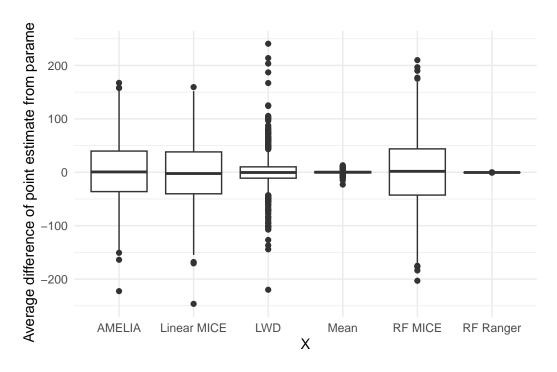


Figure 13: Average discrepancy scores - X

AMELIA performs quite well in terms of median levels of discrepancies, but still produces biased estimates on average, with some examples of extremely poor performance (in terms of bias). Turning to discrepancies between the β statistics and parameters for Z, we see a very similar story. LWD produces a distribution of discrepancies that is quite concerning while RF-MICE as implemented through the miceRanger package (miceranger) does quite well at reducing bias caused by the MAR process. AMELIA II also does quite well in reducing bias, on average, however can vary quite significantly in its ability to do so.

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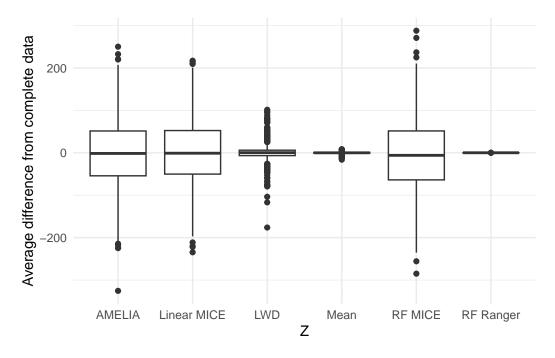


Figure 14: Average discrepancy scores - Z

Conclusions

In theory, RF-MICE is a quite flexible tool that can operate in a number of circumstances to not only discover systematic processes leading to missingness in one's data, but to also use such information to recover the values. These expectations rely on the claim that Random Forest models are optimized for discovering patterns and to use that information to make out-of-sample predictions. With RF-MICE Random forests are coupled with MICE to produce significant improvements at retrieving the true values when a MAR process is present.

Using simulated data, I demonstrate two implementations of RF-MICE in R and compare it to implementations of more common procedures for dealing with MAR processes in political science.

Overall, my simulated data and a number of measures of performance favor those theoretical

expectations.

When comparing the distribution of imputed samples to the true samples, as if the MAR process was not present, both RF-MICE implementations do quite well in recovering the true values that were missing. When examining the discrepancy between what the imputed value is and the true value, the two RF-MICE implementations provide quite small discrepancies on average.

Measuring the performance of RF-MICE in terms of reducing bias in statistical estimation, I find that RF-MICE, when implemented with the miceRanger package (miceranger), stands out as a valuable tool for researchers to use to reduce bias generated with MAR processes.

While in theory, it is nice for the applied researcher to hear about a new and powerful tool or procedure, they face many constraints. When examining how much time each implementation of a procedure took, I observed that both implementations of RF-MICE were not significantly worse in time it took to complete the procedure relative to other multiple imputation procedures.

Altogether, the simulated data suggest that RF-MICE is a valuable procedure for the applied researcher's toolbox. When dealing with missing data that one suspects may not be the result of a MCAR process, one should consider the flexibility that RF-MICE provides. It does not require the researcher to specify the variables involved in the MAR process, but also does not introduce significant computational costs nor introduce so much complexity as a procedure that it is impossible to anticipate or diagnose problems the procedure may introduce.

It is important to remind the reader that all tools have their limitations and that their value are quite dependent on the context for which they are to be applied. It is useful, however, to include tools that vary in the assumptions they make (neumayer_plumper_2017). The capabilities of RF-MICE are no different. While RF-MICE is quite flexible for addressing a number of MAR processes, it is important to note that it is not and should not be seen as a default or the sole tool for one to

use when dealing with missing data. With the number of tools and their implementations being so available to the applied researcher, one should not shy away from using multiple implementations of these tools to ensure that one's substantive conclusions are not dependent on one tool or implementation.

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