Practica_16 Casas_Mercade

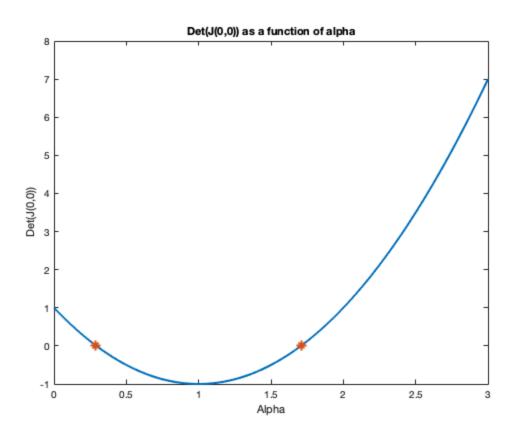
Table of Contents

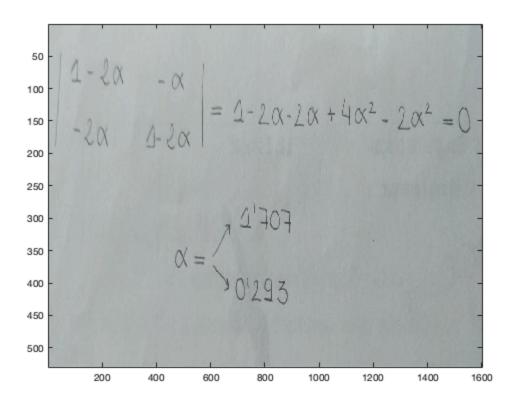
Section	A)	1
Section	B)	3
Section	C)	6
Section	C: Optional part	8

Section A)

```
clear all
close all
clc
determinants = [];
alphas = 0:0.01:3;
alphaZeros = [];
posicio = [];
figure(1)
i = 1;
for alpha = alphas
    f = @(phi)([tan(phi(1)) - alpha * (2 * sin(phi(1)) + sin(phi(2)));
 tan(phi(2)) - 2 * alpha * (sin(phi(1)) + sin(phi(2)))]);
    phi = [0, 0];
    j = jaco(f, phi);
    determinants = [determinants, det(j)];
    if abs(det(j)) < 0.01
        alphaZeros = [alphaZeros, alpha];
        posicio = [posicio i];
    end
    i = i + 1;
end
Det0 = [determinants(posicio(1)), determinants(posicio(2))];
plot(alphas, determinants, 'LineWidth', 2)
title('Det(J(0,0)) as a function of alpha')
xlabel('Alpha')
```

```
ylabel('Det(J(0,0))')
plot(alphaZeros, Det0, '*')
% The implicit function theorem (imft) states that as long as the
jacobian
% is non-singular (det non zero) the system will define phi(1) and
phi(2)
% as a unique functions of aplha, so we'll have a unique map between
% the solutions and alphas
% When the determinant is zero the uniqueness will be lost locally
nearby
% the aplha points which make the determinant 0 and new branches of
% solution may emerge.
disp('The alpha values that make zero the determinant are more less:')
disp(alphaZeros)
% Anallitically:
figure;
img = imread('analitic.jpeg');
image(img);
The alpha values that make zero the determinant are more less:
    0.2900
              1.7100
```

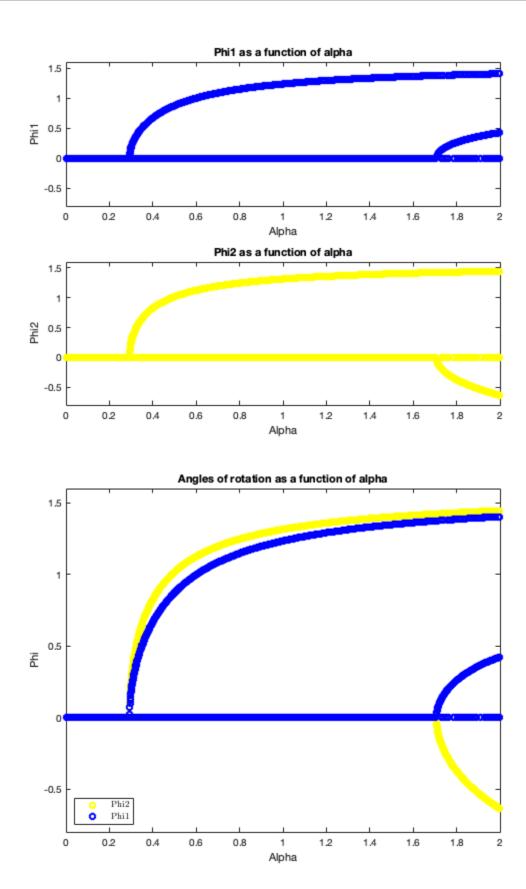




Section B)

```
x = 0.001;
alphas = 0:x:2;
% Dominis dels angles
dom1 = [0, pi / 2];
dom2 = [-pi / 2, pi / 2];
factor = [dom1(2); (dom2(1) - dom2(2))];
a = [dom1(1); dom2(1)];
aleatoryTimes = 1:20;
sol = [];
alphasol = [];
figure(2)
for alpha = alphas
    f = @(phi)([(tan(phi(1)) - alpha * (2 * sin(phi(1)) +
 sin(phi(2)))), (tan(phi(2)) - 2 * alpha * (sin(phi(1)) +
 sin(phi(2))))]);
    for i = aleatoryTimes
        aleatory = rand(2, 1);
        phi0 = aleatory .* factor - a;
        %Formula per canviar de escala i moure:
        x*(a-b) - a
```

```
[XK, resd, it] = newtonn(phi0, 1e-6, 100, f);
        % Comprobar que estigui dintre el domini
        if XK(1, end) > dom1(1) && XK(1, end) < dom1(2) && XK(2, end)
 > dom2(1) \&\& XK(2, end) < dom2(2)
            sol = [sol, XK(:, end)];
            alphasol = [alphasol, alpha];
        end
    end
end
subplot(2, 1, 1)
plot(alphasol, sol(1, :), 'o', 'Color', 'blue')
axis([0 2 -0.8 1.6])
title('Phil as a function of alpha')
xlabel('Alpha')
ylabel('Phi1')
subplot(2, 1, 2)
plot(alphasol, sol(2, :), 'o', 'Color', 'y');
axis([0 2 -0.8 1.6])
title('Phi2 as a function of alpha')
xlabel('Alpha')
ylabel('Phi2')
figure(3)
plot(alphasol, sol(2, :), 'o', 'Color', 'y');
hold on
plot(alphasol, sol(1, :), 'o', 'Color', 'blue')
axis([0 2 -0.8 1.6])
title('Angles of rotation as a function of alpha')
legend('Phi2', 'Phi1', 'Location', 'southwest', 'Interpreter', 'latex')
xlabel('Alpha')
ylabel('Phi')
hold off
```



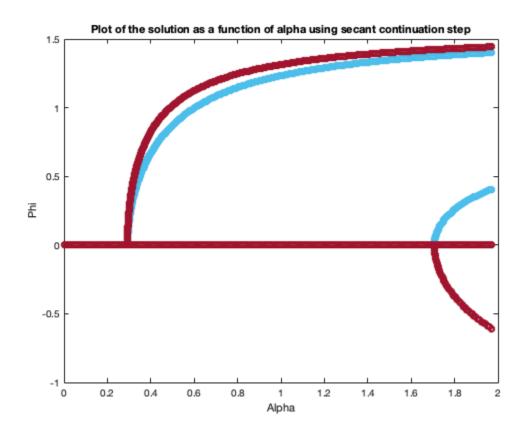
Section C)

```
%As it has been seen analitically there are two alpha's that make zero
%jacobian determinant, this alphas are 0.293 and 1.707, so the in
 order to
%obtand all the solutions with the secant continuation step we will
 take 3
%difrent y0 and y1 at the right plot of the previous exercise.
funAlpha = @(y)([tan(y(1)) - y(3) * (2 * sin(y(1)) + sin(y(2)));
 tan(y(2)) - 2 * y(3) * (sin(y(1)) + sin(y(2)))]);
figure(4)
epsilon = 0.01;
alphas = [2 - epsilon, 2 - 2 * epsilon]; %the two alpha points where
 the secant will start
MP = []; %Matrice where the 3 diffrent pair of solutions needed for
the secant will be saved.
dom1 = [0, pi / 2]; %domain of phi1
dom2 = [-pi / 2, pi / 2]; %domain of phi2
%As seen in the plot of the previous section for the two alpha chosen
to start de secant we'll
%have the 0 solution (trivial), two solution bigger than 0.6 and two
%below 0.6, we use that information to obtain them:
for jj = 1:2
    sol1 = 0; % Si es 0 es que falta trobarla:
    sol2 = 0;
    alpha = 2 - jj*epsilon;
    f = @(phi)([(tan(phi(1)) - alpha * (2 * sin(phi(1)) +
 sin(phi(2)))), (tan(phi(2)) - 2 * alpha * (sin(phi(1)) +
 sin(phi(2))));
    while sol1 == 0 || sol2 == 0
        aleatory = rand(2, 1);
        phi0 = aleatory .* factor - a;
        x*(a-b) - a
        [XK, resd, it] = newtonn(phi0, 1e-16, 100, f);
        % Comprobar que estiqui dintre el domini
        if XK(1, end) > dom1(1) && XK(1, end) < dom1(2) && XK(2, end)
 > dom2(1) \&\& XK(2, end) < dom2(2)
            % I a mes que no sigui 0:
            if XK(1, end) > epsilon | | XK(1, end) < (-0.001)% El blau
 sempre esta per sobre i nomes cal que comprobem aquest
                %Classificar si es de dalt o de sota
                if XK(1, end) > 0.6
                    MP(:, jj) = [XK(:, end); alpha];
```

```
sol1 = 1; % He trobat la solucio 1
                                               else
                                                          MP(:,jj+2) = [XK(:,end); alpha];
                                                          sol2 = 1;
                                               end
                                   end
                       end
            end
end
% We add the (0, 0) trivial solutions
MP(:,5) = [0; 0; 2-epsilon];
MP(:,6) = [0; 0; 2-2*epsilon];
disp('Initial values for the secant')
disp(MP)
s = 1; % In principle we will use s = 1 to mantain an approximate
  regular space between solutions.
% The distrance between solution will be given by the epsilon
  parameter
% defined before.
tol = 1e-6;
itmax = 100;
Y = [];
for it = 1:2:length(MP)% We launch the countinuation step at the 3
  branches of solutions found
           y0 = MP(:, it);
           y1 = MP(:, it + 1);
           y = y1;
           while y(3) < 2 \&\& y(3) > 0 \&\& s > 0
                       [y, iconv] = continuationStep(funAlpha, y0, y1, s, tol,
   itmax);
                    if iconv == 1 % No hem aconseguit soluciÃ3 i ajustem s
                                   s = s - 0.1; % Si la s arriba a 0 desistirem i no buscarem
  mes solucions
                       else
                                  y0 = y1;
                                  y1 = y;
                                   % Nomes les quardem si estan dintre el domini
                                   if y(1, end) >= dom1(1) && y(1, end) <= dom1(2) && y(2, end) <= dom1(2) && y
   end) >= dom2(1) \&\& y(2, end) <= dom2(2)
                                              Y = [Y, y]; %solucions
                                   end
                       end
                       plot(Y(end, :), Y(1:2, :), 'o');
                       hold on
            end
```

end

```
title('Plot of the solution as a function of alpha using secant
continuation step');
xlabel('Alpha')
ylabel('Phi')
hold off
Initial values for the secant
    1.4028
              1.4020
                        0.4171
                                   0.4114
                                                   0
                                                             0
    1.4444
              1.4438
                        -0.6281
                                  -0.6181
                                                   0
    1.9900
              1.9800
                         1.9900
                                   1.9800
                                             1.9900
                                                        1.9800
```



Section C: Optional part

Drawing of the pendulum at alfa = 2.14

```
%As we want the plot at a specific alpha we'll use the newton method
in
%order to explore and not the secant continuation step to find
solutions.

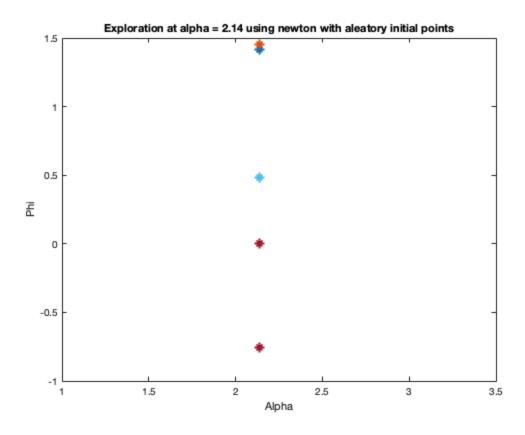
figure(5)
aleatoryTimes = 1:1:1000;
alpha = 2.14;
```

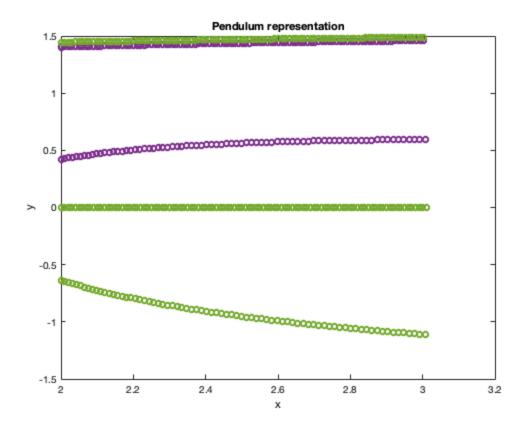
```
f = @(phi)([(tan(phi(1)) - alpha * (2 * sin(phi(1)) + sin(phi(2))))),
 (tan(phi(2)) - 2 * alpha * (sin(phi(1)) + sin(phi(2))))));
for i = aleatoryTimes
    aleatory = rand(2, 1);
    phi0 = aleatory .* factor - a;
    x*(a-b) - a
    [XK, resd, it] = newtonn(phi0, 1e-16, 100, f);
    if XK(1, end) >= dom1(1) && XK(1, end) <= dom1(2) && XK(2, end) >=
 dom2(1) \&\& XK(2, end) \le dom2(2)
            plot(alpha, XK(1, end), '*'); %phi1
            plot(alpha, XK(2,end), '*') %phi2
            hold on
    end
end
title('Exploration at alpha = 2.14 using newton with aleatory initial
points');
xlabel('Alpha')
ylabel('Phi')
hold off
% We change the direction at we launch the secant continuation step,
% go to the right
% We will get to alpha = 3;
maxAlfa = 3;
Y = [];
perDibuixar = [];
figure;
% Tirarem el continuation step en les 3 branques de solucions trobades
anteriorment:
for it = 1:2:length(MP)
    y1 = MP(:, it); % Per ferho cal canviar el sentit, ja que ara
 anirem cap a la dreta
    y0 = MP(:, it + 1);
    y = y0;
    sensePintar = 1;
    while y(3) < \max Alfa \&\& y(3) > 0 \&\& s > 0
        [y, iconv] = continuationStep(funAlpha, y0, y1, s, tol,
 itmax);
        if iconv == 1 % No hem aconsequit soluciÃ3 i ajustem s
            s = s - 0.1; % Si la s arriba a 0 desistirem i no buscarem
 mes solucions
        else
            y0 = y1;
            y1 = y;
            Y = [Y, y]; %solucions
            % When we found the pendulum we save the solutions to
 draw.
```

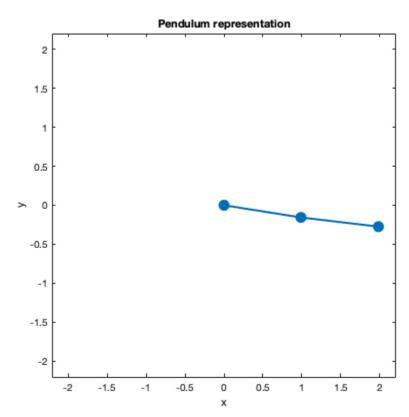
```
if abs(alpha-y(3)) < epsilon && sensePintar == 1</pre>
                perDibuixar = [perDibuixar, y];
                sensePintar = 0;
            end
        end
        plot(Y(end, :), Y(1:2, :), 'o');
        title('Exploration from alpha = 2.14 to alpha = 3 using secant
 continuation step');
        xlabel('Alpha')
        ylabel('Phi')
        hold on
    end
end
hold off
% Dibuixem els pendols:
for ii =perDibuixar
    figure;
    dibuixarPendul(ii(1), ii(2), 1);
    title('Pendulum representation')
    xlabel('x')
    ylabel('y')
    hold off
end
% Codes used:
응 {
function succes = dibuixarPendul(phi1, phi2, 1)
% Funcio que fa un plot de un pendul doble amb els angles indicats i
la longitud de les barres indicada (les dos igual)
% a entrar els angels respecte la vertical en radiants
h = plot(0, 0, 'MarkerSize', 30, 'Marker', '.', 'LineWidth', 2);
%Guardem el objecte plot en una variable per utilitzar les seves
propietats mes endavant
range = 1.1 * (1 + 1); axis([-range range -range range]); axis square;
set(gca, 'nextplot', 'replacechildren'); % Diem que en el seguent plot
es pinti a partir d'on acaba l'anterior:
Xcoord = [0, 1 * sin(phi1), 1 * sin(phi1) + 1 * sin(phi2)];
Ycoord = [0, -1 * cos(phi1), -1 * cos(phi1) - 1 * cos(phi2)];
set(h, 'XData', Xcoord, 'YData', Ycoord);
drawnow;
succes = 1;
function [y, iconv] = continuationStep(fun, y0, y1, s, tol, itmax)
```

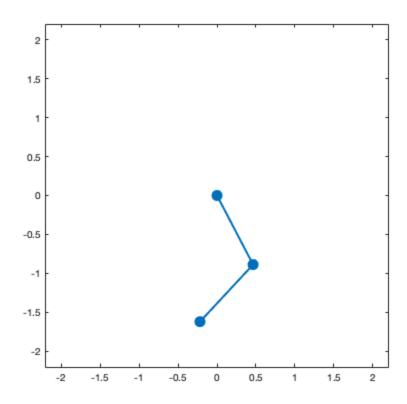
```
it = 1;
   tolk = 1;
   v = y1 - y0;
   yp = y1 + v * s; % Si s = 1 consequim que la separacii; ½ entre
 solucions sigui el maxim de "constant"
   xk = yp;
   XK = [];
   % A part de les ecuacions que teniem en el nnewton normal, li
    % imposareem que el preoducte escalar entre v i (xk(punt
   % buscat)- xk(predictor)) sigui 0
   while it < itmax && tolk > tol
        J = jaco(fun, xk); % Jacobia en la posicio anterior
       J = [J; v'];
       fk = [fun(xk); v' * (xk - yp)]; % TODO: Copiat de teoria
        [P, L, U] = PLU(J);
       Dx = pluSolve(L, U, P, -fk); %Solucio de la ecuacio J*Dx = -fk
       Dx = J fk;
       xk = xk + Dx;
       XK = [XK, xk];
       tolk = norm(Dx); % Mirem la distancia entre el anterior i
 l'actual
        it = it + 1;
   end
   y = xk;
   %Retornem si convergeix o no per modificar la s si cal:
   if it <= itmax && tolk < tol
        iconv = 0; %OK
   else
       iconv = 1; %No em arribat a enlloc
   end
end
function [XK, resd, it] = newtonn(x0, tol, itmax, fun)
    % Atencio, pirmer comprobara a a la carpeta actual si hi son
   xk = [x0];
   XK = [x0];
   resd = [norm(feval(fun, xk))];
   it = 1;
   tolk = 1;
   while it < itmax && tolk > tol
        J = jaco(fun, xk); % Jacobia en la posicio anterior
        fk = feval(fun, xk);
        %[P, L, U] = PLU(J);
        %Dx = pluSolve(L, U, P, (-fk)'); %Solucio de la ecuacio J*Dx =
 -fk
```

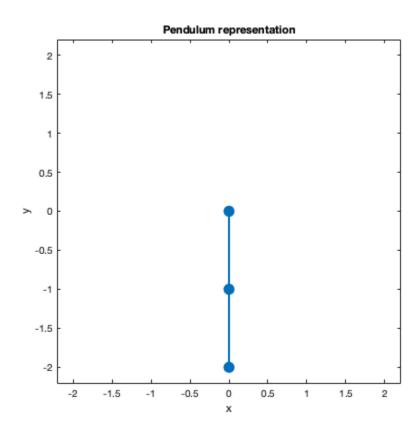
```
Dx = J \setminus (-fk)';
        xk = xk + Dx;
        XK = [XK, xk];
        resd = [resd, norm(fk)];
        tolk = norm(XK(:, end) - XK(:, end - 1));
        it = it + 1;
   end
응}
%As it can be seen, the solution to the right continue as
theoretically
%expected. We do not observe not new branches emerged using
continuationStep and
%neither using newton. This is because new branches appear when the
%jacobian's determinan is zero, and from 2,14 on it is always non
zero, as
%it has been proved in the graph in section A.
```











Published with MATLAB®	R2018b		