

Matrices and Vector Spaces

Conditions for a Vector Space

- (i) Vector set is closed under commutative and associative addition
- (ii) Vector set is closed under distributive and associative multiplication by a scalar
- (iii) Vector set contains a null vector
- (iv) Multiplication by unity leaves any vector unchanged
- (v) All vectors have a corresponding negative

Span of a vector space: The span of a vector space is defined as the set of all vectors that
can be expressed as a linear sum of the basis vectors:
$$\mathbf{x} = \alpha \mathbf{a} + \beta \mathbf{b} + \dots + \sigma \mathbf{s}$$

If \mathbf{x} is equal to $\mathbf{0}$ for some choice of $\alpha, \beta, \dots, \sigma$ then $\mathbf{a}, \mathbf{b}, \dots, \mathbf{s}$