COMP2208 - Search Methods Coursework

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1 Approach

My approach to this assignment was to first create support classes that would handle any details that didn't directly relate to the search algorithm itself. These are as follows:

1.1 Node

This class defines both a singular node in the tree structure, as well as the entire tree structure itself by means of its **parent** and **children** variables. It contains a single **Grid** object, the **value** variable. It also implements the Comparable interface, where it compares an optional **estimatedCost** variable - a feature that was specifically added for the A* Search algorithm.

1.2 Grid

A class that handles the state by means of manipulating a **char**[][] multidimensional array. This class stores the actual state of the problem, storing the location of the **agent** (\neg) and all of the non-white space blocks; it also allows for that state to be manipulated in a multitude of ways:

- Generates the start and solution state.
- Moves the agent in the grid, thereby changing the location of both the agent and the block it moves to.
- Calculates the **Manhattan distance** between the Grid and another Grid object passed to it, which is used as the heuristic for A* Search.

1.3 Search

An abstract class that defines a common start and solution state for each of the individual search methods, and provides a common **expandNode()** method, which generates the children of a given node

Using this Search class, I was able to easily implement a class for each of the four search algorithms:

1.4 Breadth First Search (BFS)

Uses a Queue to store expanded nodes, meaning nodes are checked in the order they are expanded.

1.5 Depth First Search (DFS)

Uses a Stack to store expanded nodes, meaning the last node to expanded is checked next.

1.6 Iterative Deepening Search (IDS)

Uses **Depth Limited Search (DLS)**, a modified version of **DFS** that does not expand nodes at a given **depth**, which then iteratively increases this limit.

1.7 A* Heuristic Search

Makes use of an evaluation function to determine which node to pick next, which is the **depth** of the node plus the **Manhattan distance** (heuristic) to the solution.

2 Evidence of Search Methods

When testing my search methods, I found 21 start states that each corresponded to a problem which has an optimal solution at a different depth (from 0 to 20). The solution state was always the same, as specified by the problem in the assignment briefing.

2.1 Breadth First Search (BFS)

Example 1 (depth 4):

In this initial state, the agent has three possible directions that it can move.

```
********
Breadth First Search (BFS) - Optimal Solution Depth: 4
w w w
WbaW
W W - W
Selected node (depth 0):
w w w
WbaW
w w \neg w
www
 \neg WW
WbaW
WCWW
WbaW
www
```

These three new nodes are then expanded in the order that they were first generated.

```
Selected node (depth 1):

W W W W
W b a W
W c ¬ W
W W W
W b a W
W ¬ c W
W W W
W b a W
W ¬ c W
W W W
W b a W
W c W ¬
W W W
W b a W
W c W ¬
W W W
W W W
W W W
W W W
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W W W
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W W W
W W W
W W W W
W W W W
W W W W
W W W W
W W W W
W W W W
W W W W
W W W W
W W W W
W W W W
W W W W
W W W W
```

The algorithm then expands the first child node in **Fringe 2**, which generates the first nodes that are at a depth of 2.

```
Selected node (depth 2):

W W W W
W b a W
W c W W
¬ W W W

W b a W
W c W W
W b a W
W c W W
W b a W
W c W W
W c W W
W c W W
W c W W
W c W W
W c W W
W c W W
W c W W
W w w w w
```

This process then repeats indefinitely until the correct node is found. At the 21st expansion to the fringe, we can see the correct node being found.

```
Selected node (depth 3):

W W W W
W ¬ a W
W b W W
W c W W

W W W W
¬ W a W
W b W W
W c W W

W w W W
W c W W

W w W W
W c W W

W w W W
W c W W

W w W W
W c W W

W w W W
W c W W

W w W W
W c W W

W w W W
W c W W

W w w W
W c W W

W w w W
W c W W

W w w W
W c W W

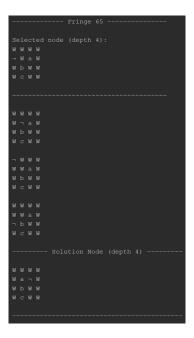
W w w W
W c W W

W w w W
W c W W

W w w w
W c W W
```

However, due to the uninformed nature of the algorithm, it does not recognise this as it only checks if it is in the goal state when taking it off the **Queue**. It therefore continues to go through each node on depth 3, and all the nodes in depth 4 that exist prior to that node - a further 44 expansions.

 ${\bf Fringe} \ {\bf 65} \ {\rm shows} \ {\rm the} \ {\rm node} \ {\rm that} \ {\rm was} \ {\rm generated} \ {\rm prior} \ {\rm to} \ {\rm the} \ {\rm goal} \ {\rm state} \ {\rm node} \ {\rm being} \ {\rm expanded}.$



The following is a breakdown of the solution of this problem, as retrieved by this search.

Example 2 (depth 14):

The original problem provided for the assignment has an optimal solution at **depth 14**, but running BFS on it causes a **Java Heap space error** due to the number of generated nodes (space complexity).

The algorithm starts in the same way that it did for the previous problem, by expanding the root node, and then by expanding each subsequent child in the order that they were generated.

```
Selected node (depth 1):

W W W W
W W W W
W W W
A D C W

W W W W
W W W
W W W
W W W
W W W
W W W
W W W
W W W
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W W
```

It then continues this process of first checking all of the nodes on a depth in the order they were generated, and then moving down to the next depth.

Eventually however, it will run into an ${\bf OutOfMemoryException}$ due to running out of Java Heap space.

2.2 Depth First Search (DFS)

Example 1 (depth 5):

Implementing DFS for this type of problem has an obvious flaw in that the nodes are generated in an ordered manner. In the case of my algorithm, this is left, right, up and down. As such, the node added to the top of the **Stack** will always be the last possible direction. In this particular example, the agent will keep moving down and then back up again, since these will be the latest nodes generated.

```
Selected node (depth 1):

W W W W
W b a W
W c W W
W W W
W b a W
W c W W
W c W W
W c W W
W c W W
W c W W
W w w W
W b a W
W c W W
W b a W
W c W W
W w w W
W w w W
W w w W
W w w w
W w w w
W w w w
W w w w
W w w w
W w w w
W w w w
W w w w
W w w w
W w w w
```

This means that unless modified accordingly, i.e. so the order of the generated nodes is randomised, the algorithm will almost certainly never find a solution.

```
Selected node (depth 3):

W W W W
W b a W
W C W W
W W D a W
W C W W
W D a W
W C W W
W D a W
W C W W
W D a W
W C W W
W W W
W W W
W D A W
W C W W
W W W W
W D A W
W C W W
W W W W
W W W W
W W W W
W W W W
W W W W
W W W W
W W W W
W W W W
W W W W
W W W W
W W W W
W W W W
W W W W
```

Eventually, this will cause an **OutOfMemoryException**, since it will repeat this process indefinitely, with the only difference being that the depth has increased by one each time.

```
Selected node (depth 206721):

W W W W
W b a W
W c W W
W w w w
W b a W
W c W W
W w w w
W b a W
W c W W
W c W W
W c W W
W c W W
W c W W
W w w
W b a W
W c W W
W w w w
W b a W
W c W W
W w w w
W b a W
W c W W
W w w w
W w w w
W w w w
W w w w
W w w w
W b a W
W c w w
W w w w
W w w w
W w w w
W w w w
```

```
Selected node (depth 206722):

W W W W
W b a W
W c ¬ W
W W W
W b a W
W ¬ c W
W W W W
W b a W
W ¬ c W
W W W W
W b a W
W c W ¬
W W W W
W b a W
W c W ¬
W W W W
W b a W
W c a W
W w w W
W b a W
W c a W
W w w W
W b a W
W w w W
W b a W
W c w W
W w w W
W b a W
W w w W
W b ¬ W
```

Example 2 (depth 5 with random order):

In order to get DFS working with this problem, the order in which the generated nodes are placed onto the **Stack** should be randomised. This is done by using the **Collections.shuffle()** function on the children list. Below, we can see the effect this has on the third and fourth node expansion.

```
Selected node (depth 2):

W W W W
W b a W
W c W W
W ¬ W W

W b a W
W c W W
W w W
W b a W
W c W W
W w W
W b a W
W c W W
W w W
W b a W
W c W W
W w w
W b a W
W c W W
W w w
W c W W
W w w
W w w
W c W W
W w w
W c W W
W c W W
W c W W
```

```
Selected node (depth 3):

W W W W
W b a W
W c W W
W W ¬ W

W C W W
W C W W
W C W W
W C W W
W C W W
W C W W
W W W W
W D a W
W C W W
W W W W
W C W W
W C W W
W C W W
W W W W
W W W W
W W W W
W W W W
W W W W
W W W W
W W W W
W W W W
W W W W
W W W W
W W W W
```

By completely arbitrary movements, the algorithm will eventually find some solution.

```
Selected node (depth 10966):

W W W W

a ¬ W W

W b W W

W c W W

W W W W

¬ a W W

W b W W

W c W W

W w W

W w W

W w W

W w W

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```

However, this solution is almost guaranteed to not be the optimal solution. The solution returned here is in 10967 steps, whereas the optimal solution for this problem is in merely 5.

```
Solution found after generating 34643 nodes: UP -> RIGHT -> LEFT -> UP -> DOWN -> DOWN -> DOWN -> LEFT -> LEFT -> RIGHT -> RIGHT -> LEFT -> UP -> RIGHT -> RIGHT -> PEPth of Solution found: 10967
```

Due to the random nature of this algorithm, the solution returned is very likely to be different each time, with the below showing what the algorithm returns on another run-through.

2.3 Iterative Deepening Search (IDS)

Example 1 (depth 6):

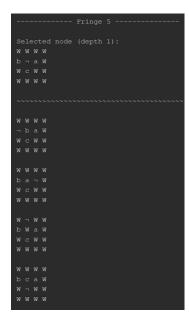
The IDS algorithm begins by calling DLS with a limit of depth 1. The agent in this initial state has three possible directions that it can move in. Each of these children are then also checked to see if they are the goal state.

The IDS then increases the limit to 2, and performs another DLS on this limit.

However, because the limit is now 2, we also expand the nodes at depth 1, and then check the nodes at depth 2 that are generated from these expansions.

```
Selected node (depth 1):

W W W W W
W b a W
C C W W
W W W W
W b a W
C C W W
W W W
W B a W
C C W W
W W W W
W W W
W W W
W W W
W W W
W W W
W W W
W W W
W W W
W W W
W W W
W W W
W W W
W W W
W W W
W W W
W W W
W W W
W W W
W W W
W W W
W W W
W W W
W W W
W W W
W W W
W W W
W W W
W W W
W W W
```



Since none of these nodes contain the goal state (which can actually be found at depth 6), we repeat this process until the goal state is found.

```
Selected node (depth 5):

W W W W
W ¬ a W
W b W W
W c W W

W ¬ W a W
W b W
W c W W

W w W
W c W W

W w W
W c W W

W w W
W c W W

W w w W
W c W W

W c W W

W c W W

W c W W

W c W W

W c W W

W c W W

W c W W

W c W W

W c W W

W c W W

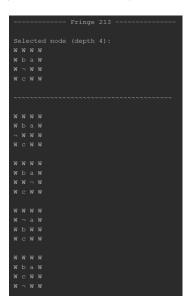
W c W W

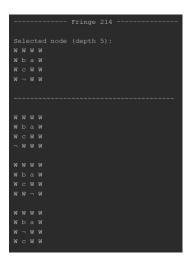
W c W W
```

If we look at the node expansions prior to this, we can see the DFS nature of the algorithm, as the next node selected is always the last generated. The next node expansion contains the goal state that was seen in the previous image (labelled **Fringe 215**).

```
Selected node (depth 3):

W W W W
W b a W
W c W W
W w W
W w W
W w W
W w W
W w W
W w W
W w W
W w W
W w W
W w W
W w W
W w W
W w W
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W w w w
W w w w
W w w w
W w w w
W w w w
W w w w
W w w w
W w w w
W w w w
```





The optimal solution was therefore found at depth 6.

```
Depth 1:
    W W W W
    W B D W
    C W W
    W W W
    W W W
    Depth 2:
    W W W
    W C W
    N W
    W W
    W W
    W W
    W W
    W C W
    W C W
    W C W
    W C W
    W C W
    W C W
    W C W
    W C W
    Depth 4:
    W W W
    W C W
    Depth 5:
    W W W
    W C W
    Depth 5:
    W W W
    W C W
    Depth 6:
    W W W
    W C W
    Depth 6:
    W W W
    W C W
    Depth 6:
    W W W
    C W
    Solution found after generating 689 nodes: DOWN -> DOWN -> RIGHT -> UP -> UP -> RIGHT
    Depth of solution found: 6
```

Example 2 (depth 15):

Whilst IDS has a better space complexity than BFS because it handles works in a DFS manner with its node expansion, it is not immune to space constraints at a large enough problem size. The following problem has an optimal solution at a depth of 15.

This means that like BFS, a failed IDS at a certain depth will cause a Java heap space error.

```
Selected node (depth 13):

W W W ¬

C b a W

W W W W

W W W W

W W W W

W W W

W W W

W W W

W W W

W W W

W W W

W W W

W W W

W W W

W W W

W W W

W W W

Exception in thread "main" java.lang.OutofMemoryError: Java heap space <1 internal call>
at java.base/java.lang.invoke.StringConcatFactorySMethodHandleInlineCopyStrategy.newArray(StringConcatFactory.java:1633)
at java.base/java.lang.invoke.DirectMethodHandleSholder.invokeStatic(DirectMethodHandleSholder)
at java.base/java.lang.invoke.LambdaFormSMH/Ox00000008000d0440.invoke(LambdaFormSMH)
at java.base/java.lang.invoke.LambdaFormSMH/Ox0000008000d7040.linkToTargetMethod(LambdaFormSMH)
at Tree.Grid.toString(Grid.java:230)
at java.base/java.lang.String.valueOf(String.java:2951)
at java.base/java.io.PrintStream.println(PrintStream.java:897)
at Search.Search.expandNode(Search.java:76)
at Search.IDS.depthLimitedSearch(IDS.java:51)
at Search.DS.search(IDS.java:26)
at Main.main(Main.java:96)
```

2.4 A* Heuristic Search

Example 1 (depth 3):

A* Search works differently to the other searches in the sense that it is an informed search, meaning the algorithm has additional information in regards to what node it should select next to expand.

Looking through a simple example, we can see that a solution that has a depth of 3 can be found by expanding 3 nodes.

Since the third child has the lowest evaluation function value (current depth of 1 plus the heuristic of 2), the **PriorityQueue** prioritises that as the next node, and thus it is selected as the next node to be expanded.

```
www
```

In the next step, we select the third child from the **Fringe 2** node expansion seen above. Despite the fact that it has a higher depth than some of the other possible nodes that can be expanded, its evaluation function is lower thanks to the fact that the heuristic is merely 1.

```
WCWW
```

We have now found a solution, which the **PriorityQueue** will select regardless as it has the lowest evaluation function value.

```
----- Solution Node (depth 3) -----
w w w
Depth 1:
WbaW
WcWW
Depth 2:
www
wwdw
Depth 3:
www
WWdW
Solution found after generating 12 nodes: UP -> UP -> RIGHT
Depth of solution found: 3
```

Example 2 (depth 15):

Since A* is a smarter searching algorithm, it is capable of solving problems that the other uninformed search methods cannot due to **Java heap space errors**. For instance, it is able to find a solution for the problem that has an optimal solution at depth 15 that IDS was unable to find.

```
*************************
\neg w w w
cbaW
c W W W
```

The next node that is expanded is the one with the lowest value from the evaluation function, which was the first child in this case.

```
w - w
wwww
```

This process continues until a solution is found - here is the last node expansion performed before the goal state is discovered.

```
w w ¬ w
```

You would have noticed that the last expanded node does not contain the solution - this is because these nodes have an equal evaluation function value, so the way that they are selected in this situation is completely down to the implementation of the Java **PriorityQueue** structure. The solution node can actually be seen being generated in the node generation labelled **Fringe 32385**, two nodes before the point at which the final expansion took place.

```
wbww
```

The following solution is then found, which corresponds to the optimal solution that exists at 15 steps.

```
c W W
Depth 11:
 c W W
  w w w
Depth 12:
 \neg w w
Depth 14:
wwdw
WcWW
Depth 15:
Wwdw
```

Solution found after generating 101800 nodes: RIGHT -> DOWN -> LEFT -> DOWN -> RIGHT -> UP -> UP -> LEFT -> DOWN -> DOWN -> DOWN -> RIGHT -> UP -> UP -> RIGHT Depth of solution found: 15

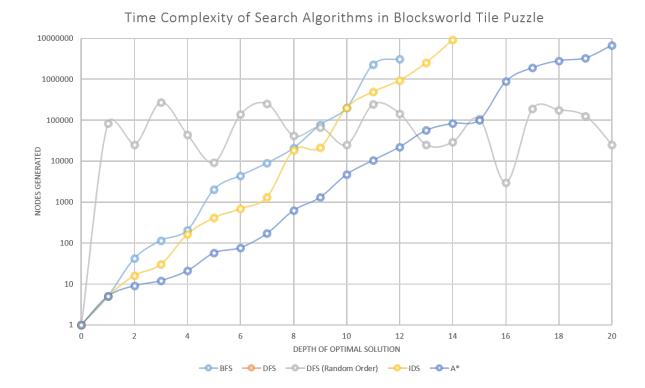
3 Scalability Study

As explained above, the scalability study was conducted using 21 states, each of which corresponded to a problem that had an optimal solution from 0 to 20. For completeness, I have attached these initial states, as seen in appendix A.

Depth of optimal solution	BFS		DFS		DFS (Random Order)	
	Nodes generated	Depth	Nodes generated	Depth	Nodes generated	Depth
0	1	0	1	0	1	1
1	5	1	Heap space error	N/A	84863	26798
2	42	2	Heap space error	N/A	25274	8012
3	115	3	Heap space error	N/A	270143	85111
4	208	4	Heap space error	N/A	44338	14000
5	2047	5	Heap space error	N/A	9288	2923
6	4445	6	Heap space error	N/A	138676	43652
7	9004	7	Heap space error	N/A	254565	80381
8	20932	8	Heap space error	N/A	41730	13157
9	77169	9	Heap space error	N/A	67296	21240
10	202095	10	Heap space error	N/A	25297	7963
11	2318900	11	Heap space error	N/A	245155	77368
12	3127458	12	Heap space error	N/A	144702	45603
13	Heap space error	N/A	Heap space error	N/A	24998	7909
14	Heap space error	N/A	Heap space error	N/A	29386	9258
15	Heap space error	N/A	Heap space error	N/A	109742	34647
16	Heap space error	N/A	Heap space error	N/A	3001	951
17	Heap space error	N/A	Heap space error	N/A	190469	60053
18	Heap space error	N/A	Heap space error	N/A	178706	56441
19	Heap space error	N/A	Heap space error	N/A	127710	40242
20	Heap space error	N/A	Heap space error	N/A	25389	8040

Double of autimal adultion	IC)S	A*		
Depth of optimal solution	Nodes generated	Depth	Nodes generated	Depth	
0	1	0	1	0	
1	5	1	5	1	
2	16	2	9	2	
3	30	3	12	3	
4	164	4	21	4	
5	412	5	57	5	
6	689	6	77	6	
7	1328	7	171	7	
8	18584	8	627	8	
9	21386	9	1302	9	
10	202171	10	4730	10	
11	494670	11	10500	11	
12	942293	12	22262	12	
13	2559398	13	56516	13	
14	9238235	14	83428	14	
15	Heap space error	N/A	101800	15	
16	Heap space error	N/A	883397	16	
17	Heap space error	N/A	1909423	17	
18	Heap space error	N/A	2844540	18	
19	Heap space error	N/A	3311656	19	
20	Heap space error	N/A	6777725	20	

The below graph visualises these results. Take note of the logarithmic scale used for the nodes generated.



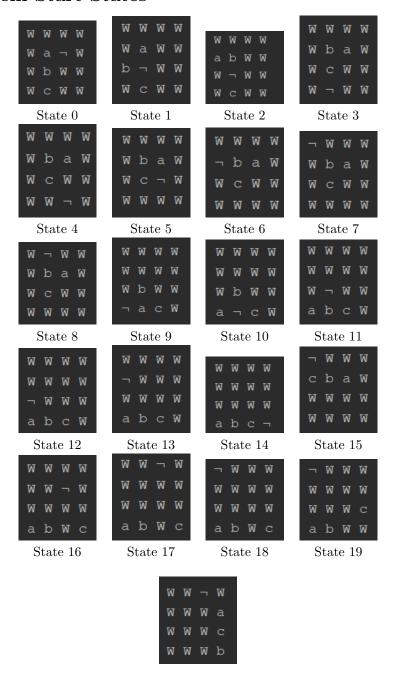
From this data, you may extrapolate that the DFS with a random order is the best performing algorithm for problems with larger depth solutions. However, although it may be quicker to find these solutions, they are almost guaranteed to not be **optimal**. It is also worth noting that due to the arbitrary nature of this algorithm, it is actually the worst performing search at the earlier depth problems.

Looking at the other algorithms, it is clear that A* is the best performing algorithm in terms of time complexity, however it is also clear that it is exponential based on the problem size. BFS and IDS would continue to rise exponentially too if they did not run into space complexity issues, but have a worse time complexity than A*. For the most part, IDS is better than BFS, but this is dependent on whereabouts in the tree structure the goal state is located.

4	Extras and Limitations

Appendices

A Problem Start States



State 20

B Code