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 pbdMPI
 pbdMPI eg's
 pbdDMAT
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 Iris
 Wrapup

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Introducing R: from Your Laptop to HPC and Big Data

Drew Schmidt Remote Data Analysis and Visualization Center University of Tennessee, Knoxville

June 17, 2013





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Affiliations and Support

The pbdR Core Team http://r-pbd.org

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Ostrouchov, Patel, and Schmidt were supported in part by the project "NICS Remote Data Analysis and Visualization Center" funded by the Office of Cyberinfrastructure of the U.S. National Science Foundation under Award No. ARRA-NSF-OCI-0906324 for NICS-RDAV center.

Chen and Ostrouchov were supported in part by the project "Visual Data Exploration and Analysis of Ultra-large Climate Data" funded by U.S. DOE Office of Science under Contract No. DE-AC05-00OR22725.

Computer Science and Mathematics Division, Oak Ridge National Laboratory, Oak Ridge, TN





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About This Presentation

Downloads

This presentation and supplemental materials are available at:

http://r-pbd.org/handouts



About This Presentation

Speaking Serial R with a Parallel Accent

The content of this presentation is based in part on the **pbdDEMO** vignette *Speaking Serial R with a Parallel Accent*

https://github.com/wrathematics/pbdDEMO/blob/master/inst/doc/pbdDEMO-guide.pdf?raw=true

It contains more examples, and sometimes added detail.



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About This Presentation

Installation Instructions

Installation instructions for setting up a pbdR environment are available:

This includes instructions for installing R, MPI, and pbdR.



About This Presentation

Conventions For Code Presentation

We will use two different forms of syntax highlighting. One for displaying results from an interactive R session:

```
1 R> "interactive"
2 [1] "interactive"
```

and one for presenting R scripts

```
1 "not interactive"
```



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- In-Depth Example Examining the Iris Dataset with pbdR



http://r-pbd.org

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Contents

- Introduction to R
 - What is R?
 - Basic Numerical Operations in R
 - R Syntax for Data Science: Not A Matlab Clone!



What is R?

What is R?

- lingua franca for data analytics and statistical computing.
- Part programming language, part data analysis package.
- Dialect of S (Bell Labs).
- Syntax designed for data.



What is R?

Who uses R?

Google, Pfizer, Merck, Bank of America, Shell^a, Oracle^b, Facebook, bing, Mozilla, okcupid^c, ebay^d, kickstarter^e, the New York Times^f

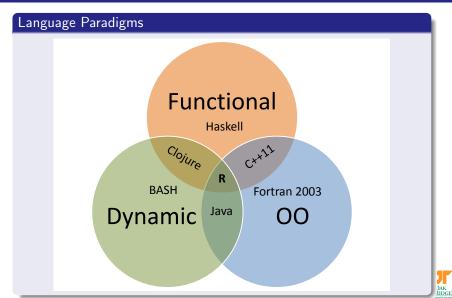
ahttps://www.nytimes.com/2009/01/07/technology/

business-computing/07program.html?_r=0



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What is R?





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What is R?

Data Types

- Storage: logical, int, double, double complex, character
- Structures: vector, matrix, array, list, dataframe
- Caveats: (Logical) TRUE, FALSE, NA

For the remainder of the tutorial, we will restrict ourselves to real number matrix computations.



What is R?

Basics (1 of 2)

• The default method is to print:

```
R> sum
function (..., na.rm = FALSE) .Primitive("sum")
```

Use <- for assignment:

```
1 R> x <- 1
2 R> x+1
3 [1] 2
```

- Naming rules: mostly like C.
- R is case sensitive.
- We use . the way most languages use _, e.g., La.svd() instead of La_svd().
- We use \$ (sometimes @) the way most languages use .



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What is R?

Basics (2 of 2)

• Use ? or ?? to search help

R> ??comm.set.seed

```
R> ?set.seed
R> ?comm.set.seed
No documentation for comm.set.seed in specified packages and libraries:
you could try ??comm.set.seed
```





What is R?

Addons and Extras

R has the Comprehensive R Archive Network (CRAN), which is a package repository like CTAN and CPAN.

From R

```
install.packages("pbdMPI") # install
library(pbdMPI) # load

From Shell
R CMD INSTALL pbdMPI_0.1-6.tar.gz
```



```
Lists (1 of 1)
         <- list(a=1, b="a")
2
  R> 1
  $a
   [1] 1
5
6
7
  $Ъ
   [1] "a"
8
  R> 1$a
   [1] 1
10
11
  R> list(x=list(a=1, b="a"), y=TRUE)
13
  $x
  $x$a
14
   [1] 1
15
16
17
  $x$b
   [1] "a"
18
19
20
21
  $ v
   [1] TRUE
```



Vectors and Matrices (1 of 2)

```
R > c(1, 2, 3, 4, 5, 6)
   [1] 1 2 3 4 5 6
3
  R > matrix(1:6, nrow=2, ncol=3)
        [,1] [,2] [,3]
   [1,]
   [2,]
8
  R > x < -matrix(1:6, nrow=2, ncol=3)
10
  R > x[, -1]
11
        [,1] [,2]
12
  [1,]
13
   [2,]
14
15
16 R> x[1, 1:2]
  [1] 1 3
17
```



Vectors and Matrices (2 of 2)

```
R> dim(x)
   [1] 2 3
3
  R> dim(x) <- NULL
  R> x
   [1] 1 2 3 4 5 6
  R > dim(x) < -c(3,2)
  R> x
         [,1] [,2]
10
   [1,]
11
   [2,]
12
                  5
   [3,]
                  6
13
```



Vector and Matrix Arithmetic (1 of 2)

```
R > 1:4 + 4:1
   [1] 5 5 5 5
3
  R > x < -matrix(0, nrow=2, ncol=3)
  R > x + 1
         [,1] [,2] [,3]
   [1,]
   [2,]
10
  R > x + 1:3
11
         [,1] [,2] [,3]
12
   [1,]
13
   [2,]
14
```



Vector and Matrix Arithmetic (2 of 2)

```
R> x <- matrix(1:6, nrow=2)
  R> x*x
         [,1]
              [,2] [,3]
   [1,]
                       25
   [2,]
6
7
                 16
                       36
  R> x %*% x
  Error in x %*% x : non-conformable arguments
10
11
  R> t(x) %*% x
         [,1] [,2] [,3]
12
   [1.]
                 11
                       17
13
   [2,]
           11
                 25
                       39
14
   [3,]
15
           17
                 39
                       61
16
17
  R> crossprod(x)
         [,1] [,2] [,3]
18
   [1,]
            5
                 11
                       17
19
   [2,]
           11
                 25
                       39
20
   [3,]
           17
                 39
                       61
21
```



Linear Algebra (1 of 2): Matrix Inverse

$$x_{n \times n}$$
 invertible $\iff \exists y_{n \times n} (xy = yx = Id_{n \times n})$



Linear Algebra (2 of 2): Singular Value Decomposition

$$x = U\Sigma V^T$$

```
R > x < - matrix(rnorm(2*3), nrow=3)
     svd(x)
  R>
  $d
  [1]
      2.4050716 0.3105008
5
6
7
  $u
             [,1] [,2]
  [1.]
        0.8582569 -0.1701879
       0.2885390 0.9402076
  [3.]
       0.4244295 -0.2950353
10
11
12
  $ v
13
               [,1]
                           [,2]
  [1,] -0.05024326 -0.99873701
14
15
  [2,]
       -0.99873701 0.05024326
```



•00000

More than just a Matlab clone...

• Data science (machine learning, statistics, data mining, ...) is mostly matrix algebra.

So what about Matlab/Python/Julia/...?

- The one you prefer depends more on your "religion" rather than differences in capabilities.
- As a data analysis package, R is king.



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Simple Statistics (1 of 2): Summary Statistics

```
R > x < -matrix(rnorm(30, mean=10, sd=3), nrow=10)
  R> mean(x)
   [1] 9.825177
  R> median(x)
   [1] 9.919243
  R> sd(as.vector(x))
  [1] 3.239388
10
11
  R> colMeans(x)
12
  [1] 9.661822 10.654686 9.159025
13
14
  R> apply(x, MARGIN=2, FUN=sd)
15
  [1] 2.101059 3.377347 4.087131
16
```



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Simple Statistics (2 of 2): Sample Covariance

$$cov(x_{n \times p}) = \frac{1}{n-1} \sum_{i=1}^{n} (x_i - \mu_x) (x_i - \mu_x)^T$$

```
1  x <- matrix(rnorm(30), nrow=10)
2  # least recommended
4  cm <- colMeans(x)
5  crossprod(sweep(x, MARGIN=2, STATS=cm))
6  # less recommended
8  crossprod(scale(x, center=TRUE, scale=FALSE))
9  # recommended
11  cov(x)</pre>
```



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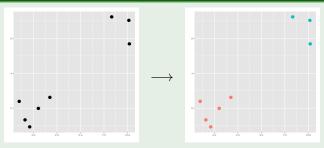
Advanced Statistics (1 of 2): Principal Components

PCA = centering + scaling + rotation (via SVD)

```
R > x < - matrix(rnorm(30), nrow=10)
2
  R> prcomp(x, retx=TRUE, scale=TRUE)
  Standard deviations:
  [1] 1.1203373 1.0617440 0.7858397
  Rotation:
                PC1
                           PC2
                                       PC3
8
  [1.] 0.71697825 -0.3275365 0.6153552
  [2.] -0.03382385  0.8653562  0.5000147
10
  [3,]
       0.69627447 0.3793133 -0.6093630
11
```



Advanced Statistics (2 of 2): k-Means Clustering



```
1 R> x <- rbind(matrix(rnorm(5*2, mean=0), ncol=2),
matrix(rnorm(3*2, mean=10), ncol=2))
```



Advanced Statistics (2 of 2): k-Means Clustering

```
R> kmeans(x, centers=2)
  K-means clustering with 2 clusters of sizes 5. 3
3
  Cluster means:
          [,1]
               [,2]
5
  1 -0.1080612 -0.2827576
  2 9.5695365 9.3191892
8
  Clustering vector:
  [1] 1 1 1 1 1 2 2 2
10
11
  Within cluster sum of squares by cluster:
  [1] 14.675072 7.912641
13
   (between SS / total SS = 93.9 %)
14
15
16
  Available components:
17
  [1] "cluster"
                    "centers"
                                    "totss"
18
      "withinss"
                  "tot.withinss"
  [6] "betweenss"
                     "size"
19
```



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- 2 In-Depth Example Examining the Iris Dataset
 - Examining the Iris Dataset
 - Cluster
 - Plot



Examining the Iris Dataset

```
The Iris Dataset
```

```
rm(list = ls())  # Clean environment

head(iris)

### Load data
X <- as.matrix(iris[, -5])  # Dimension 150 by 4
X.cid <- as.numeric(iris[, 5]) # True id</pre>
```



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Examining the Iris Dataset

Standardizing

```
### Transformation and check

X.std <- scale(X)  # Standardize

mu <- colMeans(X.std)  # Columns means are near 0

cov <- cov(X.std)  # Diagonals are near 1

print(mu)
print(cov)</pre>
```



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Examining the Iris Dataset

Projection Onto First 2 PC's



Cluster

Clustering

```
### Clustering
  set.seed (1234)
                                     Set overall seed
 X.kms <- kmeans(X.std, 3)
                                      K-means
 X.kms
 X.kms.cid <- X.kms$cluster
                                    # Classification
6
  library(EMCluster)
                                    # Model-based clustering
 X.mbc <- init.EM(X.std. 3)</pre>
                                      Initial by em-EM
 X.mbc
 X.mbc.cid <- X.mbc$class
                                    # Classification
```



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Cluster

Cluster Validation





Cluster

Cluster ID Variable

```
### Swap classification id
X.kms.cid[X.kms.cid == 2] <- 4
X.kms.cid[X.kms.cid == 3] <- 2
X.kms.cid[X.kms.cid == 4] <- 3</pre>
```

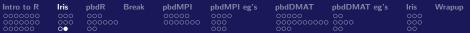


Plot

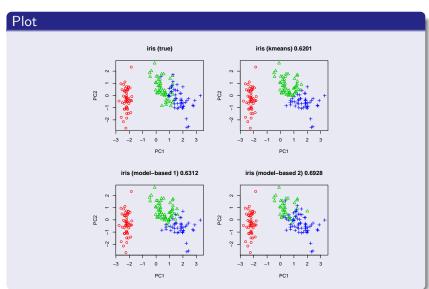
Plot

```
1 ### Display on first 2 components
  pdf("serial_plot.pdf")
3
  par(mfrow = c(2, 2))
  plot(X.prj, col = X.cid + 1, pch = X.cid,
       main = "iris (true)", xlab = "PC1", ylab = "PC2")
6
  plot(X.prj, col = X.kms.cid + 1, pch = X.kms.cid,
       main = paste("iris (k-Means)", sprintf("%.4f",
           X.kms.adjR)),
       xlab = "PC1", ylab = "PC2")
  plot(X.prj, col = X.mbc.cid + 1, pch = X.mbc.cid,
10
       main = paste("iris (Model-based)", sprintf("%.4f",
11
           X.mbc.adjR)),
       xlab = "PC1", ylab = "PC2")
12
  accuracy <- c(X.kms.adjR, X.mbc.adjR)
13
  names(accuracy) <- c("k-Means", "Model-based")</pre>
  barplot(accuracy, main = "Clustering Accuracy")
15
16
17
  dev.off()
```





Plot





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Problems with R

Problems with R

We love R! However...

- Slow.
- If you don't know what you're doing, it's really slow.
- Performance improvements usually for small machines.
- Very ram intensive.
- Chokes on big data.



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Problems with R

Problems with R: Big Data

One of R's biggest problems is an indexing limitation:

- Any one R object must (at present) be indexed by a 32-bit integer.
- Largest vector/matrix: 16gb
- Largest square matrix: 46340 × 46340



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Problems with R

R and Parallelism

The solution to many of R's problems is parallelism. However . . .

What we have

- Mostly serial.
- Parallelism mostly not distributed.
- Oata parallelism mostly explicit.

What we want

- Mostly parallel.
- Mostly distributed.
- Mostly implicit.



http://r-pbd.org pbdR Core Team Introduction to pbdR 31/97

The pbdR Project

Programming with Big Data in R (pbdR)

Goals: Productivity, Portability, Performance

Our Approach:

- Series of free^a R packages.
- Scalable, big data analytics with high-level syntax.
- Implicit management of distributed data details.
- Methods have syntax identical to R.
- Powered by state of the art numerical libraries (MPI, ScaLAPACK, PBLAS, BLACS, LAPACK, BLAS, ...)



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^aMPL, BSD, and GPL licensed

The pbdR Project

pbdR Packages pbdDEMO pbdR pbdDMAT r-pbd.org pbdADIOS pbdBASE pbdNCDF4 pbdSLAP pbdMPI High Performance Libraries ADIOS. MKL. libsci NetCDF4 ScaLAPACK LAPACK Parallel PBLAS MPI 1/0 BLAS BLACS



http://r-pbd.org pbdR Core Team Introduction to pbdR 33/97

The pbdR Project

pbdR Packages — http://code.r-pbd.org

Released to CRAN:

- pbdMPI: MPI bindings (explicit, low-level)
- pbdSLAP: Foreign library (just install it, nothing to use)
- pbdBASE: Compiled code (used by DMAT, also for devs)
- pbdDMAT: Distributed matrices (mostly implicit, high-level)
- pbdNCDF4: Parallel NetCDF4 reader
- pbdDEMO: Package demonstrations, examples, vignette written in textbook style

Future Development:

- pbdADIOS: Wrappers for ADIOS middleware
- Profiling tools
- Client/server interface for interactive sessions
- Something for you...?



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The pbdR Project

SPMD

The pbdR Packages enable high-level "Single Program/Multiple Data" (SPMD) programming:

- SPMD is a programming paradigm.
- Arguably the simplest extension of serial programming.
- Sort of like trying to explain breathing . . .
- Not to be confused with SIMD.
- SPMD utilizes MIMD architecture computers.
- Only one program is written, executed in batch independently on all processors.
- Different processors are autonomous; there is no manager.



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The pbdR Project

SPMD

SPMD codes are run in batch (non-interactively):

From the Shell

1 mpirun -np 4 Rscript my_script.R



The pbdR Project

Example Syntax

```
1 x <- x[-1, 2:5]
2 xtx <- t(x) %*% x
3 ans <- svd(solve(xtx))
```

Look familiar?

The above runs on 1 core with R or 10,000 cores with pbdR



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Installing pbdR

Installation

Installing pbdR is about as easy as possible, and generally amounts to:

```
install.packages(pbdMPI)
install.packages(pbdNCDF4)
install.packages(pbdSLAP)
install.packages(pbdBASE)
install.packages(pbdDMAT)
install.packages(pbdDEMO)
```

But this assumes you have MPI installed on your system...



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Installing pbdR



Instead, consider getting an allocation on Nautilus:

http://www.nics.tennessee.edu/getting-an-allocation





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Brief Intermission

Brief Intermission

Questions? Comments?

Don't forget to talk to us at our discussion group:

http://group.r-pbd.org/

Don't have an allocation with us?

http://www.nics.tennessee.edu/getting-an-allocation



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Basic MPI

Message Passing Interface (MPI)

- MPI: Standard for managing communications (data and instructions) between different nodes/computers.
- Implementations: OpenMPI, MPICH2, Cray MPT, ...
- Enables parallelism on distributed machines.
- Communicator: manages communications between processors.



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Basic MPI

Common MPI Operations (1 of 2)

Managing a Communicator: Create and destroy communicators.

```
init() — initialize communicator
finalize() — shut down communicator(s)
```

 Rank query: determine the processor's position in the communicator.

```
comm.rank() — "who am I?"
comm.size() — "how many of us are there?"
```

• Barrier: "computation wall"; no processor can proceed until all processors can proceed.

barrier()



Basic MPI

Quick Example 1

```
Rank Query
```

```
library(pbdMPI, quiet = TRUE)
init()

myRank <- comm.rank()
comm.print(myRank, all.rank=TRUE)

finalize()</pre>
```

Sample Output

```
1 COMM.RANK = 0
2 [1] 0
3 COMM.RANK = 1
4 [1] 1
```



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Basic MPI

Common MPI Operations (2 of 2)

- Reduction: each processor has a number x.spmd; add all of them up, find the largest/smallest,
 reduce(x.spmd, op='sum') — reduce to one allreduce(x.spmd, op='sum') — reduce to all
- Gather: each processor has a number; create a new object on some processor containing all of those numbers. gather(x.spmd) — gather to one allgather(x.spmd) — gather to all
- Broadcast: one processor has a number x.spmd that every other processor should also have.
 bcast(x.spmd)



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Basic MPI

Quick Example 2

```
library(pbdMPI, quiet = TRUE)
init()

comm.set.seed(diff=TRUE)

n <- sample(1:10, size=1)

sm <- allreduce(n, op='sum')
comm.print(sm)

gt <- allgather(n)
comm.print(unlist(gt))

finalize()</pre>
```

Sample Output

```
1 COMM.RANK = 0
2 [1] 10
3 COMM.RANK = 0
4 [1] 2 8
```



The SPMD Data Structure

The SPMD Data Structure

Throughout the examples, we will make use of the SPMD distributed matrix structure.

- **1** SPMD is *distributed*. No one processor owns all of the matrix.
- ② SPMD is *non-overlapping*. Any row owned by one processor is owned by no other processors.
- 3 SPMD is *row-contiguous*. If a processor owns one element of a row, it owns the entire row.
- SPMD is globally row-major, locally column-major.
- The last row of the local storage of a processor is adjacent (by global row) to the first row of the local storage of next processor (by communicator number) that owns data.
- SPMD is (relatively) easy to understand, but can lead to bottlenecks if you have many more columns than rows.



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The SPMD Data Structure

Understanding SPMD: Global Matrix

$$x = \begin{bmatrix} x_{11} & x_{12} & x_{13} & x_{14} & x_{15} & x_{16} & x_{17} & x_{18} & x_{19} \\ x_{21} & x_{22} & x_{23} & x_{24} & x_{25} & x_{26} & x_{27} & x_{28} & x_{29} \\ x_{31} & x_{32} & x_{33} & x_{34} & x_{35} & x_{36} & x_{37} & x_{38} & x_{39} \\ x_{41} & x_{42} & x_{43} & x_{44} & x_{45} & x_{46} & x_{47} & x_{48} & x_{49} \\ x_{51} & x_{52} & x_{53} & x_{54} & x_{55} & x_{56} & x_{57} & x_{58} & x_{59} \\ x_{61} & x_{62} & x_{63} & x_{64} & x_{65} & x_{66} & x_{67} & x_{68} & x_{69} \\ x_{71} & x_{72} & x_{73} & x_{74} & x_{75} & x_{76} & x_{77} & x_{78} & x_{79} \\ x_{81} & x_{82} & x_{83} & x_{84} & x_{85} & x_{86} & x_{87} & x_{88} & x_{89} \\ x_{91} & x_{92} & x_{93} & x_{94} & x_{95} & x_{96} & x_{97} & x_{98} & x_{99} \end{bmatrix}$$

Processors = 0 1 2 3 4 5



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The SPMD Data Structure

Understanding SPMD: Load Balanced SPMD

$$x = \begin{bmatrix} x_{11} & x_{12} & x_{13} & x_{14} & x_{15} & x_{16} & x_{17} & x_{18} & x_{19} \\ x_{21} & x_{22} & x_{23} & x_{24} & x_{25} & x_{26} & x_{27} & x_{28} & x_{29} \\ \hline x_{31} & x_{32} & x_{33} & x_{34} & x_{35} & x_{36} & x_{37} & x_{38} & x_{39} \\ x_{41} & x_{42} & x_{43} & x_{44} & x_{45} & x_{46} & x_{47} & x_{48} & x_{49} \\ \hline x_{51} & x_{52} & x_{53} & x_{54} & x_{55} & x_{56} & x_{57} & x_{58} & x_{59} \\ x_{61} & x_{62} & x_{63} & x_{64} & x_{65} & x_{66} & x_{67} & x_{68} & x_{69} \\ \hline x_{71} & x_{72} & x_{73} & x_{74} & x_{75} & x_{76} & x_{77} & x_{78} & x_{79} \\ \hline x_{81} & x_{82} & x_{83} & x_{84} & x_{85} & x_{86} & x_{87} & x_{88} & x_{89} \\ \hline x_{91} & x_{92} & x_{93} & x_{94} & x_{95} & x_{96} & x_{97} & x_{98} & x_{99} \end{bmatrix}$$

Processors = 0 1 2 3 4 5



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The SPMD Data Structure

Understanding SPMD: Local View

$$\begin{bmatrix} x_{11} & x_{12} & x_{13} & x_{14} & x_{15} & x_{16} & x_{17} & x_{18} & x_{19} \\ x_{21} & x_{22} & x_{23} & x_{24} & x_{25} & x_{26} & x_{27} & x_{28} & x_{29} \end{bmatrix}_{2\times9} \\ \begin{bmatrix} x_{31} & x_{32} & x_{33} & x_{34} & x_{35} & x_{36} & x_{37} & x_{38} & x_{39} \\ x_{41} & x_{42} & x_{43} & x_{44} & x_{45} & x_{46} & x_{47} & x_{48} & x_{49} \end{bmatrix}_{2\times9} \\ \begin{bmatrix} x_{51} & x_{52} & x_{53} & x_{54} & x_{55} & x_{56} & x_{57} & x_{58} & x_{59} \\ x_{61} & x_{62} & x_{63} & x_{64} & x_{65} & x_{66} & x_{67} & x_{68} & x_{69} \end{bmatrix}_{2\times9} \\ \begin{bmatrix} x_{71} & x_{72} & x_{73} & x_{74} & x_{75} & x_{76} & x_{77} & x_{78} & x_{79} \end{bmatrix}_{1\times9} \\ \begin{bmatrix} x_{81} & x_{82} & x_{83} & x_{84} & x_{85} & x_{86} & x_{87} & x_{88} & x_{89} \end{bmatrix}_{1\times9} \\ \begin{bmatrix} x_{91} & x_{92} & x_{93} & x_{94} & x_{95} & x_{96} & x_{97} & x_{98} & x_{99} \end{bmatrix}_{1\times9} \end{bmatrix}_{1\times9}$$

Processors = 0 1 2 3 4 5



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The SPMD Data Structure

Understanding SPMD: Non-Balanced SPMD

$$X = \begin{bmatrix} X_{11} & X_{12} & X_{13} & X_{14} & X_{15} & X_{16} & X_{17} & X_{18} & X_{19} \\ X_{21} & X_{22} & X_{23} & X_{24} & X_{25} & X_{26} & X_{27} & X_{28} & X_{29} \\ X_{31} & X_{32} & X_{33} & X_{34} & X_{35} & X_{36} & X_{37} & X_{38} & X_{39} \\ X_{41} & X_{42} & X_{43} & X_{44} & X_{45} & X_{46} & X_{47} & X_{48} & X_{49} \\ \hline X_{51} & X_{52} & X_{53} & X_{54} & X_{55} & X_{56} & X_{57} & X_{58} & X_{59} \\ X_{61} & X_{62} & X_{63} & X_{64} & X_{65} & X_{66} & X_{67} & X_{68} & X_{69} \\ \hline X_{71} & X_{72} & X_{73} & X_{74} & X_{75} & X_{76} & X_{77} & X_{78} & X_{79} \\ \hline X_{81} & X_{82} & X_{83} & X_{84} & X_{85} & X_{86} & X_{87} & X_{88} & X_{89} \\ X_{91} & X_{92} & X_{93} & X_{94} & X_{95} & X_{96} & X_{97} & X_{98} & X_{99} \end{bmatrix}$$

Processors = 0 1 2 3 4 5



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The SPMD Data Structure

```
Understanding SPMD: Local View
                                                                                               \int_{0\times9}
                                                            X<sub>16</sub>
                                                                     X<sub>17</sub>
               X_{11}
                         X_{12}
                                 X_{13}
                                          X_{14}
                                                   X_{15}
                                                                             X<sub>18</sub>
                                                                                       X_{19}
               X21
                         X22
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                                          X24
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                                                            X26
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                                                                              X28
                                                                                       X29
               X31
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                                 X33
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                                                            X36
                                                                     X37
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                                                                                      X39
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                                                            X46
               X<sub>41</sub>
                         X42
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                                                                     X57
                                                                              X58
                                                                                       X59
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                         X<sub>62</sub>
                                  X<sub>63</sub>
                                           X<sub>64</sub>
                                                    X<sub>65</sub>
                                                            X<sub>66</sub>
                                                                     X67
                                                                              X<sub>68</sub>
                                                                                       X69
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                         X72
                                  X73
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                                                                                       X79
                                           X74
                                                    X75
                                                             X76
                                                                      X77
                                                                                               \rfloor_{2\times9}
                X<sub>81</sub>
                         X82
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                                                            X86
                                                                     X87
                                                                              X88
                                                                                       X99
                X91
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                                  X93
                                           X94
                                                    X95
                                                            X96
                                                                     X97
                                                                              X98
                            Processors = 0
                                                                     3
```



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The SPMD Data Structure

Quick Comments for Using pbdMPI

Start by loading the package:

```
1 library(pbdMPI, quiet = TRUE)
```

② Always initialize before starting and finalize when finished:

```
init()
# ...
finalize()
```

- Use comm.set.seed(diff=TRUE) to generate independent streams by L'Ecuyer's method. Use comm.set.seed(diff=FALSE) to set a common seed among all processors.
- Local pieces of SPMD distributed objects will be given the suffix .spmd to visually help distinguish them from global objects. This suffix carries no semantic meaning.



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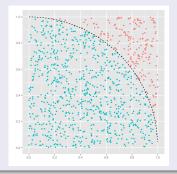
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pbdMPI Example: Monte Carlo Simulation

Example 1: Monte Carlo Simulation

Sample *N* uniform observations (x_i, y_i) in the unit square $[0,1] \times [0,1]$. Then

$$\pi pprox 4\left(rac{\#\ \textit{Inside Circle}}{\#\ \textit{Total}}
ight) = 4\left(rac{\#\ \textit{Blue}}{\#\ \textit{Blue} + \#\ \textit{Red}}
ight)$$





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pbdMPI Example: Monte Carlo Simulation

Example 1: Monte Carlo Simulation SPMD Algorithm

- Let n be big-ish; we'll take n = 50,000.
- ② Generate an $n \times 2$ matrix x of standard uniform observations.
- **3** Count the number of rows satisfying $x^2 + y^2 \le 1$
- Ask everyone else what their answer is; sum it all up.
- \odot Take this new answer, multiply by 4 and divide by n
- 1 If my rank is 0, print the result.



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pbdMPI Example: Monte Carlo Simulation

Example 1: Monte Carlo Simulation Code

Serial Code

```
N <- 50000
2 X <- matrix(runif(N * 2), ncol=2)
3 r <- sum(rowSums(X^2) <= 1)
4 PI <- 4*r/N
5 print(PI)</pre>
```

Parallel Code

```
library(pbdMPI, quiet = TRUE)
init()
comm.set.seed(diff=TRUE)

N.spmd <- 50000 / comm.size()
X.spmd <- matrix(runif(N.spmd * 2), ncol = 2)
r.spmd <- sum(rowSums(X.spmd^2) <= 1)
r <- allreduce(r.spmd)
PI <- 4*r/(N.spmd * comm.size())
comm.print(PI)
in finalize()</pre>
```



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pbdMPI Example: Monte Carlo Simulation

Note

For the remainder, we will exclude loading, init, and finalize calls.



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pbdMPI Example: Sample Covariance

Example 2: Sample Covariance

$$cov(x_{n \times p}) = \frac{1}{n-1} \sum_{i=1}^{n} (x_i - \mu_x) (x_i - \mu_x)^T$$



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pbdMPI Example: Sample Covariance

Example 2: Sample Covariance SPMD Algorithm

- \bullet Determine the total number of rows N.
- Compute the vector of column means of the full matrix.
- Subtract each column's mean from that column's entries in each local matrix.
- Ompute the crossproduct locally and reduce.
- **5** Divide by N-1.



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pbdMPI Example: Sample Covariance

Example 2: Sample Covariance Code

Serial Code

```
1 N <- nrow(X)
2 mu <- colSums(X) / N
3
4 X <- sweep(X, STATS=mu, MARGIN=2)
5 Cov.X <- crossprod(X.spmd) / (N-1)
6
7 print(Cov.X)</pre>
```

Parallel Code

```
1 N <- allreduce(nrow(X.spmd), op="sum")
2 mu <- allreduce(colSums(X.spmd) / N, op="sum")
3
4 X.spmd <- sweep(X.spmd, STATS=mu, MARGIN=2)
5 Cov.X <- allreduce(crossprod(X.spmd), op="sum") / (N-1)
6
7 comm.print(Cov.X)</pre>
```



pbdMPI Example: Linear Regression

Example 3: Linear Regression

Find β such that

$$\mathsf{y} = \mathsf{X} oldsymbol{eta} + \epsilon$$

When X is full rank,

$$\hat{\boldsymbol{eta}} = (\mathbf{X}^T\mathbf{X})^{-1}\mathbf{X}^T\mathbf{y}$$



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pbdMPI Example: Linear Regression

Example 3: Linear Regression SPMD Algorithm

- **1** Locally, compute $tx = x^T$
- 2 Locally, compute A = tx * x. Query every other processor for this result and sum up all the results.
- **3** Locally, compute B = tx * y. Query every other processor for this result and sum up all the results.
- **1** Locally, compute $A^{-1} * B$



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pbdMPI Example: Linear Regression

Example 3: Linear Regression Code

Serial Code

```
1 tX <- t(X)
2 A <- tX %*% X
3 B <- tX %*% y
4 ols <- solve(A) %*% B
```

Parallel Code

```
tX.spmd <- t(X.spmd)
tX.spmd <- t(X.spmd)
tX.spmd <- t(X.spmd %*% X.spmd, op = "sum")
tX.spmd <- allreduce(tX.spmd %*% y.spmd, op = "sum")
tY.spmd <- t(X.spmd %*% y.spmd, op = "sum")
tY.spmd <- t(X.spmd)
tX.spmd <-
```



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Introduction to Distributed Matrices

Distributed Matrices

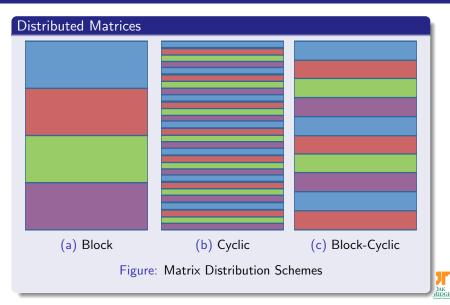
Most problems in data science

- Data structure: block-cyclic matrix distributed across a 2-dimensional grid of processors.
- No single processor should hold all of the data.
- Very robust, but very confusing data structure.



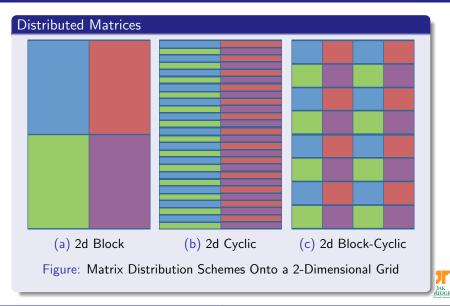
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Processor Grid Shapes

$$\begin{bmatrix} 0 \\ 1 \\ 2 \\ 3 \\ 4 \\ 5 \end{bmatrix}^{T} \qquad \begin{bmatrix} 0 \\ 1 \\ 2 \\ 3 \\ 4 \\ 5 \end{bmatrix}$$

$$\begin{bmatrix} 0 & 1 & 2 \\ 3 & 4 & 5 \end{bmatrix} \qquad \begin{bmatrix} 0 & 1 \\ 2 & 3 \\ 4 & 5 \end{bmatrix}$$

$$\begin{bmatrix} 0 & 1 & 2 \\ 3 & 4 & 5 \end{bmatrix} \qquad \begin{bmatrix} 0 & 1 \\ 2 & 3 \\ 4 & 5 \end{bmatrix}$$
(a) 1×6 (b) 2×3 (c) 3×2 (d) 6×1

Table: Processor Grid Shapes with 6 Processors



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Introduction to Distributed Matrices

Distributed Matrices

The data structure is a special R class (in the OOP sense) called ddmatrix. It is the "under the rug" storage for a block-cyclic matrix distributed onto a 2-dimensional processor grid.

with prototype

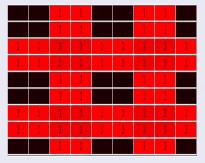
```
\label{eq:new("ddmatrix")} \text{new("ddmatrix")} = \begin{cases} \textbf{Data} &= \texttt{matrix}(0.0) \\ \textbf{dim} &= \texttt{c}(1,1) \\ \textbf{ldim} &= \texttt{c}(1,1) \\ \textbf{bldim} &= \texttt{c}(1,1) \\ \textbf{CTXT} &= 0.0 \end{cases}
```



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Distributed Matrices: The Data Structure

Example: an 9×9 matrix is distributed with a "block-cycling" factor of 2×2 on a 2×2 processor grid:



$$= \begin{cases} \textbf{Data} &= \texttt{matrix}(...) \\ \textbf{dim} &= \texttt{c}(9, 9) \\ \textbf{Idim} &= \texttt{c}(...) \\ \textbf{bIdim} &= \texttt{c}(2, 2) \\ \textbf{CTXT} &= 0 \end{cases}$$

See http://acts.nersc.gov/scalapack/hands-on/datadist.html



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Introduction to Distributed Matrices

Understanding Dmat: Global Matrix



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Introduction to Distributed Matrices

DMAT: 1-dimensional Row Block

$$X = \begin{bmatrix} x_{11} & x_{12} & x_{13} & x_{14} & x_{15} & x_{16} & x_{17} & x_{18} & x_{19} \\ x_{21} & x_{22} & x_{23} & x_{24} & x_{25} & x_{26} & x_{27} & x_{28} & x_{29} \\ x_{31} & x_{32} & x_{33} & x_{34} & x_{35} & x_{36} & x_{37} & x_{38} & x_{39} \\ \hline x_{41} & x_{42} & x_{43} & x_{44} & x_{45} & x_{46} & x_{47} & x_{48} & x_{49} \\ x_{51} & x_{52} & x_{53} & x_{54} & x_{55} & x_{56} & x_{57} & x_{58} & x_{59} \\ \hline x_{61} & x_{62} & x_{63} & x_{64} & x_{65} & x_{66} & x_{67} & x_{68} & x_{69} \\ \hline x_{71} & x_{72} & x_{73} & x_{74} & x_{75} & x_{76} & x_{77} & x_{78} & x_{79} \\ x_{81} & x_{82} & x_{83} & x_{84} & x_{85} & x_{86} & x_{87} & x_{88} & x_{89} \\ x_{91} & x_{92} & x_{93} & x_{94} & x_{95} & x_{96} & x_{97} & x_{98} & x_{99} \end{bmatrix}$$

Processor grid =
$$\begin{vmatrix} 0 & 1 \\ 2 & 3 \end{vmatrix} = \begin{vmatrix} (0,0) & (0,1) \\ (1,0) & (1,1) \end{vmatrix}$$



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Introduction to Distributed Matrices

DMAT: 2-dimensional Row Block

$$X = \begin{bmatrix} x_{11} & x_{12} & x_{13} & x_{14} & x_{15} & x_{16} & x_{17} & x_{18} & x_{19} \\ x_{21} & x_{22} & x_{23} & x_{24} & x_{25} & x_{26} & x_{27} & x_{28} & x_{29} \\ x_{31} & x_{32} & x_{33} & x_{34} & x_{35} & x_{36} & x_{37} & x_{38} & x_{39} \\ x_{41} & x_{42} & x_{43} & x_{44} & x_{45} & x_{46} & x_{47} & x_{48} & x_{49} \\ x_{51} & x_{52} & x_{53} & x_{54} & x_{55} & x_{56} & x_{57} & x_{58} & x_{59} \\ \hline x_{61} & x_{62} & x_{63} & x_{64} & x_{65} & x_{66} & x_{67} & x_{68} & x_{69} \\ x_{71} & x_{72} & x_{73} & x_{74} & x_{75} & x_{76} & x_{77} & x_{78} & x_{79} \\ x_{81} & x_{82} & x_{83} & x_{84} & x_{85} & x_{86} & x_{87} & x_{88} & x_{89} \\ x_{91} & x_{92} & x_{93} & x_{94} & x_{95} & x_{96} & x_{97} & x_{98} & x_{99} \end{bmatrix}$$

Processor grid =
$$\begin{vmatrix} 0 & 1 \\ 2 & 3 \end{vmatrix} = \begin{vmatrix} (0,0) & (0,1) \\ (1,0) & (1,1) \end{vmatrix}$$



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Introduction to Distributed Matrices

DMAT: 1-dimensional Row Cyclic

$$X = \begin{bmatrix} X_{11} & X_{12} & X_{13} & X_{14} & X_{15} & X_{16} & X_{17} & X_{18} & X_{19} \\ X_{21} & X_{22} & X_{23} & X_{24} & X_{25} & X_{26} & X_{27} & X_{28} & X_{29} \\ X_{31} & X_{32} & X_{33} & X_{34} & X_{35} & X_{36} & X_{37} & X_{38} & X_{39} \\ X_{41} & X_{42} & X_{43} & X_{44} & X_{45} & X_{46} & X_{47} & X_{48} & X_{49} \\ X_{51} & X_{52} & X_{53} & X_{54} & X_{55} & X_{56} & X_{57} & X_{58} & X_{59} \\ X_{61} & X_{62} & X_{63} & X_{64} & X_{65} & X_{66} & X_{67} & X_{68} & X_{69} \\ X_{71} & X_{72} & X_{73} & X_{74} & X_{75} & X_{76} & X_{77} & X_{78} & X_{79} \\ X_{81} & X_{82} & X_{83} & X_{84} & X_{85} & X_{86} & X_{87} & X_{88} & X_{89} \\ X_{91} & X_{92} & X_{93} & X_{94} & X_{95} & X_{96} & X_{97} & X_{98} & X_{99} \end{bmatrix}$$

Processor grid =
$$\begin{vmatrix} 0 & 1 \\ 2 & 3 \end{vmatrix} = \begin{vmatrix} (0,0) & (0,1) \\ (1,0) & (1,1) \end{vmatrix}$$



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Introduction to Distributed Matrices

DMAT: 2-dimensional Row Cyclic

$$x = \begin{bmatrix} x_{11} & x_{12} & x_{13} & x_{14} & x_{15} & x_{16} & x_{17} & x_{18} & x_{19} \\ x_{21} & x_{22} & x_{23} & x_{24} & x_{25} & x_{26} & x_{27} & x_{28} & x_{29} \\ x_{31} & x_{32} & x_{33} & x_{34} & x_{35} & x_{36} & x_{37} & x_{38} & x_{39} \\ x_{41} & x_{42} & x_{43} & x_{44} & x_{45} & x_{46} & x_{47} & x_{48} & x_{49} \\ x_{51} & x_{52} & x_{53} & x_{54} & x_{55} & x_{56} & x_{57} & x_{58} & x_{59} \\ x_{61} & x_{62} & x_{63} & x_{64} & x_{65} & x_{66} & x_{67} & x_{68} & x_{69} \\ x_{71} & x_{72} & x_{73} & x_{74} & x_{75} & x_{76} & x_{77} & x_{78} & x_{79} \\ x_{81} & x_{82} & x_{83} & x_{84} & x_{85} & x_{86} & x_{87} & x_{88} & x_{89} \\ x_{91} & x_{92} & x_{93} & x_{94} & x_{95} & x_{96} & x_{97} & x_{98} & x_{99} \end{bmatrix}$$

Processor grid =
$$\begin{vmatrix} 0 & 1 \\ 2 & 3 \end{vmatrix} = \begin{vmatrix} (0,0) & (0,1) \\ (1,0) & (1,1) \end{vmatrix}$$



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Introduction to Distributed Matrices

DMAT: 2-dimensional Block-Cyclic

$$x = \begin{bmatrix} x_{11} & x_{12} & x_{13} & x_{14} & x_{15} & x_{16} & x_{17} & x_{18} & x_{19} \\ x_{21} & x_{22} & x_{23} & x_{24} & x_{25} & x_{26} & x_{27} & x_{28} & x_{29} \\ x_{31} & x_{32} & x_{33} & x_{34} & x_{35} & x_{36} & x_{37} & x_{38} & x_{39} \\ x_{41} & x_{42} & x_{43} & x_{44} & x_{45} & x_{46} & x_{47} & x_{48} & x_{49} \\ x_{51} & x_{52} & x_{53} & x_{54} & x_{55} & x_{56} & x_{57} & x_{58} & x_{59} \\ x_{61} & x_{62} & x_{63} & x_{64} & x_{65} & x_{66} & x_{67} & x_{68} & x_{69} \\ x_{71} & x_{72} & x_{73} & x_{74} & x_{75} & x_{76} & x_{77} & x_{78} & x_{79} \\ x_{81} & x_{82} & x_{83} & x_{84} & x_{85} & x_{86} & x_{87} & x_{88} & x_{89} \\ x_{91} & x_{92} & x_{93} & x_{94} & x_{95} & x_{96} & x_{97} & x_{98} & x_{99} \end{bmatrix}$$

Processor grid =
$$\begin{vmatrix} 0 & 1 \\ 2 & 3 \end{vmatrix} = \begin{vmatrix} (0,0) & (0,1) \\ (1,0) & (1,1) \end{vmatrix}$$



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Introduction to Distributed Matrices

Understanding DMAT: Distributed with bldim = (2,2)

$$X = \begin{bmatrix} X_{11} & X_{12} & X_{13} & X_{14} & X_{15} & X_{16} & X_{17} & X_{18} & X_{19} \\ X_{21} & X_{22} & X_{23} & X_{24} & X_{25} & X_{26} & X_{27} & X_{28} & X_{29} \\ X_{31} & X_{32} & X_{33} & X_{34} & X_{35} & X_{36} & X_{37} & X_{38} & X_{39} \\ X_{41} & X_{42} & X_{43} & X_{44} & X_{45} & X_{46} & X_{47} & X_{48} & X_{49} \\ X_{51} & X_{52} & X_{53} & X_{54} & X_{55} & X_{56} & X_{57} & X_{58} & X_{59} \\ X_{61} & X_{62} & X_{63} & X_{64} & X_{65} & X_{66} & X_{67} & X_{68} & X_{69} \\ X_{71} & X_{72} & X_{73} & X_{74} & X_{75} & X_{76} & X_{77} & X_{78} & X_{79} \\ X_{81} & X_{82} & X_{83} & X_{84} & X_{85} & X_{86} & X_{87} & X_{88} & X_{89} \\ X_{91} & X_{92} & X_{93} & X_{94} & X_{95} & X_{96} & X_{97} & X_{98} & X_{99} \end{bmatrix}$$

Processor grid =
$$\begin{vmatrix} 0 & 1 & 2 \\ 3 & 4 & 5 \end{vmatrix} = \begin{vmatrix} (0,0) & (0,1) & (0,2) \\ (1,0) & (1,1) & (1,2) \end{vmatrix}$$



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X₁₃

X23

X53

X63

X93

X33

X₁₄

X24

X54

X₆₄

X94

X34

 X_{44}

X19

X29

X59

X₆₉

*X*99

X39

X49

X79

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X31

X41

X71

X81

Understanding DMAT: Local View

X32

X37

*X*₄₃ X73

Processor grid =
$$\begin{vmatrix} 0 & 1 & 2 \\ 3 & 4 & 5 \end{vmatrix}$$
 =

$$=$$
 $\begin{pmatrix} (0,0) \\ (1,0) \end{pmatrix}$

$$(1,1)$$
 $(1,2)$

 X_{16}

 X_{26}

X56 X66

*X*96

X36

X46

X86

*X*55

X95

*X*35



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Introduction to Distributed Matrices

The DMAT Data Structure

- **1** DMAT is *distributed*. No one processor owns all of the matrix.
- ② DMAT is *non-overlapping*. Any piece owned by one processor is owned by no other processors.
- OMAT can be row-contiguous or not, depending on the blocking factor used.
- OMAT is locally column-major and globally, it depends. . .
- If bldim[2] > ncol(X) and bldim[1] > nrow(X) / comm.size() then SPMD is a generalization of DMAT. Otherwise, no relation.
- **1** DMAT is confusing, but very robust.



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Introduction to Distributed Matrices

Pros and Cons of This Data Structure

Pros

 Fast for distributed matrix computations

Cons

Literally everything else

This is why we hide most of the distributed details.

The details are there if you want them (you don't want them).



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pbdDMAT

Distributed Matrix Methods

pbdDMAT has over 100 methods with *identical* syntax to R:

- `[`, rbind(), cbind(), ...
- lm.fit(), prcomp(), cov(), ...
- `%*%`, solve(), svd(), norm(), ...
- median(), mean(), rowSums(), ...

Serial Code

1 cov(x)

Parallel Code

1 cov(x)



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Comparing pbdMPI and pbdDMAT

- **pbdMPI** is MPI + some sugar.
- The SPMD data structure is not the only thing pbdMPI can handle (just a useful convention).
- **pbdDMAT** is more of a software package.
- The block-cyclic DMAT structure *must* be used for **pbdDMAT**.



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pbdDMAT

Quick Comments for Using pbdDMAT

Start by loading the package:

```
1 library(pbdDMAT, quiet = TRUE)
```

Always initialize before starting and finalize when finished:

```
init.grid() # auto-calls pbdMPI's init()
# ...
finalize()
```

- Once you have your data in the right format, the code becomes identical to serial R code. The hard part is getting the data in the right format...
- Oistributed DMAT objects will be given the suffix .dmat to visually help distinguish them from global objects. This suffix carries no semantic meaning.



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pbdDMAT Example: Old Examples Revisited

```
Sample Covariance

Serial Code

Cov.X <- cov(X)
print(Cov.X)

Parallel Code

Cov.X <- cov(X)
print(Cov.X)
```



pbdDMAT Example: Old Examples Revisited

Linear Regression Code

Serial Code

```
1 tX <- t(X)
2 A <- tX %*% X
3 B <- tX %*% y
4
5 ols <- solve(A) %*% B
6  # or
8 ols <- lm.fit(X, y)</pre>
```

Parallel Code

```
1 tX <- t(X)
2 A <- tX %*% X
3 B <- tX %*% y
4
5 ols <- solve(A) %*% B
6
7 # or
8 ols <- lm.fit(X, y)
```



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pbdDMAT Example: Generating Data

Generating Random Data

Using randomly generated matrices is the best way to "get your feet wet" with the pbd tools. You can do this in 2 ways:

- Generate a global matrix and distribute it.
- 2 Generate locally only what is needed.



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pbdDMAT Example: Generating Data

Example 1: Random Distributed Matrix Generation

Generate a global matrix and distribute it

```
library(pbdDMAT, quiet=TRUE)
  init.grid()
3
  # Common global on all processors --> distributed
  comm.set.seed(diff=FALSE)
  x <- matrix(rnorm(100), nrow=10, ncol=10)
  x.dmat <- as.ddmatrix(x)
8
  # Global on processor 0 --> distributed
  if (comm.rank() == 0) {
10
    x <- matrix(rnorm(100), nrow=10, ncol=10)
11
12
  } else {
    x <- NULL
13
14
  x.dmat <- as.ddmatrix(x)
16
  finalize()
17
```



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pbdDMAT Example: Generating Data

Example 2: Random Distributed Matrix Generation

Generate locally only what is needed

```
library(pbdDMAT, quiet=TRUE)
init.grid()

comm.set.seed(diff = TRUE) # good seeds via rlecuyer
x.dmat <- ddmatrix("rnorm", nrow=10, ncol=10)

finalize()</pre>
```



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pbdDMAT Example: Generating Data

Example 3: Random Distributed Matrix Generation

Generate locally only what is needed

```
library(pbdDMAT, quiet=TRUE)
init.grid()

zero.dmat <- ddmatrix(0, nrow=100, ncol=100)
id.dmat <- diag(1, nrow=100, ncol=100)

finalize()</pre>
```



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Example 4: Random Distributed Matrix Generation

Convert between SPMD and DMAT

```
library(pbdDEMO, quiet=TRUE)
   init.grid()
3
   comm.set.seed(diff = TRUE)
5
  N.spmd \leftarrow 1 + comm.rank()
  X.spmd <- matrix(rnorm(N.spmd * 3), ncol = 3)</pre>
8
  # convert SPMD to DMAT
9
  X.dmat <- spmd2dmat(X.spmd)</p>
10
11
12
  # convert DMAT to SPMD
13
  new.X.spmd <- dmat2spmd(X.dmat)</pre>
14
15
  # undistribute
  X <- as.matrix(X.dmat)</pre>
16
17
  finalize()
18
```



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pbdDMAT Example: Converting Between SPMD and DMAT

Distributed Matrices

pbdDEMO contains many other examples of reading and managing SPMD and DMAT data



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 - Examining the Iris Dataset
 - Cluster
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Examining the Iris Dataset

The Iris Dataset

```
rm(list = ls())
                                       # Clean environment
2
  library(pbdDMAT, quiet = TRUE) # Load library
  init.grid()
  if(comm.size() != 4)
    comm.stop("4 processors are required.")
6
  ### Load data
  X <- as.matrix(iris[, -5])</pre>
                                # Dimension 150 by 4
  X.cid <- as.numeric(iris[, 5])</pre>
                                       # True id
10
11
  ### Convert to ddmatrix
12
13
  X.dmat <- as.ddmatrix(X)
```



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Examining the Iris Dataset

Standardizing

```
### Standardized

X.std <- scale(X.dmat)

mu <- as.matrix(colMeans(X.std))

cov <- as.matrix(cov(X.std))

comm.print(mu)

comm.print(cov)</pre>
```



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Examining the Iris Dataset

Projection Onto First 2 PC's

```
1 ### SVD
2 X.svd <- svd(X.std)
3
4 ### Project on column space of singular vectors
5 A <- X.svd$u %*% diag(X.svd$d, type="ddmatrix")
6 B <- X.std %*% X.svd$v # A ~ B
7 X.prj <- as.matrix(A[, 1:2]) # Only useful for plot</pre>
```



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Cluster

Clustering

```
### Clustering
library(pmclust, quiet = TRUE)

comm.set.seed(123, diff = TRUE)

X.dmat <- X.std
PARAM.org <- set.global.dmat(K = 3)  # Preset storage
pmclustEnv$CONTROL$debug <- 0  # Disable debug
messages

PARAM.org <- initial.center.dmat(PARAM.org)
PARAM.kms <- kmeans.step.dmat(PARAM.org)  # K-means
X.kms.cid <- as.vector(.pmclustEnv$CLASS.dmat)</pre>
```



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Cluster

Cluster Validation

```
### Validation
```

- 2 X.kms.adjR <- EMCluster::RRand(X.cid, X.kms.cid)\$adjRand
- 3 comm.print(X.kms.adjR)



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Cluster

Cluster ID Variable

```
1 ### Swap classification id
2 tmp <- X.kms.cid
3 X.kms.cid[tmp == 1] <- 3
4 X.kms.cid[tmp == 2] <- 1
5 X.kms.cid[tmp == 3] <- 2</pre>
```



Plot

Plot

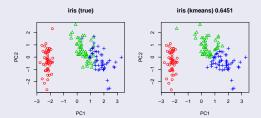
```
### Display on first 2 components
  if(comm.rank() == 0){
3
    pdf("dmat_plot.pdf")
    par(mfrow = c(2, 2))
    plot(X.prj, col = X.cid + 1, pch = X.cid,
6
          main = "iris (true)", xlab = "PC1", ylab = "PC2")
8
    plot(X.prj, col = X.kms.cid + 1, pch = X.kms.cid,
          main = paste("iris (kmeans)", sprintf("%.4f",
              X.kms.adjR)),
          xlab = "PC1", vlab = "PC2")
10
11
    dev.off()
12
13
```



•0

Plot

Plot



http://www.nics.tennessee.edu/getting-an-allocation



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Where to Learn More

The pbdDEMO package

http://cran.r-project.org/web/packages/pbdDEMO/
Vignette: http://goo.gl/eBsIh

Our Google Group:

http://group.r-pbd.org

Get an allocation with us!

http://www.nics.tennessee.edu/getting-an-allocation



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Thanks for coming!

Questions? Comments?

Please help us improve this tutorial by completing a short survey: http://www.surveymonkey.com/s/W8VLJSP



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