High Performance Computing with R

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- Writing Better R Code
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- Introduction
 - Compute Resources
 - HPC Myths



Compute Resources

Compute Resources

- Your laptop.
- Your own server.
- The cloud.
- NSF resources.



Compute Resources

XSEDE



Extreme Science and Engineering Discovery Environment

- (+) Free*!!!
- (+) Access to *massive* compute resources.
- (+) OS image and software managed by others.
- (-) 1-3 month turnaround for new applications.
- (-) Application consists of more than "here's my credit card."
- (-) Some restrictions apply.

https://www.xsede.org/allocations



HPC Myths

What is High Performance Computing (HPC)?

High Performance Computing most generally refers to the practice of aggregating computing power in a way that delivers much higher performance than one could get out of a typical desktop computer or workstation in order to solve large problems in science, engineering, or business.



HPC Myths

HPC Myths

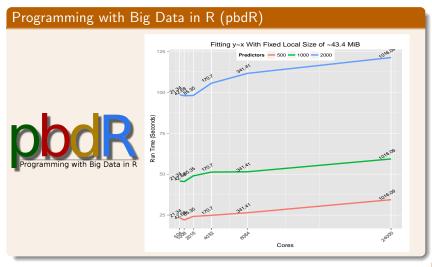
- We don't need to worry about it.
- 4 HPC requires a supercomputer.
- 4 HPC is only for academics.
- 4 HPC is too expensive.
- You can't do HPC with R.
- There's no need for HPC in biology.
- Every question requires an HPC solution.



HPC Myths



HPC Myths





HPC in the Biological Sciences

According to Manuel Peitsch, co-founder of the Swiss Institute of Bioinformatics, HPC is "essential" and plays a critical role in the life sciences in 4 ways:

- Massive amounts of data generated by modern 'omics' and genome sequencing technologies.
- Modeling increasingly large biomolecular systems using quantum mechanics/molecular mechanics and molecular dynamics.
- Modeling biological networks and simulating how network perturbations lead to adverse outcomes and disease.
- Simulation of organ function.



- Profiling and Benchmarking
 - Why Profile?
 - Profiling R Code
 - Other Ways to Profile
 - Summary



Why Profile?

Why Profile?

- Because performance matters.
- Your bottlenecks may surprise you.
- Because R is dumb.
- R users claim to be data people...so act like it!



Why Profile?

Compilers often correct bad behavior...

A Really Dumb Loop

```
int main() {
    int x, i;
    for (i=0; i<10;
        i++)
        x = 1;
    return 0;
}</pre>
```

clang -O3 example.c

clang example.c

```
main:
         .cfi_startproc
 BB#0:
        movl
                 $0, -4(\% rsp)
        movl
                 $0, -12(%rsp)
.LBB0 1:
                 $10, -12(%rsp)
        cmpl
        jge
                 .LBBO 4
 BB#2:
                 $1, -8(%rsp)
        movl
 BB#3:
                 -12(%rsp), %eax
        movl
        addl
                 $1, %eax
                 %eax, -12(%rsp)
        movl
                 .LBB0_1
        jmp
.LBB0 4:
                 $0, %eax
        movl
        ret
```



Why Profile?

R will not!

```
Dumb Loop
                                               Better Loop
  for (i in 1:n){
                                       tA \leftarrow t(A)
2
    tA \leftarrow t(A)
                                    2
     Y <- tA %*% Q
                                      for (i in 1:n){
       <- qr.Q(qr(Y))
4
                                          <- tA %*% Q
5
     Y <- A %*% Q
                                          <- qr.Q(qr(Y))
                                          <- A %*% Q
6
7
       \leftarrow qr.Q(qr(Y))
                                           <- qr.Q(qr(Y))
  }
                                   7
8
                                   8
                                      }
9 Q
                                   9
                                      Q
                                   10
```



Why Profile?

Example from the clusterGenomics Package

Exerpt from Original findW function

```
1 n <- nrow(as.matrix(dX))
2
3 while(k<=K){
4    for(i in 1:k){
5        #Sum of within-cluster dispersion:
6        d.k <- as.matrix(dX)[labX==i,labX==i]
7        D.k <- sum(d.k)
8        ...</pre>
```

Exerpt from Modified findW function

```
dX.mat <- as.matrix(dX)
n <- nrow(dX.mat)

while(k<=K){
   for(i in 1:k){
      #Sum of within-cluster dispersion:
      d.k <- dX.mat[labX==i,labX==i]
      D.k <- sum(d.k)
      ...</pre>
```

By changing just 2 lines of code, I was able to improve the speed of his method by over 350%!



Profiling R Code

Runtime Tools

Getting simple timings as a basic measure of performance is easy, and valuable.

- system.time()
- rbenchmark
- Rprof()



Profiling R Code

Performance Profiling Tools: system.time()

system.time() is a basic R utility for giving run times of expressions

```
> x <- matrix(rnorm(10000*500), nrow=10000, ncol=500)
> system.time(t(x) %*% x)
    user    system elapsed
    0.459    0.028    0.488
> system.time(crossprod(x))
    user    system elapsed
    0.234    0.000    0.234
> system.time(cov(x))[3]
elapsed
    1.428
```



Performance Profiling Tools: system.time()

Improving the rexpokit Package

```
library(rexpokitold)
system.time(expokit_dgpadm_Qmat(x))[3]
# 5.496
library(rexpokit)
system.time(expokit_dgpadm_Qmat(x))[3]
# 4.164
5.496/4.164
# 1.319885
```



Profiling R Code

Performance Profiling Tools: rbenchmark

rbenchmark is a simple package that easily benchmarks different functions:



Profiling R Code

Rprof()

A very useful tool for profiling R code

```
Rprof(filename="Rprof.out", append=FALSE, interval=0.02,
   memory.profiling=FALSE, gc.profiling=FALSE,
   line.profiling=FALSE, numfiles=100L, bufsize=10000L)
```



Profiling R Code

Rprof()

```
data(iris)
myris <- iris[1:100, ]
fam <- binomial(logit)</pre>
Rprof()
mymdl <- replicate(1, myglm <- glm(Species ~ .,
    family=fam, data=myris))
Rprof(NULL)
summaryRprof()
Rprof()
mymdl <- replicate(10, myglm <- glm(Species ~ .,
    family=fam, data=myris))
Rprof(NULL)
summaryRprof()
Rprof()
mymdl <- replicate(100, myglm <- glm(Species ~ .,</pre>
    family=fam, data=myris))
Rprof(NULL)
summaryRprof()
```



Other Ways to Profile

Other Profiling Tools

- Rprofmem()
- tracemem()
- perf (Linux)
- PAPI, TAU, ...



Profiling with **pbdPROF**

1. Rebuild **pbdR** packages

```
R CMD INSTALL
   pbdMPI_0.2-1.tar.gz \
   --configure-args= \
   "--enable-pbdPROF"
```

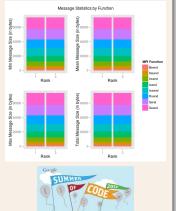
2. Run code

```
mpirun -np 64 Rscript
  my_script.R
```

3. Analyze results

```
library(pbdPROF)
prof <- read.prof(
     "profiler_output.mpiP")
plot(prof)</pre>
```

Publication-quality graphs





Summary

Summary

- Profile, profile, profile.
- Use system.time() to get a general sense of a method.
- Use **rbenchmark**'s benchmark() to compare 2 methods.
- Use Rprof() for more detailed profiling.
- Other tools exist for more hardcore applications.



- Writing Better R Code
 - Functions
 - Loops, Ply Functions, and Vectorization
 - Summary



Serial R Improvements

Slow serial code \implies slow parallel code



Functions

Function Evaluation

- In absolute terms, the abstraction is worth the price.
- Recursion sucks. Avoid at all costs.



Functions

Recursion 1

```
fib1 <- function(n)
2
     if (n == 0 || n == 1)
3
       return(1L)
     else
       return ( fib1(n-1) + fib1(n-2) )
6
7
8
9
  fib2 <- function(n)
10
11
  {
     if (n == 0 || n == 1)
12
13
       return(1L)
14
15
     f0 <- 1L
     f1 <- 1L
16
17
     i <- 1L
18
     fib <- OL
19
```



23/93

Functions

Recursion 2

```
while (i < n)
20
21
       fib <- f0 + f1
22
       f0 <- f1
23
       f1 <- fib
24
       i <- i+1
25
26
27
     return( fib )
28
29
```



Functions

Recursion 3

```
library(rbenchmark)
n < -20
benchmark(fib1(n), fib2(n))
       test replications elapsed relative
# 1 fib1(n)
                     100 2.047
                                   1023.5
# 2 fib2(n)
                     100
                           0.002
                                      1.0
system.time(fib1(45))[3]
2934.146
system.time(fib2(45))[3]
3.0616e-5
# Relative performance
2934.146/3.0616e-5
# 95837013
```



Loops, Ply Functions, and Vectorization

Loops, Plys, and Vectorization

- Loops are slow.
- apply(), Reduce() are just for loops.
- Map(), lapply(), sapply(), mapply() (and most other core ones) are not for loops.
- Vectorization is the fastest of these options, but tends to be much more memory wasteful.
- Ply functions are not vectorized.



Loops, Ply Functions, and Vectorization

Loops: Best Practices

- Profile, profile, profile.
- Evaluate how practical it is to rewrite as an lapply(), vectorize, or push to compiled code.
- Preallocate, preallocate, preallocate.



Loops, Ply Functions, and Vectorization

Loops 1

```
f1 <- function(n){
     x \leftarrow c()
2
     for (i in 1:n){
3
        x \leftarrow c(x, i^2)
5
6
7
     х
8
   }
9
10
11
   f2 <- function(n){
     x <- integer(n)
12
     for (i in 1:n){
13
        x[i] <- i^2
14
15
16
17
     х
18
```



Loops, Ply Functions, and Vectorization

Loops 2



Loops, Ply Functions, and Vectorization

Ply's: Best Practices

- Most ply's are just shorthand/higher expressions of loops.
- Generally not much faster (if at all), especially with the compiler.
- Thinking in terms of lapply() can be useful however...



Loops, Ply Functions, and Vectorization

Vectorization

- x+y
- x[, 1] <- 0
- rnorm(1000)



Loops, Ply Functions, and Vectorization

Plys and Vectorization

```
1 f3 <- function(n){
2    sapply(1:n, function(i) i^2)
3 }
4 
5 f4 <- function(n){
6    (1:n)*(1:n)
7 }</pre>
```

```
library(rbenchmark)
n <- 1000
benchmark(f1(n), f2(n), f3(n), f4(n))
   test replications elapsed relative
1 f1(n)
                  100
                        0.210
                                   210
2 f2(n)
                 100 0.096
                                    96
 f3(n)
                 100 0.084
                                    84
  f4(n)
                        0.001
                  100
                                     1
```



Loops, Ply Functions, and Vectorization

Loops, Plys, and Vectorization 1

```
f1 <- function(ind){
     sim < -0
2
     for (i in ind){
3
       if (i\%\%2 == 0)
          sum <- sum - log(i)</pre>
6
       else
          sum \leftarrow sum + log(i)
8
9
     sum
10
11
  f2 <- function(ind){
12
     sum(sapply(X=ind, FUN=function(i) if (i%%2==0) -log(i)
13
          else log(i)))
14
15
  f3 <- function(ind){
16
     sign <- replicate(length(ind), 1L)</pre>
17
     sign[seq.int(from=2, to=length(ind), by=2)] <- -1L</pre>
18
```

Loops, Ply Functions, and Vectorization

Loops, Plys, and Vectorization 2



Loops, Ply Functions, and Vectorization

Loops, Plys, and Vectorization 3



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Summary

Summary

- Avoid recursion at all costs.
- Vectorize when you can.
- Pre-allocate your data in loops.



- All About Compilers and R
 - Building R with a Different Compiler
 - The Bytecode Compiler
 - Bringing Compiled C/C++/Fortran to R
 - Summary



Building R with a Different Compiler

Better Compiler

- GNU (gcc/gfortran) and clang/gfortran are free and will compile anything, but don't produce the fastest binaries.
- Don't even bother with anything from Microsoft.
- Intel icc is very fast on intel hardware. ($\approx 20\%$ over GNU)

Better compiler \implies Faster R



Building R with a Different Compiler

Compiling R with icc and ifort

- Faster, but not painless.
- Requires Intel Composer suite license (\$\$\$)
- Improvements are most visible on Intel hardware.
- See Intel's help pages for details.



The Bytecode Compiler

The Compiler Package

- Released in 2011 (Tierney)
- Bytecode: sort of like machine code for interpreters. . .
- Improves R code speed 2-5% generally.
- Does best on loops.



The Bytecode Compiler

Bytecode Compilation

- By default, packages are not (bytecode) compiled.
- Exceptions: base (base, stats, ...) and recommended (MASS, Matrix, ...) packages.
- Downsides to package compilation: (1) bigger install size, (2) longer install process.
- Upsides: faster.



The Bytecode Compiler

Compiling a Function

```
test <- function(x) x+1
  test
  # function(x) x+1
  library(compiler)
6
  test <- cmpfun(test)</pre>
8
  test
  # function(x) x+1
  # <bytecode: 0x38c86c8>
10
11
12
  disassemble(test)
  # list(.Code, list(7L, GETFUN.OP, 1L, MAKEPROM.OP, 2L,
13
       PUSHCONSTARG. OP,
       3L, CALL.OP, OL, RETURN.OP), list(x + 1, '+',
14
  #
      list(.Code.
       list(7L, GETVAR.OP, OL, RETURN.OP), list(x)), 1))
15
```

The Bytecode Compiler



R CMD INSTALL my_package.tar.gz

The Bytecode Compiler

Compiling YOUR Package

- In the DESCRIPTION file, you can set ByteCompile: yes to require bytecode compilation (overridden by --no-byte-compile).
- Not recommended during development.
- CRAN may yell at you.



Bringing Compiled C/C++/Fortran to R

(Machine Code) Compiled Code

- Moving to compiled code can be difficult.
- But performance is very compelling.
- We will talk about one popular way on Tuesday: Rcpp.



Bringing Compiled C/C++/Fortran to R

Extra Credit

Compare the bytecode of these two functions:

```
Wasteful
   f <- function(A, Q){
      n \leftarrow ncol(A)
      for (i in 1:n) {
       tA \leftarrow t(A)
         Y <- tA %*% O
           \leftarrow qr.Q(qr(Y))
6
7
8
9
         Y <- A %*% O
         Q \leftarrow qr.Q(qr(Y))
10
11
12
```

```
Less Wasteful
```

```
1 g <- function(A, Q){
2 n <- ncol(A)
3 tA <- t(A)
4 for (i in 1:n){
5 Y <- tA %*% Q
6 Q <- qr.Q(qr(Y))
7 Y <- A %*% Q
8 Q <- qr.Q(qr(Y))
9 }
10
11 Q
12 }
```



Summary

Summary

- Compiling R itself with a different compiler can improve performance, but is non-trivial.
- The compiler package offers small, but free speedup.
- The (bytecode) compiler works best on loops.

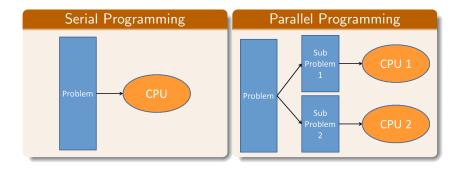


- 5 An Overview of Parallelism
 - Terminology: Parallelism
 - Choice of BLAS Library
 - Guidelines
 - Summary



Terminology: Parallelism

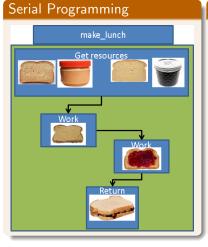
Parallelism



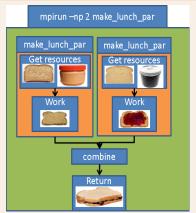


Terminology: Parallelism

Parallelism



Parallel Programming





Parallel Programming Vocabulary: Difficulty in Parallelism

- Implicit parallelism: Parallel details hidden from user Example: Using multi-threaded BLAS
- Explicit parallelism: Some assembly required...
 Example: Using the mclapply() from the parallel package
- Embarrassingly Parallel or loosely coupled: Obvious how to make parallel; lots of independence in computations. Example: Fit two independent models in parallel.
- Tightly Coupled: Opposite of embarrassingly parallel; lots of dependence in computations.
 Example: Speed up model fitting for one model.



Terminology: Parallelism

Speedup

- Wallclock Time: Time of the clock on the wall from start to finish
- Speedup: unitless measure of improvement; more is better.

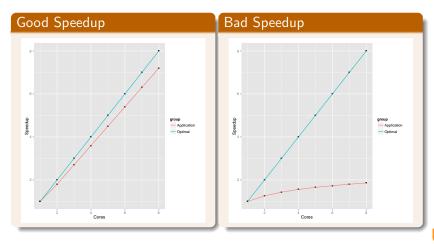
$$S_{n_1,n_2} = \frac{\text{Time for } n_1 \text{ cores}}{\text{Time for } n_2 \text{ cores}}$$

- n_1 is often taken to be 1
- In this case, comparing parallel algorithm to serial algorithm



Terminology: Parallelism

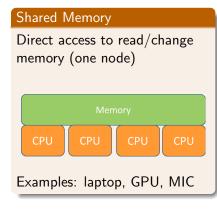
Speedup

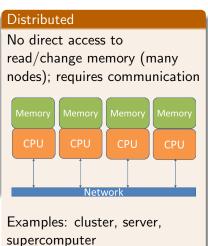




Terminology: Parallelism

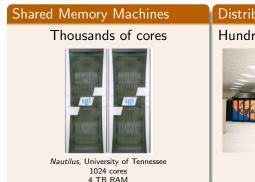
Shared and Distributed Memory Machines

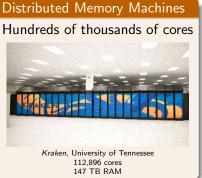




Terminology: Parallelism

Shared and Distributed Memory Machines







Terminology: Parallelism

Shared and Distributed Programming from R

Shared Memory

Examples: parallel, snow, foreach, gputools, HiPLARM

Distributed

Examples: **pbdR**, **Rmpi**, **RHadoop**, **RHIPE**

CRAN HPC Task View

For more examples, see: http://cran.r-project.org/web/views/HighPerformanceComputing.html



Choice of BLAS Library

The BLAS

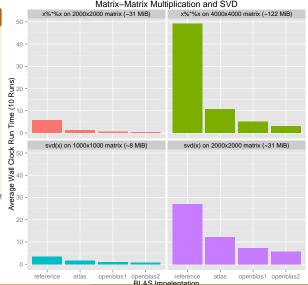
- Basic Linear Algebra Subprograms.
- Simple vector-vector (level 1), matrix-vector (level 2), and matrix-matrix (level 3).
- R uses BLAS (and LAPACK) for most linear algebra operations.
- There are different implementations available, with massively different performance.
- Several multithreaded BLAS libraries exist.



Choice of BLAS Library

Benchmark set . seed (1234) 2 3 4 5 6 7 8 9 m <- 2000 n <- 2000 x <- matrix (rnorm (m*n), m, n) object.size(x) 10 library (rbenchmark) 11 12 benchmark (x%*%x) 13 benchmark (svd(x))

Comparison of Different BLAS Implementations for Matrix–Matrix Multiplication and SVD



Choice of BLAS Library

Using openblas

On Debian and derivatives:

```
sudo apt-get install libopenblas-dev sudo update-alternatives --config libblas.so.3
```

Warning: doesn't play nice with the parallel package!



Guidelines

Independence

- Parallelism requires independence.
- Separate evaluations of R functions is embarrassingly parallel.
- For bio applications, this may mean splitting calculations by gene.



Guidelines

Portability

- Not all packages (or methods within a package) support all OS's.
- In the HPC world, that usually means "doesn't work on Windows".



Guidelines

RNG's in Parallel

- Be careful!
- Aided by rlecuyer, rsprng, and doRNG packages.



Summary

Summary

- Many kinds of parallelism available to R.
- Better/parallel BLAS is free speedup for linear algebra, but takes some work.



- 6 Shared Memory Parallelism in R
 - The parallel Package
 - The foreach Package



The parallel Package

The parallel Package

- Comes with $R \ge 2.14.0$
- Includes **multicore** + most of **snow**.
- As such, has 2 disjoint interfaces.



The parallel Package

The parallel Package: multicore Operates on fork/join paradigm. R Fork R Join

The parallel Package

The parallel Package: multicore

- (+) Data copied to child on write (handled by OS)
- (+) Very efficient.
- (-) No Windows support.
- (-) Not as efficient as threads.



The parallel Package

[1] TRUE

The parallel Package: multicore

```
mclapply(X, FUN, ...,
    mc.preschedule=TRUE, mc.set.seed=TRUE,
    mc.silent=FALSE, mc.cores=getOption("mc.cores", 2L),
    mc.cleanup=TRUE, mc.allow.recursive=TRUE)

1    x <- lapply(1:10, sqrt)
2    library(parallel)
    x.mc <- mclapply(1:10, sqrt)
5    all.equal(x.mc, x)</pre>
```



The parallel Package

The parallel Package: multicore



The parallel Package

The parallel Package: snow

- Uses sockets.
- (+) Works on all platforms.
- (-) More fiddley than mclapply().
- (-) Not as efficient as forks.



The parallel Package

The parallel Package: multicore

```
### Set up the worker processes
py.cl <- makeCluster(detectCores())
my.cl
# socket cluster with 4 nodes on host localhost
parSapply(cl, 1:5, sqrt)
stopCluster(my.cl)</pre>
```



The parallel Package

The parallel Package: Summary

All

- o detectCores()
- splitIndices()

multicore

- mclapply()
- o mcmapply()
- mcparallel()
- mccollect()
- and others...

snow

- makeCluster()
- stopCluster()
- parLapply()
- parSapply()
- and others...



The foreach Package

The foreach Package

- On Cran (Revolution Analytics).
- Main package is foreach, which is a single interface for a number of "backend" packages.
- Backends: doMC, doMPI, doParallel, doRedis, doRNG, doSNOW.



The foreach Package

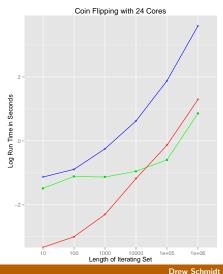
The foreach Package

- (+) Works on all platforms (with correct backend).
- (+) Can even work serial with minor notational change.
- (+) Write the code once, use whichever backend you prefer.
- (-) Really bizarre, non-R-ish synatx.
- (-) Efficiency issues ???



The foreach Package

Efficiency Issues ???



```
### Bad performance
       foreach(i=1:len)
             %dopar% tinyfun(i)
      3
        ### Expected
             performance
        foreach (i=1:ncores)
             %dopar% {
Function

    lapply

           out <-

    mclapply

                numeric(len/ncores)

    foreach

           for (j in
                1:(len/ncores))
             out[i] <-
                  tinyfun(j)
           out
      9
     10
```



The foreach Package

The foreach Package: General Procedure

- Load foreach and your backend package.
- Register your backend.
- Call foreach



The foreach Package

Using foreach: serial



The foreach Package

Using foreach: Parallel

```
library(foreach)
   library(<mybackend>)
3
  register < MyBackend > ()
5
  ### Example 1
7
8
  foreach(i=1:3) %dopar% sqrt(i)
  ### Example 2
  n <- 50
10
  reps <- 100
11
12
  x <- foreach(i=1:reps) %dopar% {
13
     sum(rnorm(n, mean=i)) / (n*reps)
14
15
```



The foreach Package

foreach backends

multicore

```
library(doParallel)
registerDoParallel(cores=ncores)
foreach(i=1:2) %dopar% Sys.getpid()
```

snow

```
library(doParallel)
cl <- makeCluster(ncores)
registerDoParallel(cl=cl)

foreach(i=1:2) %dopar% Sys.getpid()
stopCluster(cl)</pre>
```



The foreach Package

foreach Summary

- Make sure to register your backend.
- Different backends may have different performance.
- Use %dopar% for parallel foreach.
- "do", and "dopar", must appear on the same line as the foreach() call.





- Distributed Memory Parallelism
- Rmpi
- pbdMPI vs Rmpi
- Summary



Distributed Memory Parallelism

Why Distribute?

- Nodes only hold so much ram.
- Commodity hardware: $\approx 32 64$ gib.
- With a few exceptions (ff, bigmemory), R does computations in memory.
- If your problem doesn't fit in the memory of one node. . .



Distributed Memory Parallelism

Packages for Distributed Memory Parallelism in R

- Rmpi, and snow via Rmpi
- RHIPE and RHadoop ecosystem
- pbdR ecosystem (Monday)



Distributed Memory Parallelism

Hasty Explanation of MPI

- We will return to this on Monday.
- MPI = Message Passing Interface
- Recall: Distributed machines can't directly manipulate memory of other nodes.
- Can indirectly manipulate them, however. . .
- Distinct nodes collaborate by passing messages over network.



Rmpi Hello World

```
mpi.spawn.Rslaves(nslaves=2)
          2 slaves are spawned successfully. O failed.
# master (rank 0, comm 1) of size 3 is running on:
    wootabega
# slave1 (rank 1, comm 1) of size 3 is running on:
    wootabega
# slave2 (rank 2, comm 1) of size 3 is running on:
    wootabega
mpi.remote.exec(paste("I
    am", mpi.comm.rank(), "of", mpi.comm.size()))
# $slave1
 [1] "I am 1 of 3"
#
 $slave2
# [1] "I am 2 of 3"
mpi.exit()
```



Rmpi

Using Rmpi from snow

```
library(snow)
library(Rmpi)

cl <- makeCluster(2, type = "MPI")
clusterCall(cl, function() Sys.getpid())
clusterCall(cl, runif, 2)
stopCluster(cl)
mpi.quit()</pre>
```



Rmpi

Rmpi Resources

- Rmpi tutorial: http://math.acadiau.ca/ACMMaC/Rmpi/
- Rmpi manual: http:

//cran.r-project.org/web/packages/Rmpi/Rmpi.pdf



pbdMPI vs Rmpi

pbdMPI vs Rmpi

- Rmpi is interactive; pbdMPI is exclusively batch.
- **pbdMPI** is easier to install.
- **pbdMPI** has a simpler interface.
- pbdMPI integrates with other pbdR packages.



pbdMPI vs Rmpi

Example Syntax

mpi.allreduce(x, type=2)

Rmpi

pbdMPI

```
1 allreduce(x)
```

Types in R

```
1 > is.integer(1)
2 [1] FALSE
3 > is.integer(2)
4 [1] FALSE
5 > is.integer(1:2)
6 [1] TRUE
```



Summary

Summary

- Distributed parallelism is necessary when computations no longer fit in ram.
- Several options available; most go beyond the scope of this talk.
- More on pbdR Monday!



- Suppose we wish to store the square root of all integers from 1 to 10000 in a vector. Do this in each of the following ways, and compare them with **rbenchmark**:
 - for loop without initialization
 - for loop with initialization
 - Ply function
 - vectorization
- Revisit the previous example, evaluating the different implementations with Rprof().
- Ocunt the number of integer multiples of 5 or 17 which are less than 10,000,000.
 - Solve this with lapply().
 - Solve this with vectorization.
 - Solve this with mclapply() and 2 cores.



Exercises 2

The Monte Hall game is a well known "paradox" from elementary probability. From Wikipedia:

Suppose you're on a game show, and you're given the choice of three doors: Behind one door is a car; behind the others, goats. You pick a door, say No. 1, and the host, who knows what's behind the doors, opens another door, say No. 3, which has a goat. He then says to you, "Do you want to pick door No. 2?" Is it to your advantage to switch your choice?

Simulate one million trials of the Monte Hall game on 2 cores, switching doors every time, to computationally verify the elementary probability result. Compare the run time against the 1 core run time.



Exercises 3

The following is a more substantive example that utilizes multiple cores to perform a real analysis task. Run and evaluate this example. The example is modified from an example of Wei-Chen's from the pbdDEMO package. There are 148 EIAV sequences in the data set. They are sequencing from multiple blood serum collected longitudinally from one EIA horse over periodical fever cycles after EIAV infection. The virus population evolved within the sick horse over time. Some subtype can break the horse's immune system. It was to identify how many subtypes were evolving within the horse, which type is associated with disease early onset, where/which sample/time point to isolate that subtype virus. Moreover, which mutated region of sequence was critical for that subtype in order to break the immune system.



```
library(phyclust, quietly = TRUE)
  library(parallel)
3
  ### Load data
  data.path <- paste(.libPaths()[1],</pre>
       "/phyclust/data/pony524.phy", sep = "")
  pony.524 <- read.phylip(data.path)</pre>
  X <- pony.524$org
  KO <- 1
  Ka <- 2
10
  ### Find MLEs
12 ret.KO <- find.best(X, KO)</pre>
  ret.Ka <- find.best(X, Ka)
  LRT <- -2 * (ret.Ka$logL - ret.KO$logL)
15
      The user defined function
  FUN <- function(jid){
```

```
18
     X.b <- bootstrap.seq.data(ret.K0)$org</pre>
19
     ret.KO <- phyclust(X.b, KO)
20
     repeat {
21
       ret.Ka <- phyclust(X.b, Ka)
22
       if(ret.Ka$logL > ret.KO$logL){
23
         break
24
25
     }
26
27
     LRT.b <- -2 * (ret.Ka$logL - ret.K0$logL)
28
     I.R.T. b
29
30
31
  ### Task pull and summary
  ret <- mclapply(1:100, FUN)
  LRT.B <- unlist(ret)</pre>
  cat("KO: ", KO, "\n",
35
       "Ka: ", Ka, "\n",
36
```



```
37     "logL K0: ", ret.K0$logL, "\n",
38     "logL Ka: ", ret.Ka$logL, "\n",
39     "LRT: ", LRT, "\n",
40     "p-value: ", mean(LRT > LRT.B), "\n", sep = "")
```







Important Topics Not Discussed Here

- Distributed computing (for real) pbdR on Monday.
- Utilizing compiled code Rcpp on Tuesday.
- Multithreading.
- GPU's and MIC's.
- R+Hadoop.



Thanks for coming!

Questions?

