Practice 3

COMP9021, Trimester 1, 2019

1 Finding particular sequences of prime numbers

Write a program **consecutive_primes.py** that finds all sequences of 6 consecutive prime 5-digit numbers, say (a, b, c, d, e, f), with b = a + 2, c = b + 4, d = c + 6, e = d + 8, and f = e + 10. So a, b, c, d, e and f are all 5-digit prime numbers and no number between a and b, between b and c, between c and d, between d and e, and between e and f is prime.

The expected output is:

The solutions are:

13901	13903	13907	13913	13921	13931
21557	21559	21563	21569	21577	21587
28277	28279	28283	28289	28297	28307
55661	55663	55667	55673	55681	55691
68897	68899	68903	68909	68917	68927

2 Finding particular sequences of triples

Write a program triples_1.py that finds all triples of positive integers (i, j, k) such that i, j and k are two digit numbers, no digit occurs more than once in i, j and k, and the set of digits that occur in i, j or k is equal to the set of digits that occur in the product of i, j and k.

The expected output is:

```
20 x 79 x 81 = 127980

21 x 76 x 80 = 127680

28 x 71 x 90 = 178920

31 x 60 x 74 = 137640

40 x 72 x 86 = 247680

46 x 72 x 89 = 294768

49 x 50 x 81 = 198450

56 x 87 x 94 = 457968
```

3 Finding special triples of the form (n, n+1, n+2)

Write a program triples_2.py that finds all triples of consecutive positive three-digit integers each of which is the sum of two squares, that is, all triples of the form (n, n + 1, n + 2) such that:

- n, n+1 and n+2 are integers at least equal to 100 and at most equal to 999;
- each of n, n+1 and n+2 is of the form a^2+b^2 .

Hint: As we are not constrained by memory space for this problem, we might use a list that stores an integer for all indexes n in [100, 999], equal to 1 in case n is the sum of two squares, and to 0 otherwise. Then it is just a matter of finding three consecutive 1's in the list. This idea can be refined (by not storing 1s, but suitable nonzero values) to not only know that some number is of the form $a^2 + b^2$, but also know such a pair (a, b)...

The output of the program could be (the decompositions into sums of squares could differ):

```
(144, 145, 146) (equal to (0^2+12^2, 8^2+9^2, 5^2+11^2)) is a solution. (232, 233, 234) (equal to (6^2+14^2, 8^2+13^2, 3^2+15^2)) is a solution. (288, 289, 290) (equal to (12^2+12^2, 8^2+15^2, 11^2+13^2)) is a solution. (360, 361, 362) (equal to (6^2+18^2, 0^2+19^2, 1^2+19^2)) is a solution. (520, 521, 522) (equal to (14^2+18^2, 11^2+20^2, 9^2+21^2)) is a solution. (576, 577, 578) (equal to (0^2+24^2, 1^2+24^2, 17^2+17^2)) is a solution. (584, 585, 586) (equal to (10^2+22^2, 12^2+21^2, 15^2+19^2)) is a solution. (800, 801, 802) (equal to (20^2+20^2, 15^2+24^2, 19^2+21^2)) is a solution. (808, 809, 810) (equal to (18^2+22^2, 5^2+28^2, 9^2+27^2)) is a solution.
```

4 Encoding pairs of integers as natural numbers (optional)

Write a program plane_encoding.py that implements a function encode(a, b) and a function decode(n) for the one-to-one mapping from the set of pairs of integers onto the set of natural numbers, that can be graphically described as follows:

```
16
      15
            14
                   13
                         12
                   2
17
      4
             3
                         11
18
      5
             0
                   1
                         10
19
      6
             7
                   8
                          9
20
      21
            . . .
```

That is, starting from the point (0,0) of the plane, we move to (1,0) and then spiral counterclockwise:

- encode(0,0) returns 0 and decode(0) returns (0,0)
- encode(1,0) returns 1 and decode(1) returns (1,0)
- encode(1,1) returns 2 and decode(2) returns (1,1)
- encode(0,1) returns 3 and decode(3) returns (0,1)
- encode(-1,1) returns 4 and decode(4) returns (-1,1)
- encode(-1,0) returns 5 and decode(5) returns (-1,0)
- encode(-1,-1) returns 6 and decode(6) returns (-1,-1)
- encode(0,-1) returns 7 and decode(7) returns (0,-1)
- encode(1,-1) returns 8 and decode(8) returns (1,-1)
- encode(2,-1) returns 9 and decode(9) returns (2,-1)
- ...

5 Dice rolls (optional, needs a module not installed on CSE computers)

Write a program $\operatorname{dice_rolls.py}$ that prompts the user twice, for strictly positive integers s_1, \ldots, s_k intended to represent the number of sides of some dice, and for an integer N meant to represent the number of times these dice should be cast. If the first input is empty, then a single six-sided die will be used. If the first input is not empty, then any part of it which is not a strictly positive integer will be replaced by 6 (so for instance, inputting 12 0 3 -1 python 4 5A is equivalent to inputting 12 6 3 6 6 4 6). If the second input is empty or is not a strictly positive integer, then the number of rolls will be set to 1,000.

Here are possible interactions:

```
$ python3 dice_rolls.py
Enter N strictly positive integers (number of sides of N dice):
You did not enter any value, a single standard six-sided die will be rolled.

Enter the desired number of rolls:
Input was not provided or invalid, so the default value of 1,000 will be used.
$ python3 dice_rolls.py
Enter N strictly positive integers (number of sides of N dice): 2 0 3 python
Some of the values, incorrect, have been replaced with the default value of 6.

Enter the desired number of rolls: 0
Input was not provided or invalid, so the default value of 1,000 will be used.
$ python3 dice_rolls.py
Enter N strictly positive integers (number of sides of N dice): 2 4 2 7 3

Enter the desired number of rolls: 2000
```

The program should generate N times k random numbers between 1 and s_1, \ldots, s_k , respectively, sum them up, and display the N sums in the form of a histogram, created as an object of class Bar of the pygal module, that can be displayed in a browser by opening a file named dice_rolls.svg—check out render_to_file(). To create the histogram from the N sums, check out add(). The histogram should have—check out the Style class from the pygal.style module:

- as title for the histogram, Simulation for N rolls of the dice: L where L is the ordered list of the number of sides of the dice:
- as labels on the x-axis, all possible sums;
- as title for the x-axis, Possible sums;
- the major labels of the y-axis having a font size of 12 pt;
- as title for the y-axis, Counts;

- tooltips displaying, besides the count, Frequency: f where f is the count divided by N, displayed with 2 digits after the decimal point;
- bars having the colour whose rgb code is #228B22;
- no legend.

Here is one possible such histogram obtained with 2 4 2 7 3 as first input and 2000 as second input, with the cursor hovering over the bar for the sum of 13.

