# FeedForward Neural Networks

Course 3, Module 3, Lesson 1



#### **Feedforward Neural Networks**

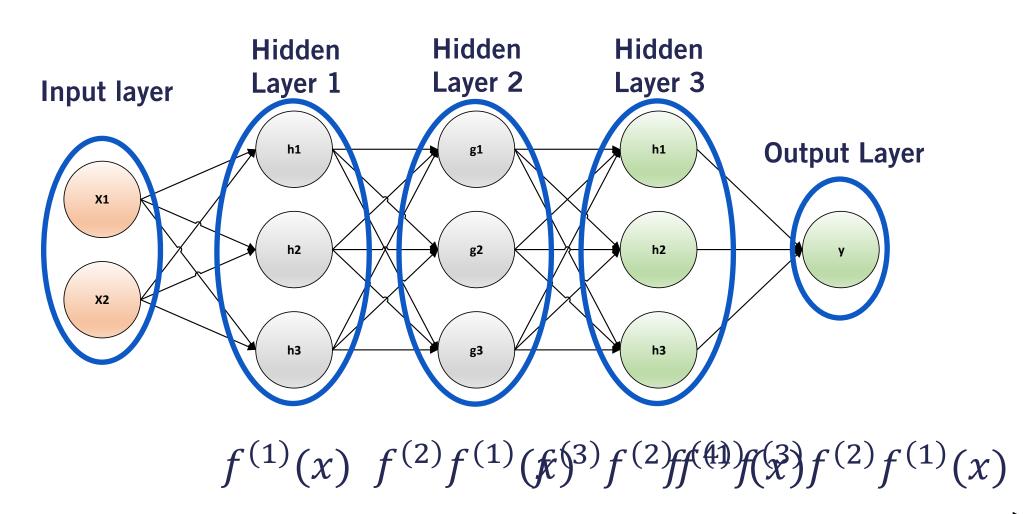
 A Feedforward Neural Network defines a mapping from input x to output y as:

$$y = f(x; \theta)$$
 learned parameters

 An N layer FNN is represented as the function composition:

$$f(x;\theta) = f^{(N)} \left( f^{(N-1)} \left( \dots f^{(2)} \left( f^{(1)}(x) \right) \right) \right)$$

# Feedforward Neural Networks: Example



#### **Feedforward Neural Networks**

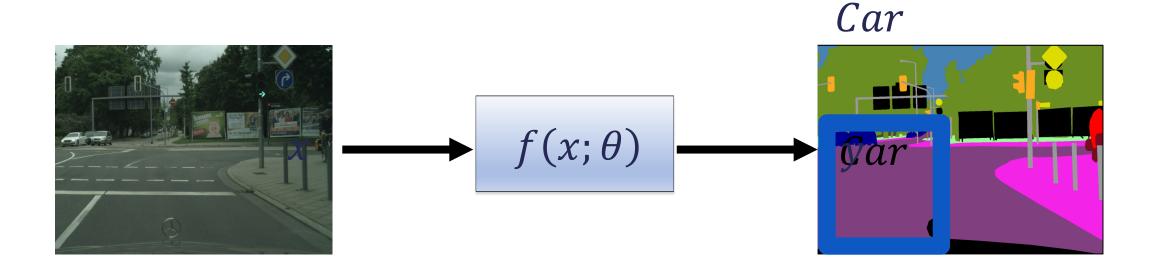
$$f(x;\theta) = f^{(N)} \left( f^{(N-1)} \left( \dots f^{(2)} \left( f^{(1)}(x) \right) \right) \right)$$

- x is called the input layer
- The final function  $f^{(N)}$  is called the **output layer**
- The functions  $f^{(1)}$  to  $f^{(N-1)}$  are called the **hidden layers**

# **Feedforward Neural Networks**

hard to model proves 5

- Functions to estimate:
  - Object Classification: Image → Label
  - Object Detection: Image → Label + Location
  - Depth Estimation: Image → Depth for every pixel
  - Semantic Segmentation: Image → Label for every pixel

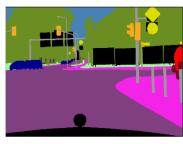


#### Mode Of Action Of Neural Networks

- Training: Give neural network examples of  $f^*(x)$ . for a wide variation of the input x. Then, optimize its parameters  $\theta$  to force  $f(x; \theta) \cong f^*(x)$
- Pairs of x and  $f^*(x)$  are called **training data**



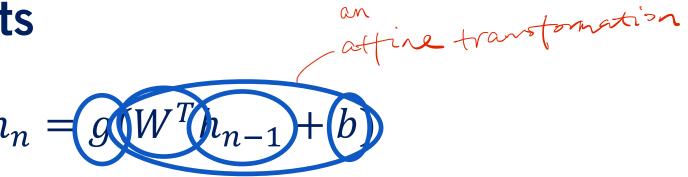
X



$$f^*(x)$$

 Only output is specified by training data! Network is free to do anything with its hidden layers

## **Hidden Units**



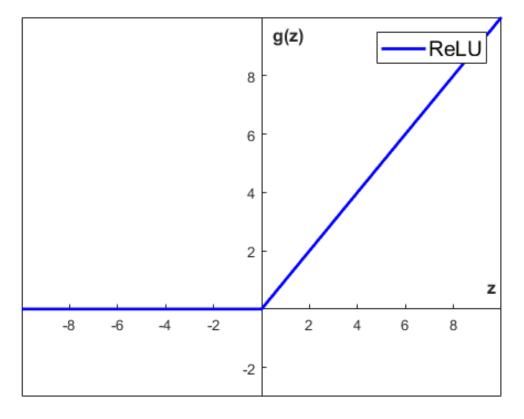
- Activation function g
- Input  $h_{n-1}$
- Weight matrix W
- Bias **b**
- Parameters  $\boldsymbol{\theta}$  are the weights and biases of all the layers of the network
- Transformed parameters passed through activation function g

### The Rectified Linear Unit: ReLU

 The ReLU hidden unit is currently the default choice of activation function for Feedforward Neural

**Networks** 

$$g(z) = \max(0, z)$$



# **Example: Hidden Layer With RELU Activation Function**

Function
$$h_{n-1} = \begin{bmatrix} -17 & 12 & -6 \\ -14 & 2 & 7 \end{bmatrix}, \quad W = \begin{bmatrix} 9 & -2 & 9 & 10 & -3 \\ -3 & 10 & 4 & 6 & 3 \end{bmatrix}, \quad b = \begin{bmatrix} -2 & -18 & -12 \\ -6 & -3 & 2 \\ -7 & 4 & -9 \\ -6 & -12 & -10 \\ -8 & 4 & -15 \end{bmatrix}$$

$$2 \times 3$$

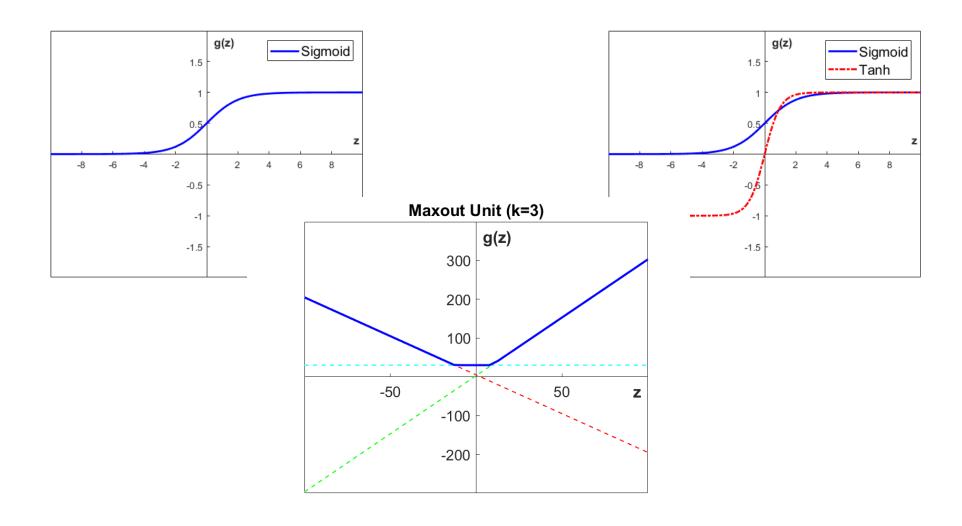
Evaluate affine transformation  $W^T h_{n-1} + b$ :

$$\begin{bmatrix} 9 & -3 \\ -2 & 10 \\ 9 & 4 \\ 10 & 6 \\ -3 & 3 \end{bmatrix} \begin{bmatrix} -17 & 12 & -6 \\ -14 & 2 & 7 \end{bmatrix} + \begin{bmatrix} -2 & -18 & -12 \\ -6 & -3 & 2 \\ -7 & 4 & -9 \\ -6 & -12 & -10 \\ -8 & 4 & -15 \end{bmatrix} = \begin{bmatrix} -113 & 84 & -87 \\ -112 & -7 & 84 \\ -216 & 120 & -35 \\ -260 & 120 & -28 \\ 1 & -26 & 24 \end{bmatrix}$$

$$h_n = \max(0, W^T h_{n-1} + b) = \begin{bmatrix} 0 & 84 & 0 \\ 0 & 0 & 84 \\ 0 & 120 & 0 \\ 0 & 120 & 0 \\ 1 & 0 & 24 \end{bmatrix}$$

5×3

## **Activation Functions**



## **Summary**

- Feedforward neural networks can be used for a variety of perception tasks related to self-driving cars
- Feedforward neural networks rely on hidden layers to implement a good approximation of a target function
- Various activation functions are available to use within hidden layers. RELU is the default baseline
- Next: Output Layers and Loss Functions