Optimization in Python

Course 4, Module 7, Lesson 3



Learning Objectives

- Know how to setup and solve a constrained optimization problem using SciPy
- Know how to pass user-defined Jacobians to the optimizer
- Know how to add parameter bounds according to the problem constraints

Minimize Function

- Many optimization algorithms available Nelder-Nead dayleg & B765
 - Specific one chosen depends on "method" parameter
- Model Jacobian passed in through "jac"
- Model constraints passed in through "constraints"
 - Different forms of constraints available
- x_0 gives initial guess for optimizer

Objective Function and Jacobian

- BFGS requires objective function as input, as well as a function to evaluate the Jacobian
- These functions will take a vector of the optimization variables as input

```
def objective function(x):
    return x[0]**2 + 4*x[0]*x[1]

def objective_jacobian(x):
    return np.array([2*x[0] + 4*x[1], 4*x[0]])
```

Result

- Upon completion, optimization returns a result variable
- The "x" member variable gives the final vector of optimized variables where the local minimum has been reached

Bounds

 Simplest constraints are inequality constraints on optimization variables, denoted as "bounds"

```
-10 \le x_0 \le 5

-3 \le x_1 \le 4 bounds = [[-10.0, 5.0], [-3.0, 4.0]]
```

- The i^{th} sub-list of the list denotes the upper and lower bounds for the i^{th} optimization variable
- Bounds are passed to "constraints" parameter in minimize function

Other Constraints

- Can also pass linear constraints and nonlinear constraints to optimizer depending on optimization algorithm
 - More details in SciPy documentation

$$\begin{bmatrix} -5 \\ 1 \end{bmatrix} \le \begin{bmatrix} 1 & 2 \\ 2 & 1 \end{bmatrix} \begin{bmatrix} x_0 \\ x_1 \end{bmatrix} \le \begin{bmatrix} 2 \\ 4 \end{bmatrix}$$

```
linear_constraint = LinearConstraint([[1, 2], [2, 1]], [2, 4])
```

 Can also combine different constraint methods in a list of constraints

Summary

- Introduced how to set up an optimization problem (L-BFGS) using SciPy
- Showed how to pass
 Jacobians and parameter
 bounds to the library's
 optimizer

```
#nlopt
import scipy.optimize as sp
import numpy as np
bounds = [[-10.0, 5.0], [-3.0, 4.0]]
x 0 = [1.0, 1.0]
linear constraint = LinearConstraint([[1, 2],
[2, 1]], [2, 4])
def objective function(x):
    return x[0]**2 + 4*x[0]*x[1]
def objective jacobian(x):
    return np.array([2*x[0] + 4*x[1], 4*x[0]])
result = sp.minimize(objective function, x 0,
method='L-BFGS-B', jac=objective jacobian,
bounds=bounds, options={'disp': True})
print(result.x)
Solution:
>>> [-8. 4.]
```



