

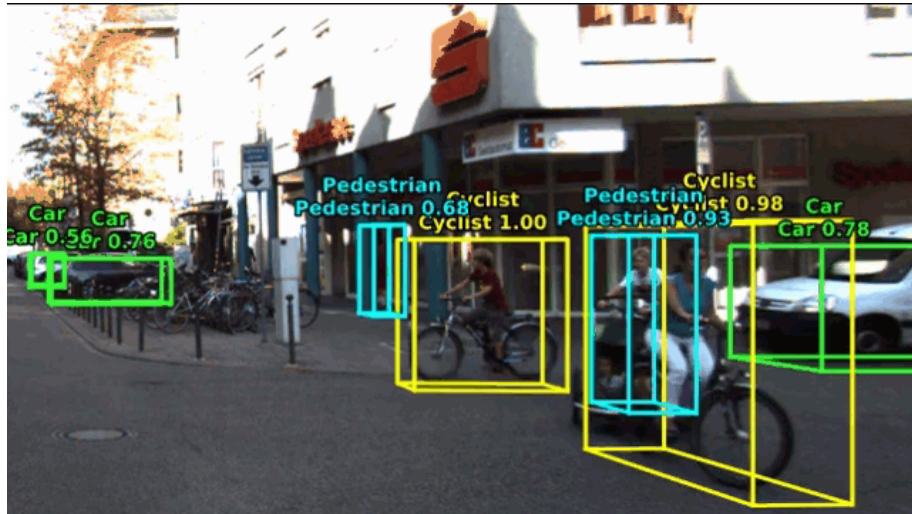
# Convolutional Neural Networks

Course 3, Module 3, Lesson 5



UNIVERSITY OF TORONTO  
FACULTY OF APPLIED SCIENCE & ENGINEERING

# ConvNets For Self-Driving Cars



Code at: <https://github.com/kujason/avod>



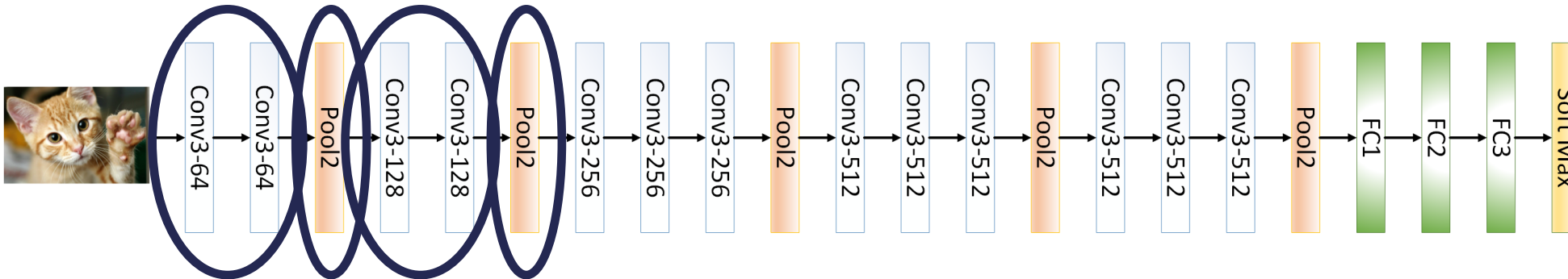
Code at: <https://github.com/oandrienko/fast-semantic-segmentation>

# Learning Objectives

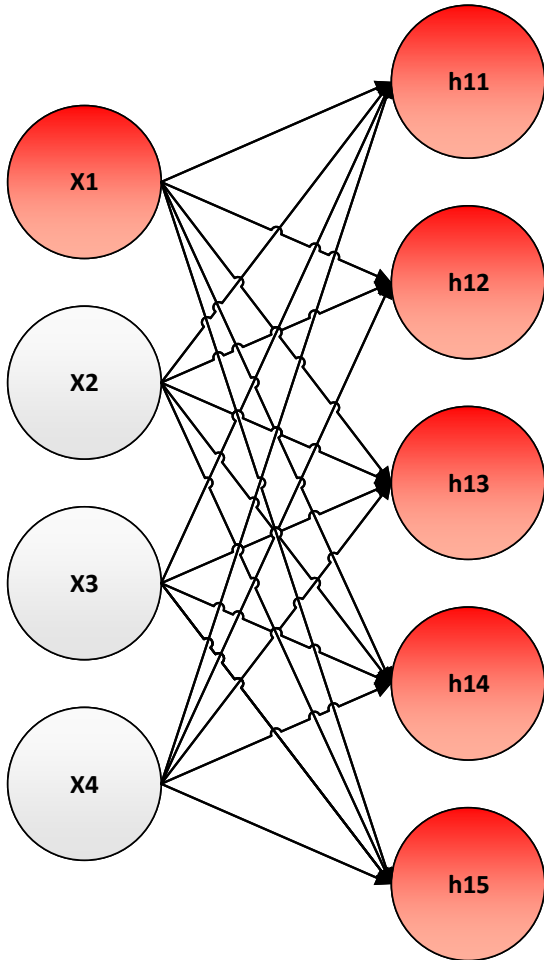
- Learn how a neural network can use cross-correlation in its hidden layers instead of general matrix multiplication, to form ConvNets
- Learn the advantages of using ConvNets over traditional neural networks for processing images

# ConvNets

- Used for processing data defined on grid
- 1D time series data, 2D images, 3D videos
- Two major type of layers:
  1. Convolution Layers
  2. Pooling Layers
- **Example: VGG 16**

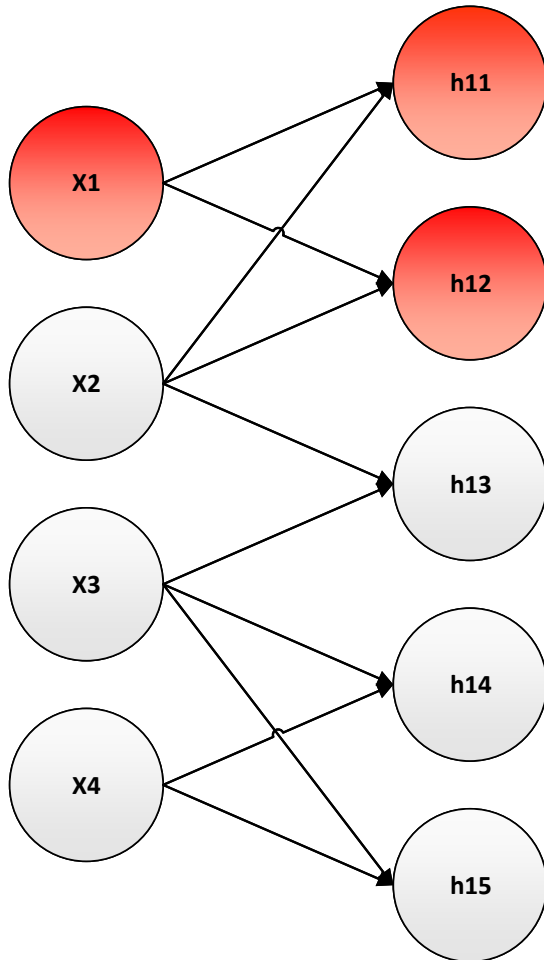


# Fully Connected VS Convolutional Layers



$$h_n = g(W^T h_{n-1} + b)$$

# Fully Connected VS Convolutional Layers



Cross-correlation

$$h_n = g(W * h_{n-1} + b)$$

# Cross Correlation

0	0	0	0	0
0	0	0	1	0
0	0	2	0	0
0	2	1	0	0
0	0	0	0	0

0	0	0	0	0
0	0	1	2	0
0	1	0	0	0
0	1	0	0	0
0	0	0	0	0

0	0	0	0	0
0	2	1	0	0
0	0	1	0	0
0	0	0	1	0
0	0	0	0	0

- **Width:** horizontal dimension of input volume
- **Height:** vertical dimension of input volume
- **Depth:** number of channels of input volume
- **Padding size:** essential to retain shape!

3

3

3

1

# Cross Correlation

0	0	0	0	0
0	0	0	1	0
0	0	2	0	0
0	2	1	0	0
0	0	0	0	0

0	0	0	0	0
0	0	1	2	0
0	1	0	0	0
0	1	0	0	0
0	0	0	0	0

0	0	0	0	0
0	2	1	0	0
0	0	1	0	0
0	0	0	1	0
0	0	0	0	0

0	-1	1
-1	-1	-1
0	-1	1

1	0	-1
-1	-1	-1
0	1	0

0	1	0
-1	1	1
-1	1	1

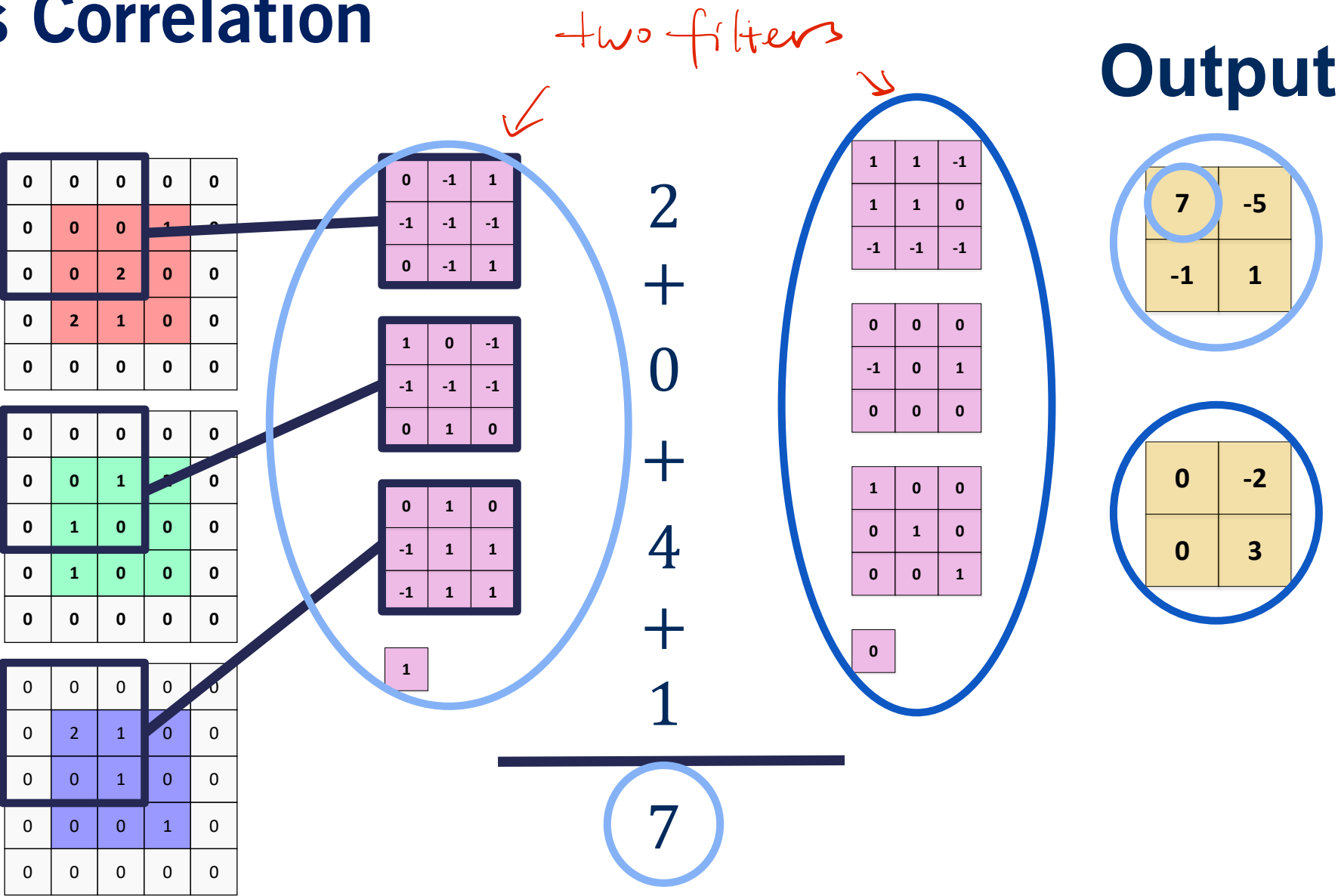
1
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**Weights**

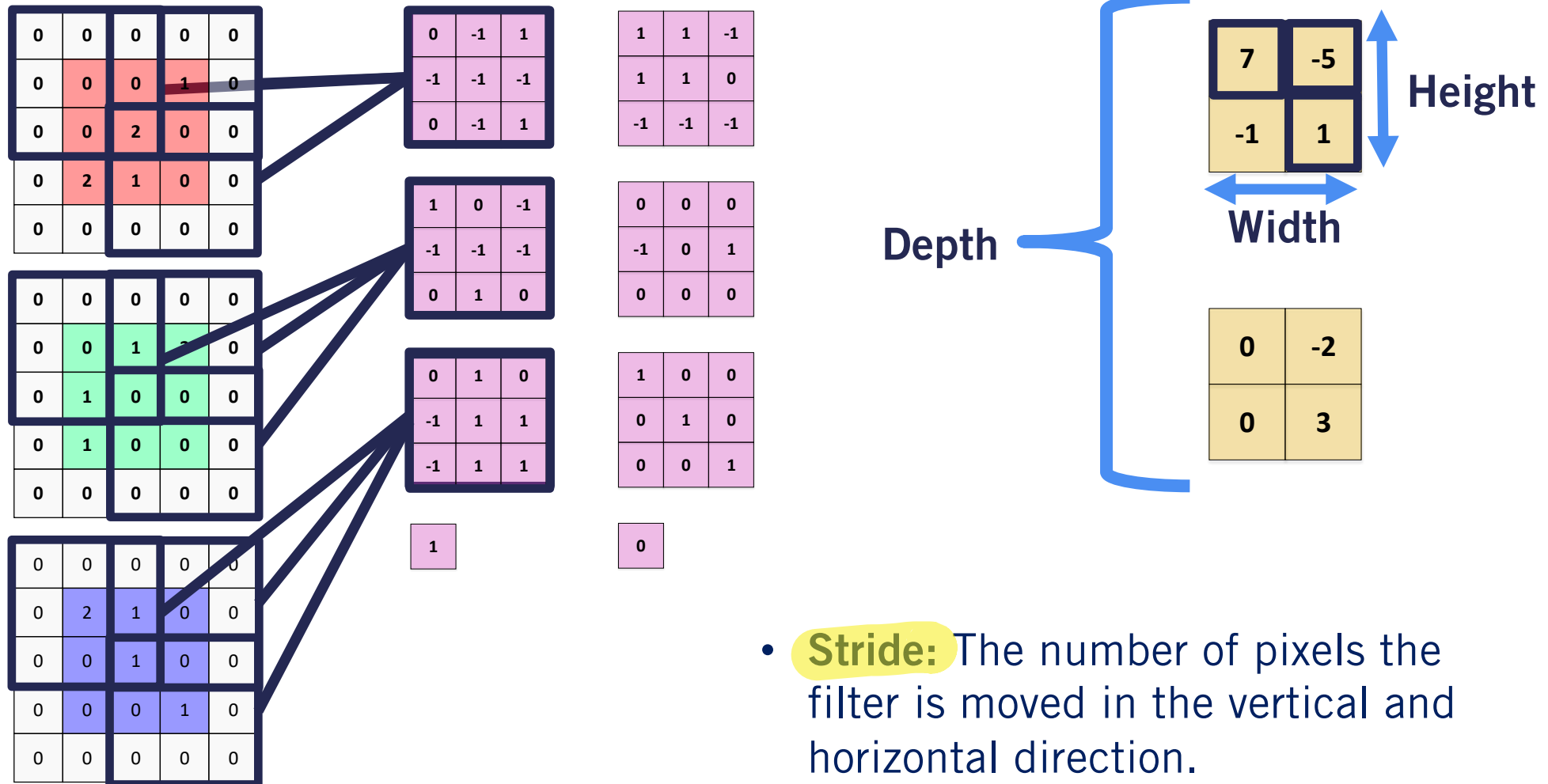
**Bias**



# Cross Correlation



# Cross Correlation



# Output Volume Shape

- Filters are size  $m \times m$
- Number of filters =  $K$
- Stride =  $S$ , Padding =  $P$

$$W_{out} = \frac{W_{in} - m + 2 \times P}{S} + 1$$

$$H_{out} = \frac{H_{in} - m + 2 \times P}{S} + 1$$

$$D_{out} = K$$

# Pooling Layers: Max Pooling

*Output invariant to small translation of the input*

$$\max(21, 8, 12, 19) = 21$$

21	8	8	12
12	19	9	7
8	10	4	3
18	9	10	9

21	12
18	10

# Output Volume Shape

- Pool size  $n \times n$
- Stride =  $S$

$$W_{out} = \frac{W_{in} - n}{S} + 1$$

$$H_{out} = \frac{H_{in} - n}{S} + 1$$

$$D_{out} = D_{in}$$

# Pooling Layers: Max Pooling

$$\max(21, 8, 12, 19) = 21$$

8	21	8	8	<del>12</del>
9	12	19	9	<del>7</del>
4	8	10	4	<del>3</del>
10	18	9	10	<del>9</del>

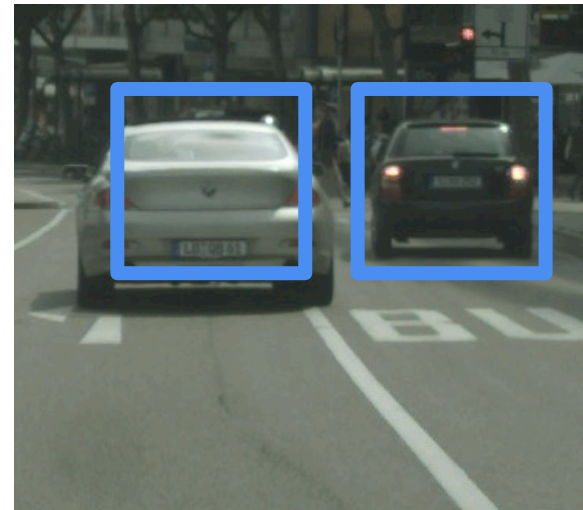
21	19
18	10

c.f.

21	12
18	10

# Advantages of ConvNets

- Convolutional neural networks are by design, a natural choice to process images
- Convolutional layers have less parameters than fully connected layers, reducing the chances of overfitting
- Convolutional layers use the same parameters to process every block of the image. Along with pooling layers, this leads to translation invariance, which is particularly important for image understanding



# Summary

- ConvNets were one of the **first** neural network models to perform well at a time where other feedforward architectures failed
- ConvNets were one of the **first** neural network models to solve important commercial applications, such as handwritten digit recognition in the early 1990s [LeCun et. al.]
- **Next: 2D Object Detection**