Trajectory Propagation

Course 4, Module 6, Lesson 1



Kinematic vs. Dynamic Model

Particle Kinematic Model

$$\ddot{x} = a$$

- Disregards mass and inertia of the robot
- Uses linear and angular velocities (and/or derivatives) as input

Particle Dynamic Model

$$M\ddot{x} + B\dot{x} = F$$

- Takes mass and inertia into consideration
- Uses forces and torques as inputs

Recall: Kinematic Bicycle Model

 x and y correspond to base link position of the robot

• θ corresponds to heading of the chassis with respect to x-axis

• δ is the steering angle input, v is the

velocity input

Do not have access to x, y directly.

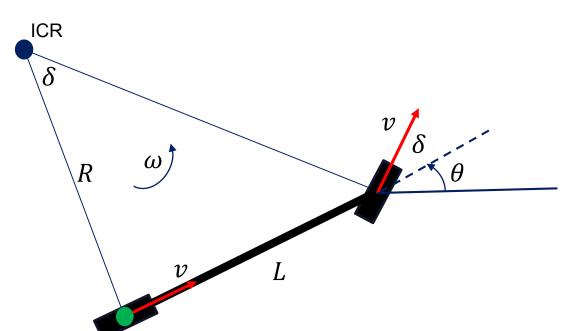
$$\dot{x} = v \cos(\theta)$$

$$\dot{y} = v \sin(\theta)$$

$$\dot{\theta} = \frac{v \tan(\delta)}{L}$$

$$\delta_{min} \le \delta \le \delta_{max}$$

$$v_{min} \le v \le v_{max}$$



Kinematic Model Discretization

- Discretization of differential equations allows for efficient computation of trajectories
- Recursive definition saves computation time

$$x_n = \sum_{i=0}^{n-1} v_i \cos(\theta_i) \Delta t = x_{n-1} + v_{n-1} \cos(\theta_{n-1}) \Delta t$$

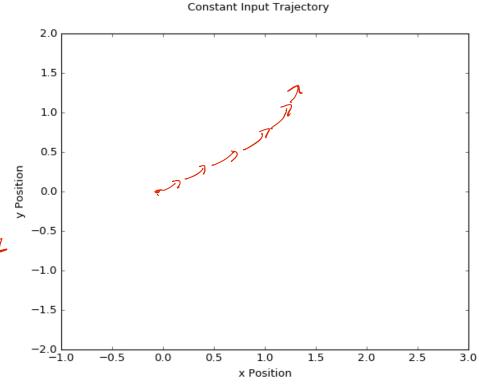
$$y_n = \sum_{i=0}^{n-1} v_i \sin(\theta_i) \Delta t = x_{n-1} + v_{n-1} \sin(\theta_{n-1}) \Delta t$$

$$\theta_n = \sum_{i=0}^{n-1} \frac{v_i \tan(\delta_i)}{L} \Delta t = \theta_{n-1} + \frac{v_{n-1} \tan(\delta_{n-1})}{L} \Delta t$$

Constant Velocity and Steering Angle Example

- For a given control sequence, we can compute the vehicle's trajectory
- Useful for prediction as well

Other guess on the cost rol inputs agents. -> estinate the future trajectory



Varying Input for Obstacle Avoidance

- To avoid obstacles, we require more complex maneuvers
- We can vary the steering input according to a steering function to navigate complex scenarios
- Main objective of local planning is to compute the control inputs (or trajectory) required to navigate to goal point without collision

