
Lenses

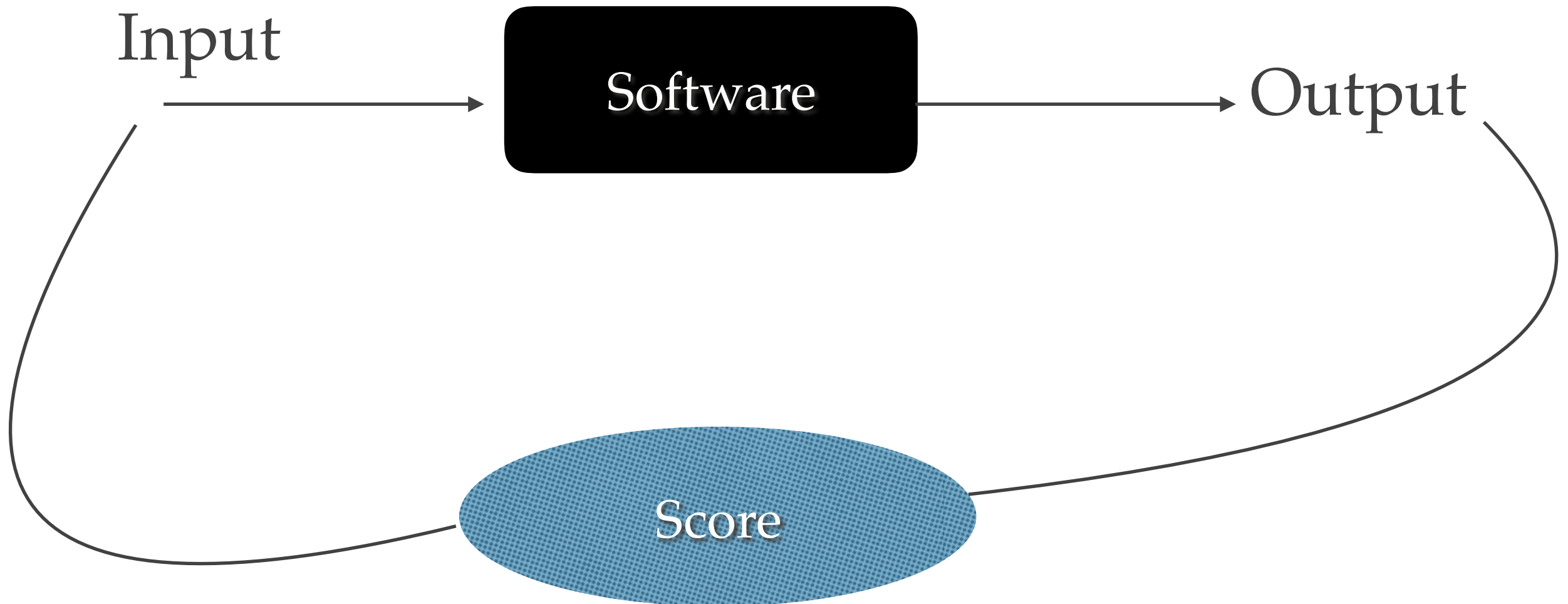
Lecture 110 of Advanced
Programming

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Andrzej Wasowski & Zhoulai Fu

IT University of Copenhagen

Automated Testing



```
Inputs = []
```

```
def score (x):
```

```
    if x is already in Inputs:  
        return 0;    //lowest score
```

```
    else:
```

```
        ...
```

```
        update Inputs to Inputs + {x}
```

```
Inputs = []
```

```
def score (x):
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```
    if x is already in Inputs:  
        return 0;  //lowest score
```

```
    else:
```

```
        ...
```

```
        update Inputs to Inputs + {x}
```

Reasoning about “score” was painful — score(x) can have different value for the same x !

Virtues of being immutable

- ❖ Safer thread
- ❖ Understandable code
- ❖ Easier to test and reason

Immutability with case classes in Scala

```
case class Street(name: String, number: Int)  
case class Address(country: String, city: String, street: Street)
```

Scala Quiz: When you create a *case class*, a _____ method is generated for your case class allowing you to return objects with modified fields.

Scala Quiz: When you create a *case class*, a **copy** method is generated for your case class allowing you to return objects with modified fields.

```
case class Street(name: String, number: Int)
case class Address(country: String, city: String, street: Street)
```

Try this exercise in a group of 2-3 (5 minutes)

```
case class Street(name: String, number: Int)
case class Address(country: String, city: String, street: Street)
```

Exercise

- ❖ Create a street
- ❖ Create an address based on the street
- ❖ Change the street number

What if the field is further nested?

```
// imperative
a.b.c.d.e += 1

// functional
a.copy(
  b = a.b.copy(
    c = a.b.c.copy(
      d = a.b.c.d.copy(
        e = a.b.c.d.e +
          1))))
```



Natural reaction

- ❖ 1. FP programming sucks
- ❖ 2. We should do something

Lens

A Lens is an abstraction from functional programming which helps to deal with a problem of updating complex immutable nested objects.

- ❖ - case class A(i : Int)
- ❖ - val v = A (5)
- ❖ How can I change “i” field to 6?
 - ❖ v.copy(i = 6)
 - ❖ Lens automates, and generalizes “copy” to deal with nested fields

Monocle Lens

- ❖ Monocle is a scala library
- ❖ - import monocle.Lens
- ❖ - To change the “a” field of the “case class A(a:Int)”:
 - ❖ `val l=Lense[A,Int](getter)(setter)`
 - ❖ - getter: A=>Int
 - ❖ - setter: Int =>A =>A

Laws are useful for testing and reasoning

“Property-based law testing is one of the most powerful tools in the scala ecosystem. “

- ❖ $x * x \geq 0$ holds for reals
- ❖ $(a + b) + c = a + (b + c)$ holds for integers
- ❖ $\text{read}(\text{write}(a, i, v), i) = v$ holds for arrays

Law of get-set for Lens

if you `get` a value from `a` and `set` it back in, the result is an object identical to the original `a`.

- ❖ - `case class A(i:int)`
- ❖ - `l.set(l.get(a)) (a) == a`

Law of set-get for Lens

if you **set** a value, you always **get** the same value back

- ❖ - case class A(i:int)
- ❖ - $l.get(l.set(i)) (v)) == I$

Laws for Lens

A `Lens` must satisfy all properties defined in `LensLaws` from the `core` module. You can check the validity of your own `Lenses` using `LensTests` from the `law` module.

From Monocle package homepage

How laws help computer scientists reasoning

Are there array a , integers b and c that satisfy the following constraint?

$$b + 2 = c, \quad f(\text{read}(\text{write}(a, b, 3), c-2)) \neq f(c-b+1)$$

Demo on Blackboard

The bigger picture – The view-update problem

**Combinators for bidirectional tree transformations: A
linguistic approach to the view-update problem**

J. Foster, Michael Greenwald, Jonathan Moore, Benjamin Pierce, Alan
Schmitt



Concrete data

The diagram consists of two blue, textured ovals. The left oval is labeled 'Concrete data' and the right oval is labeled 'Abstract view'. They are positioned horizontally, with the 'Concrete data' oval on the left and the 'Abstract view' oval on the right.

Abstract view

The view-update problem:

Update on View must be correctly reflected
on updates on Data



Concrete data



Abstract view

$$c = \left\{ \begin{array}{l} \text{Pat} \mapsto \left\{ \begin{array}{l} \text{Phone} \mapsto 333-4444 \\ \text{URL} \mapsto \text{http://pat.com} \end{array} \right\} \\ \text{Chris} \mapsto \left\{ \begin{array}{l} \text{Phone} \mapsto 888-9999 \\ \text{URL} \mapsto \text{http://chris.org} \end{array} \right\} \end{array} \right\}$$

$$a = \left\{ \begin{array}{l} \text{Pat} \mapsto 333-4444 \\ \text{Chris} \mapsto 888-9999 \end{array} \right\}$$

Basic Structures

When f is a partial function, we write $f(a) \downarrow$ if f is defined on argument a and $f(a) = \perp$ otherwise. We write $f(a) \sqsubseteq b$ for $f(a) = \perp \vee f(a) = b$. We write $\text{dom}(f)$ for $\{s \mid f(s) \downarrow\}$, the set of arguments on which f is defined. When $S \subseteq \mathcal{V}$, we write $f(S)$ for $\{r \mid s \in S \wedge f(s) \downarrow \wedge f(s) = r\}$ and $\text{ran}(f)$ for $f(\mathcal{V})$. We take function application to be strict: $f(g(x)) \downarrow$ implies $g(x) \downarrow$.

3.1 Definition [Lenses]: A *lens* l comprises a partial function $l \nearrow$ from \mathcal{V} to \mathcal{V} , called the *get function* of l , and a partial function $l \searrow$ from $\mathcal{V} \times \mathcal{V}$ to \mathcal{V} , called the *putback function*.

The intuition behind the notations $l \nearrow$ and $l \searrow$ is that the *get* part of a lens “lifts” an abstract view out of a concrete one, while the *putback* part “pushes down” a new abstract view into an existing concrete view. We often say “put a into c (using l)” instead of “apply the *putback* function (of l) to (a, c) .”

Demo on Blackboard

3.2 Definition [Well-behaved lenses]: Let l be a lens and let C and A be subsets of \mathcal{V} . We say that l is a *well behaved* lens from C to A , written $l \in C \rightleftharpoons A$, if it maps arguments in C to results in A and vice versa

$$\begin{array}{ll} l \nearrow (C) \subseteq A & (\text{GET}) \\ l \searrow (A \times C) \subseteq C & (\text{PUT}) \end{array}$$

and its *get* and *putback* functions obey the following laws:

$$\begin{array}{lll} l \searrow (l \nearrow c, c) \sqsubseteq c & \text{for all } c \in C & (\text{GETPUT}) \\ l \nearrow (l \searrow (a, c)) \sqsubseteq a & \text{for all } (a, c) \in A \times C & (\text{PUTGET}) \end{array}$$

Demo on Blackboard

Conclusions

- **We want “copy” for the sake of immutability**
- **We want “lens” to avoid nested copy**
- **Monocle is a Scala implementation**
- **Laws are to be obeyed for using lens**
- **The bigger picture is the view-update problem [foster07, morris12]**

Backup slides

An example of a lens satisfying PUTGET but not GETPUT is the following. Suppose $C = \text{string} \times \text{int}$ and $A = \text{string}$, and define l by:

$$l \nearrow (s, n) = s \qquad l \searrow (s', (s, n)) = (s', 0)$$

Then $l \searrow (l \nearrow (s, 1), (s, 1)) = (s, 0) \not\sqsubseteq (s, 1)$. Intuitively, the law fails because the *putback* function has “side effects”: it modifies information in the concrete view that is not reflected in the abstract view.

An example of a lens satisfying GETPUT but not PUTGET is the following. Let $C = \text{string}$ and $A = \text{string} \times \text{int}$, and define l by :

$$l \nearrow s = (s, 0) \qquad l \searrow ((s', n), s) = s'$$

PUTGET fails here because some information contained in the abstract view does not get propagated to the new concrete view. For example, $l \nearrow (l \searrow ((s', 1), s)) = l \nearrow s' = (s', 0) \not\sqsubseteq (s', 1)$.