

Advanced Programming

Partial Computations (Option)



PROCESS AND SYSTEM MODELS GROUP

- Primary Constructors
- Dynamic Virtual Dispatch
- Variance of Type Parameters
- Option
- Programming without pattern matching!
- For comprehensions
- In the next episode ...



The Primary Constructor

```
class Person (val name: String, val age: Int) {
println ("Just constructed a person")
def description = s"$name is $age years old"
}
```

```
1 class Person {
    private String name;
    private int age:
    public String name() { return name; }
    public int age() { return age; }
    public Person(String name, int age) {
      this.name = name:
      this.age = age:
      System.out.println("Just constructed a person");
12
13
    public String description ()
    { return name + "is " + age + " years old"; }
15 }
```

- Parameters become fields
- 'val' parameters become values, 'var' become variables
- If no parameter list, primary constructor takes none
- Constructor initializes fields and executes top-level statements of the class
- Like for all functions, parameters can take default values, reducing the need for overloading
- Note: primary constructors are used with case classes
- Known from F# and C# as well

Mentimeter: Dynamic Dispatch in Java

- printable printable printable
- square printable triangle printable
- square printable printable printable
- square square triangle triangle
- square square printable printable
- The program will crash, or fail to type check

(dynamically dispatched)

In Scala, like in Java,

all instance methods are virtual

The Problem with Covariance of Java Arrays

```
1 class A {}:
2 class B extends A {};
3 class C extends A {}:
5 class Variance {
6
                                                                        В
   static void problem () {
      B[] b = { new B() };
     A[] a = b;
      a[0] = new C():
11
12 };
```

- All type checks compile
- Runtime type error in line 11. Why?
- Not always covariance is desired.
- Covariance is good, for immutable containers storing elements of the parameter type.

Code in option/src/main/java/adpro/variance/Variance, java and the corresponding test in option/src/test/scala/adpro/variance/

Variance of Type Parameters

- Write A <: B to say that A is a **subtype of** B (values of A fit where Bs are expected)
- **Example**: if class A extends a class B then A <: B. Same for traits.
- Assume a generic type T[B]: B is a **covariant** parameter of T if for each A <: B we have that T[A] <: T[B] So we can use T[A] values where T[B]s are expected
- In Scala write T[+B] to specify that B is a covariant type parameter.
- Covariance common in pure programs. Scala lists are covariant (List[+B]).
- A is a contravariant parameter of T if whenever A <: B we have that T[B] <: T[A]</p>
- Contravariance is needed if A is a return type, and in some impure situations. In Scala, write TI-A1 to specify contravariance
- Invariance means that there is no automatic subtypes of generic type T: Invariance is default in Scala (when you omit the -/+)
- Recall that Java and C# generics also support variance of type parameters.
- Java has covariant arrays (problem). Scala has invariant arrays.

Contravariance

```
1 class Cell[-T] (init: T) {
2    private var current = init
3    def get = current
4    def set (x: T) { current = x }
5 }
6 object Cell {
7    val c1: Cell[String] = Cell[String] ("abc")
8    val c2: Cell[Any] = c1
9    c2.set (1)
10    val s: String = c1.get
11 }
```

- If cell covariant: I. 10 would assign a string to integer (like with our Java example)
- Can do things to cell[Any] that we cannot do to cell[String] (assigning a number)
- Scala compiler detects this in I. 4 (⊤ used in a contravariant position, on a value that will be assigned). It detects the **wrong design** of the Cell (if covariant).
- So cell **contravariant**, note the [-T] annotation.
- Compiler flags the assignment in I. 8 (wrong use of the cell)

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- **■** For comprehensions
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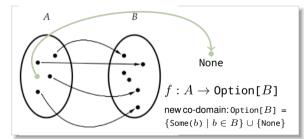


Quiz: Variance of Type Parameters

```
1 abstract class A
3 abstract class B extends A
5 // Will the following code type check if T is
6 // (a) invariant,
7 // (b) covariant,
8 // (c) contravariant ?
10 val T[A] = new T[B]
```

Partial Functions

A function $f:A\to B$ is a binary relation on sets A and B such that for every $a\in A$ there exists precisely one such $b\in B$ that $(a,b)\in f.$



- A function f is **total**, if for each $a \in A$ there exists a $b \in B$ such that f(a) = b
- A function is **partial** otherwise.

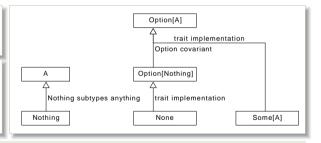
- Computations are functions
- If an argument value for a call is illegal (crash, exception) then partial function
- Object-oriented languages handle partiality with exceptions
- Advantage: handle the missing values separately, not mixing with the main logics implementation. This is valuable
- Scala has exceptions, but we don't use them in this course. Why?
- Need another way to handle partiality, but keep the main advantage of exceptions
- Idea: store the result in a special value by growing the domain, to contain the failure, and provide an API for handling failures non-locally.

Example (Option)

```
1 def mean (xs: List[Double]): Double = xs match {
   case Nil => throw new ArithmeticException ("empty list")
   case => xs.sum / xs.length
4 }
                                   // .sum and .length are standard library methods on sequences
```

What is the domain and co-domain of the function above?

```
5 sealed trait Option[+A]
6 case class Some[+A] (get: A) extends Option[A]
7 case object None extends Option[Nothing]
8 def mean (xs: List[Double]): Option[Double] =
   xs match {
   case Nil => None
  case _ => Some (xs.sun / xs.length)
12
```



Referentially transparent (!), but we still need to figure out how to **defer** error processing (like with exception handling)

Option in the Standard Library Methods (Examples)

How other types use Option

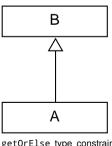
- Option is defined in the standard library
- In the course we make our own implementation for pedagogical purposes.
- trait Map[K, +V]
 - def get(key: K): Option[V]
 Optionally returns the value associated with a key
 - def find(p: ((K, V)) =>Boolean): Option[(K, V)]
 Finds the first element of the collection satisfying a predicate, if any
- class List[+A]
 - def headOption: Option[A] Optionally selects the first element.
 - def lastOption: Option[A] Optionally selects the last element.

Option API

What Option itself offers

```
1 trait Option[+A] {
    def map[B] (f :A => B) :Option[B]
    def flatMap[B] (f :A => Option[B]) :Option[B]
    def filter(f: A => Boolean) :Option[A]
    def getOrElse[B >: A] (default: => B) :B
6 }
```

- Implement these functions in homework exercises
- Let's try using them (Mentimeter)
 - List(1,2,3).headOption.map { /10.0} ?
 - List().headOption.map {_ /10.0} ?
- An interesting type parameter on getOrElse, with a constraint on B
 - Get a value of any type B from an Option[A], if B is a **super-type** of A (so implicit upcasting, as needed)
 - Another case of interesting interplay between object-oriented and functional programming type systems



getOrElse type constraint

Localized Error Handling in the Option Monad

```
1 list.headOption
2    .map (\_ / 10.0)
3    .map (\_ + 2)
4    .flatMap (something that can fail)
5    .map (something that cannot fail)
6    ...
```

- A failure can occur in line 2 (or in line 5)
- The entire code is written **ignoring** a possible failure, like with exceptions
- All the computation steps are in the Option monad (informal for now)
- Handling the error is done **arbitrarily far** (maybe in a different function) by deciding what to do, if None is received.
- A default or error value (like -1 in C) can be injected with getOrElse:

```
6 ...
7 .getOrElse (-1)
```

What does this compute?

Explain to your neighbour

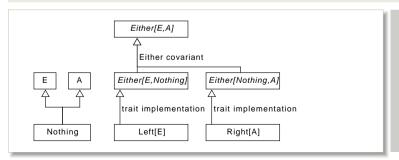
- 1 List(2,3,4)
- 2 .headOption
- 3 .filter { _ % 2 == 0 }
- 4 .map { _ / 2 }

Either: Failures with diagnostic info

Recall that exceptions carry failure data objects

```
1 sealed trait Either[+E.+A]
2 case class Left[+E](value :E) extends Either[E,Nothing]
3 case class Right[+A](value: A) extends Either[Nothing, A]
```

- Two time parameters: left (error, E) and rright (aka correct, value, A)
- Mnemonic: right is synonym for correct, which is a synonym for succesful



If you need to arow the failure info along the call-stack fashion. then E should be a collection, for instance a Either[List[Msg]], where Msg is the error message type.

For-Yield Comprehensions

```
2 Some(4)
   .flatMap (x1 => (if (x1%2==0) Some (x1/2) else None)
     .flatMap (x2 => Some (x2+1)
       .map(x3 \Rightarrow x3.toString))
```

```
_{2} Some(4).flatMap (x1 =>
   (if (x1\%2 == 0) Some (x1/2) else None).flatMap (x2 =>
     Some (x2+1).map(x3 =>
       x3.toString) ) )
```

```
For-comprehensions correspond
  to Haskell's do-ntoation or F#
  computation expressions.
```

- Work for any type with map and flatMap
- Other functions (like filter) also integrated
- Not to be confused with other uses of for in scala (mostly impure loops iterating over collections)

```
Some(4).flatMap (x1 =>
3 (if (x1\%2 == 0) Some (x1/2) else None).flatMap (x2 => 1)
                                   Some (x2+1).map(x3 =>
5 x3.toString) ) )
```

```
1 for {
2 \times 1 < - Some (4)
x^2 < -if(x^{1/2}=0) Some (x^{1/2}) else None
   x3 < - Some (x2+1)
5 } vield (x3.toString)
```

List is also a monad

For-comprehensions work on lists, too

```
1 for {
2  x <- List(3,4,5)
3  incremented = x + 1
4  duplicated <- List(incremented,incremented) if incremented % 2 == 0
5 } yield (duplicated) // map identity</pre>
```

- **Exercise:** Rewrite the above code using map and flatMap.
- '<-' translates to flatMap</p>
- '=' translates to map
- if translates to filter
- 'yield' translates to map

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In the next episode ...

- A very nice week, beautiful ideas, simple but powerful API
- We learn call-by-name and laziness
- We implement a **stream library** (the lazy parallel of Lists)
- Happy reading! and See you next week!