

$$\textcircled{1} \quad J\ddot{q} + k\dot{q} + mga \cos(q) = \tau \quad a = \frac{l}{2} \quad J = \frac{4}{3}ma^2 \quad \begin{array}{l} \text{"}\tau\text{" - input} \\ \text{"}q\text{" - output} \end{array}$$

$y = q \rightarrow$ salida del sistema (equivalencia)

$$\left. \begin{array}{l} x_1 = y = q \\ x_2 = \dot{y} = \dot{q} \end{array} \right\} \text{equivalencias y derivadas}$$

$$x_1 = q \quad \therefore \dot{x}_1 = \dot{q} \quad \therefore \dot{x}_1 = x_2$$

$$x_2 = \dot{q} \quad \therefore \dot{x}_2 = \ddot{q}$$

$$J\dot{x}_2 + kx_2 + mga \cos(x_1) = \tau$$

$$\dot{x}_2 = \left(\tau - kx_2 - mga \cos(x_1) \right) \frac{1}{J} \quad \dot{x}_1 = x_2$$

$$\dot{x}_1 = 0x_1 + x_2 + 0\tau$$

$$\dot{x}_2 = -\frac{mga \cos(x_1)}{J} - \frac{k}{J}x_2 + \frac{\tau}{J}$$

$$\dot{x} = \begin{bmatrix} 0 & 1 \\ -\frac{mga}{J} \cos(x_1) & -\frac{k}{J} \end{bmatrix} x + \begin{bmatrix} 0 \\ \frac{1}{J} \end{bmatrix} \tau$$

$$y = \begin{bmatrix} 0 & 1 \end{bmatrix} x + 0\tau$$

$$\textcircled{2} \quad L \ddot{q} + R \dot{q} + \frac{1}{c} q = E$$

"E" - input

"q" = output

$$y = q$$

$$x_1 = q$$

$$x_1 = y = q$$

$$\dot{x}_1 = \dot{q} = x_2$$

$$x_2 = \dot{y} = \dot{q}$$

$$\dot{x}_2 = \ddot{q}$$

$$L \dot{x}_2 + R x_2 + \frac{x_1}{c} = E$$

$$\dot{x}_2 = \left(E - R x_2 - \frac{x_1}{c} \right) \frac{1}{L}$$

$$\dot{x}_1 = 0 x_1 + x_2 + 0 E$$

$$\dot{x}_2 = -\frac{x_1}{cL} - \frac{R}{L} x_2 + \frac{1}{LE} E$$

$$\dot{x} = \overset{A}{\begin{bmatrix} 0 & 1 \\ -\frac{1}{cL} & -\frac{R}{L} \end{bmatrix}} x + \overset{B}{\begin{bmatrix} 0 \\ \frac{1}{L} \end{bmatrix}} E$$

$$y = \overset{C}{[0 \quad 1]} x + \overset{D}{0} E$$

$$\textcircled{3} \tau^2 \ddot{y} + 2\varepsilon\tau \dot{y} + y = x$$

"x" - input
"y" - output

$$y_1 = y$$

$$\dot{y}_1 = \dot{y} = \dot{y}_2$$

$$\ddot{y}_2 = \ddot{y}$$

$$\ddot{y}_2 \tau + 2\varepsilon\tau \dot{y}_2 + y_1 = x$$

$$\dot{y}_2 = \frac{1}{\tau} (x - 2\varepsilon\tau y_2 - y_1) \quad \dot{y}_1 = y_2$$

$$\dot{y}_1 = 0y_1 + y_2 + 0x$$

$$\dot{y}_2 = -\frac{y_1}{\tau} - 2\varepsilon y_2 + \frac{x}{\tau}$$

$$\overset{A}{x} = \begin{bmatrix} 0 & 1 \\ -\frac{1}{\tau} & -2\varepsilon \end{bmatrix} \overset{B}{y} + \begin{bmatrix} 0 \\ \frac{1}{\tau} \end{bmatrix} x$$

$$\overset{C}{y} = \begin{bmatrix} 0 & 1 \end{bmatrix} \overset{D}{y} + 0x$$