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Luleå Tekniska Universitet
F7024T Multifysik, simulering och beräkning

Assignment 3: Fluid flow past cylinder. Drag and lift forces

With supervisor
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Abstract

This work contains the result and analysis of the third COMSOL-laboratory exercise where the drag and lift force of a fluid, in this case water, on a cylinder has been simulated. It is found that the drag coefficient decreases logarithmically drastically compared to the Reynold number, going from $C_D \approx 200$ to $C_D \approx 3$ between $Re = 0$ and $Re = 50$, see fig. 1. Compared to wind tunnel data the drag coefficient seems to start at a higher value for low Reynold numbers, but decreased faster. System did not converge for Reynold numbers much higher than 300, which is around where the system should change from laminar to turbulent flow[a].

Secondly, introducing a rotation speed Ω, a negative linear dependency between the lift coefficient C_L and the dimensionless coefficient $Q = \frac{\Omega a}{V_\infty}$ could be observed. The linear plot started at $C_L = 0$ for $Q = 0$, and decreases[b] with ≈ 7 for each increase in the rotational coefficient Q.

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[a]Derived from the only table at [2]

[b]Note that the negative sign only determines the rotation direction and is of little importance.

1 Introduction

COMSOL Multiphysics® is a general-purpose software platform, based on advanced numerical methods. It is a powerful tool useful to simulate flows; fields; forces and such in models provided either by files or built directly in COMSOL.

This report is a part of a written documentation of the COMSOL-laboratory exercises made in the course Multiphysics, Simulation and Computation at Luleå University of Technology. These exercises serve as practice in formulating mathematical models to describe physical and technical problems in a way that is suitable for implementation of the finite element method.

This work contains the result and analysis of the third COMSOL-laboratory exercise where the drag and lift force of a fluid, in this case water, on a cylinder has been simulated. This is done in two distinct studies.

In the first study the drag force will be simulated in which there will be no rotational speed on the affected cylinder. In this study the inflow speed, V_∞, will be a function of the Reynold number, see eq. (1), to easily perform parametric sweeps. The drag coefficient C_D can be calculated using eq. (2), where F_D is the drag force extracted by COMSOL, A_{proj} the area projected in the direction of the stream. The assignment is to look how the Reynolds number affects the drag coefficient.

$$Re = \frac{V_\infty 2a\rho}{\mu} \qquad (1)$$

$$C_D = \frac{2F_D}{\rho V_\infty^2 A_{proj}} \qquad (2)$$

The second study will introduce a rotational velocity, Ω, to the affected cylinder. This will generate an lift force on the water surrounding the cylinder. A lift coefficient can be calculated using eq. (3) where F_D is the lift force and is calculated using eq. (4). The assign-ment is to compare how the rotational speed coefficient (Q) affects the lift coefficient C_L.

$$C_L = \frac{2F_L}{\rho V_\infty^2 A_{proj}} \qquad (3)$$

$$F_L = \rho V_\infty \Omega 2\pi a^2 \qquad (4)$$

Drag and lift coefficients are dimensionless coefficients commonly used in fluid dynamics. The drag coefficient quantifies the drag or resistance of an object in a fluid environment such as air or water, while the lift coefficient relates the lift generated by an object to the properties of the fluid surrounding the object. Both drag and lift coefficients are relevant when building or simulating objects such as the wings of an airplane or looking at the fluid movements when an object is placed in the middle of a stream.[3][4]

2 Method

2.1 General

The exact method to calculate the coefficients and simulate the system is detailed and well explained in the instructions[1], but the general way to go about it is the same as most COMSOL projects.

1. Choose system type (fluids, laminar, 2D).

2. Introduce global parameters.

3. Build geometry.

4. Set study specifications for your system type:

   - Set fluid parameters.
   - Set Boundary conditions.
   - Set initial conditions.

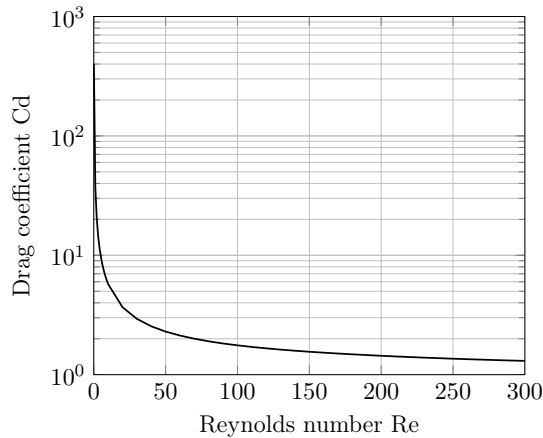5. Build a mesh grid of your geometry.

6. Compute system.

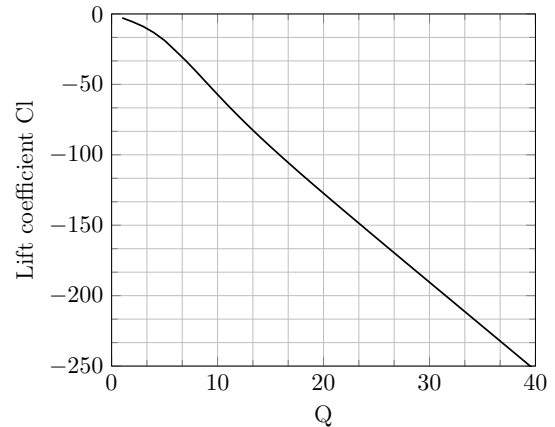*Figure 1: Drag coefficient compared to Reynold number*

Figure 2: Lift coefficient compared to $Q = \frac{\Omega a}{V_\infty}$

3   Results

3.1   Cd

Stuff

3.2   Cl

stuff

There are only two values not given or found by any formula to complete eqs. (2) and (3) is the drag and lift forces, F_D and F_L respectively. These can be found simply by integrating your system in the x, resp. y-directions.

When all values to calculate C_D and C_L are known (where simulations are run to find F_D and F_L) a global evaluation can be made on the simulation results.

4   Discussion and closing words

4.1   3.1

References

[1] Hans Åkerstedt, Multiphysics F7024T, Assignment #3a, *Fluid flow past cylinder. Drag and lift forces*, rev. 2017-03-27.

[2] *Water Flow in Tubes - Reynolds Number*, The Engineering Toolbox, http://www.engineeringtoolbox.com/ reynold-number-water-flow-pipes-d_ 574.html

2.2   Drag coefficient - C_D

To compare the drag coefficient to Reynolds number we need some way to increase the Reynolds number without messing up the system or any rules. Conveniently the only variable depending on Reynold (and vice versa) is the inflow speed, V_∞, see eq. (1). It is therefore very easy to make this speed a function of Reynolds number so that

[3] *Drag coefficient*, Wikipedia,
    https://en.wikipedia.org/wiki/Drag_
    coefficient

[4] *Lift coefficient*, Wikipedia,
    https://en.wikipedia.org/wiki/Lift_
    coefficient