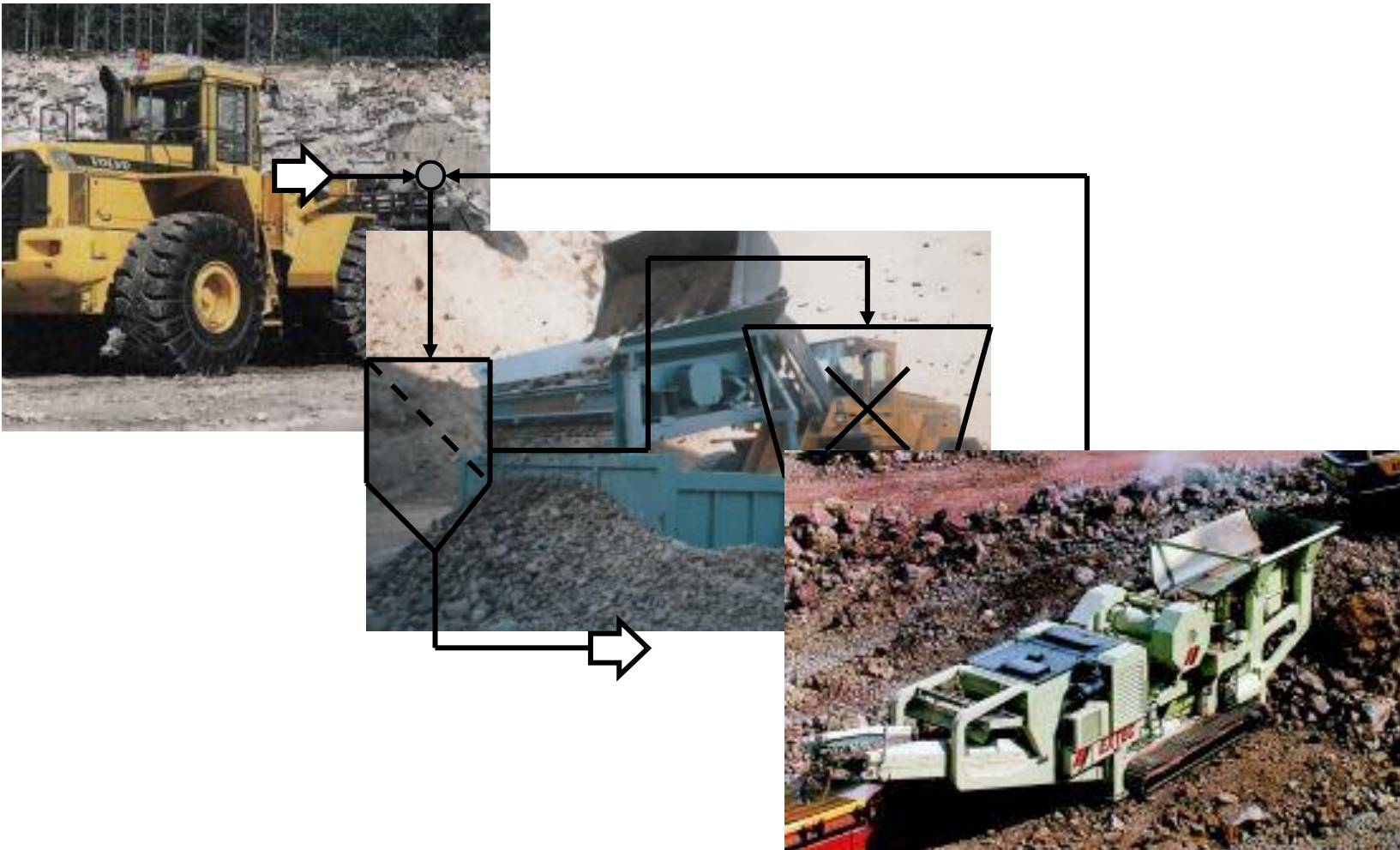


Steady-state and Dynamic Flowsheet Simulations of Solids Processes: Part I

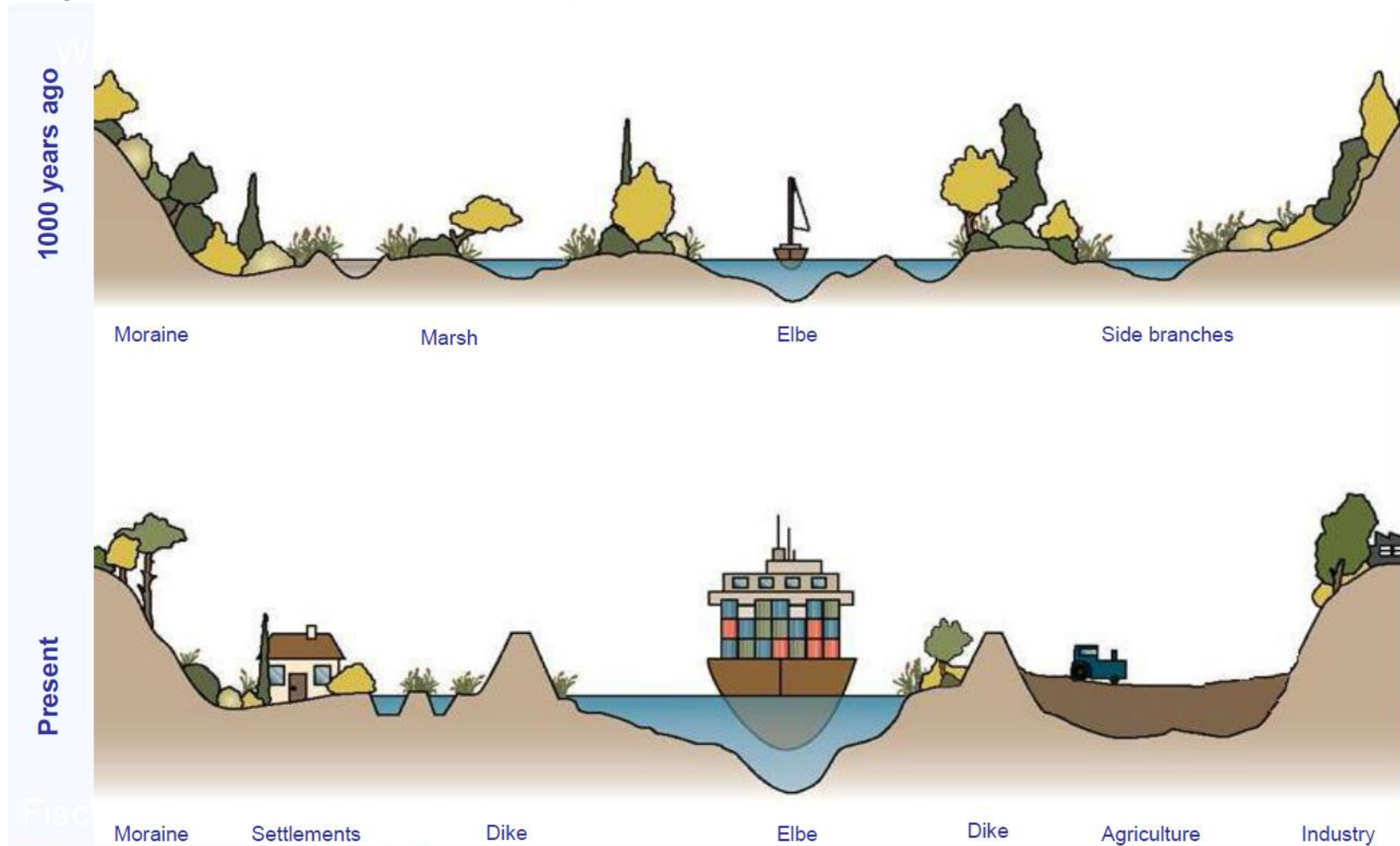
Asst.-Prof. Dr.-Ing. Maksym Dosta

dosta@tuhh.de

- Most industrial processes consist of complex interconnection of different apparatuses and production steps



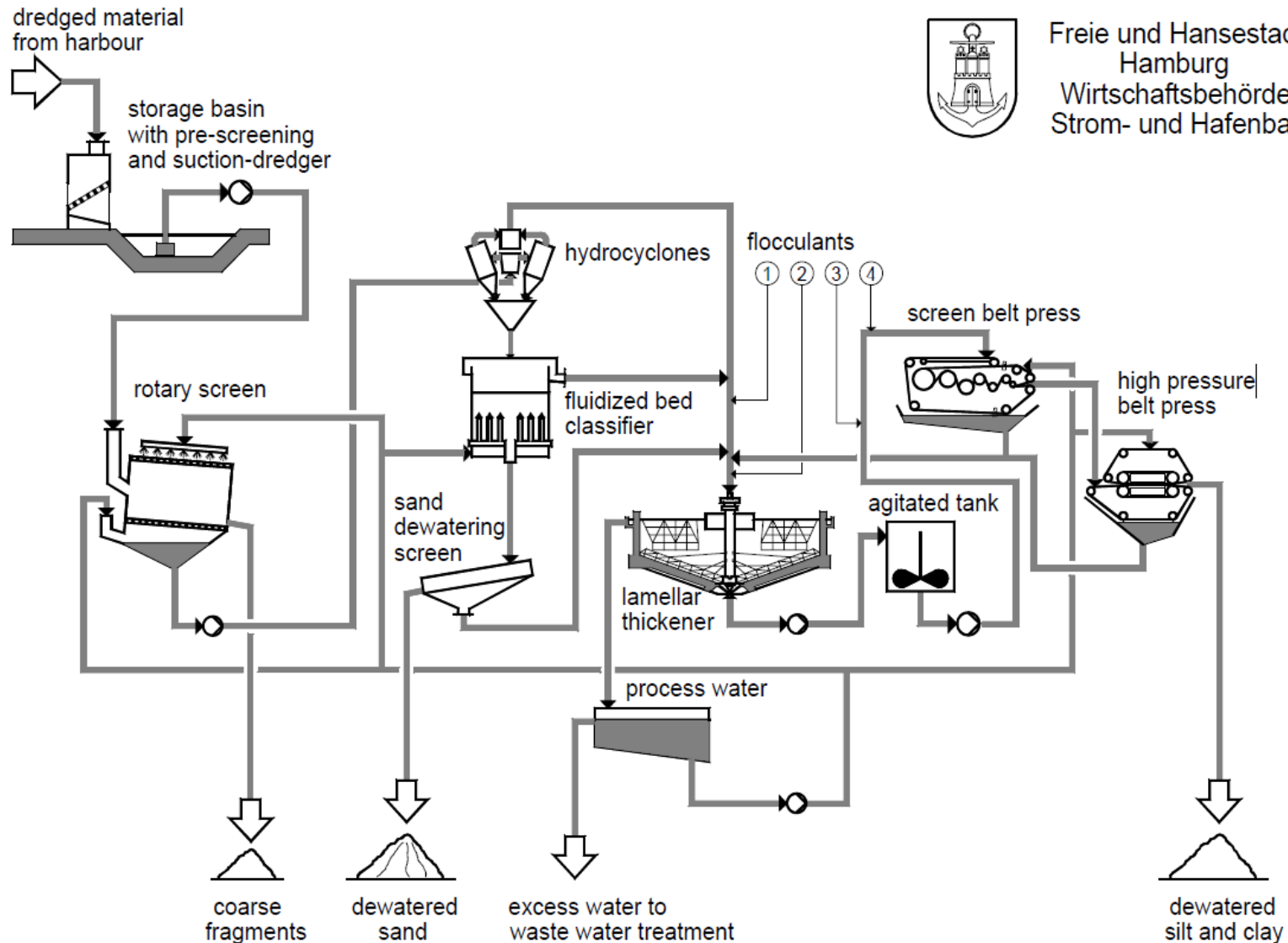
- Dredging in port Hamburg has a long tradition (first steam dredger was bought in the mid. 19th century)



A. Netzband. Sediment management concept of the port Hamburg, Hamburg Port Authority.

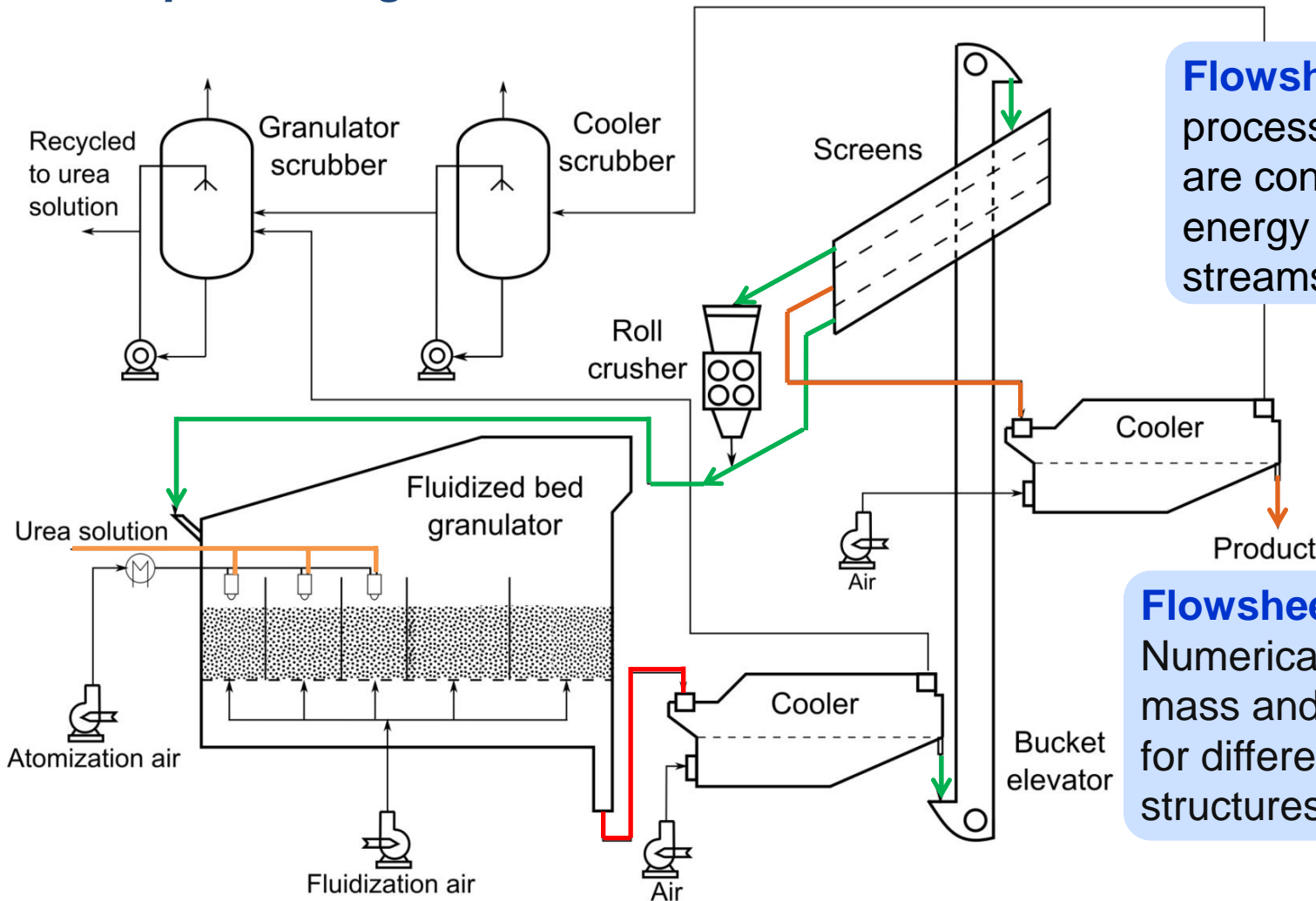


Freie und Hansestadt
Hamburg
Wirtschaftsbehörde
Strom- und Hafenbau





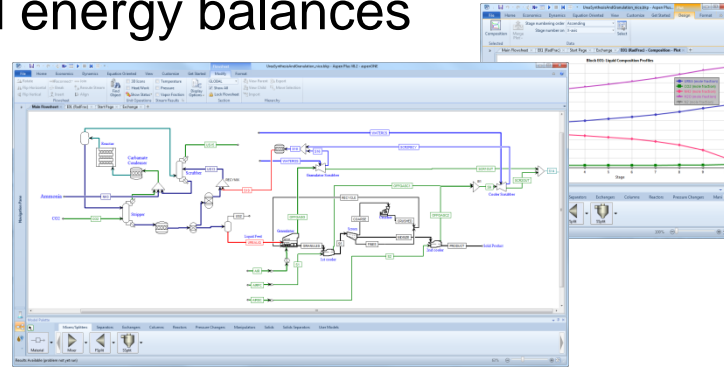
Example: Urea granulation



Flowsheet: Network of process units, which are connected by energy and material streams

Flowsheet simulation: Numerical calculation of mass and energy balances for different process structures

- Flowsheeting is:
 - the use of a computer program to model a production process
 - used to obtain mass and energy balances

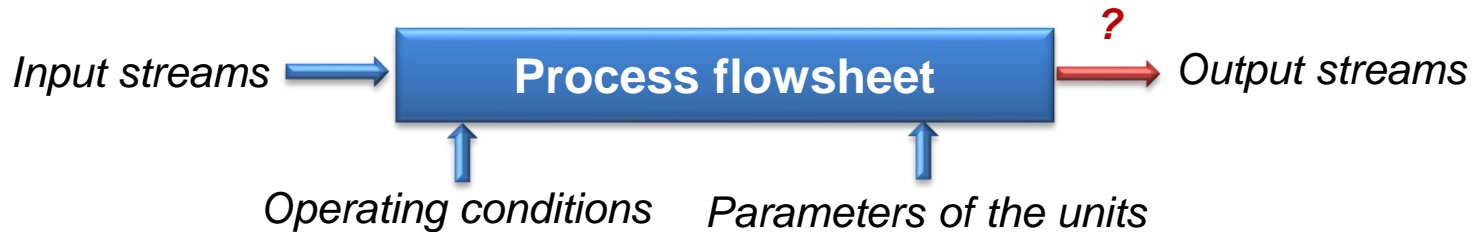


- Flowsheeting is used for:
 - planning purposes, e.g. rough sizing and costing of equipment
 - testing hypotheses, e.g. process behavior, process alternatives
 - process optimization, e.g. operating conditions, process alternatives
- What does flowsheet simulation not address:
 - detailed apparatus layout (e.g. influence of the change of the nozzle position in a granulator)

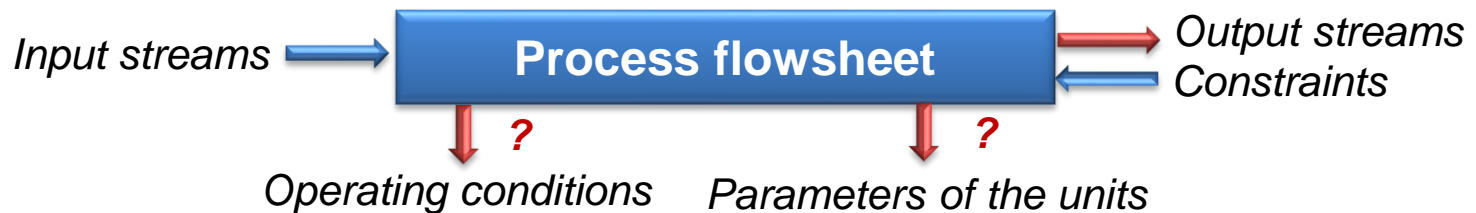
- flowsheet simulation is **more efficient** compared to the manual subsequent calculation of models for different apparatuses
- shows **effects** of changes of one processes unit on **the entire process**
- **reduces the measurement efforts** required to obtain the material and population balance for all streams of a process
- allows for **holistic optimization of complex processes** with regard to energy, quality, yield, ..
- **structured library of process models** allows easy access to up-to-date modeling knowledge
- **operator training** – the simulator gives an answer to:
,What happens when I change this parameter?‘

- With help of process simulator, three main types of problems can be solved:

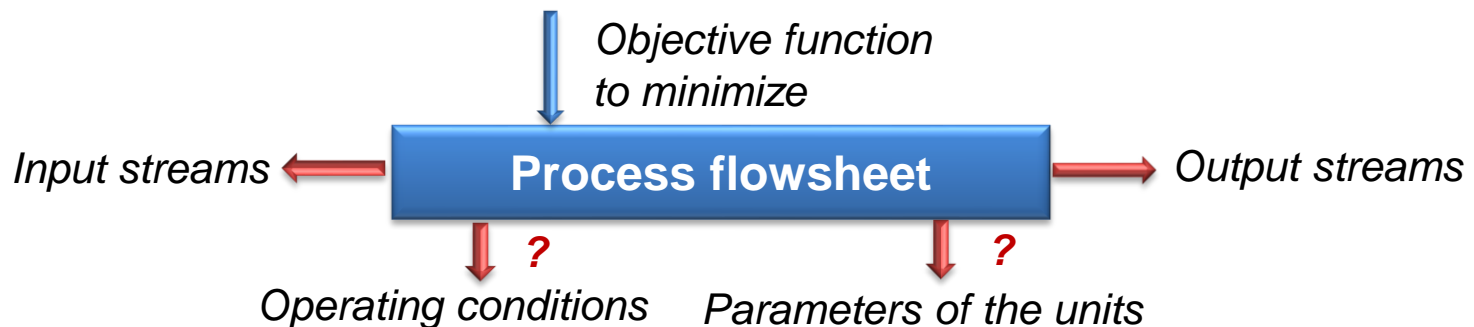
- Simulation**



- Design**



- Optimization**



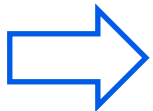
- flowsheet simulation is **well established in industry**
 - for **modeling, simulation, design and optimization of fluid processes**
 - common tools are Aspen Plus, Aspen Hysis, Pro/II, UniSim, ...
- in contrast, **solids processes** are mostly designed **unit by unit**
 - numerical models exist for unit operations, but in different tools (Excel, Matlab, C/C++ or FORTRAN code etc.)
 - the **entire process is normally not simulated** at once
- **Why? Because in the past most simulation packages were...**
 - **not well suited** to describe solids processes
 - lack of unit operation models
 - insufficient data structure to describe a disperse phase
 - mostly **limited** to quite narrow industrial sectors (e.g. mining, gravel and sand etc.)

Fluid processes

- concentrated parameters
(pressure, temperature,...)
- completely characterized by
chemical composition
 - phase equilibrium
 - mixture properties

Solids processes

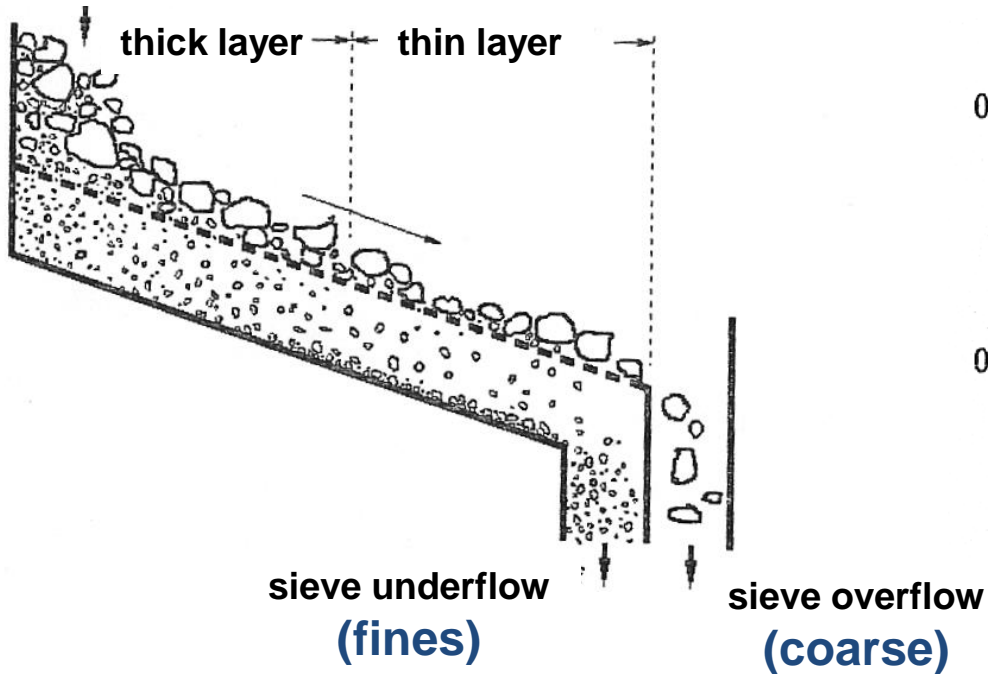
- distributed parameters
(particle size distribution,...)
- characterization requires
more information
 - particle size distribution
for each particle type
 - moisture content
for each particle type
 - ...
- bulk properties cannot be calculated
from single particles properties



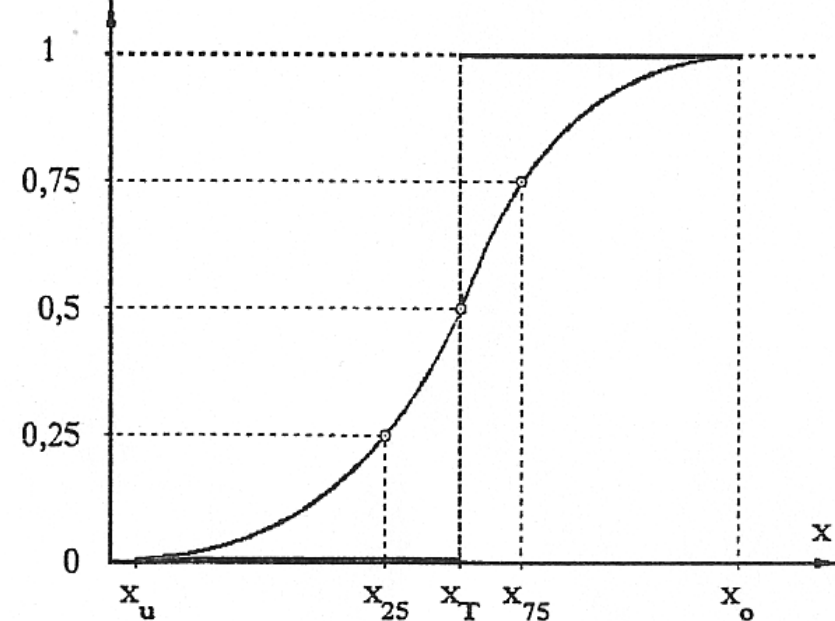
Complex structure for material streams is needed

- Continuous sieving

feed



- Separation efficiency

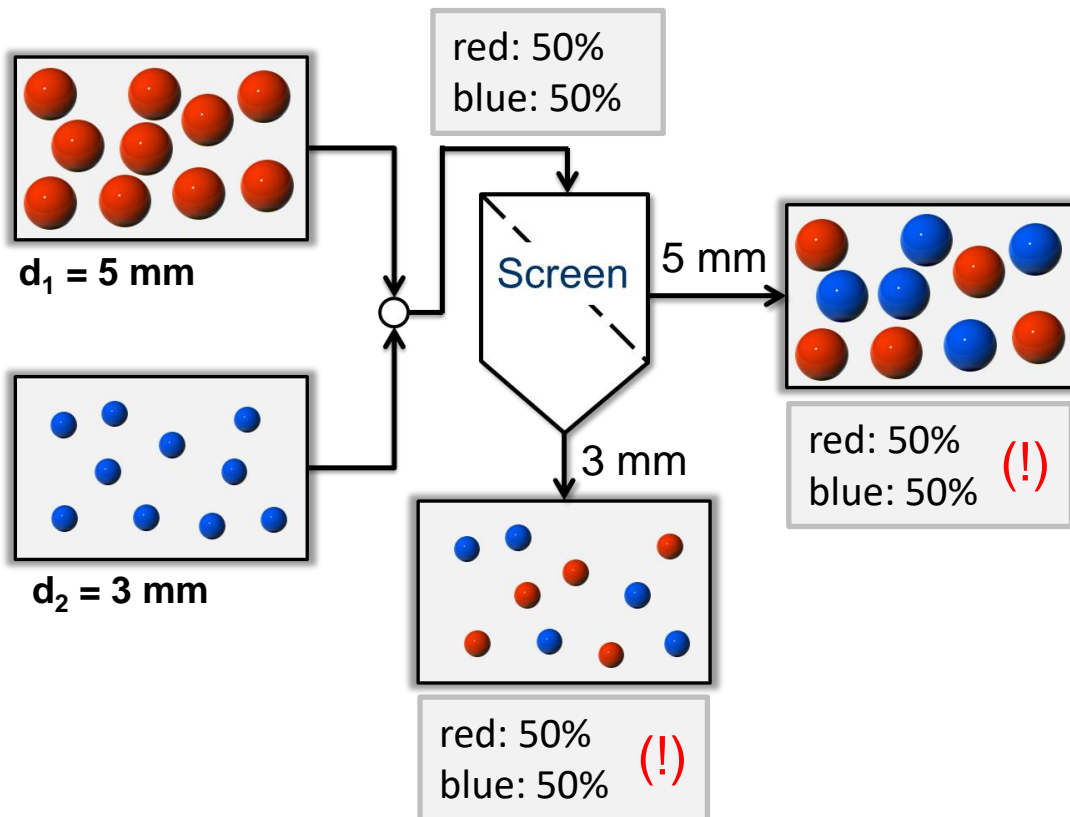


- Separation efficiency

$$T(x) = g \cdot \frac{q_{coarse}(x)}{q_{input}(x)}$$

g – coarse mass fraction

- Distributed properties (particle size distribution, porosity distribution...) are used for description of solids materials
- Characterization of solids can require more information: shape factors, particle strength...
- Size-dependent secondary attributes can be used: residual moisture, density...



Treatment of solids without consideration of dependent distributed properties may lead to their mixing and incorrect handling

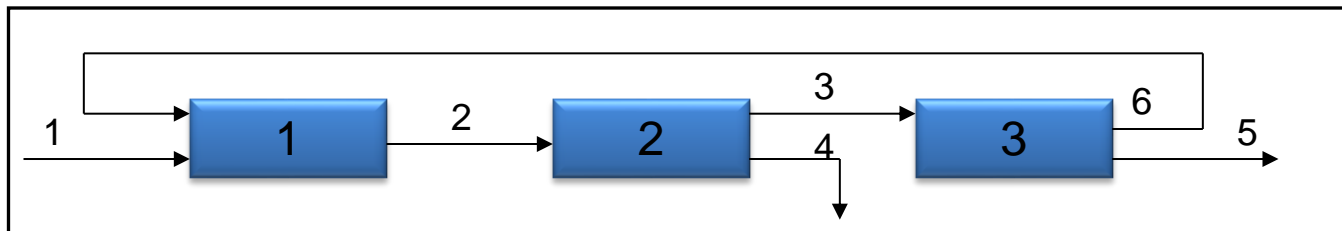
- Mathematical model of specific process consists of:

- **Functional model**

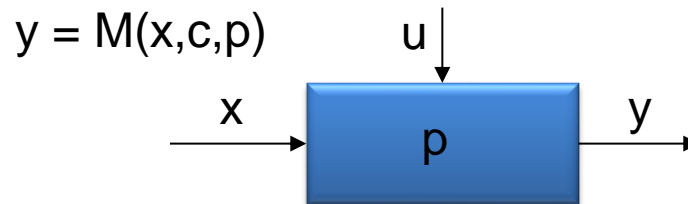
Functional model describes mathematical dependencies between Input and Output variables of each process element

- **Structural model**

Structural model describes coupling between elements according to the structure of investigated process

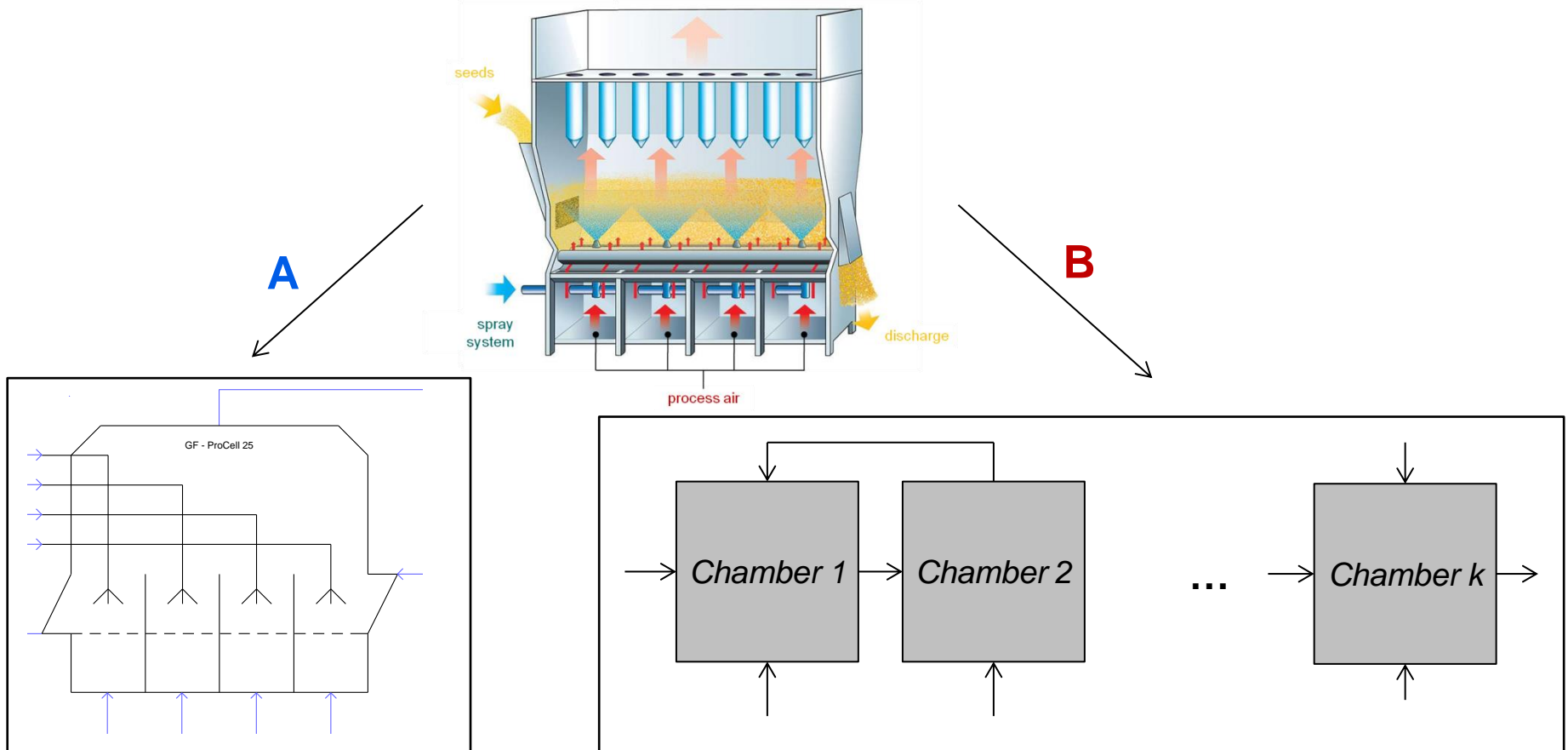


- **Functional model** can consist of:
 - Balance equations (mass and/or energy)
 - State equations (i.e. ideal gas law)
 - Equations of process kinetics (i.e. reaction kinetics)
- Model M transforms vector of input variables x into vector of output variables y



x Input variables
y Output variables
u Operating conditions
p Model parameters

- **Functional model** can describe:
 - Single apparatus, for example screen
 - Group of apparatuses or process substeps, for example circulated fluidized bed



- **A**: smaller computational effort (unnecessary initialization and copy operations can be avoided)
- **B**: higher flexibility of process configuration

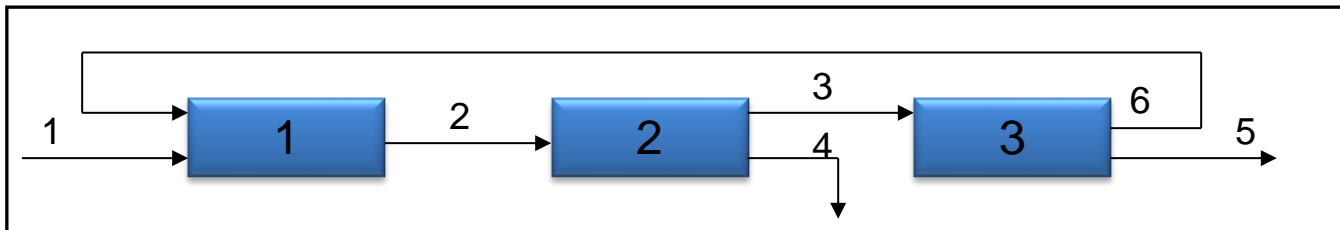
- Structural model describes coupling between units
→ represents process structure

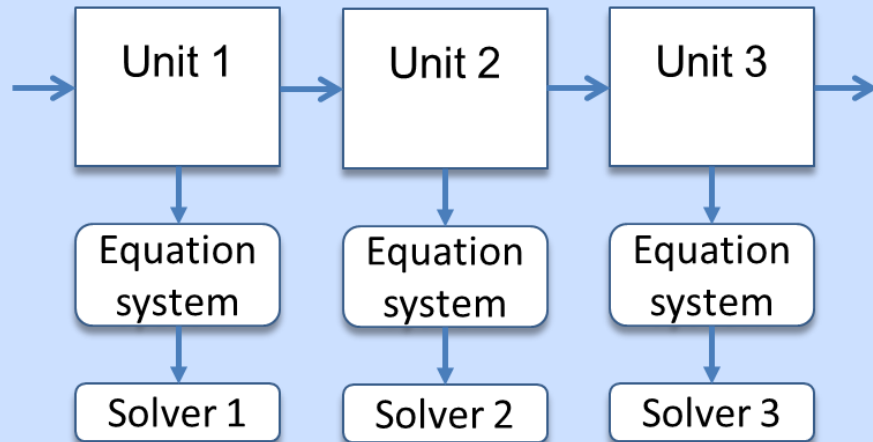
- Example **Incidence Matrix**:

Each row is related to one column, each row is related to unit

$$s_{ij} = \begin{cases} -1, & \text{if stream } u_j \text{ is output of unit } x_i \\ 1, & \text{if stream } u_j \text{ is the input of unit } x_i \\ 0, & \text{otherwise} \end{cases}$$

$$S = \begin{matrix} i \rightarrow & \begin{matrix} 1 & 2 & 3 & 4 & 5 & 6 \end{matrix} \\ \begin{pmatrix} -1 & 0 & 0 & 1 & 1 & 0 \\ 1 & -1 & 0 & 0 & 0 & 1 \\ 0 & 1 & -1 & -1 & 0 & 0 \\ 0 & 0 & 1 & 0 & -1 & -1 \end{pmatrix} & \begin{matrix} \downarrow j \\ 0 \\ 1 \\ 2 \\ 3 \end{matrix} \end{matrix} \quad \text{Element 0: Environment}$$

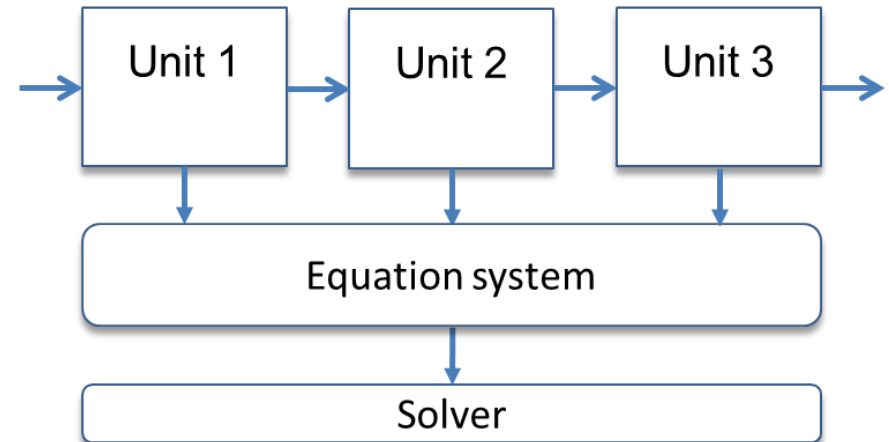




Sequential-modular (modular)

- Conceptual simplicity
- Correspondence to the physical structure of processes
- Higher flexibility
- Possibility to use different numerical methods to calculate models
- Difficulties in processing flowsheets with recycle streams

Examples: ASPEN Plus, ChemCad, HySim



Equation-oriented (simultaneous)

- Equations are homogenized and calculated by one solver
- Better convergence rate, especially for complex flowsheets with recycles
- Difficulties with simultaneous simulation of fast and slow changed components
- Usage with heterogeneous models is complicated

Examples: SpeedUp, gProms, DIVA, Diana

Unit 1

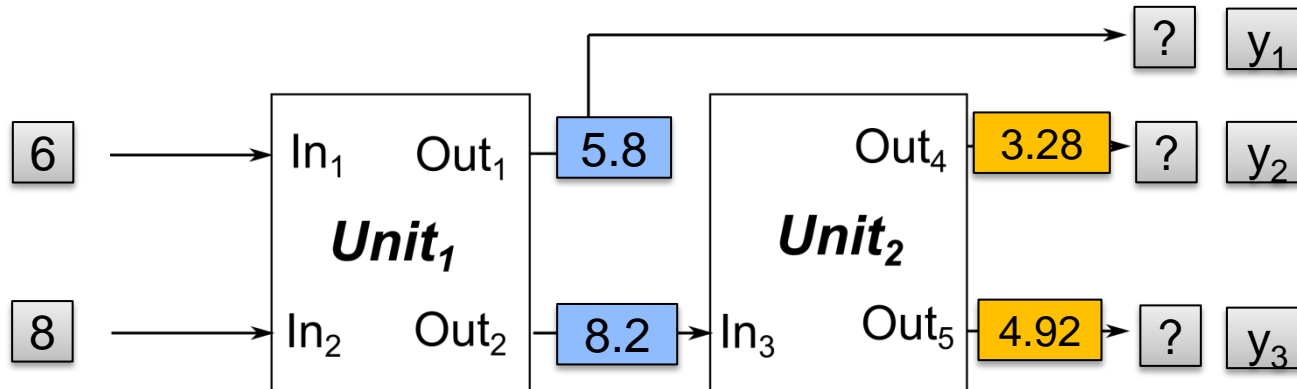
$$Out_1 = 0.3 \cdot In_1 + 0.5 \cdot In_2$$

$$Out_2 = 0.7 \cdot In_1 + 0.5 \cdot In_2$$

Unit 2

$$Out_4 = 0.4 \cdot In_3$$

$$Out_5 = 0.6 \cdot In_3$$



Equation-oriented approach

$$\begin{cases} Out_1 = 0.3 \cdot In_1 + 0.5 \cdot In_2 \\ Out_2 = 0.7 \cdot In_1 + 0.5 \cdot In_2 \\ Out_4 = 0.4 \cdot In_3 \\ Out_5 = 0.6 \cdot In_3 \end{cases}$$

Modular approach

1. Calculation of Unit₁

2. Calculation of Unit₂

Unit 1

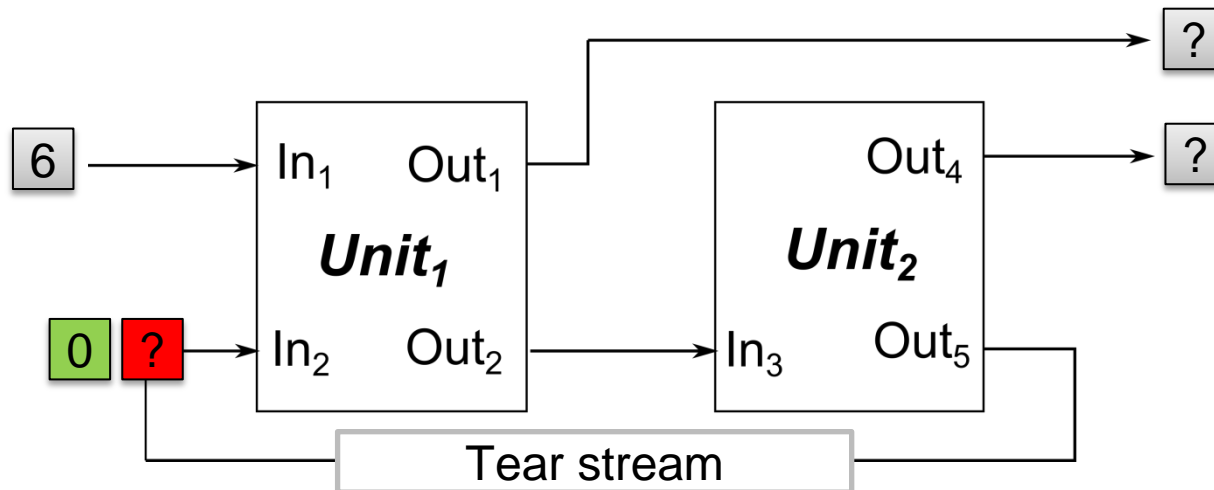
$$Out_1 = 0.3 \cdot In_1 + 0.5 \cdot In_2$$

$$Out_2 = 0.7 \cdot In_1 + 0.5 \cdot In_2$$

Unit 2

$$Out_4 = 0.4 \cdot In_3$$

$$Out_5 = 0.6 \cdot In_3$$



Iteration 1

Unit₁: $Out_1 = 1.8$
 $Out_2 = 4.2$

Unit₂: $Out_4 = 1.68$
 $Out_5 = 2.52$

Tear stream

Iteration 0: 0
 Iteration 1: 2.52
 Difference: 2.52

Iteration 2

Unit₁: $Out_1 = 3.06$
 $Out_2 = 5.46$

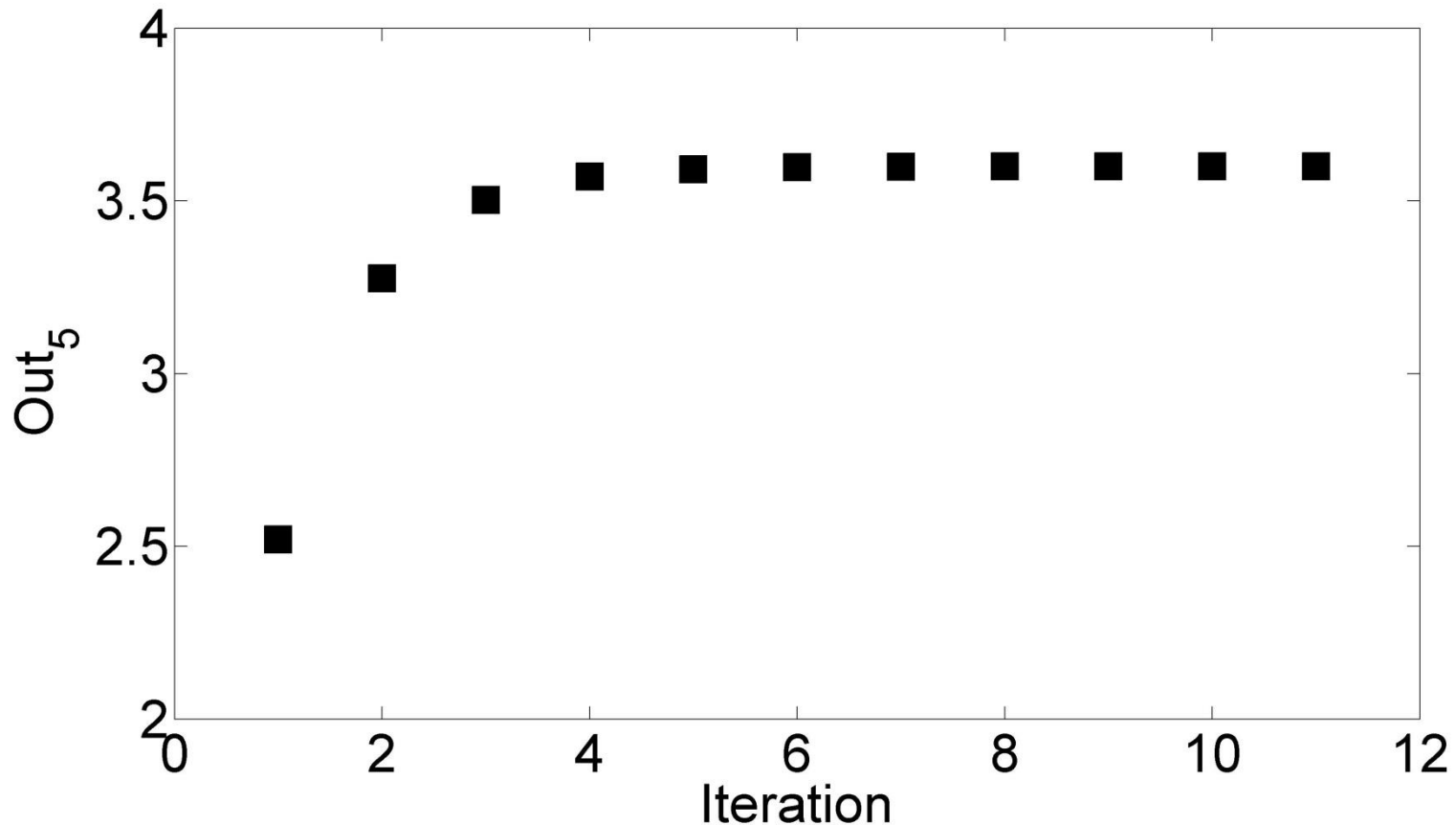
Unit₂: $Out_4 = 2.184$
 $Out_5 = 3.276$

Tear stream

Iteration 1: 2.52
 Iteration 2: 3.276
 Difference: 0.756

Unit 1

Unit 2



Unit₂: $Out_4 = 1.68$
 $Out_5 = 2.52$

Iteration 1: 2.52
Difference: 2.52

Unit₂: $Out_4 = 2.184$
 $Out_5 = 3.276$

Iteration 2: 3.276
Difference: 0.756

Unit 1

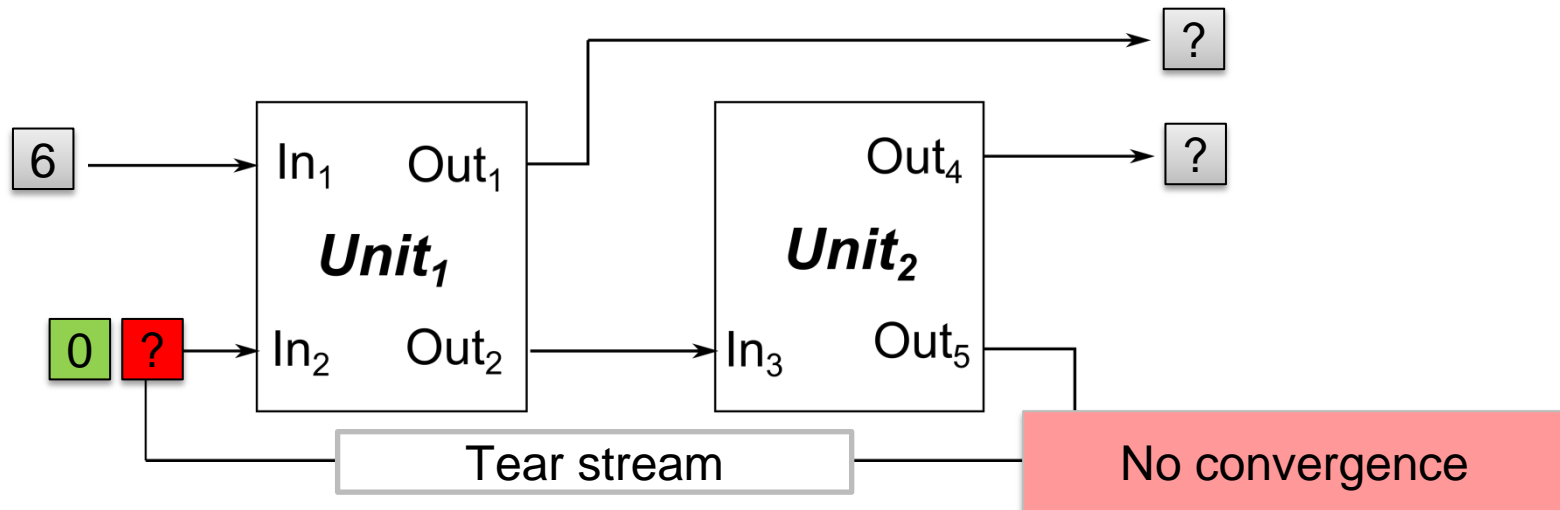
$$Out_1 = 0.3 \cdot In_1 + 0.5 \cdot In_2$$

$$Out_2 = 0.7 \cdot In_1 + 2 \cdot In_2$$

Unit 2

$$Out_4 = 0.4 \cdot In_3$$

$$Out_5 = 0.6 \cdot In_3$$



Iteration 1

Unit₁: Out₁ = 1.8
Out₂ = 4.2

Unit₂: Out₄ = 1.68
Out₅ = 2.52

Tear stream

Iteration 0: 0
Iteration 1: 2.52
Difference: 2.52

Iteration 2

Unit₁: Out₁ = 3.06
Out₂ = 9.24

Unit₂: Out₄ = 3.696
Out₅ = 5.544

Tear stream

Iteration 1: 2.52
Iteration 2: 5.544
Difference: 3.024

- To improve calculation performance the convergence methods can be applied

x – represents guessed tear variable

$F(x)$ – calculated value after new unit calculation

- Direct substitution:

$$x_k = F(x_k)$$

- Relaxation-acceleration:

$$x_{k+1} = \lambda \cdot F(x_k) + (1 - \lambda)x_k$$

- Wegstein's method – implements parabolic extrapolation using results of two previous iterations

$$x_{k+1} = q \cdot x_k + (1 - q)F(x_k)$$

$$q = \frac{s}{s - 1}$$

$$s = \frac{F(x_k) - F(x_{k-1})}{x_k - x_{k-1}}$$

- Steffensen's method:

$$X_k = X_{k-3} - \frac{(X_{k-2} - X_{k-3})^2}{X_{k-2} - 2X_{k-3} + X_{k-4}}$$

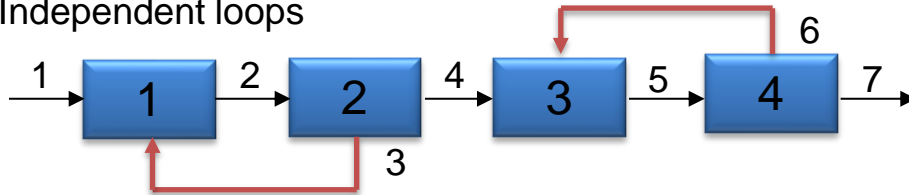
- Calculation sequence plays important role in the case of modular approach
- Recycle stream denotes process stream that returns material or enthalpy from downstream process unit back to upstream process unit
- Complex schemes, consisting of large number of recycle streams cannot be easily solved
- Units connected with recycle streams form loops
- Loops are solved iteratively via cutting of recycle streams
- Tearing - providing initial guess, such as total flow, PSD, composition, temperature, etc.
- A tear stream is not necessary recycle stream

No loops



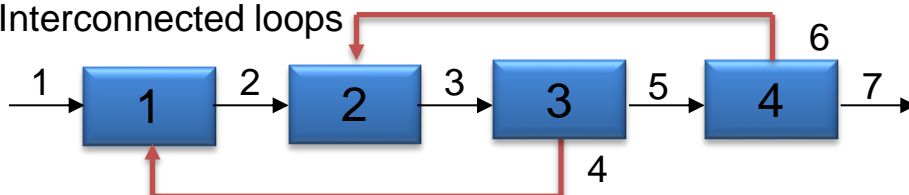
Flowsheet can be directly calculated without any iteration (no recycle streams)

Independent loops



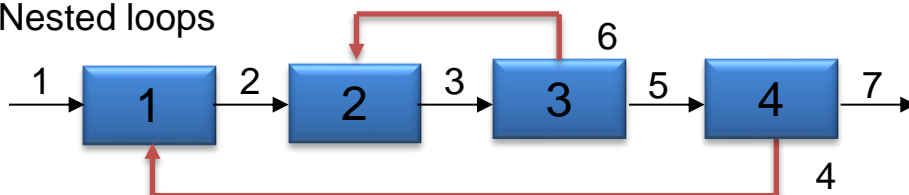
Several recycle streams co-exist, however both loops can be solved separately

Interconnected loops



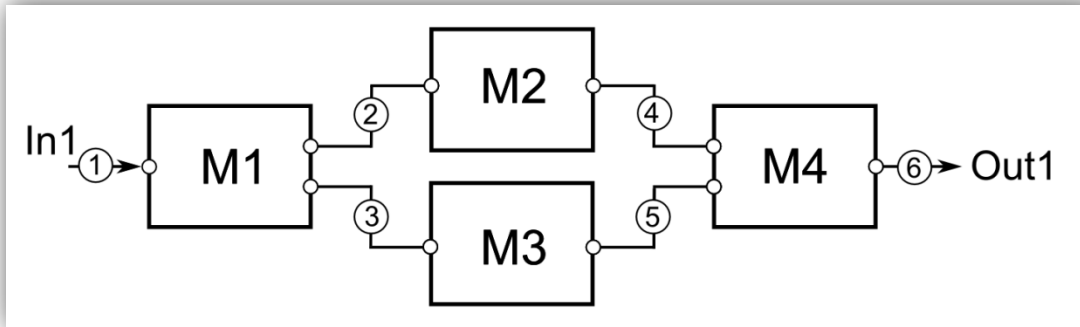
Several recycle streams co-exist, whole scheme should be solved iteratively

Nested loops



Recycle include another recycle stream

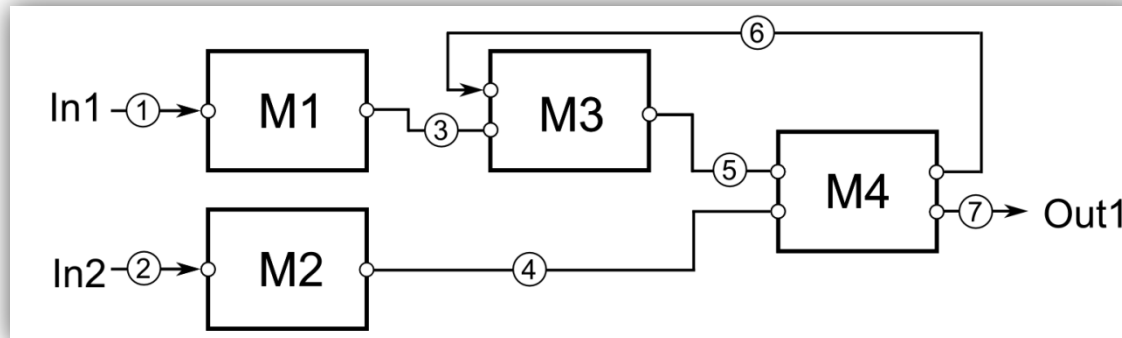
Example 1



Calculation sequence 1

Step 1	Step 2	Step 3	Step 4
M1	M2	M3	M4

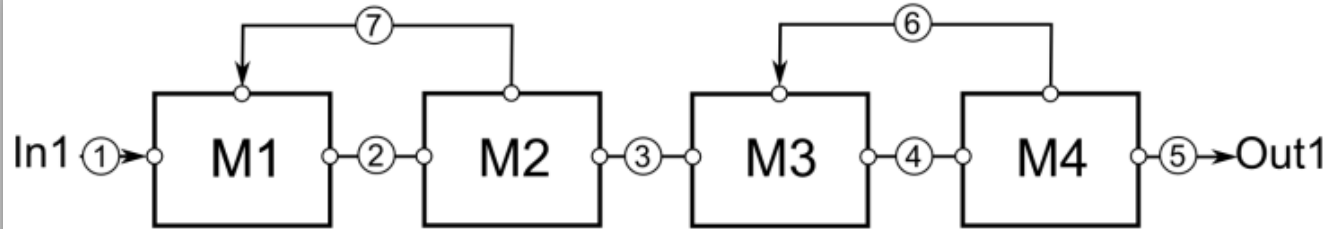
Example 2



Calculation sequence 2

Step 1	Step 2	Step 3 (iterative until convergence)
M1	M2	M3; M4; S6

Example 3:



Calculation
sequence 3

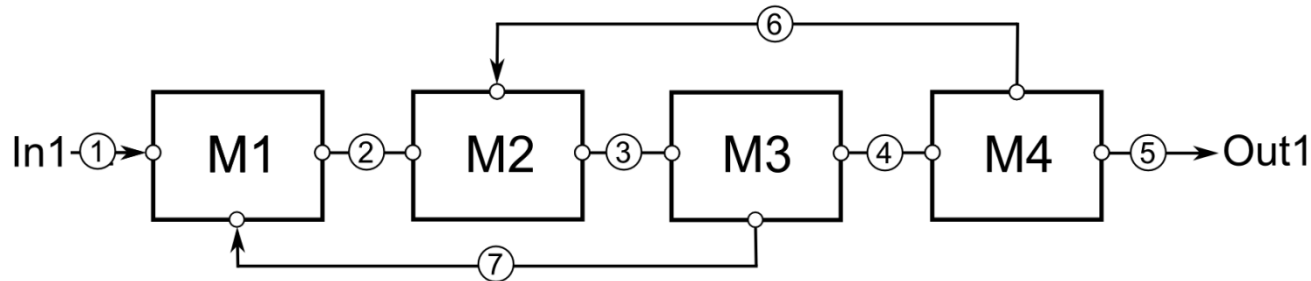
Step 1 (iterative until
convergence)

M1; M2; **S7**

Step 2 (iterative until
convergence)

M3; M4; **S6**

Example 4:



Calculation
sequence 4

Step 1 (iterative until convergence)

M1; M2; M3; M4; **S6; S7**

- Approximation of calculation sequence is performed in two steps:

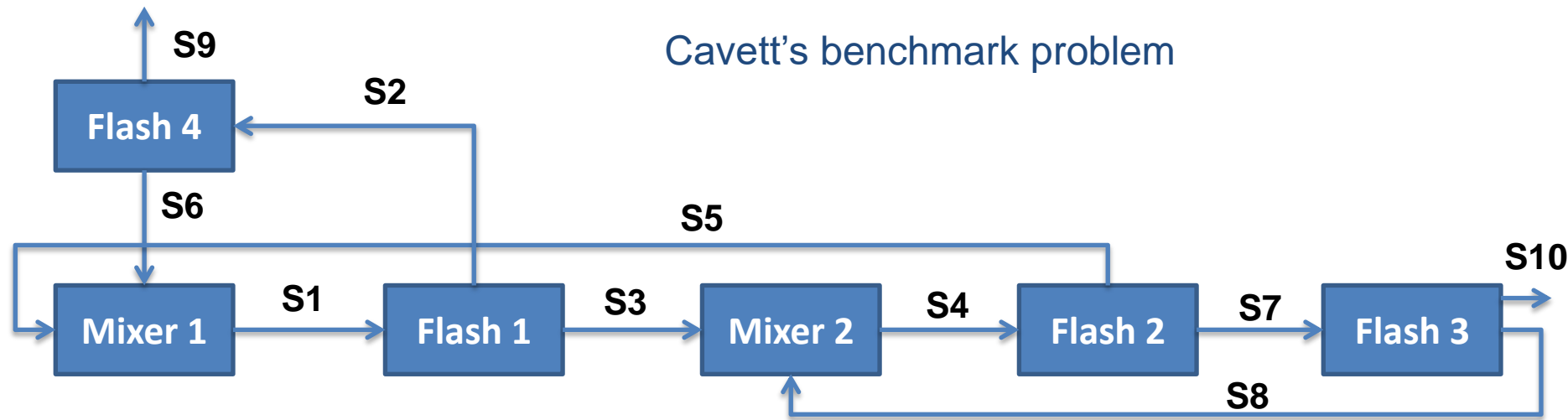
1. Units which are related to one loop should be identified and combined in separate blocks

- Existing algorithms
 - Sargent und Westerberg algorithm
 - Loopfinder algorithm according to Forder und Hutchinson
 - ...

2. Specification of tear streams on optimal position

- Criteria for selection of tear streams
 - Minimal number of tear streams
 - Availability of initial data for first iteration
- Existing algorithms
 - Barkley und Motard algorithm
 - ItFinder-algorithm according to Forder und Hutchinson
 - ...

- Main idea of algorithm – path tracing and identifying information paths
- The stack of visited nodes is built
- Each cycle appears as a group of nodes



- Three different sets of tear streams are possible:

- S1-S4
- S5-S6-S8
- S6-S4

R.H. Cavett (1963). Application of numerical methods to the convergence of simulated processes involving recycle loops.

