

Derivatives in L^AT_EX

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So, we're going to find the derivative of that interesting function:

$$\frac{\frac{x+x^2 \cdot 3 \cdot x-3}{\sin(x)}}{\cos(2+x)} \cdot \lg(x)$$

But first of all lets try to simplify it!

LOL! No more easy

It's as easy as a breathe to understand that the derivative of VARIABLE is 1!

Elementary:

$$(x)' = 1$$

DECIMAL LOGARITHM is the best LOGARITHM because it's used for stellar magnetudes and decibels. So

$$(\lg(f(x)))' = \frac{1}{f(x) \cdot \ln(10)} \cdot f'(x)$$

So:

$$(\lg(x))' = \frac{1}{x \cdot \ln(10)} \cdot 1$$

It's as easy as a breathe to understand that the derivative of VARIABLE is 1!

It's really easy to see:

$$(x)' = 1$$

Only a fool does not know that the derivative of NUMBER is 0!

Easy:

$$(2)' = 0$$

As we know the derivative of ADDITION is ADDITION of derivatives!

In that case:

$$(2+x)' = 0 + 1$$

COSINUS is not very simple function, we'd use special formula

$$(\cos(f(x)))' = -\sin(f(x)) \cdot f'(x)$$

It's really easy to see:

$$(\cos(2+x))' = -1 \cdot \sin(2+x) \cdot (0+1)$$

It's as easy as a breathe to understand that the derivative of VARIABLE is 1!

Then:

$$(x)' = 1$$

SINUS is really difficult function that's why we should use formula

$$(\sin(f(x)))' = \cos(f(x)) \cdot f'(x)$$

Then:

$$(\sin(x))' = \cos(x) \cdot 1$$

Only a fool does not know that the derivative of NUMBER is 0!

Clearly:

$$(3)' = 0$$

It's as easy as a breathe to understand that the derivative of VARIABLE is 1!

It's really easy to see:

$$(x)' = 1$$

Only a fool does not know that the derivative of NUMBER is 0!

You can see:

$$(3)' = 0$$

It's as easy as a breathe to understand that the derivative of VARIABLE is 1!

You can see:

$$(x)' = 1$$

Function to the POWER of number is interesting

$$(f^a(x))' = a \cdot f^{a-1}(x) \cdot f'(x)$$

Elementary:

$$(x^2)' = 2 \cdot x^1 \cdot 1$$

It's clear that the derivative of MULTIPLICATION is given by formula

$$(f(x) \cdot g(x))' = f'(x) \cdot g(x) + g'(x) \cdot f(x)$$

So:

$$(x^2 \cdot 3)' = 2 \cdot x^1 \cdot 1 \cdot 3 + 0 \cdot x^2$$

It's clear that the derivative of MULTIPLICATION is given by formula

$$(f(x) \cdot g(x))' = f'(x) \cdot g(x) + g'(x) \cdot f(x)$$

Elementary:

$$(x^2 \cdot 3 \cdot x)' = (2 \cdot x^1 \cdot 1 \cdot 3 + 0 \cdot x^2) \cdot x + 1 \cdot x^2 \cdot 3$$

It's as easy as a breathe to understand that the derivative of VARIABLE is 1!

Elementary:

$$(x)' = 1$$

As we know the derivative of ADDITION is ADDITION of derivatives!
You can see:

$$(x + x^2 \cdot 3 \cdot x)' = 1 + (2 \cdot x^1 \cdot 1 \cdot 3 + 0 \cdot x^2) \cdot x + 1 \cdot x^2 \cdot 3$$

Everybody knows that the derivative of SUBTRACT is SUBTRACT of derivatives!

Clearly:

$$(x + x^2 \cdot 3 \cdot x - 3)' = 1 + (2 \cdot x^1 \cdot 1 \cdot 3 + 0 \cdot x^2) \cdot x + 1 \cdot x^2 \cdot 3 - 0$$

Not difficult to notice that the derivative of DIVISION is given by formula

$$\left(\frac{f(x)}{g(x)}\right)' = \frac{f'(x) \cdot g(x) - g'(x) \cdot f(x)}{g^2(x)}$$

So:

$$\left(\frac{x + x^2 \cdot 3 \cdot x - 3}{\sin(x)}\right)' = \frac{(1 + (2 \cdot x^1 \cdot 1 \cdot 3 + 0 \cdot x^2) \cdot x + 1 \cdot x^2 \cdot 3 - 0) \cdot \sin(x) - \cos(x) \cdot 1 \cdot (x + x^2 \cdot 3 \cdot x - 3)}{\sin^2(x)}$$

Not difficult to notice that the derivative of DIVISION is given by formula

$$\left(\frac{f(x)}{g(x)}\right)' = \frac{f'(x) \cdot g(x) - g'(x) \cdot f(x)}{g^2(x)}$$

It's clear that:

$$\left(\frac{\frac{x+x^2 \cdot 3 \cdot x - 3}{\sin(x)}}{\cos(2+x)}\right)' = \frac{\frac{(1+(2 \cdot x^1 \cdot 1 \cdot 3 + 0 \cdot x^2) \cdot x + 1 \cdot x^2 \cdot 3 - 0) \cdot \sin(x) - \cos(x) \cdot 1 \cdot (x+x^2 \cdot 3 \cdot x - 3)}{\sin^2(x)} \cdot \cos(2+x) - (-1) \cdot \sin(2+x)}{\cos^2(2+x)}$$

It's clear that the derivative of MULTIPLICATION is given by formula

$$(f(x) \cdot g(x))' = f'(x) \cdot g(x) + g'(x) \cdot f(x)$$

Elementary:

$$\left(\frac{\frac{x+x^2 \cdot 3 \cdot x-3}{\sin(x)}}{\cos(2+x)} \cdot \lg(x) \right)' = \frac{\frac{(1+(2 \cdot x^1 \cdot 1 \cdot 3+0 \cdot x^2)) \cdot x+1 \cdot x^2 \cdot 3-0}{\sin^2(x)} \cdot \sin(x) - \cos(x) \cdot 1 \cdot (x+x^2 \cdot 3 \cdot x-3)}{\cos^2(2+x)} \cdot \cos(2+x) - 1 \cdot \sin(2+x)$$

Lets try to simplify our REALLY BIG derivative

$$\frac{\frac{(1+(2 \cdot x^1 \cdot 1 \cdot 3+0 \cdot x^2)) \cdot x+1 \cdot x^2 \cdot 3-0}{\sin^2(x)} \cdot \sin(x) - \cos(x) \cdot 1 \cdot (x+x^2 \cdot 3 \cdot x-3)}{\cos^2(2+x)} \cdot \cos(2+x) - 1 \cdot \sin(2+x) \cdot (0+1) \cdot \frac{x+x^2 \cdot 3 \cdot x-3}{\sin(x)}$$

It's really easy to see:

$$\frac{\frac{(1+(2 \cdot x^1 \cdot 1 \cdot 3+0 \cdot x^2)) \cdot x+1 \cdot x^2 \cdot 3}{\sin^2(x)} \cdot \sin(x) - \cos(x) \cdot 1 \cdot (x+x^2 \cdot 3 \cdot x-3)}{\cos^2(2+x)} \cdot \cos(2+x) - 1 \cdot \sin(2+x) \cdot 1 \cdot \frac{x+x^2 \cdot 3 \cdot x-3}{\sin(x)} \cdot \lg(x) +$$

Clearly:

$$\frac{\frac{(1+(2 \cdot x^1 \cdot 3+0 \cdot x^2)) \cdot x+1 \cdot x^2 \cdot 3}{\sin^2(x)} \cdot \sin(x) - \cos(x) \cdot 1 \cdot (x+x^2 \cdot 3 \cdot x-3)}{\cos^2(2+x)} \cdot \cos(2+x) - 1 \cdot \sin(2+x) \cdot 1 \cdot \frac{x+x^2 \cdot 3 \cdot x-3}{\sin(x)} \cdot \lg(x) +$$

As you can see:

$$\frac{\frac{(1+(2 \cdot x \cdot 3+0 \cdot x^2)) \cdot x+1 \cdot x^2 \cdot 3}{\sin^2(x)} \cdot \sin(x) - \cos(x) \cdot 1 \cdot (x+x^2 \cdot 3 \cdot x-3)}{\cos^2(2+x)} \cdot \cos(2+x) - 1 \cdot \sin(2+x) \cdot 1 \cdot \frac{x+x^2 \cdot 3 \cdot x-3}{\sin(x)} \cdot \lg(x) +$$

Clearly:

$$\frac{\frac{(1+(2 \cdot x \cdot 3+0)) \cdot x+1 \cdot x^2 \cdot 3}{\sin^2(x)} \cdot \sin(x) - \cos(x) \cdot 1 \cdot (x+x^2 \cdot 3 \cdot x-3)}{\cos^2(2+x)} \cdot \cos(2+x) - 1 \cdot \sin(2+x) \cdot 1 \cdot \frac{x+x^2 \cdot 3 \cdot x-3}{\sin(x)} \cdot \lg(x) +$$

Clearly:

$$\frac{\frac{(1+2 \cdot x \cdot 3 \cdot x+1 \cdot x^2 \cdot 3) \cdot \sin(x) - \cos(x) \cdot 1 \cdot (x+x^2 \cdot 3 \cdot x-3)}{\sin^2(x)} \cdot \cos(2+x) - 1 \cdot \sin(2+x) \cdot 1 \cdot \frac{x+x^2 \cdot 3 \cdot x-3}{\sin(x)} \cdot \lg(x) + \frac{1}{x \cdot \ln(10)}}$$

Elementary:

$$\frac{\frac{(1+2 \cdot x \cdot 3 \cdot x+x^2 \cdot 3) \cdot \sin(x) - \cos(x) \cdot 1 \cdot (x+x^2 \cdot 3 \cdot x-3)}{\sin^2(x)} \cdot \cos(2+x) - 1 \cdot \sin(2+x) \cdot 1 \cdot \frac{x+x^2 \cdot 3 \cdot x-3}{\sin(x)} \cdot \lg(x) + \frac{1}{x \cdot \ln(10)}}$$

It's clear that:

$$\frac{\frac{(1+2x \cdot 3 \cdot x + x^2 \cdot 3) \cdot \sin(x) - \cos(x) \cdot (x + x^2 \cdot 3 \cdot x - 3)}{\sin^2(x)} \cdot \cos(2+x) - -1 \cdot \sin(2+x) \cdot 1 \cdot \frac{x+x^2 \cdot 3 \cdot x - 3}{\sin(x)}}{\cos^2(2+x)} \cdot \lg(x) + \frac{1}{x \cdot \ln(10)}$$

Then:

$$\frac{\frac{(1+2x \cdot 3 \cdot x + x^2 \cdot 3) \cdot \sin(x) - \cos(x) \cdot (x + x^2 \cdot 3 \cdot x - 3)}{\sin^2(x)} \cdot \cos(2+x) - -1 \cdot \sin(2+x) \cdot \frac{x+x^2 \cdot 3 \cdot x - 3}{\sin(x)}}{\cos^2(2+x)} \cdot \lg(x) + \frac{1}{x \cdot \ln(10)} \cdot 1 \cdot \frac{x}{\sin(x)}$$

You can see:

$$\frac{\frac{(1+2x \cdot 3 \cdot x + x^2 \cdot 3) \cdot \sin(x) - \cos(x) \cdot (x + x^2 \cdot 3 \cdot x - 3)}{\sin^2(x)} \cdot \cos(2+x) - -1 \cdot \sin(2+x) \cdot \frac{x+x^2 \cdot 3 \cdot x - 3}{\sin(x)}}{\cos^2(2+x)} \cdot \lg(x) + \frac{1}{x \cdot \ln(10)} \cdot \frac{x}{\sin(x)}$$

EEEE! That looks like really easy nice

$$\frac{\frac{(1+2x \cdot 3 \cdot x + x^2 \cdot 3) \cdot \sin(x) - \cos(x) \cdot (x + x^2 \cdot 3 \cdot x - 3)}{\sin^2(x)} \cdot \cos(2+x) - -1 \cdot \sin(2+x) \cdot \frac{x+x^2 \cdot 3 \cdot x - 3}{\sin(x)}}{\cos^2(2+x)} \cdot \lg(x) + \frac{1}{x \cdot \ln(10)} \cdot \frac{x}{\sin(x)}$$

Derivatives are really easy!