

Data Structure and Algorithms [CO2003]

Chapter 4 - List

Lecturer: Duc Dung Nguyen, PhD. Contact: nddung@hcmut.edu.vn

Faculty of Computer Science and Engineering Hochiminh city University of Technology

Contents



- 1. Linear list concepts
- 2. Array implementation
- 3. Singly linked list
- 4. Other linked lists
- 5. Comparison of implementations of list

Outcomes



- L.O.2.1 Depict the following concepts: (a) array list and linked list, including single link and double links, and multiple links; (b) stack; and (c) queue and circular queue.
- L.O.2.2 Describe storage structures by using pseudocode for: (a) array list and linked list, including single link and double links, and multiple links; (b) stack; and (c) queue and circular queue.
- L.O.2.3 List necessary methods supplied for list, stack, and queue, and describe them using pseudocode.
- L.O.2.4 Implement list, stack, and queue using C/C++.

Outcomes



- L.O.2.5 Use list, stack, and queue for problems in real-life, and choose an appropriate implementation type (array vs. link).
- L.O.2.6 Analyze the complexity and develop experiment (program) to evaluate the efficiency of methods supplied for list, stack, and queue.
- L.O.8.4 Develop recursive implementations for methods supplied for the following structures: list, tree, heap, searching, and graphs.
- L.O.1.2 Analyze algorithms and use Big-O notation to characterize the computational complexity of algorithms composed by using the following control structures: sequence, branching, and iteration (not recursion).





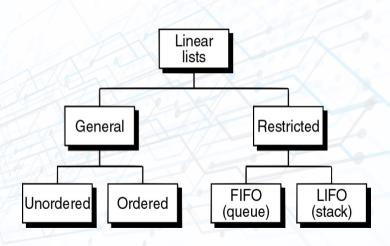
Definition

A linear list is a data structure in which each element has a unique successor.

Example

- Array
- Linked list







General list:

- No restrictions on which operation can be used on the list.
- No restrictions on where data can be inserted/deleted.
- Unordered list (random list): Data are not in particular order.
- Ordered list: data are arranged according to a key.



Restricted list:

- Only some operations can be used on the list.
- Data can be inserted/deleted only at the ends of the list.
- Queue: FIFO (First-In-First-Out).
- Stack: LIFO (Last-In-First-Out).

List ADT



Definition

A list of elements of type T is a finite sequence of elements of T.

Basic operations:

- Construct a list, leaving it empty.
- Insert an element.
- Remove an element.
- Search an element.
- Retrieve an element.
- Traverse the list, performing a given operation on each element.

List ADT

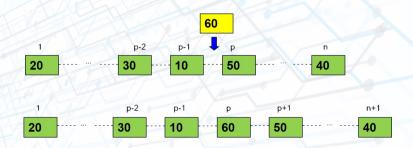


Extended operations:

- Determine whether the list is empty or not.
- Determine whether the list is full or not.
- Find the size of the list.
- Clear the list to make it empty.
- Replace an element with another element.
- Merge two ordered list.
- Append an unordered list to another.



- Insert an element at a specified position p in the list
 - Only with General Unordered List.



Any element formerly at position p and all later have their position numbers increased by 1.

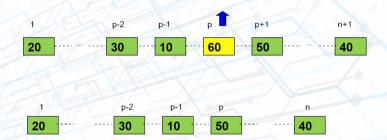
Insertion



- Insert an element with a given data
 - With General Unordered List: can be made at any position in the list (at the beginning, in the middle, at the end).
 - With General Ordered List: data must be inserted so that the ordering of the list is maintained (searching appropriate position is needed).
 - With Restricted List: depend on it own definition (FIFO or LIFO).



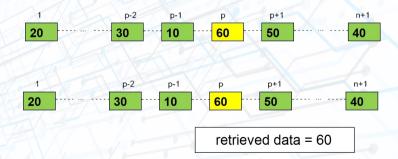
- Remove an element at a specified position p in the list
 - With General Unordered List and General Ordered List.



The element at position p is removed from the list, and all subsequent elements have their position numbers decreased by 1.



- Retrieve an element at a specified position p in the list
 - With General Unordered List and General Ordered List.



All elements remain unchanged.

Removal, Retrieval



- Remove/ Retrieve an element with a given data
 - With General Unordered List and General Ordered List: Searching is needed in order to locate the data being deleted/ retrieved.

Success of Basic Operations

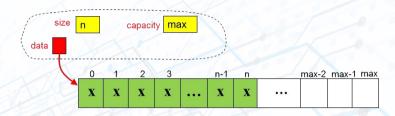


- Insertion is successful when the list is not full.
- Removal, Retrieval are successful when the list is not empty.



Dynamically Allocated Array





```
List // Contiguous Implementation of List
// number of used elements (mandatory)
size <integer>
// (Dynamically Allocated Array)
data <dynamic array of <DataType> >
capacity <integer>
End List
```



```
class DynamicArray {
private:
   int size;
   int capacity;
   int *storage;

public:
   DynamicArray() {
    capacity = 10;
    size = 0;
   storage = new int[capacity];
}
```



```
DynamicArray(int capacity) {
  this -> capacity = capacity;
  size = 0;
  storage = new int[capacity];
}
~DynamicArray() {
  delete[] storage;
}
```



```
void setCapacity(int);
void ensureCapacity(int);
void pack();
void trim();

void rangeCheck(int);
void set(int, int);
int get(int);
void removeAt(int);
void insertAt(int, int);

void print();
};
```





```
void DynamicArray::ensureCapacity(int minCapacity) {
   if (minCapacity > capacity) {
     int newCapacity = (capacity*3)/2 + 1;
     if (newCapacity < minCapacity)
        newCapacity = minCapacity;
     setCapacity(newCapacity);
   }
}</pre>
```



```
void DynamicArray::pack() {
  if (size <= capacity / 2) {
    int newCapacity = (size * 3) / 2 + 1;
    setCapacity(newCapacity);
  }
}

void DynamicArray::trim() {
  int newCapacity = size;
  setCapacity(newCapacity);
}</pre>
```



```
void DynamicArray::rangeCheck(int index) {
  if (index < 0 | index >= size)
    throw "Index wout of bounds!";
void DynamicArray::set(int index, int value) {
 rangeCheck(index);
 storage[index] = value;
int DynamicArray::get(int index)
 rangeCheck(index);
 return storage[index];
```



```
void DynamicArray::insertAt(int index, int value)
  if (index < 0 || index > size)
    throw "Index out of bounds!";
 ensureCapacity(size + 1);
 int moveCount = size - index;
  if (moveCount != 0)
   memmove(storage + index + 1,
        storage + index.
        sizeof(int) * moveCount);
  storage[index] = value;
  size++:
```



Dynamic Array: Using



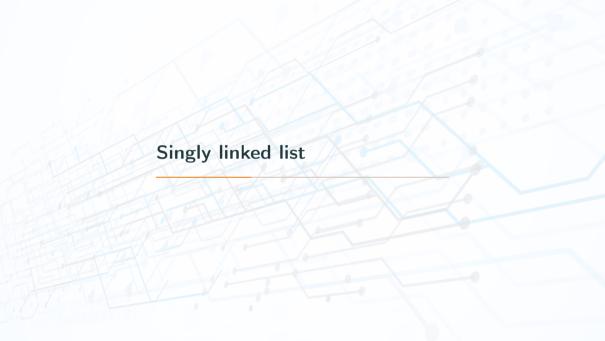
```
void DynamicArray::print() {
    for (int i=0; i < this -> size; i++) {
        cout << storage[i] << "";
int main() .
  cout << "Dynamic Array" << endl;
  DynamicArray* da = new DynamicArray(10);
 da->insertAt(0, 55);
 // ...
 da->print();
  return 0;
```

Contiguous Implementation of List



In processing a contiguous list with n elements:

- Insert and Remove operate in time approximately proportional to n (require physical shifting).
- Clear, Empty, Full, Size, Replace, and Retrieve in constant time.



Linked List



Definition

A linked list is an ordered collection of data in which each element contains the location of the next element.

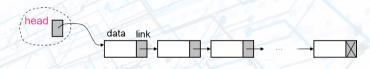


Figure 1: Singly Linked List

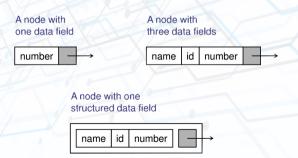
```
list // Linked Implementation of List
  head <pointer>
  count <integer> // number of elements (optional)
end list
```



The elements in a linked list are called nodes.

A node in a linked list is a structure that has at least two fields:

- the data,
- the address of the next node.





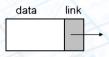
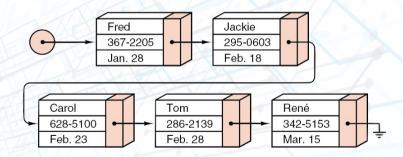


Figure 2: Linked list node structure

```
node
data <dataType>
link <pointer>
end node
```

```
// General dataType:
dataType
  key <keyType>
  field1 <...>
  field2 <...>
    ...
  fieldn <...>
end dataType
```







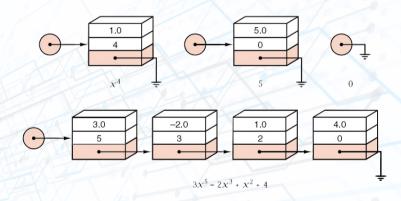


Figure 3: List representing polynomial

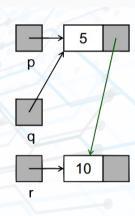


```
node
  data <dataType>
  link <pointer>
end node
```

```
struct Node {
   int data;
   Node *link;
};
```



```
#include <iostream>
using namespace std:
struct Node {
   int data:
   Node *link;
int main () {
  Node *p = new Node();
  p\rightarrow data = 5;
  cout << p->data << endl;
  Node *q = p:
  cout << q->data << endl;
  Node *r = new Node();
  r\rightarrow data = 10;
  q \rightarrow link = r;
  cout << p->link ->data << endl;
```



struct Node {

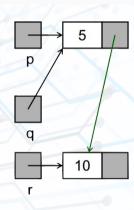


```
int data;
    Node *link;
template < class | ItemType>
struct Node {
   ItemType data;
   Node<ItemType> *link;
```

```
struct Node {
   float data;
   Node *link;
}:
```



```
#include <iostream>
using namespace std:
template < class | temType>
struct Node {
  ItemType data;
  Node<ItemType> *link:
};
int main () {
  Node < int > *p = new Node < int > ();
  p\rightarrow data = 5;
  cout << p->data << endl;
  Node < int > *q = p;
  cout << q->data << endl;
  Node < int > *r = new Node < int > ();
  r\rightarrow data = 10;
  q \rightarrow link = r;
  cout << p->link ->data << endl:
```



Node implementation in C++



```
template < class | temType>
class Node {
  ItemType data;
  Node<ItemType> *link;
  public:
    Node(){
      this -> link = NULL:
    Node(ItemType data){
      this -> data = data;
      this \rightarrow link = NULL;
```

Linked list implementation in C++



```
template <class List_ItemType>
class LinkedList {
  Node<List_ItemType> *head;
  int count;

public:
    LinkedList();
    ~LinkedList();
};
```

```
list
  head <pointer>
  count <integer>
end list
```

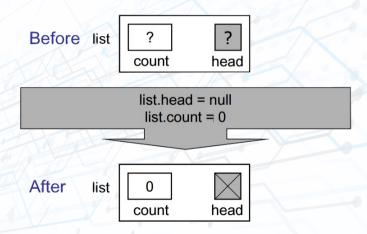
Linked list operations



- Create an empty linked list
- Insert a node into a linked list
- Delete a node from a linked list
- Traverse a linked list
- Destroy a linked list

Create an empty linked list





Create an empty linked list



Algorithm createList(ref list <metadata>)

Initializes metadata for a linked list

Pre: list is a metadata structure passed by reference

Post: metadata initialized

list.head = null

list.count = 0

return

End createList

Create an empty linked list



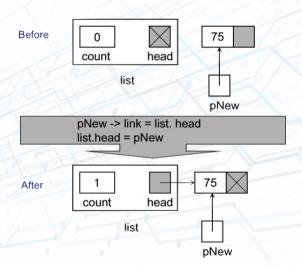
```
template < class List ItemType>
class LinkedList {
  Node<List ItemType> *head;
  int count:
  public:
    LinkedList();
    ~LinkedList();
template < class List ItemType>
LinkedList <List ItemType >:: LinkedList(){
  this ->head = NULL;
  this -> count = 0;
```



- 1. Allocate memory for the new node and set up data.
- 2. Locate the pointer p in the list, which will point to the new node:
 - If the new node becomes the first element in the List: p is list.head.
 - Otherwise: p is pPre->link, where pPre points to the predecessor of the new node.
- 3. Point the new node to its successor.
- 4. Point the pointer p to the new node.

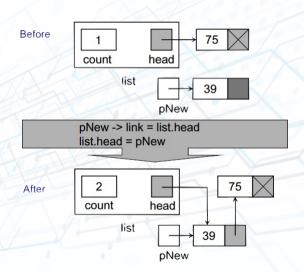
Insert into an empty linked list





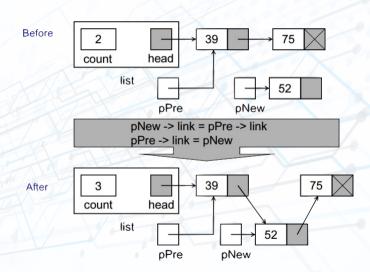
Insert at the beginning





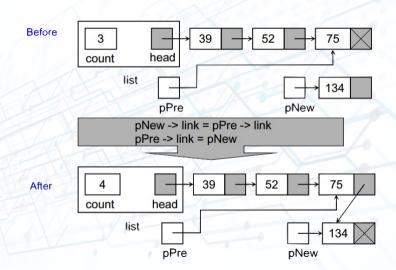
Insert in the middle





Insert at the end







- Insertion is successful when allocation memory for the new node is successful.
- There is no difference between insertion at the beginning of the list and insertion into an empty list.

```
pNew->link = list.head
list.head = pNew
```

• There is no difference between insertion in the middle and insertion at the end of the list.

```
pNew->link = pPre->link
pPre->link = pNew
```



Algorithm insertNode(ref list <metadata>,
val pPre <node pointer>,
val dataIn <dataType>)
Inserts data into a new node in the linked list.



```
allocate(pNew)
if memory overflow then
    return false
end
pNew -> data = dataIn
if pPre = null then
    // Adding at the beginning or into empty list
    pNew -> link = list.head
    list.head = pNew
else
    // Adding in the middle or at the end
    pNew -> link = pPre -> link
    pPre -> link = pNew
end
list.count = list.count + 1
return true
End insertNode
```



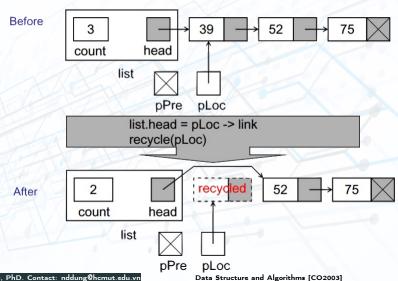
```
template < class List Item Type >
int LinkedList<List ItemType >:: InsertNode(Node<List ItemType > *pPre, List ItemType value) {
  Node<List ItemType> *pNew = new Node<List ItemType >();
  if (pNew == NULL)
    return 0:
  pNew->data = value:
  if (pPre== NULL){
    pNew->link = this->head;
    this -> head = pNew;
  } else {
    pNew->link = pPre->link;
    pPre \rightarrow link = pNew;
  this -> count++:
  return 1:
```



- 1. Locate the pointer p in the list which points to the node to be deleted (pLoc will hold the node to be deleted).
 - If that node is the first element in the List: p is list.head.
 - Otherwise: p is pPre->link, where pPre points to the predecessor of the node to be deleted.
- 2. p points to the successor of the node to be deleted.
- 3. Recycle the memory of the deleted node.

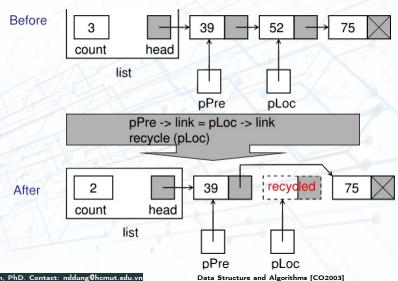
Delete first node





General deletion case







- Removal is successful when the node to be deleted is found.
- There is no difference between deleting the node from the beginning of the list and deleting the only node in the list.

```
list .head = pLoc->link
recycle(pLoc)
```

• There is no difference between deleting a node from the middle and deleting a node from the end of the list.

```
pPre->link = pLoc->link
recycle(pLoc)
```



```
Algorithm deleteNode(ref list <metadata>,
val pPre <node pointer>,
val pLoc <node pointer>,
ref dataOut <dataType>)
```

Deletes data from a linked list and returns it to calling module.

Pre: list is metadata structure to a valid list

pPre is a pointer to predecessor node

pLoc is a pointer to node to be deleted

dataOut is variable to receive deleted data

Post: data have been deleted and returned to caller



```
dataOut = pLoc -> data
if pPre = null then
   // Delete first node
   list.head = pLoc -> link
else
   // Delete other nodes
   pPre -> link = pLoc -> link
end
list.count = list.count - 1
recycle (pLoc)
return
End deleteNode
```



```
template < class List Item Type >
List ItemType LinkedList <List ItemType > :: DeleteNode(Node < List ItemType > *pPre,
                                                   Node<List ItemType> *pLoc) {
  List ItemType result = pLoc->data;
  if (pPre== NULL){
    this -> head = pLoc-> link;
   else {
    pPre->link = pLoc->link:
  this -> count --:
  delete pLoc;
  return result;
```



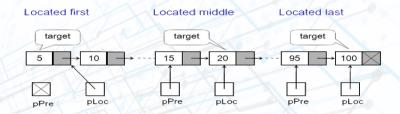
- Sequence Search has to be used for the linked list.
- Function Search of List ADT:

```
<ErrorCode> Search (val target <dataType>,
    ref pPre <pointer>, ref pLoc <pointer>)
```

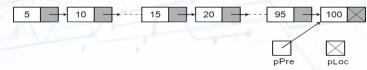
Searches a node and returns a pointer to it if found.



Successful Searches



Unsuccessful Searches





Searches a node in a singly linked list and return a pointer to it if found.

Pre: target is the value need to be found

Post: pLoc points to the first node which is equal target, or is NULL if not found. pPre points to the predecessor of the first node which is equal target, or points to the last node if not found.

Return found or notFound



```
pPre = NULL
pLoc = list.head
while (pLoc is not NULL) AND (target != pLoc ->data) do
   pPre = pLoc
   pLoc = pLoc -> link
end
if pLoc is NULL then
   return notFound
else
   return found
end
End Search
```



```
template < class List Item Type >
int LinkedList < List ItemType >:: Search (
        List ItemType value,
        Node<List ItemType>* &pPre,
        Node<List ItemType>* &pLoc){
  pPre = NULL:
  pLoc = this ->head;
  while (pLoc != NULL && pLoc->data != value){
    pPre = pLoc;
    pLoc = pLoc->link;
  return (pLoc != NULL);
  // found: 1; notfound: 0
```

Traverse a linked list



Traverse module controls the loop: calling a user-supplied algorithm to process data

Algorithm Traverse(ref <void> process (ref Data <DataType>))

Traverses the list, performing the given operation on each element.

Pre: process is user-supplied

Post: The action specified by process has been performed on every element in the list, beginning at the first element and doing each in turn.

```
pWalker = list.head
while pWalker not null do
process(pWalker -> data)
pWalker = pWalker -> link
end
```

Lecturer: Duc Dung Nguyen, PhD. Contact: nddung@hcmut.edu.vn

Traverse a linked list



```
template < class List Item Type >
void LinkedList < List ItemType >:: Traverse() {
  Node < List ItemType > *p = head;
  while (p != NULL){
    p->data++; // process data here!!!
    p = p \rightarrow link:
template < class List Item Type >
void LinkedList < List ItemType >::
        Traverse2(List ItemType *&visit){
  Node<List ItemType> *p = this->head;
  int i = 0:
  while (p != NULL \&\& i < this -> count)
    visit[i] = p->data;
    p = p \rightarrow link;
    i + +:
```

Destroy a linked list



```
Algorithm destroyList (val list <metadata>)
Deletes all data in list.
Pre: list is metadata structure to a valid list
Post: all data deleted
while list head not null do
   dltPtr = list.head
   list.head = this.head -> link
   recycle (dltPtr)
end
No data left in list. Reset metadata
list.count = 0
return
```

Destroy a linked list



```
template < class List Item Type >
void LinkedList < List ItemType >:: Clear(){
  Node<List ItemType> *temp;
  while (this -> head != NULL){
    temp = this ->head:
    this -> head = this -> head -> link;
    delete temp;
  this -> count = 0:
template < class List Item Type >
LinkedList < List ItemType >:: ~ LinkedList(){
  this -> Clear ();
```

Linked list implementation in C++



```
template < class List Item Type >
class LinkedList{
  Node<List ItemType>* head;
  int count:
protected:
  int InsertNode(Node<List ItemType>* pPre,
                List ItemType value);
  List ItemType DeleteNode(Node<List ItemType>* pPre,
                        Node<List ItemType>* pLoc);
  int Search (List Item Type value,
                Node<List ItemType>* &pPre,
                Node<List ItemType>* &pLoc);
```

Linked list implementation in C++



```
template < class List Item Type >
class LinkedList{
protected:
 // ...
public:
  LinkedList();
 ~LinkedList();
  void InsertFirst (List ItemType value);
  void InsertLast(List ItemType value);
  int InsertItem(List ItemType value, int position);
  void DeleteFirst();
  void DeleteLast();
  int Deleteltem (int postion);
  int GetItem(int position, List ItemType &dataOut);
  void Traverse();
  LinkedList <List ItemType >* Clone();
  void Print2Console();
  void Clear();
```

Linked list implementation in C++



How to use Linked List data structure?

Linked list implementation in C++



How to use Linked List data structure?

```
// ...
int value;
LinkedList<int>* myList2 = myList->Clone();
cout << "List_2:" << endl;
myList2->Print2Console();
myList2->Getltem(1, value);
cout << "Value_uat_position_u1:_u" << value;

delete myList;
delete myList;
return 1;</pre>
```

Sample Solution: Insert



```
template < class List ItemType>
int LinkedList <List ItemType >::InsertItem(
        List ItemType value, int position) {
  if (position < 0 || position > this -> count)
    return 0:
  Node<List ItemType> *newPtr, *pPre;
  newPtr = new Node<List ItemType >();
  if (newPtr == NULL)
  return 0:
  newPtr->data = value:
  if (head == NULL) {
    head = newPtr:
    newPtr->link = NULL:
  } else if (position == 0) {
    newPtr->link = head:
    head = newPtr:
```

Sample Solution: Insert



```
else {
 // Find the position of pPre
  pPre = this->head;
  for (int i = 0; i < position -1; i++)
   pPre = pPre->link;
 // Insert new node
  newPtr->link = pPre->link;
  pPre->link = newPtr:
this -> count++;
return 1;
```

Sample Solution: Delete



```
template < class List ItemType>
int LinkedList < List ItemType >:: DeleteItem (int position) {
  if (position < 0 || position > this -> count)
    return 0:
  Node < List Item Type > * dItPtr , *pPre;
  if (position == 0) {
    dltPtr = head:
    head = head->link:
  } else {
    pPre= this->head;
    for (int i = 0; i < position -1; i++)
      pPre = pPre->link;
    dltPtr = pPre->link:
    pPre->link = dltPtr->link:
  delete dltPtr;
  this -> count --:
  return 1:
```

Sample Solution: Clone



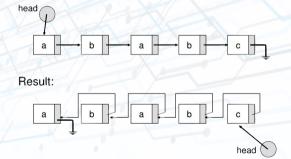
```
template < class List ItemType>
LinkedList <List ItemType >*
         LinkedList < List ItemType > :: Clone(){
  LinkedList <List ItemType>* result =
        new LinkedList < List ItemType >();
  Node<List ItemType>* p = this->head;
  while (p != NULL) {
    result -> InsertLast (p->data);
    p = p \rightarrow link:
  result -> count = this -> count;
  return result;
```

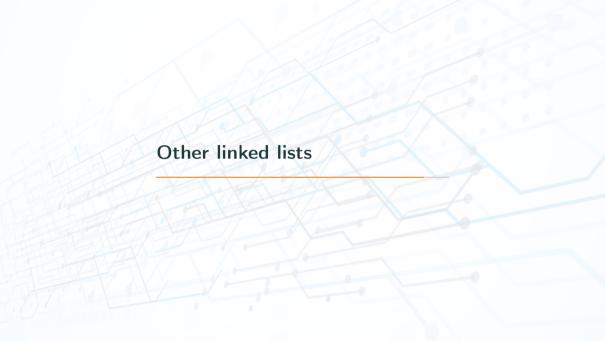
Reverse a linked list



Exercise

```
template <class List_ItemType>
void LinkedList<List_ItemType>::Reverse(){
   // ...
}
```





Doubly Linked List



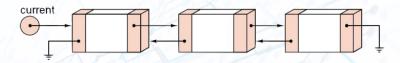


Figure 4: Doubly Linked List allows going forward and backward.

```
node
  data <dataType>
  next <pointer>
  previous <pointer>
end node
```

```
list
  current <pointer>
end list
```

Doubly Linked List



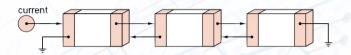


Figure 5: Doubly Linked List allows going forward and backward.

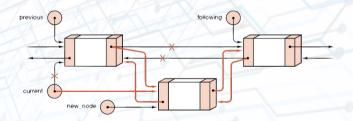
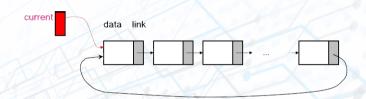


Figure 6: Insert an element in Doubly Linked List.

Circularly Linked List



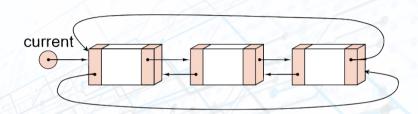


node
 data <dataType>
 link <pointer>
end node

list
 current <pointer>
end list

Double circularly Linked List





node
 data <dataType>
 next <pointer>
 previous <pointer>
end node

list
 current <pointer>
end list

Comparison of implementations of list

Arrays: Pros and Cons



• Pros:

Access to an array element is fast since we can compute its location quickly.

· Cons:

- If we want to insert or delete an element, we have to shift subsequent elements which slows our computation down.
- We need a large enough block of memory to hold our array.

Linked Lists: Pros and Cons



• Pros:

• Inserting and deleting data does not require us to move/shift subsequent data elements.

· Cons:

• If we want to access a specific element, we need to traverse the list from the head of the list to find it which can take longer than an array access.

Comparison of implementations of list



- Contiguous storage is generally preferable when:
 - the entries are individually very small;
 - the size of the list is known when the program is written;
 - few insertions or deletions need to be made except at the end of the list; and
 - random access is important.
- Linked storage proves superior when:
 - the entries are large;
 - the size of the list is not known in advance; and
 - flexibility is needed in inserting, deleting, and rearranging the entries.