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(национальный исследовательский университет)»  
(МГТУ им. Н.Э. Баумана)

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ФАКУЛЬТЕТ \_\_\_\_\_ Информатика, искусственный интеллект и системы управления \_\_\_\_\_

КАФЕДРА \_\_\_\_\_ Системы обработки информации и управления \_\_\_\_\_

## **ОТЧЁТ К ЛАБОРАТОРНОЙ РАБОТЕ №6**

***НА ТЕМУ:***

**Разработка системы предсказания поведения на  
основании графовых моделей**

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Группа: ИУ5-23М

Преподаватель: Гапанюк Ю.Е.

2022 г.

Цель лабораторной работы: обучение работе с предварительной обработкой графовых типов данных и обучением нейронных сетей на графовых данных.

Задание:

- Подготовить датасет графовых данных
- Подобрать модель и гиперпараметры обучения для получения качества  $AUC > 0.65$

# Лабораторная работа №6:

## "Разработка системы предсказания поведения на основании графовых моделей"

*Цель:* обучение работе с графовым типом данных и графовыми нейронными сетями.

*Задача:* подготовить графовый датасет из базы данных о покупках и построить модель предсказания совершения покупки.

## Графовые нейронные сети

**Графовые нейронные сети** - тип нейронной сети, которая напрямую работает со структурой графа. Типичным применением GNN являются:

- Классификация узлов;
- Предсказание связей;
- Графовая классификация;
- Распознавание движений;
- Рекомендательные системы.

В данной лабораторной работе будет происходить работа над **графовыми сверточными сетями**. Отличаются они от сверточных нейронных сетей нефиксированной структурой, функция свертки не является .

Подробнее можно прочитать тут: <https://towardsdatascience.com/understanding-graph-convolutional-networks-for-node-classification-a2bfdb7aba7b>

Тут можно почитать современные подходы к использованию графовых сверточных сетей <https://paperswithcode.com/method/gcn>

## Датасет

В качестве базы данных предлагаем использовать датасет о покупках пользователей в одном магазине товаров RecSys Challenge 2015 (<https://www.kaggle.com/datasets/chadgostopp/recsys-challenge-2015>).

Скачать датасет можно отсюда: <https://drive.google.com/drive/folders/1gtAeXPTj-c0RwVOKreMrZ3bfSmCwl2y-?usp=sharing> (lite-версия является облегченной версией исходного датасета, рекомендуем использовать её)

Также рекомендуем загружать данные в виде архива и распаковывать через пакет zipfile или/и скачивать датасет в собственный Google Drive и примонтировать его в колаб.

## Установка библиотек, выгрузка исходных датасетов

```
In [5]: import torch
        print(torch.__version__)
```

```
1.11.0+cu113
```

```
In [7]: # Install pytorch geometric
        !pip install gdown
        !pip install torch
        !pip install torch-sparse -f https://pytorch-geometric.com/whl/torch-1.11.0%2Bcu113.html
        !pip install torch-cluster -f https://pytorch-geometric.com/whl/torch-1.11.0%2Bcu113.html
        !pip install torch-spline-conv -f https://pytorch-geometric.com/whl/torch-1.11.0%2Bcu113.html
        !pip install torch-geometric -f https://pytorch-geometric.com/whl/torch-1.11.0%2Bcu113.html
```

Looking in indexes: <https://pypi.org/simple>, <https://us-python.pkg.dev/colab-wheels/public/simple/>  
Requirement already satisfied: gdown in [/usr/local/lib/python3.7/dist-packages](#) (4.4.0)  
Requirement already satisfied: six in [/usr/local/lib/python3.7/dist-packages](#) (from gdown) (1.15.0)  
Requirement already satisfied: requests[socks] in [/usr/local/lib/python3.7/dist-packages](#) (from gdown) (2.23.0)  
Requirement already satisfied: tqdm in [/usr/local/lib/python3.7/dist-packages](#) (from gdown) (4.64.0)  
Requirement already satisfied: filelock in [/usr/local/lib/python3.7/dist-packages](#) (from gdown) (3.7.0)  
Requirement already satisfied: beautifulsoup4 in [/usr/local/lib/python3.7/dist-packages](#) (from gdown) (4.6.3)  
Requirement already satisfied: idna<3,>=2.5 in [/usr/local/lib/python3.7/dist-packages](#) (from requests[socks]->gdown) (2.10)  
Requirement already satisfied: chardet<4,>=3.0.2 in [/usr/local/lib/python3.7/dist-packages](#) (from requests[socks]->gdown) (3.0.4)  
Requirement already satisfied: certifi>=2017.4.17 in [/usr/local/lib/python3.7/dist-packages](#) (from requests[socks]->gdown) (2022.5.18.1)  
Requirement already satisfied: urllib3!=1.25.0,!>=1.25.1,<1.26,>=1.21.1 in [/usr/local/lib/python3.7/dist-packages](#) (from requests[socks]->gdown) (1.24.3)  
Requirement already satisfied: PySocks!=1.5.7,>=1.5.6 in [/usr/local/lib/python3.7/dist-packages](#) (from requests[socks]->gdown) (1.7.1)  
Looking in indexes: <https://pypi.org/simple>, <https://us-python.pkg.dev/colab-wheels/public/simple/>  
Requirement already satisfied: torch in [/usr/local/lib/python3.7/dist-packages](#) (1.11.0+cu113)  
Requirement already satisfied: typing-extensions in [/usr/local/lib/python3.7/dist-packages](#) (from torch) (4.2.0)  
Looking in indexes: <https://pypi.org/simple>, <https://us-python.pkg.dev/colab-wheels/public/simple/>  
Looking in links: <https://pytorch-geometric.com/whl/torch-1.11.0%2Bcu113.html>  
Requirement already satisfied: torch-sparse in [/usr/local/lib/python3.7/dist-packages](#) (0.6.13)  
Requirement already satisfied: scipy in [/usr/local/lib/python3.7/dist-packages](#) (from torch-sparse) (1.4.1)  
Requirement already satisfied: numpy>=1.13.3 in [/usr/local/lib/python3.7/dist-packages](#) (from scipy->torch-sparse) (1.21.6)  
Looking in indexes: <https://pypi.org/simple>, <https://us-python.pkg.dev/colab-wheels/public/simple/>  
Looking in links: <https://pytorch-geometric.com/whl/torch-1.11.0%2Bcu113.html>  
Requirement already satisfied: torch-cluster in [/usr/local/lib/python3.7/dist-packages](#) (1.6.0)  
Looking in indexes: <https://pypi.org/simple>, <https://us-python.pkg.dev/colab-wheels/public/simple/>  
Looking in links: <https://pytorch-geometric.com/whl/torch-1.11.0%2Bcu113.html>  
Requirement already satisfied: torch-spline-conv in [/usr/local/lib/python3.7/dist-packages](#) (1.2.1)  
Looking in indexes: <https://pypi.org/simple>, <https://us-python.pkg.dev/colab-wheels/public/simple/>  
Looking in links: <https://pytorch-geometric.com/whl/torch-1.11.0%2Bcu113.html>  
Requirement already satisfied: torch-geometric in [/usr/local/lib/python3.7/dist-packages](#) (2.0.4)  
Requirement already satisfied: pyparsing in [/usr/local/lib/python3.7/dist-packages](#) (from torch-geometric) (3.0.9)  
Requirement already satisfied: pandas in [/usr/local/lib/python3.7/dist-packages](#) (from torch-geometric) (1.3.5)  
Requirement already satisfied: requests in [/usr/local/lib/python3.7/dist-packages](#) (from torch-geometric) (2.23.0)  
Requirement already satisfied: tqdm in [/usr/local/lib/python3.7/dist-packages](#) (from torch-geometric) (4.64.0)  
Requirement already satisfied: scipy in [/usr/local/lib/python3.7/dist-packages](#) (from torch-geometric) (1.4.1)  
Requirement already satisfied: scikit-learn in [/usr/local/lib/python3.7/dist-packages](#) (from torch-geometric) (1.0.2)  
Requirement already satisfied: Jinja2 in [/usr/local/lib/python3.7/dist-packages](#) (from torch-geometric) (2.11.3)  
Requirement already satisfied: numpy in [/usr/local/lib/python3.7/dist-packages](#) (from torch-geometric) (1.21.6)  
Requirement already satisfied: MarkupSafe>=0.23 in [/usr/local/lib/python3.7/dist-packages](#) (from Jinja2->torch-geometric) (2.0.1)  
Requirement already satisfied: python-dateutil>=2.7.3 in [/usr/local/lib/python3.7/dist-packages](#) (from pandas->torch-geometric) (2.8.2)  
Requirement already satisfied: pytz>=2017.3 in [/usr/local/lib/python3.7/dist-packages](#) (from pandas->torch-geometric) (2022.1)  
Requirement already satisfied: six>=1.5 in [/usr/local/lib/python3.7/dist-packages](#) (from python-dateutil>=2.7.3->pandas->torch-geometric) (1.15.0)  
Requirement already satisfied: chardet<4,>=3.0.2 in [/usr/local/lib/python3.7/dist-packages](#) (from requests->torch-geometric) (3.0.4)  
Requirement already satisfied: idna<3,>=2.5 in [/usr/local/lib/python3.7/dist-packages](#) (from requests->torch-geometric) (2.10)  
Requirement already satisfied: pandas!=1.25.0,!>=1.25.1,<1.26,>=1.21.1 in [/usr/local/lib/python3.7/dist-packages](#) (from requests->torch-geometric) (1.24.3)  
Requirement already satisfied: certifi>=2017.4.17 in [/usr/local/lib/python3.7/dist-packages](#) (from requests->torch-geometric) (2022.5.18.1)  
Requirement already satisfied: joblib>=0.11 in [/usr/local/lib/python3.7/dist-packages](#) (from scikit-learn->torch-geometric) (1.1.0)  
Requirement already satisfied: threadpoolctl>=2.0.0 in [/usr/local/lib/python3.7/dist-packages](#) (from scikit-learn->torch-geometric) (3.1.0)

```
In [8]: !pip install torch-scatter -f https://data.pyg.org/whl/torch-1.11.0%2Bcu113.html
```

Looking in indexes: <https://pypi.org/simple>, <https://us-python.pkg.dev/colab-wheels/public/simple/>

Looking in links: <https://data.pyg.org/whl/torch-1.11.0%2Bcu113.html>

Collecting torch-scatter

Downloading [https://data.pyg.org/whl/torch-1.11.0%2Bcu113/torch\\_scatter-2.0.9-cp37-cp37m-linux\\_x86\\_64.whl](https://data.pyg.org/whl/torch-1.11.0%2Bcu113/torch_scatter-2.0.9-cp37-cp37m-linux_x86_64.whl) (7.9 MB)

 7.9 MB 53.1 MB/s

Installing collected packages: torch-scatter

Successfully installed torch-scatter-2.0.9

```
In [9]: import numpy as np
import pandas as pd
import pickle
import csv
import os

from sklearn.preprocessing import LabelEncoder

import torch

# PyG - PyTorch Geometric
from torch_geometric.data import Data, DataLoader, InMemoryDataset

from tqdm import tqdm

RANDOM_SEED = 42 #@param { type: "integer" }
BASE_DIR = '/content/' #@param { type: "string" }
np.random.seed(RANDOM_SEED)
```

```
In [11]: # Check if CUDA is available for colab
torch.cuda.is_available
```

```
Out[11]: <function torch.cuda.is_available>
```

```
In [12]: !gdown --id 1ebYsQlb6PRQM0E7Cnx1CwWVFDNJKYuzR
```

```
category=FutureWarning,
Downloading...
From: https://drive.google.com/uc?id=1ebYsQlb6PRQMOE7Cnx1CwWVFDNjKYuzR
To: /content/yoochoose-data-lite.zip
100% 49.8M/49.8M [00:01<00:00, 35.2MB/s]
In [13]: # Unpack files from zip-file
import zipfile
with zipfile.ZipFile(BASE_DIR + 'yoochoose-data-lite.zip', 'r') as zip_ref:
    zip_ref.extractall(BASE_DIR)
```

## Анализ исходных данных

```
In [14]: # Read dataset of items in store
df = pd.read_csv(BASE_DIR + 'yoochoose-clicks-lite.dat')
# df.columns = ['session_id', 'timestamp', 'item_id', 'category']
df.head()
```

/usr/local/lib/python3.7/dist-packages/IPython/core/interactiveshell.py:2882: DtypeWarning: Columns (3) have mixed types.Specify dtype option on import or set low\_memory=False.

```
exec(code_obj, self.user_global_ns, self.user_ns)
Out[14]:
```

	session_id	timestamp	item_id	category
0	9	2014-04-06T11:26:24.127Z	214576500	0
1	9	2014-04-06T11:28:54.654Z	214576500	0
2	9	2014-04-06T11:29:13.479Z	214576500	0
3	19	2014-04-01T20:52:12.357Z	214561790	0
4	19	2014-04-01T20:52:13.758Z	214561790	0

```
In [15]: # Read dataset of purchases
buy_df = pd.read_csv(BASE_DIR + 'yoochoose-buys-lite.dat')
# buy_df.columns = ['session_id', 'timestamp', 'item_id', 'price', 'quantity']
buy_df.head()
```

```
Out[15]:
```

	session_id	timestamp	item_id	price	quantity
0	420374	2014-04-06T18:44:58.314Z	214537888	12462	1
1	420374	2014-04-06T18:44:58.325Z	214537850	10471	1
2	489758	2014-04-06T09:59:52.422Z	214826955	1360	2
3	489758	2014-04-06T09:59:52.476Z	214826715	732	2
4	489758	2014-04-06T09:59:52.578Z	214827026	1046	1

```
In [16]: # Filter out item session with length < 2
df['valid_session'] = df.session_id.map(df.groupby('session_id')['item_id'].size() > 2)
df = df.loc[df.valid_session].drop('valid_session',axis=1)
df.nunique()
```

```
Out[16]:session_id    1000000
timestamp    5557758
item_id      37644
category      275
dtype: int64
```

```
In [17]: # Randomly sample a couple of them
NUM_SESSIONS = 50000 #@param { type: "integer" }
sampled_session_id = np.random.choice(df.session_id.unique(), NUM_SESSIONS, replace=False)
df = df.loc[df.session_id.isin(sampled_session_id)]
df.nunique()
```

```
Out[17]:session_id    50000
timestamp    278442
item_id      18461
category      110
dtype: int64
```

```
In [18]: # Average length of session
df.groupby('session_id')['item_id'].size().mean()
```

```
Out[18]:5.56902
```

```
In [19]: # Encode item and category id in item dataset so that ids will be in range (0,len(df.item.unique()))
item_encoder = LabelEncoder()
category_encoder = LabelEncoder()
df['item_id'] = item_encoder.fit_transform(df.item_id)
df['category'] = category_encoder.fit_transform(df.category.apply(str))
df.head()
```

Out[19]:

	session_id	timestamp	item_id	price	category
	0	9	2014-04-06T11:26:24.127Z	3496	0
	1	9	2014-04-06T11:28:54.654Z	3496	0
	2	9	2014-04-06T11:29:13.479Z	3496	0
	102	171	2014-04-03T17:45:25.575Z	10049	0
	103	171	2014-04-03T17:45:33.177Z	10137	0

In [20]:

```
# Encode item and category id in purchase dataset
buy_df = buy_df.loc[buy_df.session_id.isin(df.session_id)]
buy_df['item_id'] = item_encoder.transform(buy_df.item_id)
buy_df.head()
```

/usr/local/lib/python3.7/dist-packages/ipykernel\_launcher.py:3: SettingWithCopyWarning:  
A value is trying to be set on a copy of a slice from a DataFrame.  
Try using .loc[row\_indexer,col\_indexer] = value instead

See the caveats in the documentation: [https://pandas.pydata.org/pandas-docs/stable/user\\_guide/indexing.html#returning-a-view-versus-a-copy](https://pandas.pydata.org/pandas-docs/stable/user_guide/indexing.html#returning-a-view-versus-a-copy)  
This is separate from the ipykernel package so we can avoid doing imports until

Out[20]:

	session_id	timestamp	item_id	price	quantity
46	489491	2014-04-06T12:41:34.047Z	12633	1046	4
47	489491	2014-04-06T12:41:34.091Z	12634	627	2
61	70353	2014-04-06T10:55:06.086Z	14345	41783	1
62	489671	2014-04-03T15:48:37.392Z	12489	4188	1
63	489671	2014-04-03T15:59:35.495Z	12489	4188	1

In [21]:

```
# Get item dictionary with grouping by session
buy_item_dict = dict(buy_df.groupby('session_id')['item_id'].apply(list))
buy_item_dict
```

Out[21]:

{714: [14720, 14915, 14917, 3089],
6016: [15154],
9797: [12459, 11831],
9862: [13621],
10457: [10079, 2951],
10587: [11764],
10678: [6310, 3914],
13476: [13631, 12881, 12878, 12880, 12852],
16953: [2883, 7739],
19029: [8276, 2171, 10385, 11419],
19958: [10059, 10059],
23548: [11236],
24439: [12506, 12497],
28709: [4037],
29647: [12830, 12827],
33907: [2480, 6012],
34541: [627, 12827],
36548: [14720, 14916],
38019: [11222, 11227],
38261: [3447],
41333: [11839, 12826, 11839],
41598: [10712, 10711, 2034, 10713],
43834: [11203, 11203],
44153: [15075, 15088],
44813: [12819, 12634],
48974: [7428, 12774],
49886: [2373, 11207, 11221, 10625],
54961: [1965, 11360, 12812, 7803],
55877: [4804],
62553: [12793],
64802: [11317],
69277: [7933],
70353: [14345],
71832: [11839, 12362],
73271: [11236, 11236, 11237],
74083: [12864],
79937: [11884, 11825, 11825, 11884],
87673: [12608],
88198: [11201, 11201],
88723: [11236, 11236],
89393: [11236],
91903: [11200],
92224: [255],
93282: [14842,
5737,
5733,
421,
4275,

4489,  
7043,  
7047,  
5739,  
4498,  
7048,  
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7140,  
2065,  
2071,  
2066],  
100952: [9849, 9849],  
103133: [11228],  
104659: [11424, 4839, 8471],  
108344: [13479, 11221, 11208],  
110788: [1187],  
114461: [2376, 12826],  
116004: [9730],  
116373: [9868],  
122179: [316],  
125163: [3548, 5766],  
126769: [3318, 12770, 12769],  
127311: [12831, 12552, 12846, 12342, 12772, 12773],  
128359: [4483],  
128562: [11476, 12787, 12812, 12552],  
132646: [5654],  
136192: [12880, 12852, 12878],  
138344: [4827],  
142132: [627, 12767],  
142902: [11226, 11226],  
143246: [4791],  
144241: [12632],  
150664: [12825, 11333, 13046, 12839, 10484],  
150723: [12621, 13444, 12619, 4145],  
150926: [12812, 12787, 12813],  
152571: [3943],  
157247: [8285],  
160843: [11792],  
164104: [12839, 12825, 12616, 9932],  
169179: [10715, 10714],  
171209: [12789],  
171554: [15058],  
172101: [11469, 8711, 8721, 12629],  
172324: [14720, 14915, 14917, 14916],  
175289: [12634],  
175897: [11223],  
177247: [12634, 12632],  
177641: [2248],  
182148: [13793, 12367],  
185409: [11200],  
187838: [3409],  
188339: [12630, 12788],  
188726: [11605],  
189138: [12812, 12787],  
192869: [12766],  
193483: [6333],  
197056: [13481, 13481, 13481],  
197889: [12557],  
198147: [11221],  
198939: [12557],  
201316: [12360],  
202037: [13479, 11227, 11202],  
203623: [8253],  
204676: [11236, 11236],  
205377: [12496, 12497, 12506, 12497, 12506, 12496],  
212573: [4254],  
214007: [12632],  
218862: [15058],  
219736: [12633],  
221904: [6044, 7972, 12619],  
222178: [9269],  
222293: [12881, 12852, 12880, 13631, 11658, 12878],  
223497: [12571, 12549, 7670, 12674, 7697, 12548, 12550, 8303, 12625, 8306],  
224769: [3914],  
224788: [4483],  
227657: [11226, 10534, 11249],  
229858: [14618, 576],  
232349: [179, 4804],  
232521: [12321, 12321],  
239123: [12677, 12632],  
239224: [4901, 4901],  
241053: [12813, 15582, 15554, 15560, 15249, 15446],  
242477: [12789, 12634, 1032, 12632]

242636: [390],  
243838: [14989, 13981],  
245392: [7934, 10052, 12793],  
245427: [4484],  
245733: [12417, 12770, 12630],  
247706: [3718],  
248291: [11203, 11222],  
249438: [15015],  
251596: [12374],  
251777: [1835],  
256753: [11206],  
257992: [446, 11372, 12489, 9358],  
259584: [15304, 15303, 15064],  
260656: [16],  
270696: [7436, 1105, 7436, 1105],  
272839: [10292],  
276266: [9791],  
277534: [11521, 12832, 337],  
283099: [15058],  
284831: [11225],  
285344: [12506, 12503, 12497, 12557, 12506, 12497, 12503, 12557],  
287659: [8278],  
291433: [13666, 12620, 12618, 2971],  
294559: [8190],  
295229: [8293, 7924, 7908, 6489, 12548, 11740, 12550, 12832, 7919],  
295338: [12601],  
295684: [12766, 10480, 12443, 627, 12830],  
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```

## Сборка выборки для обучения

```

In [22]: # Transform df into tensor data
def transform_dataset(df, buy_item_dict):
    data_list = []

    # Group by session
    grouped = df.groupby('session_id')
    for session_id, group in tqdm(grouped):
        le = LabelEncoder()
        sess_item_id = le.fit_transform(group.item_id)
        group = group.reset_index(drop=True)
        group['sess_item_id'] = sess_item_id

    #get input features
    node_features = group.loc[group.session_id==session_id,
                             ['sess_item_id','item_id','category']].sort_values('sess_item_id')[['item_id','category']].drop_duplicates().values
    node_features = torch.LongTensor(node_features).unsqueeze(1)
    target_nodes = group.sess_item_id.values[1:]
    source_nodes = group.sess_item_id.values[:-1]

    edge_index = torch.tensor([source_nodes,
                               target_nodes], dtype=torch.long)
    x = node_features

    #get result

```

```

if session_id in buy_item_dict:
    positive_indices = le.transform(buy_item_dict[session_id])
    label = np.zeros(len(node_features))
    label[positive_indices] = 1
else:
    label = [0] * len(node_features)

y = torch.FloatTensor(label)

data = Data(x=x, edge_index=edge_index, y=y)

data_list.append(data)

return data_list

# Pytorch class for creating datasets
class YooChooseDataset(InMemoryDataset):
    def __init__(self, root, transform=None, pre_transform=None):
        super(YooChooseDataset, self).__init__(root, transform, pre_transform)
        self.data, self.slices = torch.load(self.processed_paths[0])

    @property
    def raw_file_names(self):
        return []

    @property
    def processed_file_names(self):
        return [BASE_DIR+'yoochoose_click_binary_100000_sess.dataset']

    def download(self):
        pass

    def process(self):
        data_list = transform_dataset(df, buy_item_dict)

        data, slices = self.collate(data_list)
        torch.save((data, slices), self.processed_paths[0])

```

```

In [23]: # Prepare dataset
dataset = YooChooseDataset('.')

```

Processing...

```

0%|          | 0/50000 [00:00<?, ?it/s]usr/local/lib/python3.7/dist-packages/ipykernel_launcher.py:21: UserWarning: Creating a tensor from a list of numpy.ndarrays is extremely slow. Please consider converting the list to a single numpy.ndarray with numpy.array() before converting to a tensor. (Triggered internally at ../torch/csrc/utils/tensor_new.cpp:210.)
100%|██████████| 50000/50000 [02:51<00:00, 292.20it/s]
Done!

```

## Разделение выборки

```

In [24]: # train_test_split
dataset = dataset.shuffle()
one_tenth_length = int(len(dataset) * 0.1)
train_dataset = dataset[:one_tenth_length * 8]
val_dataset = dataset[one_tenth_length*8:one_tenth_length * 9]
test_dataset = dataset[one_tenth_length*9:]
len(train_dataset), len(val_dataset), len(test_dataset)

```

```

Out[24]:(40000, 5000, 5000)

```

```

In [25]: # Load dataset into PyG loaders
batch_size= 512
train_loader = DataLoader(train_dataset, batch_size=batch_size)
val_loader = DataLoader(val_dataset, batch_size=batch_size)
test_loader = DataLoader(test_dataset, batch_size=batch_size)

```

```

/usr/local/lib/python3.7/dist-packages/torch_geometric/deprecation.py:12: UserWarning: 'data.DataLoader' is deprecated, use 'loader.DataLoader' instead
warnings.warn(out)

```

```

In [26]: # Load dataset into PyG loaders
num_items = df.item_id.max() +1
num_categories = df.category.max()+1
num_items , num_categories

```

```

Out[26]:(18461, 109)

```

## Настройка модели для обучения

```

In [27]: embed_dim = 128
from torch_geometric.nn import GraphConv, TopKPooling, GatedGraphConv, SAGEConv, SGConv
from torch_geometric.nn import global_mean_pool as gap, global_max_pool as gmp
import torch.nn.functional as F

class Net(torch.nn.Module):
    def __init__(self):
        super(Net, self).__init__()

```

*# Model Structure*

```
self.conv1 = GraphConv(embed_dim * 2, 128)
self.pool1 = TopKPooling(128, ratio=0.9)
self.conv2 = GraphConv(128, 128)
self.pool2 = TopKPooling(128, ratio=0.9)
self.conv3 = GraphConv(128, 128)
self.pool3 = TopKPooling(128, ratio=0.9)
self.item_embedding = torch.nn.Embedding(num_embeddings=num_items, embedding_dim=embed_dim)
self.category_embedding = torch.nn.Embedding(num_embeddings=num_categories, embedding_dim=embed_dim)
self.lin1 = torch.nn.Linear(256, 256)
self.lin2 = torch.nn.Linear(256, 128)
self.bn1 = torch.nn.BatchNorm1d(128)
self.bn2 = torch.nn.BatchNorm1d(64)
self.act1 = torch.nn.ReLU()
self.act2 = torch.nn.ReLU()
```

*# Forward step of a model*

```
def forward(self, data):
    x, edge_index, batch = data.x, data.edge_index, data.batch

    item_id = x[:, :, 0]
    category = x[:, :, 1]

    emb_item = self.item_embedding(item_id).squeeze(1)
    emb_category = self.category_embedding(category).squeeze(1)

    x = torch.cat([emb_item, emb_category], dim=1)
    # print(x.shape)
    x = F.relu(self.conv1(x, edge_index))
    # print(x.shape)
    r = self.pool1(x, edge_index, None, batch)
    # print(r)
    x, edge_index, _, batch, _, _ = self.pool1(x, edge_index, None, batch)
    x1 = torch.cat([gmp(x, batch), gap(x, batch)], dim=1)

    x = F.relu(self.conv2(x, edge_index))

    x, edge_index, _, batch, _, _ = self.pool2(x, edge_index, None, batch)
    x2 = torch.cat([gmp(x, batch), gap(x, batch)], dim=1)

    x = F.relu(self.conv3(x, edge_index))

    x, edge_index, _, batch, _, _ = self.pool3(x, edge_index, None, batch)
    x3 = torch.cat([gmp(x, batch), gap(x, batch)], dim=1)

    x = x1 + x2 + x3

    x = self.lin1(x)
    x = self.act1(x)
    x = self.lin2(x)
    x = F.dropout(x, p=0.5, training=self.training)
    x = self.act2(x)

    outputs = []
    for i in range(x.size(0)):
        output = torch.matmul(emb_item[data.batch == i], x[i, :])

        outputs.append(output)

    x = torch.cat(outputs, dim=0)
    x = torch.sigmoid(x)

    return x
```

## Обучение нейронной сверточной сети

```
In [28]: # Enable CUDA computing
device = torch.device('cuda')
model = Net().to(device)
# Choose optimizer and criterion for learning
optimizer = torch.optim.Adam(model.parameters(), lr=0.001)
crit = torch.nn.BCELoss()
```

```
In [29]: # Train function
def train():
    model.train()

    loss_all = 0
    for data in train_loader:
        data = data.to(device)
        optimizer.zero_grad()
```

```

output = model(data)

label = data.y.to(device)
loss = crit(output, label)
loss.backward()
loss_all += data.num_graphs * loss.item()
optimizer.step()
return loss_all / len(train_dataset)

```

```

In [30]: # Evaluate result of a model
from sklearn.metrics import roc_auc_score
def evaluate(loader):
    model.eval()

    predictions = []
    labels = []

    with torch.no_grad():
        for data in loader:

            data = data.to(device)
            pred = model(data).detach().cpu().numpy()

            label = data.y.detach().cpu().numpy()
            predictions.append(pred)
            labels.append(label)

    predictions = np.hstack(predictions)
    labels = np.hstack(labels)

    return roc_auc_score(labels, predictions)

```

```

In [35]: # Train a model
NUM_EPOCHS = 10 # @param { type: "integer" }
for epoch in tqdm(range(NUM_EPOCHS)):
    loss = train()
    train_acc = evaluate(train_loader)
    val_acc = evaluate(val_loader)
    test_acc = evaluate(test_loader)
    print('Epoch: {03d}, Loss: {:.5f}, Train Auc: {:.5f}, Val Auc: {:.5f}, Test Auc: {:.5f}'.
          format(epoch, loss, train_acc, val_acc, test_acc))

```

```

10%|███████| 1/10 [00:35<05:23, 35.93s/it]
Epoch: 000, Loss: 0.24028, Train Auc: 0.84039, Val Auc: 0.62623, Test Auc: 0.59887
20%|███████| 2/10 [01:11<04:47, 35.98s/it]
Epoch: 001, Loss: 0.22922, Train Auc: 0.86706, Val Auc: 0.63198, Test Auc: 0.60424
30%|███████| 3/10 [01:47<04:10, 35.80s/it]
Epoch: 002, Loss: 0.21912, Train Auc: 0.88446, Val Auc: 0.63376, Test Auc: 0.60278
40%|███████| 4/10 [02:23<03:34, 35.78s/it]
Epoch: 003, Loss: 0.21538, Train Auc: 0.87072, Val Auc: 0.63450, Test Auc: 0.60192
50%|███████| 5/10 [02:58<02:58, 35.71s/it]
Epoch: 004, Loss: 0.21220, Train Auc: 0.88758, Val Auc: 0.63205, Test Auc: 0.60194
60%|███████| 6/10 [03:34<02:22, 35.71s/it]
Epoch: 005, Loss: 0.20281, Train Auc: 0.92588, Val Auc: 0.63424, Test Auc: 0.60568
70%|███████| 7/10 [04:10<01:47, 35.70s/it]
Epoch: 006, Loss: 0.19073, Train Auc: 0.94636, Val Auc: 0.63971, Test Auc: 0.61654
80%|███████| 8/10 [04:45<01:11, 35.67s/it]
Epoch: 007, Loss: 0.18077, Train Auc: 0.94925, Val Auc: 0.64910, Test Auc: 0.62152
90%|███████| 9/10 [05:21<00:35, 35.78s/it]
Epoch: 008, Loss: 0.17200, Train Auc: 0.95785, Val Auc: 0.64362, Test Auc: 0.61380
100%|███████| 10/10 [05:57<00:00, 35.75s/it]
Epoch: 009, Loss: 0.16390, Train Auc: 0.96162, Val Auc: 0.64302, Test Auc: 0.61275

```

## Проверка результата с помощью примеров

```

In [32]: # Подход №1 - из да т а с е т а
evaluate(DataLoader(test_dataset[40:60], batch_size=10))

```

```

/usr/local/lib/python3.7/dist-packages/torch_geometric/deprecation.py:12: UserWarning: 'data.DataLoader' is deprecated, use 'loader.DataLoader' instead
  warnings.warn(out)

```

```

Out[32]: 0.4247311827956989

```

```

In [33]: # Подход №2 - через создание сессии покупки

```

```

test_df = pd.DataFrame([
    [-1, 15219, 0],
    [-1, 15431, 0],
    [-1, 14371, 0],
    [-1, 15745, 0],
    [-2, 14594, 0],
    [-2, 16972, 11],
    [-2, 16943, 0],
    [-3, 17284, 0]
], columns=['session_id', 'item_id', 'category'])

test_data = transform_dataset(test_df, buy_item_dict)

```

```
test_data = DataLoader(test_data, batch_size=1)
```

```
with torch.no_grad():  
    model.eval()  
    for data in test_data:  
        data = data.to(device)  
        pred = model(data).detach().cpu().numpy()  
  
    print(data, pred)
```

```
100%|██████████| 3/3 [00:00<00:00, 179.58it/s]
```

```
DataBatch(x=[1, 1, 2], edge_index=[2, 0], y=[1], batch=[1], ptr=[2]) [0.00837703]
```

```
DataBatch(x=[3, 1, 2], edge_index=[2, 2], y=[3], batch=[3], ptr=[2]) [0.15967393 0.04956234 0.3698206 ]
```

```
DataBatch(x=[4, 1, 2], edge_index=[2, 3], y=[4], batch=[4], ptr=[2]) [0.04389836 0.04406342 0.19375472 0.03810767]
```

```
/usr/local/lib/python3.7/dist-packages/torch_geometric/deprecation.py:12: UserWarning: 'data.DataLoader' is deprecated, use 'loader.DataLoader' instead  
warnings.warn(out)
```