Research Track 2 statistical analysis

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Chapter 1

Introduction

I want to know which algorithm is faster between professor's one and mine. For doing this I have chosen to measure the time needed for executing an entire lap of the arena by the robot. I measured a sample of 30 observations for each algorithm every time with a different arena disposition. I have chosen to measure 30 observations because for the Central limit theorem I am sure that my sample has a normal distribution.

Chapter 2

Development

The null hypothesis is: "Professor's algorithm is as fast as mine".

I want to reject the null hypothesis and for doing this I used the so called paired T-test. I can use this test because of normal distribution.

2.1 Observations

| | prof time(s) | my time(s) | difference(s) |
|----------------|--------------|------------|---------------|
| observation 1 | 184,85 | 235,06 | 50,21 |
| observation 2 | 177,57 | 226,46 | 48,89 |
| observation 3 | 185,24 | 222,04 | 36,8 |
| observation 4 | 176,04 | 218,43 | 42,39 |
| observation 5 | 193,32 | 231,13 | 37,81 |
| observation 6 | 172,84 | 227,01 | 54,17 |
| observation 7 | 185,99 | 214,89 | 28,9 |
| observation 8 | 182,17 | 222,06 | 39,89 |
| observation 9 | 172,07 | 230,48 | 58,41 |
| observation 10 | 181,67 | 232,72 | 51,05 |
| observation 11 | 182,93 | 223,94 | 41,01 |
| observation 12 | 179,98 | 220,57 | 40,59 |
| observation 13 | 175,9 | 219,1 | 43,2 |
| observation 14 | 171,62 | 214,81 | 43,19 |
| observation 15 | 169,62 | 217,77 | 48,15 |
| observation 16 | 208,7 | 186,89 | -21,81 |
| observation 17 | 174,45 | 203,64 | 29,19 |
| observation 18 | 183,55 | 206,97 | 23,42 |
| observation 19 | 175,69 | 208,46 | 32,77 |
| observation 20 | 213,42 | 225,18 | 11,76 |
| observation 21 | 199,81 | 220,76 | 20,95 |
| observation 22 | 216,24 | 226,11 | 9,87 |
| observation 23 | 205,37 | 232,24 | 26,87 |
| observation 24 | 203,36 | 223,12 | 19,76 |
| observation 25 | 213,06 | 224,44 | 11,38 |
| observation 26 | 210,6 | 235,46 | 24,86 |
| observation 27 | 200,54 | 230,95 | 30,41 |
| observation 28 | 176,85 | 218,18 | 41,33 |
| observation 29 | 183,4 | 205,18 | 21,78 |
| observation 30 | 190,44 | 215,18 | 24,74 |

2.2 data

- DoF = 29
- $\bullet\,$ Set confidence level to 95%

Calculating the mean and standard deviation of the differences:

$$\overline{d} = 32,398$$

$$S_d = 16,572$$

Therefore:

$$SE(\overline{d}) = \frac{S_d}{\sqrt{30}} = 3,02.$$

Finally:

$$t = \frac{\overline{d}}{SE(\overline{d})} = 10, 7.$$

Chapter 3

Conclusions

Checking in the table provided I can conclude that I can reject the null hypothesis with a confidence of 99% because:

$$t = 10, 7 > 3.659$$

So I can conclude that professor's algorithm is not as fast as mine.

We can say also that professor's algorithm is faster than mine, because the mean of the differences of the times:

$$\overline{d} = 32,398 > 0.$$