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Problems 1 - Calculus II

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1. Find the intersection of the lines $\langle 2, 1, 0 \rangle + t\langle -1, -1, -1 \rangle$ and $\langle 3, 0, 5 \rangle + t\langle 2, 0, 6 \rangle$.
2. Find the equation of the plane that contains the point $(1, 3, 0)$ and the line given by $x = 3 + 2t, y = -4t, z = 7 - t$.
3. Find the equation of the plane through the points $A = (1, 3, 2)$, $B = (5, 2, 0)$ and $C = (3, -1, 6)$.
4. Find the intersection, if any, of the line $x = 2 + 3t, y = -4t, z = 5 + t$ and the plane $4x + 5y - 2z = 18$.
5. Given two planes $\pi_1 : x + y + z = 1$ and $\pi_2 : x - 2y + 3z = 1$, find the line of intersection.
6. Sketch each of the quadric surface $y^2 = 4x^2 + 16z^2$.
7. Sketch the quadric surface: $z = \frac{x^2}{4} + \frac{y^2}{4} - 6$.
8. Compute the volume of the parallelepiped formed by three vectors $\vec{u} = \langle 1, 2, 4 \rangle$, $\vec{v} = \langle -5, 3, -7 \rangle$, $\vec{w} = \langle -1, 4, 2 \rangle$.
9. Convert the coordinates $(-2, 2, 3)$ from Cartesian to cylindrical.
10. Convert the coordinates $(2\sqrt{3}, 6, -4)$ from Cartesian to spherical.
11. Convert the coordinates $(1, \frac{\pi}{2}, 1)$ from cylindrical to spherical.
12. Change the equation $x^2 + y^2 - z^2 = 1$ to spherical coordinates.
13. If A, B and C are three points, find $\overrightarrow{AB} + \overrightarrow{BC} + \overrightarrow{CA}$.

14. Find the angle between the vectors $\vec{u} = \langle 3, 3, 0 \rangle$ and $\vec{v} = \langle 1, 0, 0 \rangle$.
15. Let $\vec{u} = \langle 1, 1, 0 \rangle$ and $\vec{v} = \langle 2, 4, 2 \rangle$. Find a unit vector that is perpendicular to both \vec{u} and \vec{v} .
16. Find the area of the parallelogram with vertices $(0, 0)$, $(1, 2)$, $(3, 7)$ and $(2, 5)$.
17. Find the distance from $(2, -1, -1)$ to the plane $2x - 3y + z = 2$.
18. Find the distance from $(1, 0, 1)$ to the line $\langle 3, 2, 1 \rangle + t\langle 2, -1, -2 \rangle$.
19. Find an equation for the sphere with radius 1 and center at $(0, 1, 0)$ in spherical coordinates.
20. Find the cosine of the angle between the planes $x + y + z = 2$ and $x + 2y + 3z = 8$.