STAT 139: Final Project

Danny Kim, Christopher Lee, Karina Wang, Daniel Son

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EDA

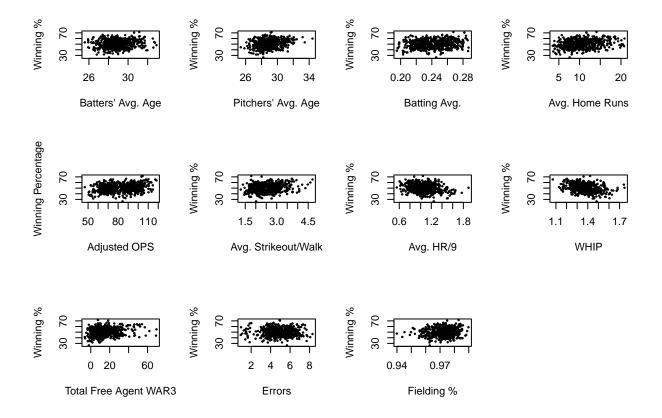
```
library(dplyr)
## Attaching package: 'dplyr'
## The following objects are masked from 'package:stats':
##
       filter, lag
## The following objects are masked from 'package:base':
##
##
       intersect, setdiff, setequal, union
# Load team data
team_data = list()
team_wins <- list()</pre>
drop = c("W", "L")
for (year in 1997:2022) {
 df1 = read.csv(paste("data/teams_data/batting", year, ".csv", sep=""))
 df2 = read.csv(paste("data/teams_data/pitching", year, ".csv", sep=""))
 df3 = read.csv(paste("data/teams_data/fielding", year, ".csv", sep=""))
  df_tot = merge(merge(df1, df2, by="Tm", suffixes=c(".bat", ".pitch")), df3, by="Tm", suffixes=c("", "
  df_tot = df_tot[
    !(df_tot$Tm %in% c("", "League Average")),
    !(names(df_tot) %in% drop)
  df_tot$Tm = factor(df_tot$Tm)
 team_data[[year]] = df_tot
  team_wins[[year]] = df_tot[, c("Tm", "W.L.")]
# Load player data
years <- 1997:2022
bps <- c("batting", "pitching", "fielding")</pre>
player_data <- list()</pre>
for (year in years) {
```

```
player_data[[year]] <- list()</pre>
  for (bp in bps) {
    player_data[[year]][[bp]] <- read.csv(paste("data/player_data/", bp, year, ".csv", sep=""))</pre>
    quant_cols <- names(select_if(player_data[[year]][[bp]], is.numeric))</pre>
    for (col in quant_cols) {
      # impute data with mean
      df <- player_data[[year]][[bp]]</pre>
      player_data[[year]][[bp]][is.na(player_data[[year]][[bp]][,col]),col] <- mean(df[,col], na.rm=TRU</pre>
    }
  }
}
fa_data = list()
for (year in years) {
  fa_data[[year]] = read.csv(paste("data/fa_data/fa", year, ".csv", sep=""))
  fa_data[[year]]$WAR3[is.na(fa_data[[year]]$WAR3)] = 0
}
# Data Cleaning for the Team Data
team_wins <- list()</pre>
for (year in years) {
  team_wins[[year]] <- team_data[[year]][!(team_data[[year]]$Tm %in% c("", "League Average")), c("Tm",
# Clean player data
for (year in years) {
  for (bp in bps) {
    player_data[[year]][[bp]]$year <- year</pre>
    player_data[[year]][[bp]]$year_adj <- year - 1997</pre>
  }
}
for (year in years) {
  player_data[[year]][["pitching"]] = player_data[[year]][["pitching"]][!is.infinite(player_data[[year])
long_team_names <- team_data[[year]][!(team_data[[year]]$Tm %in% c("", "League Average")),]$Tm
short_team_names <- c("ARI", "ATL", "BAL", "BOS", "CHC", "CHW", "CIN", "CLE", "COL", "DET",
                       "HOU", "KCR", "LAA", "LAD", "MIA", "MIL", "MIN", "NYM", "NYY", "OAK",
                       "PHI", "PIT", "SDP", "SFG", "SEA", "STL", "TBR", "TEX", "TOR", "WSN")
agg_data <- list()</pre>
for (year in years) {
  agg_data[[year]] <- list()</pre>
  for (bp in bps) {
    quant_cols <- names(select_if(player_data[[year]][[bp]], is.numeric))</pre>
    agg_data[[year]][[bp]] <- player_data[[year]][[bp]][, c("Tm", quant_cols)] %>%
      group_by(Tm) %>%
      summarise(across(quant_cols, ~weighted.mean(., w = G)))
    agg data[[year]][[bp]] <- agg data[[year]][[bp]][!(agg data[[year]][[bp]]$Tm == "TOT"),]
    agg_data[[year]][[bp]]$long_Tm <- factor(</pre>
      agg data[[year]][[bp]]$Tm,
      levels=short_team_names,
      labels=long_team_names
```

```
)
  }
}
## Warning: Using an external vector in selections was deprecated in tidyselect 1.1.0.
## i Please use 'all_of()' or 'any_of()' instead.
##
##
     data %>% select(quant_cols)
##
##
     # Now:
##
     data %>% select(all_of(quant_cols))
##
## See <https://tidyselect.r-lib.org/reference/faq-external-vector.html>.
player_combo <- list()</pre>
for (year in years) {
  player_combo[[year]] <- merge(merge(agg_data[[year]][[bps[1]]], agg_data[[year]][[bps[2]]], by="Tm",</pre>
agg_fa_data <- list()</pre>
for (year in years) {
  agg_fa_data[[year]] = fa_data[[year]] %>% group_by(To.Team) %>% summarise(tot_fa_war3=sum(WAR3), num_
# add response variable to player data
player_with_wins <- list()</pre>
for (year in 1997:2021) {
  player_with_wins[[year]] <- merge(player_combo[[year]], team_wins[[year+1]], by.x="long_Tm.pitch", by</pre>
}
player_with_wins_fa <- list()</pre>
for (year in 1997:2021) {
 player_with_wins_fa[[year]] <- merge(player_with_wins[[year]], agg_fa_data[[year]], by.x="long_Tm.pit</pre>
player_with_wins_combined = bind_rows(player_with_wins_fa, )
player_with_wins_combined$W.L..same_year = 100 * player_with_wins_combined$W.L..same_year
player_with_wins_combined$W.L..next_year = 100 * player_with_wins_combined$W.L..next_year
drop_cols = c("long_Tm.pitch", "Rk.bat", "G.bat", "long_Tm.bat", "Rk.pitch", "W", "L", "G.pitch", "long
               "Age", "GS", "CG", "GS.field", "CG.field", "Rdrs", "Rdrs.yr", "Rgood")
player_with_wins_combined = player_with_wins_combined[, !(names(player_with_wins_combined) %in% drop_co
n.rows = nrow(player_with_wins_combined)
n.train = 0.8 * n.rows
train.rows = sample(n.rows, n.train)
train.df = player_with_wins_combined[train.rows,]
colnames(train.df)[colnames(train.df) == 'OPS.'] <- 'OPSplus'</pre>
colnames(train.df)[colnames(train.df) == 'ERA.'] <- 'ERAplus'</pre>
test.df = player_with_wins_combined[-train.rows,]
colnames(test.df)[colnames(test.df) == 'OPS.'] <- 'OPSplus'</pre>
colnames(test.df)[colnames(test.df) == 'ERA.'] <- 'ERAplus'</pre>
```

```
names(train.df)
    [1] "Tm"
                          "Age.bat"
                                            "PA"
                                                             "AB"
##
    [5] "R.bat"
                          "H.bat"
                                            "X2B"
                                                             "X3B"
                          "RBI"
                                                             "CS"
##
  [9] "HR.bat"
                                            "SB"
## [13] "BB.bat"
                          "SO.bat"
                                            "BA"
                                                             "0BP"
## [17] "SLG"
                          "OPS"
                                                             "TB"
                                            "OPSplus"
## [21] "GDP"
                          "HBP.bat"
                                            "SH"
                                                             "SF"
## [25] "IBB.bat"
                          "year.bat"
                                            "year_adj.bat"
                                                             "Age.pitch"
                          "ERA"
                                            "GF"
                                                             "SHO"
## [29] "W.L..same_year"
## [33] "SV"
                                            "H.pitch"
                                                             "R.pitch"
                                                             "IBB.pitch"
## [37] "ER"
                          "HR.pitch"
                                            "BB.pitch"
                                                             "WP"
## [41] "SO.pitch"
                          "HBP.pitch"
                                            "BK"
## [45] "BF"
                          "ERAplus"
                                            "FTP"
                                                             "WHTP"
## [49] "H9"
                          "HR9"
                                            "BB9"
                                                             "S09"
## [53] "SO.W"
                          "year.pitch"
                                            "year_adj.pitch" "Rk"
                          "Inn"
                                            "Ch"
                                                             "P0"
## [57] "G"
                          "E"
                                            "DP"
## [61] "A"
                                                             "Fld."
                                            "RF.9"
## [65] "Rtot"
                          "Rtot.vr"
                                                             "RF.G"
## [69] "year"
                                            "W.L..next_year" "tot_fa_war3"
                          "year_adj"
## [73] "num_fas"
# Explore Potential Predictors
par(mfrow=c(3,4))
plot(W.L..next_year ~ Age.bat, data=train.df,
     xlab="Batters' Avg. Age", ylab="Winning %", cex=0.3)
plot(W.L..next_year ~ Age.pitch, data=train.df,
     xlab="Pitchers' Avg. Age", ylab="Winning %", cex=0.3)
plot(W.L..next_year ~ BA, data=train.df,
     xlab="Batting Avg.", ylab="Winning %", cex=0.3)
plot(W.L..next_year ~ HR.bat, data=train.df,
     xlab="Avg. Home Runs", ylab="Winning %", cex=0.3)
plot(W.L..next_year ~ OPSplus, data=train.df,
     xlab="Adjusted OPS", ylab="Winning Percentage", cex=0.3)
plot(W.L..next year ~ SO.W, data=train.df,
     xlab="Avg. Strikeout/Walk", ylab="Winning %", cex=0.3)
plot(W.L..next_year ~ HR9, data=train.df,
     xlab="Avg. HR/9", ylab="Winning %", cex=0.3)
plot(W.L..next_year ~ WHIP, data=train.df,
     xlab="WHIP", ylab="Winning %", cex=0.3)
plot(W.L..next_year ~ tot_fa_war3, data=train.df,
     xlab="Total Free Agent WAR3", ylab="Winning %", cex=0.3)
plot(W.L..next_year ~ E, data=train.df,
     xlab="Errors", ylab="Winning %", cex=0.3)
plot(W.L..next_year ~ Fld., data=train.df,
     xlab="Fielding %", ylab="Winning %", cex=0.3)
```

train.df

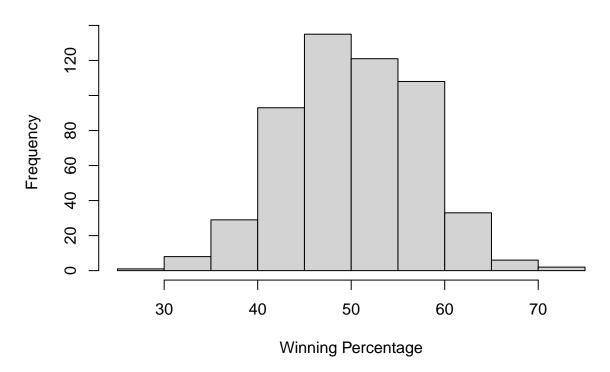


Summary statistics for winpct summary(train.df\$W.L..next_year)

Min. 1st Qu. Median Mean 3rd Qu. Max. ## 26.50 45.10 50.60 50.36 55.60 71.60

Histogram for winpct

Distribution of Winning Percentage

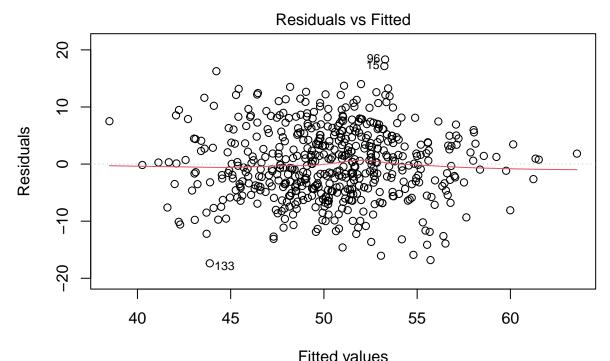


```
# Correlation matrix
cor(train.df[, c("W.L..next year", "Age.bat", "Age.pitch", "BA", "HR.bat", "OPS", "SO.W", "HR9", "WHIP"
```

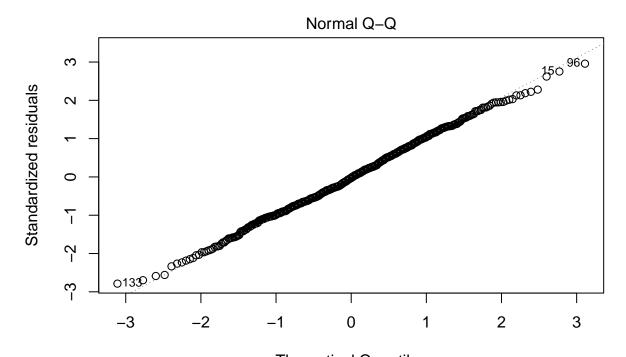
```
W.L..next_year
                                                                 BA
                                                                          HR.bat
                                    Age.bat
                                              Age.pitch
## W.L..next_year
                     1.0000000
                                 0.11752497
                                             0.23987636
                                                         0.16874627
                                                                     0.258708974
## Age.bat
                                 1.00000000
                                             0.51739922
                                                         0.18611215
                     0.11752497
                                                                     0.145672229
                                             1.00000000
                                                         0.12552375
## Age.pitch
                     0.23987636
                                 0.51739922
                                                                     0.197981229
## BA
                     0.16874627
                                 0.18611215
                                             0.12552375
                                                         1.00000000
                                                                     0.546066555
## HR.bat
                     0.25870897
                                 0.14567223
                                             0.19798123
                                                         0.54606655
                                                                     1.000000000
## OPS
                     0.24261108
                                 0.15356491
                                             0.17370956
                                                         0.91233483
                                                                     0.710686591
## SO.W
                     0.22686755 -0.09351711
                                             0.01936649
                                                        -0.14304072
                                                                     0.054107022
## HR9
                    -0.23045821 -0.16419856 -0.09426396
                                                         0.04534340
                                                                     0.133878994
## WHIP
                    -0.33712072 -0.02977710 -0.10110815
                                                         0.16008020 -0.007431268
                     0.20721613
                                 0.26224621
                                             0.27976753
                                                         0.11804017
                                                                     0.143102559
## tot_fa_war3
## E
                     0.02741697
                                 0.01968936
                                             0.07974133
                                                         0.17313857
                                                                     0.255708854
## Fld.
                     0.13427519 0.14194469
                                             0.17685246
                                                         0.03896246
                                                                     0.098147047
                          OPS
                                     SO.W
                                                  HR9
                                                              WHIP tot_fa_war3
                  ## W.L..next_year
                                                                    0.20721613
## Age.bat
                  0.153564912 - 0.09351711 - 0.16419856 - 0.029777095
                                                                    0.26224621
                  0.173709563 0.01936649 -0.09426396 -0.101108153
                                                                    0.27976753
## Age.pitch
## BA
                  0.912334826 -0.14304072 0.04534340
                                                      0.160080201
                  0.710686591 0.05410702
## HR.bat
                                           0.13387899 -0.007431268
                                                                    0.14310256
## OPS
                  1.000000000 -0.02618238
                                           0.18153117
                                                       0.115646503
                                                                    0.16496218
## SO.W
                 -0.026182377
                               1.00000000 -0.06308450 -0.736753156
                                                                   0.08645535
## HR9
                  0.181531167 -0.06308450
                                           1.00000000
                                                      0.430177101 -0.01349860
                  0.115646503 -0.73675316  0.43017710  1.000000000 -0.06761557
## WHIP
```

```
## tot_fa_war3
                  ## E
                  0.076113343 - 0.35243217 - 0.14754817 0.242938573 - 0.06308137
## Fld.
                  ##
                          Ε
                                    Fld.
## W.L..next_year 0.02741697 0.134275193
                  0.01968936 0.141944693
## Age.bat
## Age.pitch
                0.07974133 0.176852463
## BA
                  0.17313857 0.038962460
## HR.bat
                 0.25570885 0.098147047
## OPS
                 0.07611334 0.009629124
## SO.W
                 -0.35243217 0.030016567
## HR9
                 -0.14754817 -0.125996475
## WHIP
                 0.24293857 -0.159494533
## tot_fa_war3
                -0.06308137 0.075995676
## E
                 1.00000000 -0.076249214
                 -0.07624921 1.000000000
## Fld.
cor(train.df[, c("W.L..next_year", "Age.bat", "Age.pitch", "BA", "HR.bat", "OPS", "SO.W", "HR9", "WHIP"
                 W.L..next year
                                              Age.pitch
                                    Age.bat
                                                                BA
## W.L..next_year
                     1.00000000 0.0138121177 0.057540666 0.028475305 6.693033e-02
                     0.01381212 1.0000000000 0.267701949 0.034637732 2.122040e-02
## Age.bat
                    0.05754067 0.2677019489 1.000000000 0.015756213 3.919657e-02
## Age.pitch
                    0.02847531 0.0346377324 0.015756213 1.000000000 2.981887e-01
## BA
                    0.06693033 0.0212203982 0.039196567 0.298188682 1.000000e+00
## HR.bat
## OPS
                   0.05886013 0.0235821823 0.030175012 0.832354834 5.050754e-01
## SO.W
                   0.05146888 0.0087454507 0.000375061 0.020460646 2.927570e-03
                    0.05311098 0.0269611677 0.008885694 0.002056024 1.792359e-02
## HR9
                    0.11365038 0.0008866754 0.010222859 0.025625671 5.522375e-05
## WHIP
## tot_fa_war3
                    0.04293852 0.0687730731 0.078269872 0.013933483 2.047834e-02
## E
                     0.00075169 0.0003876710 0.006358680 0.029976964 6.538702e-02
## Fld.
                     0.01802983 0.0201482959 0.031276794 0.001518073 9.632843e-03
                                     SO.W
                          OPS
                                                   HR9
                                                              WHIP tot_fa_war3
## W.L..next_year 5.886013e-02 0.0514688845 0.0531109847 1.136504e-01 0.0429385233
                 2.358218e-02 0.0087454507 0.0269611677 8.866754e-04 0.0687730731
## Age.bat
## Age.pitch
                 3.017501e-02 0.0003750610 0.0088856940 1.022286e-02 0.0782698721
## BA
                 8.323548e-01 0.0204606462 0.0020560240 2.562567e-02 0.0139334829
                 5.050754e-01 0.0029275698 0.0179235850 5.522375e-05 0.0204783423
## HR.bat
## OPS
                 1.000000e+00 0.0006855169 0.0329535647 1.337411e-02 0.0272125192
## SO.W
                 6.855169e-04 1.0000000000 0.0039796540 5.428052e-01 0.0074745276
## HR9
                 3.295356e-02 0.0039796540 1.0000000000 1.850523e-01 0.0001822121
## WHIP
                1.337411e-02 0.5428052136 0.1850523384 1.000000e+00 0.0045718657
                 2.721252e-02 0.0074745276 0.0001822121 4.571866e-03 1.0000000000
## tot_fa_war3
## E
                 5.793241e-03 0.1242084357 0.0217704625 5.901915e-02 0.0039792599
                 9.272003e-05 0.0009009943 0.0158751118 2.543851e-02 0.0057753428
## Fld.
                           Ε
                                    Fld.
## W.L..next_year 0.000751690 1.802983e-02
                 0.000387671 2.014830e-02
## Age.bat
                 0.006358680 3.127679e-02
## Age.pitch
                 0.029976964 1.518073e-03
## BA
## HR.bat
                 0.065387018 9.632843e-03
## OPS
                 0.005793241 9.272003e-05
## SO.W
                 0.124208436 9.009943e-04
                 0.021770462 1.587511e-02
## HR9
```

```
## WHIP
                0.059019150 2.543851e-02
## tot_fa_war3
                0.003979260 5.775343e-03
## E
                1.000000000 5.813943e-03
## Fld.
                0.005813943 1.000000e+00
# Baseline Multiple Regression Model
baseline <- lm(W.L..next_year ~ Age.bat + Age.pitch + BA + HR.bat +
                OPS + SO.W + HR9 + WHIP + tot_fa_war3 + E + Fld. , data = train.df)
summary(baseline)
##
## Call:
## lm(formula = W.L..next_year ~ Age.bat + Age.pitch + BA + HR.bat +
      OPS + SO.W + HR9 + WHIP + tot fa war3 + E + Fld., data = train.df)
## Residuals:
                    Median
##
       Min
                1Q
                                 3Q
                                         Max
## -17.3800 -4.2722 -0.1538 4.3981 18.3189
## Coefficients:
               Estimate Std. Error t value Pr(>|t|)
## (Intercept) -10.25614 39.36219 -0.261 0.794536
## Age.bat
               -0.23314
                         0.26826 -0.869 0.385202
                                   2.349 0.019189 *
## Age.pitch
                0.62222
                          0.26487
             -139.86386 41.80505 -3.346 0.000880 ***
## BA
## HR.bat
              ## OPS
               76.68698 16.81169 4.562 6.33e-06 ***
## SO.W
               -0.06723
                         0.81235 -0.083 0.934071
## HR9
               -6.61423 1.77749 -3.721 0.000220 ***
## WHIP
              -18.85895 4.85443 -3.885 0.000115 ***
              0.06583
                        0.02349 2.802 0.005264 **
## tot_fa_war3
## E
                0.54056
                         0.27910 1.937 0.053311 .
## Fld.
               61.87723 38.16033 1.622 0.105511
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Residual standard error: 6.281 on 524 degrees of freedom
## Multiple R-squared: 0.271, Adjusted R-squared: 0.2557
## F-statistic: 17.71 on 11 and 524 DF, p-value: < 2.2e-16
# Asssess Linear Model Assumptions
plot(baseline, which=c(1,2))
```



Fitted values Im(W.L..next_year ~ Age.bat + Age.pitch + BA + HR.bat + OPS + SO.W + HR9 + ..



Theoretical Quantiles
Im(W.L..next_year ~ Age.bat + Age.pitch + BA + HR.bat + OPS + SO.W + HR9 + ...

```
RMSE <- function(y,yhat){
    SSE = sum((y-yhat)^2)
    SST = sum((y - mean(y))^2)
    return(sqrt(SSE/length(y)))
}

R2 <- function(y,yhat) {
    SSE = sum((y-yhat)^2)
    SST = sum((y-mean(y))^2)
    r.squared <- 1 - (SSE / SST)
    return(r.squared)
}
baseline.trainRMSE = RMSE(train.df$W.L..next_year, predict(baseline, newdata=train.df))
baseline.testRMSE = RMSE(test.df$W.L..next_year, predict(baseline, newdata=test.df))
baseline.trainR2 = R2(train.df$W.L..next_year, predict(baseline, newdata=train.df))
baseline.testR2 = R2(test.df$W.L..next_year, predict(baseline, newdata=test.df))</pre>
```

Linear Regression

```
## [9] "HR.bat"
                         "RBI"
                                           "SB"
                                                             "CS"
## [13] "BB.bat"
                         "SO.bat"
                                           "BA"
                                                             "OBP"
                         "OPS"
                                                             "TB"
## [17] "SLG"
                                           "OPSplus"
## [21] "GDP"
                         "HBP.bat"
                                           "SH"
                                                             "SF"
## [25] "IBB.bat"
                         "year.bat"
                                           "year_adj.bat"
                                                             "Age.pitch"
## [29] "W.L..same_year" "ERA"
                                           "GF"
                                                            "SHO"
                         "IP"
## [33] "SV"
                                           "H.pitch"
                                                             "R.pitch"
                                           "BB.pitch"
## [37] "ER"
                                                            "IBB.pitch"
                          "HR.pitch"
## [41] "SO.pitch"
                         "HBP.pitch"
                                           "BK"
                                                             יי קשיי
## [45] "BF"
                         "ERAplus"
                                           "FIP"
                                                            "WHIP"
## [49] "H9"
                         "HR9"
                                           "BB9"
                                                             "S09"
## [53] "SO.W"
                         "year.pitch"
                                           "year_adj.pitch" "Rk"
## [57] "G"
                         "Inn"
                         "E"
                                           "DP"
## [61] "A"
                                                            "Fld."
## [65] "Rtot"
                         "Rtot.yr"
                                           "RF.9"
                                                            "RF.G"
## [69] "year"
                         "year_adj"
                                           "W.L..next_year" "tot_fa_war3"
## [73] "num_fas"
# full linear regression models
# ignore Rk.bat, R.bat, RBI, year.bat, year_adj.bat, W, L, R.pitch, year.pitch
# year_adj.pitch, Rk, WL..next_year, year, year_adj, ERA, ERAplus
# Rtot, Rtot.yr, Rdrs, Rgood (hard to interpret)
lm.full <- lm(W.L..next_year ~ Age.bat + PA + AB + H.bat + X2B + X3B +</pre>
                HR.bat + SB + CS + BB.bat + SO.bat + BA + OBP + SLG + OPS + OPSplus +
                TB + GDP + HBP.bat + SH + SF + IBB.bat + Age.pitch + W.L..same_year +
                GF + SHO + SV + IP + H.pitch + HR.pitch +
                BB.pitch + IBB.pitch + SO.pitch + HBP.pitch + BK + WP + BF +
                FIP + WHIP + H9 + HR9 + BB9 + S09 + S0.W +
                G + Inn + Ch + PO + A + E + DP + Fld. +
                RF.9 + RF.G + tot_fa_war3 + num_fas,
              data = train.df)
lmfull.trainRMSE = RMSE(train.df$W.L..next_year, predict(lm.full, newdata=train.df))
## Warning in predict.lm(lm.full, newdata = train.df): prediction from a rank-
## deficient fit may be misleading
lmfull.testRMSE = RMSE(test.df$W.L..next_year, predict(lm.full, newdata=test.df))
## Warning in predict.lm(lm.full, newdata = test.df): prediction from a rank-
## deficient fit may be misleading
lmfull.trainR2 = R2(train.df$\W.L..next_year, predict(lm.full, newdata=train.df))
## Warning in predict.lm(lm.full, newdata = train.df): prediction from a rank-
## deficient fit may be misleading
lmfull.testR2 = R2(test.df$W.L..next_year, predict(lm.full, newdata=test.df))
## Warning in predict.lm(lm.full, newdata = test.df): prediction from a rank-
## deficient fit may be misleading
```

```
lm.fullinteraction <- lm(W.L..next_year ~ (Age.bat + PA + AB + H.bat + X2B + X3B +</pre>
                HR.bat + SB + CS + BB.bat + SO.bat + BA + OBP + SLG + OPS + OPSplus +
                TB + GDP + HBP.bat + SH + SF + IBB.bat + Age.pitch + W.L..same_year +
                GF + SHO + SV + IP + H.pitch + HR.pitch +
                BB.pitch + IBB.pitch + SO.pitch + HBP.pitch + BK + WP + BF +
                FIP + WHIP + H9 + HR9 + BB9 + S09 + S0.W +
                G + Inn + Ch + PO + A + E + DP + Fld. +
                RF.9 + RF.G + tot fa war3 + num fas)^2, data = train.df)
lmfullinteraction.trainRMSE = RMSE(train.df$W.L..next_year, predict(lm.fullinteraction, newdata=train.d
## Warning in predict.lm(lm.fullinteraction, newdata = train.df): prediction from a
## rank-deficient fit may be misleading
lmfullinteraction.testRMSE = RMSE(test.df$W.L..next_year, predict(lm.fullinteraction, newdata=test.df))
## Warning in predict.lm(lm.fullinteraction, newdata = test.df): prediction from a
## rank-deficient fit may be misleading
lmfullinteraction.trainR2 = R2(train.df$W.L..next_year, predict(lm.fullinteraction, newdata=train.df))
## Warning in predict.lm(lm.fullinteraction, newdata = train.df): prediction from a
## rank-deficient fit may be misleading
lmfullinteraction.testR2 = R2(test.df$W.L..next_year, predict(lm.fullinteraction, newdata=test.df))
## Warning in predict.lm(lm.fullinteraction, newdata = test.df): prediction from a
## rank-deficient fit may be misleading
# Ridge Regression
set.seed(139)
library(glmnet)
## Loading required package: Matrix
## Loaded glmnet 4.1-4
library(caret)
## Loading required package: ggplot2
## Loading required package: lattice
##
## Attaching package: 'caret'
## The following objects are masked _by_ '.GlobalEnv':
##
##
       R2, RMSE
```

```
##
                        Overall
## Age.bat
                  5.752159e-01
## PA
                  4.169554e-03
## AB
                  7.168485e-03
## H.bat
                  3.168249e-05
## X2B
                  8.584614e-03
## X3B
                  1.109549e+00
## HR.bat
                  2.119815e-01
## SB
                  6.806400e-02
## CS
                  3.390557e-02
## BB.bat
                  1.414319e-01
## SO.bat
                  3.652799e-02
## BA
                  5.997285e+00
## OBP
                  2.554351e+01
## SLG
                  1.418188e+01
## OPS
                  9.939370e+00
## OPSplus
                  7.547341e-03
## TB
                  6.824692e-03
## GDP
                  2.307993e-01
## HBP.bat
                  2.386825e-01
## SH
                  8.981258e-02
## SF
                  8.497103e-02
## IBB.bat
                  2.708115e-01
## Age.pitch
                  4.154787e-01
## W.L..same_year 2.058143e-02
## GF
                  8.157071e-02
## SHO
                  6.247652e+00
## SV
                  3.289460e-01
## IP
                  4.275370e-03
                  1.211208e-02
## H.pitch
## HR.pitch
                  2.097323e-01
## BB.pitch
                  1.333564e-02
## IBB.pitch
                  1.673001e-01
## SO.pitch
                  2.530369e-02
## HBP.pitch
                  1.453254e-01
## BK
                  1.185275e+00
## WP
                  2.455001e-02
## BF
                  7.827181e-05
## FIP
                  6.498817e-01
## WHIP
                  5.841223e+00
## H9
                  1.214867e+00
## HR9
                  2.030656e+00
## BB9
                  8.721206e-02
## S09
                  2.270999e-01
## SO.W
                  3.418090e-01
## G
                  2.707582e-02
```

```
## Inn
                 3.372902e-03
## Ch
                 2.487647e-04
                 1.125522e-03
## PO
                 2.452944e-03
## A
## E
                 3.082556e-01
## DP
                 7.332010e-02
## Fld.
                 4.450743e+01
## RF.9
                 2.287439e+00
## RF.G
                 2.650137e+00
## tot_fa_war3 7.077088e-02
## num_fas
                  1.333073e-01
X.full.test = model.matrix(lm.full, data=test.df)[,-1] # drop intercept
yhats.full.train = predict(ridges.full, X.full)
ridgesfull.trainRMSE = RMSE(train.df$W.L..next_year, yhats.full.train) # train RMSE
ridgesfull.trainR2 = R2(train.df$W.L..next_year, yhats.full.train) # train R2
yhats.full.test = predict(ridges.full, X.full.test)
{\it \#plot(RMSE.ridges.full.test~log(ridges.full\$lambda,~10),~type='l')}
ridgesfull.testRMSE = RMSE(test.df$W.L..next_year, yhats.full.test) # test RMSE
ridgesfull.testR2 = R2(test.df$W.L..next_year, yhats.full.test) # test R2
set.seed(139)
# regularize full interaction model
X.fullinteraction = model.matrix(lm.fullinteraction)[,-1] # drop intercept
best_lambda = cv.glmnet(X.fullinteraction, train.df$W.L..next_year, alpha=0,
                        lambda=10^seq(-4, 4, 0.1))$lambda.min
ridges.fullinteraction = glmnet(X.fullinteraction, train.df$W.L..next_year, alpha=0,
                     lambda=best_lambda)
X.fullinteraction.test = model.matrix(lm.fullinteraction, data=test.df)[,-1] # drop intercept
yhats.fullinteraction.train = predict(ridges.fullinteraction, X.fullinteraction)
ridgesfullinteraction.trainRMSE = RMSE(train.df$W.L..next year, yhats.fullinteraction.train) # train RM
ridgesfullinteraction.trainR2 = R2(train.df$W.L..next_year, yhats.fullinteraction.train) # train R2
yhats.fullinteraction.test = predict(ridges.fullinteraction, X.fullinteraction.test)
#plot(RMSE.ridges.fullinteraction.test~log(ridges.fullinteraction$lambda, 10), type='l')
ridgesfullinteraction.testRMSE = RMSE(test.df$W.L..next_year, yhats.fullinteraction.test) # train RMSE
ridgesfullinteraction.testR2 = R2(test.df$W.L..next_year, yhats.fullinteraction.test) # train R2
# Lasso Regression
# regularize full model
set.seed(139)
best_lambda = cv.glmnet(X.full, train.df$W.L..next_year, alpha=1,
                        lambda=10^seq(-4, 4, 0.1))$lambda.min
lassos.full = glmnet(X.full, train.df$W.L..next_year, alpha=1,
                     lambda=best_lambda)
varImp(lassos.full, lambda=best_lambda)
##
                       Overall
## Age.bat
                 0.760403704
```

```
## PA
                    0.00000000
## AB
                    0.013798186
                    0.00000000
## H.bat
## X2B
                    0.00000000
## X3B
                    1.138148047
## HR.bat
                    0.293888771
## SB
                    0.041199529
## CS
                    0.00000000
## BB.bat
                    0.215962524
## SO.bat
                    0.062850770
## BA
                    0.00000000
## OBP
                   10.863462973
## SLG
                    7.962457059
                   17.605036197
## OPS
                    0.00000000
## OPSplus
## TB
                    0.00000000
## GDP
                    0.207791848
## HBP.bat
                    0.248262694
## SH
                    0.00000000
## SF
                    0.00000000
## IBB.bat
                    0.114433745
## Age.pitch
                    0.406103170
## W.L..same_year
                   0.000000000
## GF
                    0.00000000
## SHO
                    5.947455726
## SV
                    0.248392153
## IP
                    0.00000000
## H.pitch
                    0.00000000
## HR.pitch
                    0.298752976
## BB.pitch
                    0.00000000
## IBB.pitch
                    0.071047986
## SO.pitch
                    0.031290182
## HBP.pitch
                    0.049407289
## BK
                    0.759943266
## WP
                    0.00000000
## BF
                    0.00000000
## FIP
                    0.758780126
## WHIP
                    5.875680328
## H9
                    1.601681602
## HR9
                    1.505850813
## BB9
                    0.00000000
## S09
                    0.066333113
## SO.W
                    0.183684122
## G
                    0.00000000
## Inn
                    0.007817371
## Ch
                    0.00000000
## PO
                    0.00000000
## A
                    0.00000000
## E
                    0.245624203
## DP
                    0.070496142
## Fld.
                  37.971227099
## RF.9
                    3.210209394
## RF.G
                    3.901945224
## tot_fa_war3
                    0.079787301
```

```
## num fas
                  0.132404107
yhats.full.train = predict(lassos.full, X.full)
lassosfull.trainRMSE = RMSE(train.df$W.L..next_year, yhats.full.train) # train RMSE
lassosfull.trainR2 = R2(train.df$W.L..next_year, yhats.full.train) # train R2
yhats.full.test = predict(lassos.full, X.full.test)
#plot(RMSE.lassos.full.test~log(ridges.full$lambda, 10), type='l')
lassosfull.testRMSE = RMSE(test.df$W.L..next_year, yhats.full.test) # test RMSE
lassosfull.testR2 = R2(test.df$W.L..next year, yhats.full.test) # test RMSE
# regularize full interaction model
set.seed(139)
best_lambda = cv.glmnet(X.fullinteraction, train.df$W.L..next_year, alpha=1,
                        lambda=10^seq(-4, 4, 0.1))$lambda.min
lassos.fullinteraction = glmnet(X.fullinteraction, train.df$W.L..next_year, alpha=1,
                     lambda=best_lambda)
yhats.fullinteraction.train = predict(lassos.fullinteraction, X.fullinteraction)
lassosfullinteraction.trainRMSE = RMSE(train.df$W.L..next_year, yhats.fullinteraction.train) # train RM
lassosfullinteraction.trainR2 = R2(train.df$W.L..next_year, yhats.fullinteraction.train) # train R2
yhats.fullinteraction.test = predict(lassos.fullinteraction, X.fullinteraction.test)
#plot(RMSE.lassos.fullinteraction.test~log(lassos.fullinteraction$lambda, 10), type='l')
lassosfullinteraction.testRMSE = RMSE(test.df$W.L..next_year, yhats.fullinteraction.test) # train RMSE
lassosfullinteraction.testR2 = R2(test.df$W.L..next_year, yhats.fullinteraction.test) # train R2
lm.step = step(lm.full, scope=c(lower=formula(W.L..next_year~1),
                                upper=lm.fullinteraction), trace=0, direction="both")
formula(lm.step)
## W.L..next_year ~ Age.bat + PA + AB + H.bat + X3B + OPS + HBP.bat +
       Age.pitch + SHO + SO.pitch + BF + H9 + HR9 + BB9 + Inn +
##
##
       RF.9 + RF.G + tot_fa_war3 + num_fas
lmstep.trainRMSE = RMSE(train.df$\W.L..next_year, predict(lm.step, newdata=train.df))
lmstep.testRMSE = RMSE(test.df$W.L..next_year, predict(lm.step, newdata=test.df))
lmstep.trainR2 = R2(train.df$W.L..next_year, predict(lm.step, newdata=train.df))
lmstep.testR2 = R2(test.df$W.L..next_year, predict(lm.step, newdata=test.df))
# model comparison
RMSE.df = data.frame(trainRMSE = c(baseline.trainRMSE,
                                   lmfull.trainRMSE,
                                   lmfullinteraction.trainRMSE,
                                   ridgesfull.trainRMSE,
                                   ridgesfullinteraction.trainRMSE,
                                   lassosfull.trainRMSE,
                                   lassosfullinteraction.trainRMSE,
                                   lmstep.trainRMSE),
                     testRMSE = c(baseline.testRMSE,
                                   lmfull.testRMSE,
                                   lmfullinteraction.testRMSE,
```

```
ridgesfull.testRMSE,
                                    ridgesfullinteraction.testRMSE,
                                    lassosfull.testRMSE,
                                    lassosfullinteraction.testRMSE,
                                    lmstep.testRMSE),
                     trainR2 = c(baseline.trainR2,
                                    lmfull.trainR2.
                                    lmfullinteraction.trainR2,
                                    ridgesfull.trainR2,
                                    ridgesfullinteraction.trainR2,
                                    lassosfull.trainR2,
                                    lassosfullinteraction.trainR2,
                                    lmstep.trainR2),
                     testR2 = c(baseline.testR2,
                                    lmfull.testR2,
                                    lmfullinteraction.testR2,
                                    ridgesfull.testR2,
                                    ridgesfullinteraction.testR2,
                                    lassosfull.testR2,
                                    lassosfullinteraction.testR2,
                                    lmstep.testR2))
rownames(RMSE.df) <- c("baseline", "full", "full interaction",</pre>
                        "ridge full", "ridge full interaction",
                        "lasso full", "lasso full interaction",
                        "step")
RMSE.df
```

```
##
                           trainRMSE
                                        testRMSE trainR2
                                                                 testR2
## baseline
                        6.210565e+00
                                        7.326775 0.2709964 2.591406e-01
## full
                        5.660738e+00
                                       7.068803 0.3943615 3.103929e-01
## full interaction
                        6.096283e-07 58781.849584 1.0000000 -4.768662e+07
                        5.764690e+00 7.079809 0.3719137 3.082437e-01
## ridge full
## ridge full interaction 5.721998e+00 6.991096 0.3811822 3.254711e-01
## lasso full
                        5.737253e+00 7.066628 0.3778781 3.108171e-01
## lasso full interaction 5.656210e+00
                                        7.119921 0.3953298 3.003830e-01
                        5.764326e+00
                                        7.075806 0.3719930 3.090257e-01
## step
```

Decision Tree/Random Forest

```
set.seed(139)
library(rpart)

RMSE = function(y,yhat){
   return(sqrt(mean((y-yhat)^2)))
}

test.df = subset(test.df, test.df$Tm != 'CLE')
tree1 = rpart(formula(lm.full),data=train.df, control = list(minsplit=1,cp=0,maxdepth=20))
yhat.tree1.train = predict(tree1)
yhat.tree1.test = predict(tree1, newdata = test.df)
RMSE.tree1.train = RMSE(train.df$W.L..next_year,yhat.tree1.train)
```

```
RMSE.tree1.test = RMSE(test.df$W.L..next_year,yhat.tree1.test)
data.frame(train=RMSE.tree1.train,test=RMSE.tree1.test)
##
        train
                  test
## 1 3.879832 8.406397
set.seed(139)
best.cp = tree1$cptable[,"CP"][which.min(tree1$cptable[,"xerror"])]
tree2 = prune(tree1,best.cp)
yhat.tree2.train = predict(tree2)
yhat.tree2.test = predict(tree2,newdata=test.df)
RMSE.tree2.train = RMSE(train.df$W.L..next_year,yhat.tree2.train)
RMSE.tree2.test = RMSE(test.df$W.L..next year,yhat.tree2.test)
data.frame(train=RMSE.tree2.train,test=RMSE.tree2.test)
##
        train
                  test
## 1 6.226519 7.778095
set.seed(139)
tree3 = rpart(W.L..next_year~W.L..same_year + Age.pitch + WHIP,
              data=train.df, control = list(minsplit=1, cp=0, maxdepth=20))
yhat.tree3.train = predict(tree3)
yhat.tree3.test = predict(tree3, newdata = test.df)
RMSE.tree3.train = RMSE(train.df$W.L..next_year,yhat.tree3.train)
RMSE.tree3.test = RMSE(test.df$W.L..next_year,yhat.tree3.test)
data.frame(train=RMSE.tree3.train,test=RMSE.tree3.test)
##
        train
## 1 5.259777 8.073087
set.seed(139)
best.cp = tree3$cptable[,"CP"][which.min(tree3$cptable[,"xerror"])]
tree4 = prune(tree3,best.cp)
yhat.tree4.train = predict(tree4)
yhat.tree4.test = predict(tree4,newdata=test.df)
RMSE.tree4.train = RMSE(train.df$W.L..next_year,yhat.tree4.train)
RMSE.tree4.test = RMSE(test.df$W.L..next_year,yhat.tree4.test)
data.frame(train=RMSE.tree4.train,test=RMSE.tree4.test)
##
       train
                  test
## 1 6.669579 7.866976
library(randomForest)
## randomForest 4.7-1.1
## Type rfNews() to see new features/changes/bug fixes.
## Attaching package: 'randomForest'
```

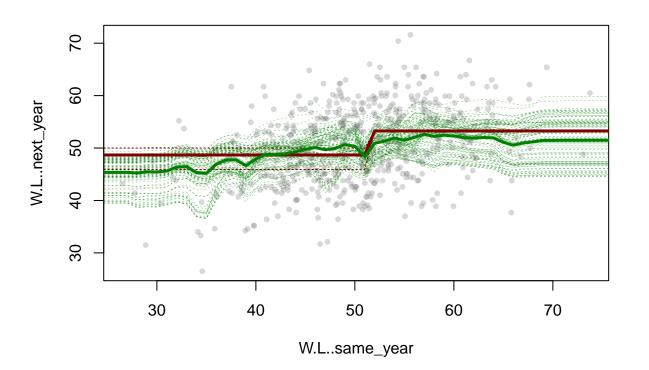
```
## The following object is masked from 'package:ggplot2':
##
       margin
##
## The following object is masked from 'package:dplyr':
##
##
       combine
set.seed(139)
maxnodes = c(100, 200, 500)
ntree= 200
rmses.bag = rep(NA,length(maxnodes))
bestRMSE = sd(train.df$W.L..next_year)
for(i in 1:length(maxnodes)){
  bagtemp = randomForest(formula(lm.full),data=train.df,
                        mtry=56, maxnodes=maxnodes[i], ntree=ntree)
 rmses.bag[i]=RMSE(train.df$W.L..next_year, bagtemp$predicted)
  if(rmses.bag[i] < bestRMSE) {</pre>
    best_maxnodes = maxnodes[i]
    bestRMSE=rmses.bag[i]
    bag=bagtemp
  }
}
data.frame(maxnodes=maxnodes, RMSE=rmses.bag)
    maxnodes
##
                  RMSE
## 1
         100 6.472173
## 2
          200 6.359278
## 3
         500 6.401620
yhat.bag.train = predict(bag)
yhat.bag.test = predict(bag, newdata = test.df)
RMSE.bag.train = RMSE(train.df$W.L..next_year,yhat.bag.train)
RMSE.bag.test = RMSE(test.df$W.L..next_year,yhat.bag.test)
data.frame(train=RMSE.bag.train,test=RMSE.bag.test)
##
        train
## 1 6.359278 7.44455
library(randomForest)
set.seed(139)
maxnodes = c(100, 200, 500)
mtry = c(15, 25, 35, 45, 55)
ntree=200
pars = expand.grid(maxnodes=maxnodes,mtry=mtry)
RMSEs = rep(NA,nrow(pars))
bestRMSE = sd(train.df$W.L..next_year)
for(i in 1:nrow(pars)){
 rftemp = randomForest(formula(lm.full), data=train.df,
                        mtry=pars$mtry[i], maxnodes=pars$maxnodes[i], ntree=ntree)
```

```
RMSEs[i]=RMSE(train.df$W.L..next_year, rftemp$predicted)
  if(RMSEs[i] < bestRMSE) {</pre>
   best_maxnodes = maxnodes[i]
   bestRMSE=RMSEs[i]
   rf1=rftemp
 }
}
data.frame(maxnodes=pars$maxnodes,mtry=pars$mtry,RMSE=RMSEs)
##
     maxnodes mtry
                        RMSE
## 1
          100 15 6.412723
## 2
          200 15 6.338991
## 3
          500 15 6.357269
## 4
          100 25 6.359432
## 5
          200
                25 6.371718
## 6
          500 25 6.361043
## 7
          100 35 6.423718
## 8
          200 35 6.420993
## 9
          500
                35 6.400056
## 10
          100 45 6.422853
## 11
          200 45 6.394741
## 12
          500 45 6.425398
## 13
          100 55 6.434080
          200 55 6.455467
## 14
## 15
          500 55 6.388878
pars[which(RMSEs==bestRMSE),]
    maxnodes mtry
## 2
         200
                15
yhat.rf1.train = predict(rf1)
yhat.rf1.test = predict(rf1, newdata = test.df)
RMSE.rf1.train = RMSE(train.df$W.L..next_year,yhat.rf1.train)
RMSE.rf1.test = RMSE(test.df$W.L..next_year,yhat.rf1.test)
data.frame(train=RMSE.tree1.train,test=RMSE.rf1.test)
##
        train
                  test
## 1 3.879832 7.451836
importance(rf1)
##
                  IncNodePurity
## Age.bat
                       398.4691
## PA
                       195.4966
## AB
                      277.5608
## H.bat
                      182.8005
## X2B
                      344.1605
## X3B
                      462.1844
## HR.bat
                     597.0227
## SB
                      339.0336
```

```
## CS
                        335.9434
## BB.bat
                        852.8076
## SO.bat
                        273.7432
## BA
                        345.0928
## OBP
                        720.1636
## SLG
                        507.0741
## OPS
                        585.1021
## OPSplus
                        583.9218
## TB
                        202.3875
## GDP
                        389.0385
## HBP.bat
                        391.1010
## SH
                        362.8479
## SF
                        332.2869
## IBB.bat
                        455.8381
                        722.7145
## Age.pitch
## W.L..same_year
                       1567.6407
## GF
                        240.0901
## SHO
                        402.4193
## SV
                        873.7227
## IP
                        475.8722
## H.pitch
                        333.2561
## HR.pitch
                        361.4512
                        287.0998
## BB.pitch
## IBB.pitch
                        377.2656
## SO.pitch
                       1106.5547
## HBP.pitch
                        334.5743
## BK
                        531.9950
## WP
                        379.8389
## BF
                        372.3941
## FIP
                        872.2285
## WHIP
                       1244.4283
## H9
                       1384.2177
## HR9
                        612.7717
## BB9
                        427.3121
## SO9
                        392.7926
## SO.W
                        382.4849
## G
                        536.2027
## Inn
                        304.1023
## Ch
                        354.4777
## PO
                        329.7342
## A
                        293.8184
## E
                        409.1964
## DP
                        298.7246
## Fld.
                        431.3260
## RF.9
                        395.7701
## RF.G
                        374.6570
                        792.5348
## tot_fa_war3
                        336.3583
## num_fas
library(randomForest)
set.seed(139)
maxnodes = c(100, 200, 500)
mtry = c(1,2,3)
ntree=200
```

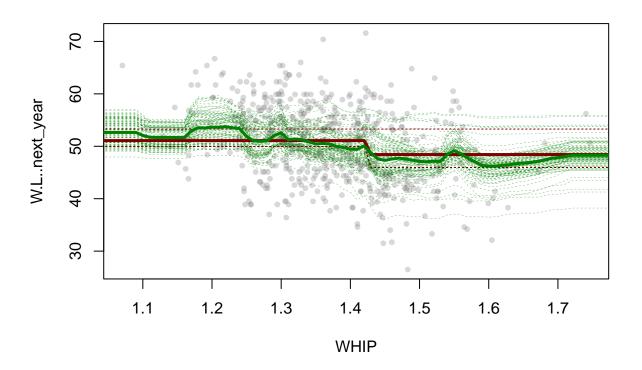
```
pars = expand.grid(maxnodes=maxnodes,mtry=mtry)
RMSEs = rep(NA,nrow(pars))
bestRMSE = sd(train.df$W.L..next_year)
for(i in 1:nrow(pars)){
  rftemp = randomForest(W.L..next_year ~ W.L..same_year + Age.pitch + WHIP, data=train.df,
                        mtry=pars$mtry[i], maxnodes=pars$maxnodes[i], ntree=ntree)
 RMSEs[i]=RMSE(train.df$W.L..next_year, rftemp$predicted)
  if(RMSEs[i] < bestRMSE) {</pre>
   best_maxnodes = maxnodes[i]
   bestRMSE=RMSEs[i]
   rf2=rftemp
 }
}
data.frame(maxnodes=pars$maxnodes,mtry=pars$mtry,RMSE=RMSEs)
##
                       RMSE
    maxnodes mtry
## 1
         100
                 1 6.670368
## 2
         200
              1 6.705663
## 3
         500 1 6.651213
## 4
         100
                2 6.668633
               2 6.723444
## 5
         200
## 6
          500 2 6.751639
## 7
          100
                3 6.649184
## 8
          200
                 3 6.726162
## 9
          500
                 3 6.706977
pars[which(RMSEs==bestRMSE),]
##
    maxnodes mtry
## 7
          100
yhat.rf2.train = predict(rf2)
yhat.rf2.test = predict(rf2, newdata = test.df)
RMSE.rf2.train = RMSE(train.df$W.L..next_year,yhat.rf2.train)
RMSE.rf2.test = RMSE(test.df$W.L..next_year,yhat.rf2.test)
data.frame(train=RMSE.tree1.train,test=RMSE.rf2.test)
##
        train
                  test
## 1 3.879832 7.575087
importance(rf2)
##
                  IncNodePurity
## W.L..same_year
                       8539.024
## Age.pitch
                       6240.002
## WHIP
                      7168.020
```

```
set.seed(139)
samp = sample(nrow(train.df),100)
dummy_df = train.df[samp,]
dummyx = seq(0,100,1)
plot(W.L..next_year~W.L..same_year, data=train.df,cex=0.8,pch=16,col=rgb(0.5,0.5,0.5,0.3))
yhats = matrix(NA, nrow=nrow(dummy_df), ncol=length(dummyx))
yhats.rf=matrix(NA,nrow=nrow(dummy_df),ncol=length(dummyx))
for(i in 1:nrow(dummy df)){
  rows=dummy_df[rep(i,length(dummyx)),]
  rows$W.L..same_year=dummyx
  yhat = predict(tree4, new=rows)
  lines(yhat~dummyx,col=rgb(0.5,0,0,0.5),lwd=0.5,lty=2:3)
  yhats[i,]=yhat
  yhat.rf = predict(rf2,new=rows)
  lines(yhat.rf~dummyx,col=rgb(0,0.5,0,0.5),lwd=0.5,lty=2:3)
  yhats.rf[i,]=yhat.rf
}
mean_yhat = apply(yhats,2,mean)
mean_yhat.rf = apply(yhats.rf,2,mean)
lines(mean_yhat~dummyx,col=rgb(0.5,0,0,1),lwd=3)
lines(mean_yhat.rf~dummyx,col=rgb(0,0.5,0,1),lwd=3)
```



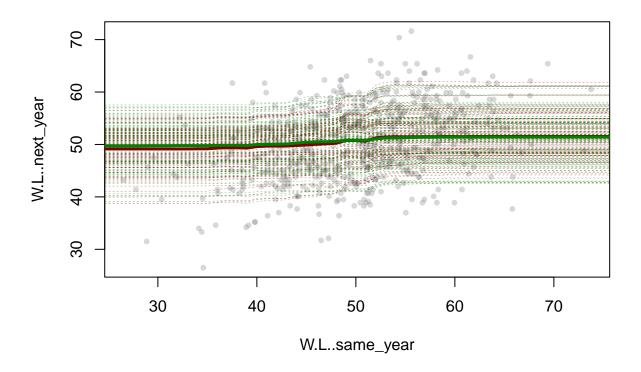
```
samp = sample(nrow(train.df),100)
dummy_df = train.df[samp,]
dummyx = seq(1,2,.01)
```

```
plot(W.L..next_year~WHIP, data=train.df,cex=0.8,pch=16,col=rgb(0.5,0.5,0.5,0.3))
yhats = matrix(NA, nrow=nrow(dummy_df), ncol=length(dummyx))
yhats.rf=matrix(NA, nrow=nrow(dummy_df), ncol=length(dummyx))
for(i in 1:nrow(dummy_df)){
  rows=dummy_df[rep(i,length(dummyx)),]
  rows$WHIP=dummyx
  yhat = predict(tree4, new=rows)
  lines(yhat~dummyx,col=rgb(0.5,0,0,0.5),lwd=0.5,lty=2:3)
  yhats[i,]=yhat
  yhat.rf = predict(rf2,new=rows)
  lines(yhat.rf~dummyx,col=rgb(0,0.5,0,0.5),lwd=0.5,lty=2:3)
  yhats.rf[i,]=yhat.rf
mean_yhat = apply(yhats,2,mean)
mean_yhat.rf = apply(yhats.rf,2,mean)
lines(mean_yhat~dummyx,col=rgb(0.5,0,0,1),lwd=3)
lines(mean_yhat.rf~dummyx,col=rgb(0,0.5,0,1),lwd=3)
```



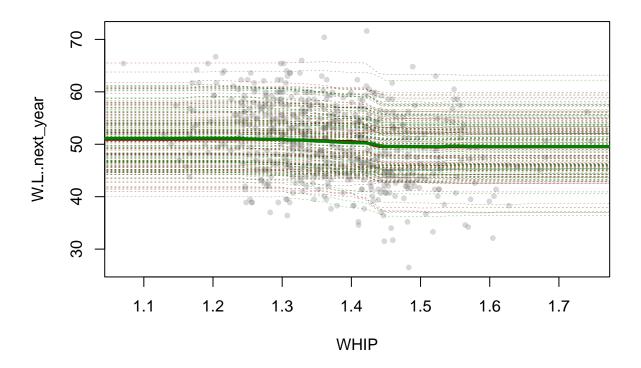
```
set.seed(139)
samp = sample(nrow(train.df),100)
dummy_df = train.df[samp,]
dummyx = seq(0,100,1)
plot(W.L..next_year~W.L..same_year, data=train.df,cex=0.8,pch=16,col=rgb(0.5,0.5,0.5,0.3))
yhats = matrix(NA,nrow=nrow(dummy_df),ncol=length(dummyx))
yhats.rf=matrix(NA,nrow=nrow(dummy_df),ncol=length(dummyx))
```

```
for(i in 1:nrow(dummy_df)){
   rows=dummy_df[rep(i,length(dummyx)),]
   rows$W.L..same_year=dummyx
   yhat = predict(bag,new=rows)
   lines(yhat~dummyx,col=rgb(0.5,0,0,0.5),lwd=0.5,lty=2:3)
   yhats[i,]=yhat
   yhat.rf = predict(rf1,new=rows)
   lines(yhat.rf~dummyx,col=rgb(0,0.5,0,0.5),lwd=0.5,lty=2:3)
   yhats.rf[i,]=yhat.rf
}
mean_yhat = apply(yhats,2,mean)
mean_yhat.rf = apply(yhats.rf,2,mean)
lines(mean_yhat~dummyx,col=rgb(0.5,0,0,1),lwd=3)
lines(mean_yhat.rf~dummyx,col=rgb(0,0.5,0,1),lwd=3)
```



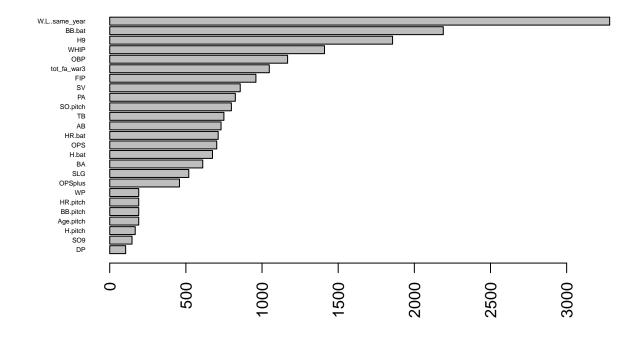
```
samp = sample(nrow(train.df),100)
dummy_df = train.df[samp,]
dummyx = seq(1,2,.01)
plot(W.L..next_year~WHIP, data=train.df,cex=0.8,pch=16,col=rgb(0.5,0.5,0.5,0.3))
yhats = matrix(NA,nrow=nrow(dummy_df),ncol=length(dummyx))
yhats.rf=matrix(NA,nrow=nrow(dummy_df),ncol=length(dummyx))
for(i in 1:nrow(dummy_df)){
   rows=dummy_df[rep(i,length(dummyx)),]
   rows$WHIP=dummyx
   yhat = predict(bag,new=rows)
```

```
lines(yhat~dummyx,col=rgb(0.5,0,0,0.5),lwd=0.5,lty=2:3)
yhats[i,]=yhat
yhat.rf = predict(rf1,new=rows)
lines(yhat.rf~dummyx,col=rgb(0,0.5,0,0.5),lwd=0.5,lty=2:3)
yhats.rf[i,]=yhat.rf
}
mean_yhat = apply(yhats,2,mean)
mean_yhat.rf = apply(yhats.rf,2,mean)
lines(mean_yhat~dummyx,col=rgb(0.5,0,0,1),lwd=3)
lines(mean_yhat.rf~dummyx,col=rgb(0,0.5,0,1),lwd=3)
```



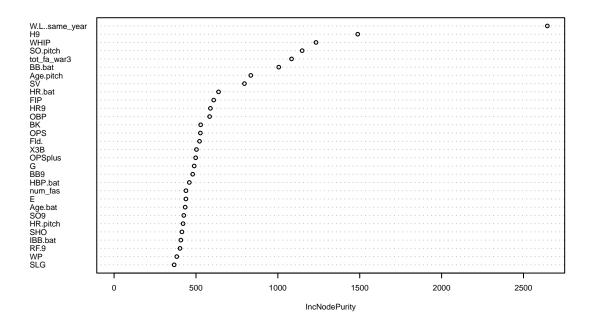
barplot(sort(tree2\$variable.importance),horiz = T,las=2,cex.names = 0.4, main='Variable Importance for

Variable Importance for tree2



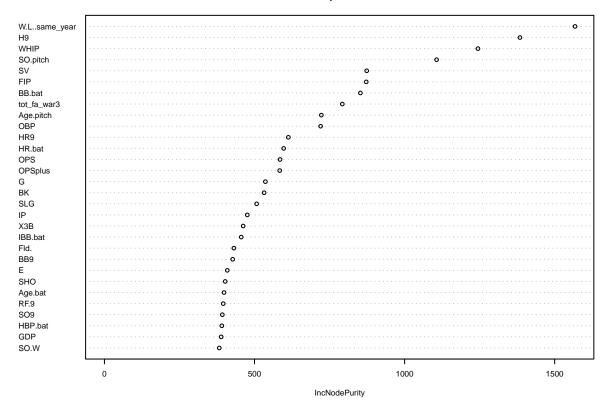
varImpPlot(bag, cex=0.5, main='Variable Importance for bag')

Variable Importance for bag



varImpPlot(rf1,cex=0.5, main='Variable Importance for rf1')

Variable Importance for rf1



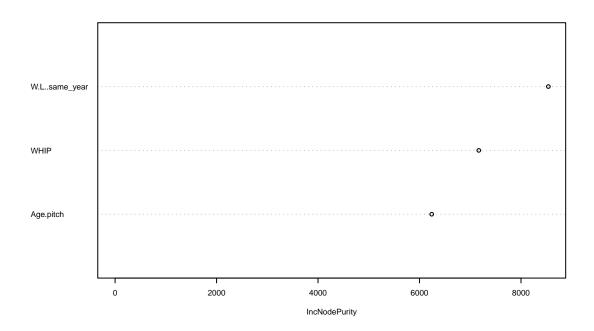
barplot(sort(tree4\$variable.importance),horiz = T,las=2,cex.names = 0.6, main='Variable Importance for

Variable Importance for tree4



varImpPlot(rf2, cex=0.5, main='Variable Importance for rf2')

Variable Importance for rf2



```
tab <- matrix(c(RMSE.tree1.train, RMSE.tree1.test,</pre>
  RMSE.tree2.train, RMSE.tree2.test,
  RMSE.bag.train, RMSE.bag.test,
  RMSE.rf1.train, RMSE.rf1.test,
  RMSE.rf2.train, RMSE.rf2.test,
  RMSE.tree4.train, RMSE.tree4.test), nrow=6, byrow = TRUE
colnames(tab) <- c('train','test')</pre>
rownames(tab) <- c('tree1','tree2','bag', 'rf1', 'rf2', 'tree4')</pre>
tab <- as.table(tab)</pre>
tab
##
            train
                       test
## tree1 3.879832 8.406397
## tree2 6.226519 7.778095
## bag
        6.359278 7.444550
## rf1
         6.338991 7.451836
## rf2
         6.649184 7.575087
## tree4 6.669579 7.866976
library(lme4)
set.seed(139)
# for (i in 1997:2022){
# lmer_model <- lmer(team_data[[i]]$W.L.~poly(team_data[[i]]$BatAqe, 2, raw = TRUE) + (1 + poly(team_
```

```
summary(lmer_model)
# }
lmer_model <- lmer(train.df$W.L..next_year ~ poly(train.df$Age.bat, 2, raw = FALSE) + (1 + poly(train.df</pre>
summary(lmer_model)
## Linear mixed model fit by REML ['lmerMod']
## Formula: train.df$W.L..next_year ~ poly(train.df$Age.bat, 2, raw = FALSE) +
       ((1 | train.df$Tm) + (0 + poly(train.df$Age.bat, 2, raw = FALSE) |
##
           train.df$Tm))
## REML criterion at convergence: 3562.1
##
## Scaled residuals:
##
       Min
                1Q Median
                                30
                                       Max
## -3.1945 -0.7110 0.0377 0.6549 3.3518
##
## Random effects:
## Groups
                  Name
                                                           Variance Std.Dev. Corr
## train.df.Tm
                  (Intercept)
                                                            11.27
                                                                     3.357
## train.df.Tm.1 poly(train.df$Age.bat, 2, raw = FALSE)1 299.31
                                                                    17.300
##
                  poly(train.df$Age.bat, 2, raw = FALSE)2 153.86
                                                                    12.404
                                                                             -1.00
## Residual
                                                            41.61
                                                                     6.451
## Number of obs: 536, groups: train.df$Tm, 29
## Fixed effects:
##
                                           Estimate Std. Error t value
## (Intercept)
                                             50.1414
                                                        0.6908 72.585
## poly(train.df$Age.bat, 2, raw = FALSE)1 -3.3801
                                                         8.2867 -0.408
## poly(train.df$Age.bat, 2, raw = FALSE)2 4.0653
                                                         7.6890
                                                                  0.529
##
## Correlation of Fixed Effects:
                      (Intr) p(.$A.,2,r=FALSE)1
## p(.$A.,2,r=FALSE)1 -0.003
## p(.$A.,2,r=FALSE)2 0.028 -0.134
lmer_model <- lmer(train.df$W.L..next_year ~ poly(train.df$BA, 2, raw = FALSE) + (1 + poly(train.df$BA,</pre>
## boundary (singular) fit: see help('isSingular')
summary(lmer_model)
## Linear mixed model fit by REML ['lmerMod']
## Formula: train.df$W.L..next_year ~ poly(train.df$BA, 2, raw = FALSE) +
##
       ((1 | train.df$Tm) + (0 + poly(train.df$BA, 2, raw = FALSE) |
           train.df$Tm))
##
##
## REML criterion at convergence: 3545.3
## Scaled residuals:
##
       Min
                1Q Median
                                3Q
                                       Max
```

```
## -3.0813 -0.6780 -0.0020 0.6808 3.1719
##
## Random effects:
## Groups
                                                     Variance Std.Dev. Corr
                  Name
## train.df.Tm
                  (Intercept)
                                                     1.137e+01 3.3716324
## train.df.Tm.1 poly(train.df$BA, 2, raw = FALSE)1 1.858e-07 0.0004311
                  poly(train.df$BA, 2, raw = FALSE)2 1.262e-08 0.0001124 1.00
## Residual
                                                     4.083e+01 6.3895753
## Number of obs: 536, groups: train.df$Tm, 29
##
## Fixed effects:
##
                                      Estimate Std. Error t value
                                                   0.6892 72.827
## (Intercept)
                                       50.1940
## poly(train.df$BA, 2, raw = FALSE)1 35.8076
                                                   8.4294
                                                          4.248
## poly(train.df$BA, 2, raw = FALSE)2
                                                   6.7529
                                                            0.996
                                       6.7245
##
## Correlation of Fixed Effects:
                      (Intr) p(.$BA,2,r=FALSE)1
## p(.$BA,2,r=FALSE)1 0.010
## p(.$BA,2,r=FALSE)2 0.005
## optimizer (nloptwrap) convergence code: 0 (OK)
## boundary (singular) fit: see help('isSingular')
# lmer_model <- lmer(W.L..next_year ~ Age.bat + PA + AB + H.bat + X2B + X3B +
                \# HR.bat + SB + CS + BB.bat + SO.bat + BA + OBP + SLG + OPS + OPSplus +
                \# TB + GDP + HBP.bat + SH + SF + IBB.bat + Age.pitch + W.L..same_year +
                \# GF + SHO + SV + IP + H.pitch + HR.pitch +
                # BB.pitch + IBB.pitch + SO.pitch + HBP.pitch + BK + WP + BF +
                # FIP + WHIP + H9 + HR9 + BB9 + S09 + S0.W +
                \# G + Inn + Ch + PO + A + E + DP + Fld. +
                \# RF.9 + RF.G + tot_fa_war3 + num_fas // Tm, data = train.df, verbose=TRUE)
summary(lmer model)
## Linear mixed model fit by REML ['lmerMod']
## Formula: train.df$W.L..next_year ~ poly(train.df$BA, 2, raw = FALSE) +
       ((1 | train.df$Tm) + (0 + poly(train.df$BA, 2, raw = FALSE) |
##
           train.df$Tm))
## REML criterion at convergence: 3545.3
##
## Scaled residuals:
      Min
                10 Median
                                3Q
                                       Max
## -3.0813 -0.6780 -0.0020 0.6808 3.1719
## Random effects:
                                                     Variance Std.Dev. Corr
## Groups
                 Name
## train.df.Tm
                  (Intercept)
                                                     1.137e+01 3.3716324
## train.df.Tm.1 poly(train.df$BA, 2, raw = FALSE)1 1.858e-07 0.0004311
##
                  poly(train.df$BA, 2, raw = FALSE)2 1.262e-08 0.0001124 1.00
## Residual
                                                     4.083e+01 6.3895753
## Number of obs: 536, groups: train.df$Tm, 29
##
```

```
## Fixed effects:
##
                                      Estimate Std. Error t value
## (Intercept)
                                       50.1940
                                                   0.6892 72.827
## poly(train.df$BA, 2, raw = FALSE)1 35.8076
                                                   8.4294 4.248
## poly(train.df$BA, 2, raw = FALSE)2
                                       6.7245
                                                   6.7529 0.996
##
## Correlation of Fixed Effects:
                      (Intr) p(.$BA,2,r=FALSE)1
## p(.$BA,2,r=FALSE)1 0.010
## p(.$BA,2,r=FALSE)2 0.005 0.016
## optimizer (nloptwrap) convergence code: 0 (OK)
## boundary (singular) fit: see help('isSingular')
set.seed(139)
lmer.varmodel <- lmer(W.L..next_year ~ WHIP + W.L..same_year + Age.pitch + (1 + WHIP + W.L..same_year +</pre>
## Warning in checkConv(attr(opt, "derivs"), opt$par, ctrl = control$checkConv, :
## unable to evaluate scaled gradient
## Warning in checkConv(attr(opt, "derivs"), opt$par, ctrl = control$checkConv, :
## Model failed to converge: degenerate Hessian with 1 negative eigenvalues
# summary(lmer.varmodel)
# predict(lmer.varmodel)
RMSE(train.df$W.L..next_year, predict(lmer.varmodel))
## [1] 5.971771
RMSE(test.df$W.L..next_year, predict(lmer.varmodel, newdata=test.df))
## [1] 7.244459
set.seed(139)
lmer.varmodel <- lmer(W.L..next_year ~ WHIP + W.L..same_year + Age.pitch | Tm, data = train.df)</pre>
## boundary (singular) fit: see help('isSingular')
# summary(lmer.varmodel)
# predict(lmer.varmodel)
RMSE(train.df$W.L..next_year, predict(lmer.varmodel))
## [1] 5.872679
RMSE(test.df$W.L..next_year, predict(lmer.varmodel, newdata=test.df))
## [1] 7.224486
```

```
set.seed(139)
lmer.varmodel <- lmer(W.L..next_year ~ WHIP + W.L..same_year + Age.pitch + tot_fa_war3 | Tm, data = tra</pre>
## boundary (singular) fit: see help('isSingular')
# summary(lmer.varmodel)
# predict(lmer.varmodel)
RMSE(train.df$W.L..next_year, predict(lmer.varmodel))
## [1] 5.750696
RMSE(test.df$W.L..next_year, predict(lmer.varmodel, newdata=test.df))
## [1] 7.259757
set.seed(139)
lmer.varmodel <- lmer(W.L..next_year ~ WHIP + W.L..same_year + Age.pitch + H9 | Tm, data = train.df)</pre>
## boundary (singular) fit: see help('isSingular')
# summary(lmer.varmodel)
# predict(lmer.varmodel)
RMSE(train.df$W.L..next_year, predict(lmer.varmodel))
## [1] 5.644522
RMSE(test.df$W.L..next_year, predict(lmer.varmodel, newdata=test.df))
## [1] 7.153371
set.seed(139)
lmer.varmodel <- lmer(W.L..next_year ~ WHIP + W.L..same_year + Age.pitch + H9 + (1 + WHIP + W.L..same_y</pre>
## boundary (singular) fit: see help('isSingular')
# summary(lmer.varmodel)
# predict(lmer.varmodel)
RMSE(train.df$W.L..next_year, predict(lmer.varmodel))
## [1] 5.714458
RMSE(test.df$W.L..next_year, predict(lmer.varmodel, newdata=test.df))
## [1] 7.13684
```

```
set.seed(139)
lmer.varmodel <- lmer(W.L..next_year ~ Age.bat + PA + AB | Tm, data = train.df)</pre>
## Warning in checkConv(attr(opt, "derivs"), opt$par, ctrl = control$checkConv, :
## unable to evaluate scaled gradient
## Warning in checkConv(attr(opt, "derivs"), opt$par, ctrl = control$checkConv, :
## Model failed to converge: degenerate Hessian with 2 negative eigenvalues
RMSE(train.df$W.L..next_year, predict(lmer.varmodel))
## [1] 5.903281
RMSE(test.df$W.L..next_year, predict(lmer.varmodel, newdata=test.df))
## [1] 7.389564
set.seed(139)
lmer.varmodel <- lmer(W.L..next_year ~ Age.bat + PA + AB + (1 + Age.bat + PA + AB | Tm) , data = train.</pre>
## Warning in checkConv(attr(opt, "derivs"), opt$par, ctrl = control$checkConv, :
## unable to evaluate scaled gradient
## Warning in checkConv(attr(opt, "derivs"), opt$par, ctrl = control$checkConv, :
## Model failed to converge: degenerate Hessian with 4 negative eigenvalues
RMSE(train.df$W.L..next_year, predict(lmer.varmodel))
## [1] 5.953489
RMSE(test.df$W.L..next_year, predict(lmer.varmodel, newdata=test.df))
## [1] 7.31225
```