
ReNet: A Recurrent Neural Network Based Alternative to Convolutional Networks

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Abstract

In this paper, we propose a deep neural network architecture for object recognition based on recurrent neural networks. The proposed network, called ReNet, replaces the ubiquitous convolution+pooling layer of the deep convolutional neural network with four recurrent neural networks that sweep horizontally and vertically in both directions across the image. We evaluate the proposed ReNet on three widely-used benchmark datasets; MNIST, CIFAR-10 and SVHN. The result suggests that ReNet is a viable alternative to the deep convolutional neural network, and that further investigation is needed.

1 Introduction

Convolutional neural networks [CNN, Fukushima, 1980, LeCun et al., 1989] have become the method of choice for object recognition [see, e.g., Krizhevsky et al., 2012]. They have proved to be successful at a variety of benchmark problems including, but not limited to, handwritten digit recognition [see, e.g., Ciresan et al., 2012b], natural image classification [see, e.g., Lin et al., 2014, Simonyan and Zisserman, 2015, Szegedy et al., 2014], house number recognition [see, e.g., Goodfellow et al., 2014] and traffic sign recognition [see, e.g., Ciresan et al., 2012a]. Furthermore, image representations from CNNs trained to recognize objects on a large set of more than one million images [Simonyan and Zisserman, 2015, Szegedy et al., 2014] have been found to be extremely helpful in performing other computer vision tasks such as image caption generation [see, e.g., Vinyals et al., 2014, Xu et al., 2015], video description generation [see, e.g., Yao et al., 2015] and object localization/detection [see, e.g., Sermanet et al., 2014].

While the CNN has been successful in computer vision, recurrent neural networks (RNN) have become the method of choice for modeling sequential data, such as text and sound. Natural language processing (NLP) applications include language modeling [see, e.g., Mikolov, 2012], and machine translation [Sutskever et al., 2014, Cho et al., 2014, Bahdanau et al., 2015]. Other popular areas of application include speech recognition [Chorowski et al., 2014, Graves and Jaitly, 2014] and offline handwriting recognition/generation [Graves and Schmidhuber, 2009, Graves et al., 2008, Graves, 2013]. The recent revival of RNNs has largely been due to advances in learning algorithms [Pascanu et al., 2013, Martens and Sutskever, 2011] and model architectures [Pascanu et al., 2014, Hochreiter and Schmidhuber, 1997, Cho et al., 2014].

RNNs have previously been extended to multi-dimensional tasks and applied to object recognition [Graves and Schmidhuber, 2009]. The architecture proposed here is related and inspired by this

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earlier work, but our model relies on purely uni-dimensional RNNs coupled in a novel way, rather than on a multi-dimensional RNN. The basic idea behind the proposed ReNet architecture is to replace each convolutional layer (with convolution+pooling making up a layer) in the CNN with four RNNs that sweep over lower-layer features in different directions: (1) bottom to top, (2) top to bottom, (3) left to right and (4) right to left. The recurrent layer ensures that each feature activation in its output is an activation at the specific location *with respect to the whole image*, in contrast to the usual convolution+pooling layer which only has a local context window. The lowest layer of the model sweeps over the input image, with subsequent layers operating on extracted representations from the layer below, forming a hierarchical representation of the input.

Graves and Schmidhuber [2009] have demonstrated an RNN-based object recognition system for off-line Arabic handwriting recognition. The main difference between ReNet and the model of Graves and Schmidhuber [2009] is that we use the usual sequence RNN, instead of the multidimensional RNN. We make the latter two parts of a single layer, usually (horizontal) RNNs or one (horizontal) bidirectional RNN, work on the hidden states computed by the first two (vertical) RNNs, or one (vertical) bidirectional RNN. This allows us to use a plain RNN, instead of the more complex multi-dimensional RNN, while making each output activation of the layer be computed with respect to the whole input image. Furthermore, the proposed variant is more easily parallelizable, as each RNN is dependent only along a horizontal or vertical sequence of patches. This architectural distinction results in our model being much more amenable to distributed computing than that of Graves and Schmidhuber [2009].

In this work, we test the proposed ReNet on several widely used object recognition benchmarks, namely MNIST [LeCun et al., 1999], CIFAR-10 [Krizhevsky and Hinton, 2009] and SVHN [Netzer et al., 2011]. Our experiments reveal that the model performs comparably to convolutional neural networks on all these datasets with only cursory exploration of hyperparameters, suggesting the potential of RNNs as a competitive alternative to CNNs for image related tasks.

2 Model Description

Let us denote by $x \in \mathbb{R}^{w \times h \times c}$ the input image from the layer below, where w , h and c are the width, height and feature dimensionality, or the number of channels, respectively. Given a receptive field (or patch) size of $w_p \times h_p$, we split the input image x into a set of $I \times J$ (non-overlapping) patches $X = \{x_{i,j}\}$, where $I = \frac{w}{w_p}$, $J = \frac{h}{h_p}$ and $x_{i,j} \in \mathbb{R}^{w_p \times h_p \times c}$ is the (i, j) -th patch of the input image. The first index i is the horizontal index and the other index j is the vertical index.

First, we sweep the image vertically with two RNNs, with one RNN working in a bottom-up direction and the other working in a top-down direction. Each RNN takes as an input one (flattened) patch at a time and updates its hidden state, working along each column j of the split input image X .

$$z_{i,j}^F = f_{\text{VFW}}(z_{i,j-1}^F, x_{i,j}), \text{ for } j = 1, \dots, J \quad (1)$$

$$z_{i,j}^R = f_{\text{VREV}}(z_{i,j+1}^R, x_{i,j}), \text{ for } j = J, \dots, 1 \quad (2)$$

Note that f_{VFW} and f_{VREV} return the activation of the recurrent hidden state, and may be implemented either as a simple tanh layer, as a gated recurrent layer [Cho et al., 2014] or as a long short-term memory layer [Hochreiter and Schmidhuber, 1997].

After this vertical, bidirectional sweep, we concatenate the intermediate hidden states $z_{i,j}^F$ and $z_{i,j}^R$ at each location (i, j) to get a composite feature map $V = \{z_{i,j}\}_{i=1, \dots, I}^{j=1, \dots, J}$, where $z_{i,j} \in \mathbb{R}^{1 \times h_p \times 2d}$ and d is the number of recurrent units. Each $z_{i,j}$ is now the activation of a feature detector at the location (i, j) with respect to all the pixels in the j -th column of the original input ($x_{i,j}$ for all i).

Next we sweep over the obtained feature map V horizontally with two RNNs (f_{HFW} and f_{HREV}). In a similar manner as the vertical sweep, these RNNs work along each row of V resulting in the output

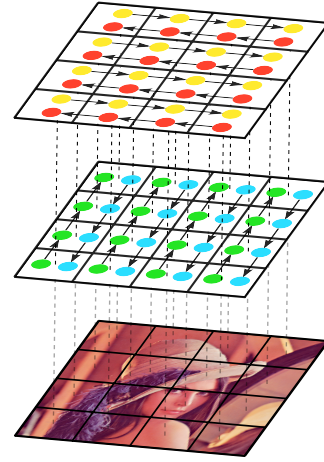


Figure 1: A one-layer ReNet

feature map $H = \{z'_{i,j}\}$, where $z'_{i,j} \in \mathbb{R}^{1 \times 1 \times 2d}$. Now, each vector $z'_{i,j}$ represents the features of the original image patch $x_{i,j}$ in the context of the whole image.

Let us denote by ϕ the function from the input image map of X to the output feature map H (see Fig. 1 for a graphical illustration.) Clearly, we can stack multiple ϕ 's to make the proposed ReNet deeper and capture increasingly complex features of the input image. After any number of recurrent layers are applied to an input image, the activation at the last recurrent layer may be flattened and fed into a differentiable classifier. In our experiments we used several fully-connected layers followed by a softmax classifier (as shown in Fig. 2).

The deep ReNet is a smooth, continuous function, and the parameters (those from the RNNs as well as from the fully-connected layers) can be estimated by the stochastic gradient descent algorithm with the gradient computed by backpropagation algorithm [see, e.g., Rumelhart et al., 1986] to maximize the log-likelihood.

3 Differences between LeNet and ReNet

There are many similarities and differences between the proposed ReNet and a convolutional neural network. In this section we use LeNet to refer to the canonical convolutional neural network as shown by LeCun et al. [1989]. Here we highlight a few key points of comparison between ReNet and LeNet.

At each layer, both networks apply the same set of filters to patches of the input image or the feature map from the layer below. It is a common practice to overlap those patches for LeNet, but we *do not* overlap the patches for the proposed implementation of ReNet. This design choice was made based on the fact that lateral connections, which span across the whole image, will help resolve small displacements of features across multiple consecutive patches.

The lateral connections which span the whole image should help extract a more compact feature representation of the input image at each layer. This can be accomplished by the lateral connections removing/resolving redundant features at different locations of the image. The lack of this type of lateral connection in LeNet may lead to many more levels of convolution+pooling layers in order to detect redundant features from different parts of the image.

LeNet max-pools the activations of each filter over a small region to achieve local translation invariance. In contrast, the proposed ReNet does not use any pooling due to the existence of powerful, learned lateral connections. The lateral connection in ReNet can emulate the local competition among features induced by the max-pooling in LeNet. This does not mean that it is not possible to use max-pooling in ReNet. The use of max-pooling in the ReNet could be helpful in reducing the dimensionality of the feature map, resulting in lower computational cost.

Max-pooling as used in LeNet may prove problematic when building a convolutional autoencoder whose decoder is an inverse¹ of LeNet, as the max operator is not invertible. The proposed ReNet is end-to-end smooth and differentiable, making it more suited to be used as a decoder in the autoencoder or any of its probabilistic variants [see, e.g., Kingma and Welling, 2014].

The main disadvantage of ReNet is that it is not easily parallelizable, due to the sequential nature of the recurrent neural network (RNN). LeNet, on the other hand, is highly parallelizable due to the independence of computing activations at each layer. However, it may be the case that the introduction of sequential, lateral connections results in more efficient parametrization, requiring a smaller number of parameters with overall fewer computations, although this needs to be further explored.

4 Experiments

4.1 Datasets

We evaluated the proposed ReNet on three widely-used benchmark datasets; MNIST, CIFAR-10 and the Street View Housing Numbers (SVHN). In this section we describe each dataset in detail.

¹ All the forward arrows from the input to the output in the original LeNet are reversed.

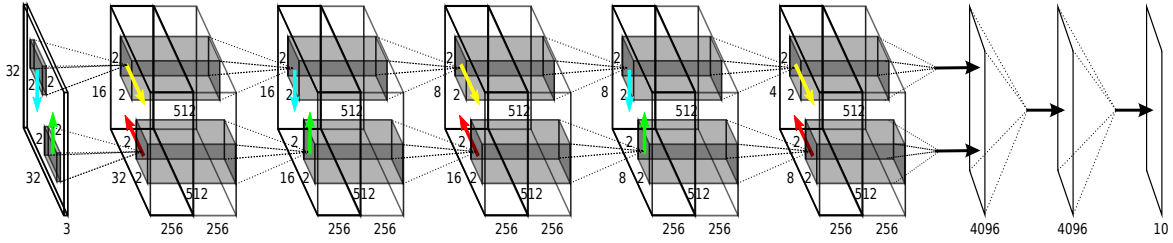


Figure 2: The ReNet network used for SVHN classification

MNIST The MNIST dataset [LeCun et al., 1999] consists of 70,000 handwritten digits from 0 to 9, centered on a 28×28 square canvas. Each pixel represents the grayscale in the range of $[0, 255]$.² We split the dataset into 50,000 training samples, 10,000 validation samples and 10,000 test samples, following the standard split.

CIFAR-10 The CIFAR-10 dataset [Krizhevsky and Hinton, 2009] is a curated subset of the 80 million tiny images dataset, originally released by Torralba et al. [2008]. CIFAR-10 contains 60,000 images each of which belongs to one of ten categories; airplane, automobile, bird, cat, deer, dog, frog, horse, ship and truck. Each image is 32 pixels wide and 32 pixels high with 3 color channels (red, green and blue.) Following the standard procedure, we split the dataset into 40,000 training, 10,000 validation and 10,000 test samples. We applied zero-phase component analysis (ZCA) and normalized each pixel to have zero-mean and unit-variance across the training samples, as suggested by Krizhevsky and Hinton [2009].

Street View House Numbers The Street View House Numbers (SVHN) dataset [Netzer et al., 2011] consists of cropped images representing house numbers captured by Google StreetView vehicles as a part of the Google Maps mapping process. These images consist of digits 0 through 9 with values in the range of $[0, 255]$ in each of 3 red-green-blue color channels. Each image is 32 pixels wide and 32 pixels high giving a sample dimensionality (32, 32, 3). The number of samples we used for training, valid, and test sets is 543,949, 60,439, and 26,032 respectively. We normalized each pixel to have zero-mean and unit-variance across the training samples.

4.1.1 Data Augmentation

It has been known that augmenting training data often leads to better generalization [see, e.g., Krizhevsky et al., 2012]. We decided to employ two primary data augmentations in the following experiments: *flipping* and *shifting*.

For flipping, we either flipped each sample horizontally with 25% chance, flipped it vertically with 25% chance, or left it unchanged. This allows lets the model observe “mirror images” of the original image during training. In the case of shifting, we either shifted the image by 2 pixels to the left (25% chance), 2 pixels to the right (25% chance) or left it as it was. After this first processing, we further either shifted it by 2 pixels to the top (25% chance), 2 pixels to the bottom (25% chance) or left it as it was. This two-step procedure makes the model more robust to slight shifting of an object in the image. The shifting was done without padding the borders of the image, preserving the original size but dropping the pixels which are shifted out of the input while shifting in zeros.

The choice of whether to apply these augmentation procedures on each dataset was chosen on a per-case basis in order to maximize validation performance.

4.2 Model Architectures

Gated Recurrent Units Gated recurrent units [GRU, Cho et al., 2014] and long short-term memory units [LSTM, Hochreiter and Schmidhuber, 1997] have been successful in many applications using recurrent neural networks [see, e.g., Cho et al., 2014, Sutskever et al., 2014, Xu et al., 2015].

² We scaled each pixel by dividing it with 255.

	MNIST	CIFAR-10	SVHN
N_{RE}	2	3	3
$w_p \times h_p$	$[2 \times 2] - [2 \times 2]$	$[2 \times 2] - [2 \times 2] - [2 \times 2]$	$[2 \times 2] - [2 \times 2] - [2 \times 2]$
d_{RE}	256–256	320–320–320	256–256–256
N_{FC}	2	1	2
d_{FC}	4096–4096	4096	4096–4096
f_{FC}	$\max(0, x)$	$\max(0, x)$	$\max(0, x)$
Flipping	no	yes	no
Shifting	yes	yes	yes

Table 1: Model architectures used in the experiments. Each row shows respectively the number of ReNet layers, the size of the patches, the number of neurons of each ReNet layer, the number of fully connected layers, the number of neurons of the fully connected layers, their activation function and the data augmentation procedure employed.

To show that the ReNet model performs well independently of the specific implementation of the recurrent units, we decided to use the GRU on MNIST and CIFAR-10, with LSTM units on SVHN.

The hidden state of the GRU at time t is computed by

$$h_t = (1 - u_t) \odot h_{t-1} + u_t \odot \tilde{h}_t,$$

where

$$\tilde{h}_t = \tanh(Wx_t + U(r_t \odot h_{t-1}) + b)$$

and

$$[u_t; r_t] = \sigma(W_g x_t + U_g h_{t-1} + b_g).$$

For more details on the LSTM unit, as well as for an in-depth comparison among different recurrent units, we refer the reader to [Chung et al., 2015].

General Architecture The principal parameters that define the architecture of the proposed ReNet are the number of ReNet layers (N_{RE}), their corresponding receptive field sizes ($w_p \times h_p$) and feature dimensionality (d_{RE}), the number of fully-connected layers (N_{FC}) and their corresponding numbers (d_{FC}) and types (f_{FC}) of hidden units.

In this introductory work, we did not focus on extensive hyperparameter search to find the optimal validation set performance. We chose instead to focus the experiments on a small set of hyperparameters, with the only aim to show the potential of the proposed model. Refer to Table 1 for a summary of the settings that performed best on the validation set of the studied datasets and to Fig. 2 for a graphical illustration of the model we selected for SVHN.

4.3 Training

To train the networks we used a recently proposed adaptive learning rate algorithm, called Adam [Kingma and Ba, 2014]. In order to reduce overfitting we applied dropout [Srivastava et al., 2014] after each layer, including both the proposed ReNet layer (after the horizontal and vertical sweeps) and the fully-connected layers. The input was also corrupted by masking out each variable with probability 0.2. Finally, each optimization run was early stopped based on validation error.

Note that unlike many previous works, we did not retrain the model (selected based on the validation performance) using both the training and validation samples. This experiment design choice is consistent with our declared goal to show a proof of concept rather than stressing absolute performance. There are many potential areas of exploration for future work.

5 Results and Analysis

In Table 2, we present the results on three datasets, along with previously reported results.

Test Error	Model
0.28%	[Wan et al., 2013]★
0.31%	[Graham, 2014a]★
0.35%	[Ciresan et al., 2010]
0.39%	[Mairal et al., 2014]★
0.39%	[Lee et al., 2014]★
0.4%	[Simard et al., 2003]★
0.44%	[Graham, 2014b]★
0.45%	[Goodfellow et al., 2013]★
0.45%	ReNet
0.47%	[Lin et al., 2014]★
0.52%	[Azzopardi and Petkov, 2013]

(a) MNIST

Test Error	Model
4.5%	[Graham, 2014b]★
6.28%	[Graham, 2014a]★
8.8%	[Lin et al., 2014]★
9.35%	[Goodfellow et al., 2013]★
9.39%	[Springenberg and Riedmiller, 2013]★
9.5%	[Snoek et al., 2012]★
11%	[Krizhevsky et al., 2012]★
11.10%	[Wan et al., 2013]★
12.35%	ReNet
15.13%	[Zeiler and Fergus, 2013]★
15.6%	[Hinton et al., 2012]★

(b) CIFAR-10

Test Error	Model
1.92%	[Lee et al., 2014]★
2.23%	[Wan et al., 2013]★
2.35%	[Lin et al., 2014]★
2.38%	ReNet
2.47%	[Goodfellow et al., 2013]★
2.8%	[Zeiler and Fergus, 2013]★

(c) SVHN

Table 2: Generalization errors obtained by the proposed ReNet along with those reported by previous works on each of the three datasets. ★ denotes a convolutional neural network. We only list the results reported by a single model, i.e., no ensembling of multiple models. In the case of SVHN, we report results from models trained on the Format 2 (cropped digit) dataset only.

It is clear that the proposed ReNet performs comparably to deep convolutional neural networks which are the *de facto* standard for object recognition. This suggests that the proposed ReNet is a viable alternative to convolutional neural networks (CNN), even on tasks where CNNs have historically dominated. However, it is important to notice that the proposed ReNet does not outperform state-of-the-art convolutional neural networks on any of the three benchmark datasets, which calls for more research in the future.

6 Discussion

Choice of Recurrent Units Note that the proposed architecture is independent of the chosen recurrent units. We observed in preliminary experiments that gated recurrent units, either the GRU or the LSTM, outperform a usual sigmoidal unit (affine transformation followed by an element-wise sigmoid function.) This indirectly confirms that the model utilizes long-term dependencies across an input image, and the gated recurrent units help capture these dependencies.

Analysis of the Trained ReNet In this paper, we evaluated the proposed ReNet only quantitatively. However, the accuracies on the test sets do not reveal what kind of image structures the ReNet has captured in order to perform object recognition. Due to the large differences between ReNet and LeNet discussed in Sec. 3, we expect that the internal behavior of ReNet will differ from that of LeNet significantly. Further investigation along the line of [Zeiler and Fergus, 2014] will be needed, as well exploring ensembles which combine RNNs and CNNs for bagged prediction.

Computationally Efficient Implementation As discussed in Sec. 3, the proposed ReNet is less parallelizable due to the sequential nature of the recurrent neural network (RNN). Although this sequential nature cannot be addressed directly, our construction of ReNet allows the forward and backward RNNs to be run independently from each other, which allows for parallel computation. Furthermore, we can use many parallelization tricks widely used for training convolutional neural networks such as parallelizing fully-connected layers [Krizhevsky, 2014], having separate sets of kernels/features in different processors [Krizhevsky et al., 2012] and exploiting data parallelism.

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