Table 1: Model 1

Estimator	IMSE	IMSE   $Y < q_{.25}$	IMSE   $q_{.25} < Y < q_{.5}$	IMSE   $q_{.5} < Y < q_{.75}$	IMSE   $q_{.75} < Y$
(12) $\hat{f}_{\hat{\mu},\text{nonpar}}$	0.086(1)	0.059(1)	0.0054(1)	0.0081(1)	0.014(1)
(13) $\hat{f}_{\mu,\xi}$	$0.068 \ (0.78)$	0.054 (0.91)	0.0043 (0.8)	$0.0042 \ (0.51)$	$0.0054 \ (0.39)$
(14) $\hat{f}_{\mu,\hat{\xi}}$	0.069 (0.79)	$0.054 \ (0.92)$	0.0047 (0.87)	$0.0042 \ (0.51)$	0.0054 (0.4)
(15) $\hat{f}_{\hat{\mu},\mathrm{par}}$	0.094(1.1)	0.068(1.1)	0.0047 (0.87)	0.0038 (0.46)	0.018(1.3)
(20) $f_{\hat{\mu},\text{nonpar}}^{\dagger}$	$0.081\ (0.93)$	$0.058 \; (0.98)$	$0.0046 \ (0.85)$	$0.0066 \ (0.81)$	$0.012 \ (0.84)$
$(21) f_{\mu,\xi}^{\dagger}$	0.07(0.8)	0.058 (0.99)	0.0029 (0.53)	0.0034 (0.41)	$0.0049 \ (0.35)$
$(22) f_{\mu,\hat{\xi}}^{\bar{\tau},\hat{s}}$	0.07 (0.81)	$0.059 \ (0.99)$	$0.0032 \ (0.59)$	$0.0034 \ (0.41)$	$0.005 \ (0.36)$
(23) $f_{\hat{\mu}, \text{par}}^{\dagger}$	0.1(1.2)	0.075(1.3)	0.0063 (1.2)	$0.0046 \ (0.56)$	0.017(1.2)
(25) $f_{\hat{\omega},\text{nonpar}}^{\dagger}$	0.32(3.6)	0.19(3.2)	0.034(6.2)	0.049(6)	0.043(3.1)
(26) $f_{\hat{\omega}, \text{par}}^{\dagger}$	0.1(1.2)	0.076(1.3)	0.0062(1.2)	$0.0044 \ (0.55)$	0.016(1.1)
(4) p	0.06 (0.69)	0.04 (0.67)	0.011(2)	0.0038 (0.46)	0.0055(0.4)
f	0 (0)	0 (0)	0 (0)	0 (0)	0 (0)
(hat25) $\hat{f}_{\hat{\omega},\text{nonpar}}$	0.36(4.2)	0.2(3.4)	0.037(6.9)	0.055 (6.8)	0.068(4.9)
(hat26) $\hat{f}_{\hat{\omega},par}$	0.094(1.1)	0.069(1.2)	$0.0046 \ (0.86)$	0.0037 (0.46)	0.017(1.2)
$\hat{\mu}$ , nonpar	0.02(0.23)	7.9e-07 (1.3e-05)	$1e-05 \ (0.0019)$	$7.7e-05 \ (0.0095)$	0.02(1.4)
$\mu, \xi$	0 (0)	0 (0)	0 (0)	0 (0)	0 (0)
$\mu,\hat{\xi}$	$2e-04 \ (0.0023)$	3.1e-08 (5.2e-07)	3.8e-07 (7.1e-05)	$2.5e-06 \ (0.00031)$	$0.00019 \ (0.014)$
$\hat{\mu}, \mathrm{par}$	0.003(0.035)	$2.1e-05 \ (0.00036)$	2.6e-05 (0.0048)	$4.2e-05 \ (0.0052)$	$0.0029 \ (0.21)$
$\hat{\omega},  ext{nonpar}$	0.02(0.24)	$4.5e-05 \ (0.00076)$	$0.00016 \ (0.03)$	$0.00041 \ (0.05)$	0.02(1.4)
$\hat{\omega}$ , par	$0.003 \ (0.035)$	2.4e-05 (4e-04)	$3e-05 \ (0.0055)$	5e-05 (0.0061)	0.0029 (0.21)

Table 2: Model 2

Estimator	IMSE	IMSE   $Y < q_{.25}$	IMSE   $q_{.25} < Y < q_{.5}$	IMSE   $q_{.5} < Y < q_{.75}$	IMSE   $q_{.75} < Y$
(12) $\hat{f}_{\hat{\mu},\text{nonpar}}$	0.0023(1)	0.0019(1)	0.00023(1)	7.4e-05(1)	0.00015(1)
(13) $\hat{f}_{\mu,\xi}$	0.0033(1.4)	0.0029(1.5)	$0.00022 \ (0.93)$	0.00013(1.8)	5.7e-05 (0.38)
(14) $\hat{f}_{\mu,\hat{\xi}}$	0.0097(4.1)	0.0069(3.7)	0.00084(3.6)	0.00053 (7.2)	0.0014 (9.5)
(15) $\hat{f}_{\hat{\mu},\mathrm{par}}$	0.0065(2.8)	0.0045(2.4)	0.00037(1.6)	0.0012(17)	0.00036(2.4)
(20) $f_{\hat{\mu}, \underset{\downarrow}{\text{nonpar}}}^{\dagger}$	0.0037(1.6)	0.0032(1.7)	$0.00016 \ (0.68)$	0.00011 (1.5)	0.00022 (1.5)
$(21) f_{\mu,\xi}^{\dagger}$	0.00088 (0.37)	$0.00048 \ (0.25)$	$0.00021\ (0.9)$	0.00013(1.8)	5.6e-05 (0.37)
$(22) f_{\mu,\hat{\mathcal{E}}}^{\dagger,\varsigma}$	0.012(5)	0.0088(4.7)	0.0011 (4.6)	0.00045 (6.1)	0.0013 (8.7)
(23) $f_{\hat{\mu}, \text{par}}^{\dagger}$	0.0078(3.3)	0.006(3.2)	0.00035 (1.5)	0.0011(15)	0.00034(2.3)
(25) $f_{\hat{\omega},\text{nonpar}}^{\dagger}$	0.0015 (0.64)	$0.00084 \ (0.45)$	$0.00021 \ (0.91)$	0.00034(4.6)	$0.00011 \ (0.74)$
(26) $f_{\hat{\omega}, par}^{\dagger}$	0.0091(3.9)	0.0065 (3.5)	0.00042(1.8)	0.0016(21)	0.00053(3.5)
(4) p	0.041(17)	0.024(13)	0.0081(35)	0.00078(11)	0.0075(50)
f	0 (0)	0 (0)	0 (0)	0 (0)	0 (0)
(hat25) $\hat{f}_{\hat{\omega},\text{nonpar}}$	0.0046(2)	0.0039(2.1)	3e-04 (1.3)	0.00034(4.6)	1e-04 (0.7)
(hat26) $\hat{f}_{\hat{\omega},par}$	0.0079(3.4)	0.0051(2.7)	0.00045(1.9)	0.0017(24)	0.00054(3.6)
$\hat{\mu}$ , nonpar	0.008(3.4)	0.0046(2.4)	0.00082(3.5)	0.00018(2.5)	0.0023(16)
$\mu, \xi$	0 (0)	0 (0)	0 (0)	0 (0)	0 (0)
$\mu,\hat{\xi}$	0.061(26)	0.0027(1.4)	0.00063(2.7)	0.00015(2.1)	0.057(380)
$\hat{\mu}$ , par	0.14(58)	0.00083 (0.44)	0.00036(1.5)	0.0031(42)	0.13(870)
$\hat{\omega}$ , nonpar	0.0046(2)	$0.00016 \ (0.088)$	$0.00017 \ (0.74)$	0.00027(3.7)	0.004(27)
$\hat{\omega}, \mathrm{par}$	2.2 (920)	0.00091 (0.48)	0.00048 (2)	0.0044 (59)	2.2 (14000)

Table 3: Model 3

Estimator	IMSE	IMSE   $Y < q_{.25}$	IMSE   $q_{.25} < Y < q_{.5}$	IMSE   $q_{.5} < Y < q_{.75}$	IMSE   $q_{.75} < Y$
$\hat{f}_{\hat{\mu},  ext{nonpar}}$	0.00213(1)	0.000524(1)	0.000738(1)	0.000653(1)	0.000219(1)
$\hat{f}_{\mu,\xi}$	0.12(56.4)	$0.0213 \ (40.6)$	0.0408 (62.5)	0.0393(180)	0.019(25.8)
$\hat{f}_{\mu,\hat{\xi}}$	0.12 (56.4)	0.0213 (40.6)	0.0408 (186)	0.0393 (53.3)	0.019(29.1)
$\hat{f}_{\hat{\mu}, \mathrm{par(rough)}}$	113 (52900)	113 (215000)	0.0243 (111)	$0.0165\ (25.3)$	0.00301 (4.08)
$\hat{f}_{\hat{\mu},\mathrm{par}}$	$0.0291\ (13.6)$	0.00376 (17.1)	0.0165 (31.5)	$0.00763\ (10.3)$	0.00125 (1.91)
$ ilde{f}_{\hat{\mu},  ext{nonpar}}$	1.09(509)	0.018(24.4)	0.0314(60)	0.235 (1070)	0.802(1230)
$ ilde{f}_{\mu,\xi}$	$0.0591\ (27.7)$	0.016 (30.6)	0.0292 (133)	$0.0127\ (17.1)$	0.00124 (1.89)
$ ilde{f}_{\mu,\hat{\mathcal{E}}}$	$0.0591\ (27.7)$	0.016 (73.1)	0.0292 (39.5)	0.0127 (19.4)	0.00124 (2.36)
$\tilde{f}_{\hat{\mu}, \mathrm{par(rough)}}$	113 (52900)	113 (173000)	0.0243 (46.4)	0.0165 (75.4)	0.00301 (4.08)
$ ilde{f}_{\hat{\mu},\mathrm{par}}$	0.0429 (20.1)	0.0065 (8.8)	0.0215(33)	0.0122 (23.2)	0.00274 (12.5)
$f_{\hat{\mu}, \mathrm{nonpar}}^{\dagger}$	0.187 (87.8)	0.0198(37.8)	0.0373 (57.2)	0.0226 (103)	0.108(146)
$f_{\mu,\varepsilon}^{\dagger}$	1210000 (5.69e+08)	10600 (20200000)	$27200 \ (1.24e+08)$	372000 (5.03e+08)	805000 (1.23e+09
$f^\dagger_{\mu,\xi} \ f^\dagger_{\mu,\hat{\xi}}$	1210000 (5.69e+08)	10600 (48300000)	27200 (51900000)	372000 (5.03e+08)	805000 (1.23e+09
$f_{\hat{\mu}, \text{par(rough)}}^{\dagger}$	161 (75200)	139 (266000)	2.68 (12200)	8.28 (11200)	$10.1\ (15400)$
$f_{\hat{\mu},\mathrm{par}}^{\dagger}$	$0.0227\ (10.6)$	0.00146 (2.79)	0.00727 (33.2)	$0.00674\ (10.3)$	0.00721 (9.77)
$f_{\hat{\omega}, \text{nonpar}}^{\dagger}$	0.211 (98.9)	0.0193 (88.1)	$0.0364 \ (49.3)$	0.0206 (39.3)	0.135 (206)
$f_{\hat{\omega},\mathrm{par}}^{\dagger}$	0.0236(11)	0.00129(1.75)	$0.00721\ (13.8)$	0.00712(32.5)	0.00795 (12.2)
p	$0.0591\ (27.7)$	0.016 (30.6)	0.0292 (133)	0.0127(17.1)	0.00124 (1.89)
$\hat{f}_{\hat{\omega},  ext{nonpar}}$	0.126 (58.9)	0.0216 (41.2)	0.0415 (189)	0.0414 (56.1)	0.0213 (32.6)
$\hat{f}_{\hat{\omega},\mathrm{par}}$	0.0285(13.4)	0.00381 (17.4)	$0.0162\ (21.9)$	0.00727 (13.9)	0.00126 (1.93)
$ ilde{f}_{\hat{\omega}_2 ext{nonpar}}$	0.772(362)	0.0174(33.2)	0.0322(147)	0.0207 (28.1)	0.702 (1070)
$\widetilde{f}_{\hat{\omega},\mathrm{par}}$	0.0429 (20.1)	$0.00676 \ (12.9)$	0.0216 (29.2)	0.0119 (18.3)	0.00265 (12.1)

Table 4: Model 4

Estimator	IMSE	$\mathrm{IMSE} \mid Y {<} q_{.25}$	IMSE   $q_{.25} < Y < q_{.5}$	IMSE   $q_{.5} < Y < q_{.75}$	IMSE   $q_{.7}$
(12) $\hat{f}_{\hat{\mu},\text{nonpar}}$	0.0028 (1)	0.00046 (1)	0.00057 (1)	0.00058 (1)	0.0012 (
$(13) \hat{f}_{\mu,\xi}$	8.5e+45 (3e+48)	9.4e+44 (2e+48)	$2.6e+45 \ (4.6e+48)$	2.9e+45 (5e+48)	2.1e+45 (1.7)
(14) $\hat{f}_{\mu,\hat{\xi}}$	3.1e+46 (1.1e+49)	2.7e+45 (5.8e+48)	8.8e+45 (1.5e+49)	$1.1e+46 \ (1.8e+49)$	8.9e + 45 (7.4)
(15) $\hat{f}_{\hat{\mu},\mathrm{par}}$	0.0032(1.2)	0.00049(1.1)	0.00068(1.2)	0.00053 (0.91)	0.0016 (1
(20) $f_{\hat{\mu},\text{nonpar}}^{\dagger}$	0.003 (1.1)	0.00068 (1.5)	$0.00052 \ (0.92)$	0.00067(1.2)	0.0011 (0.
$(21) f_{\mu,\xi}^{\dagger}$	$0.0026 \ (0.94)$	$0.00043 \ (0.93)$	$0.00054 \ (0.94)$	0.00055 (0.95)	0.0011 (0.
$(22) f^{\dagger}_{\mu,\hat{\xi}}$	0.0027 (0.96)	0.00046 (1)	$0.00054 \ (0.95)$	$0.00056 \ (0.96)$	0.0012 (0.
$(23) f_{\hat{\mu}, \text{par}}^{\dagger}$	$0.0027 \ (0.96)$	0.00046(1)	$0.00054 \ (0.95)$	$0.00056 \ (0.97)$	0.0012 (0.
(25) $f_{\hat{\omega},\text{nonpar}}^{\dagger}$	0.003(1.1)	7e-04 (1.5)	$0.00051 \ (0.89)$	0.00065(1.1)	0.0011 (0.
(26) $f_{\hat{\omega}, par}^{\dagger}$	0.0027 (0.96)	0.00046 (1)	$0.00054 \ (0.95)$	$0.00056 \ (0.96)$	0.0012 (0.
(4) p	0.016(5.8)	0.008 (17)	0.00077(1.4)	0.0035(6.2)	0.004 (3.
f	$0 \ (0)$	0 (0)	0 (0)	0 (0)	0(0)
(hat25) $\hat{f}_{\hat{\omega},\text{nonpar}}$	0.0027 (0.96)	0.00047(1)	$0.00054 \ (0.94)$	$0.00054 \ (0.95)$	0.0012 (0.
(hat26) $\hat{f}_{\hat{\omega}, par}$	0.0032(1.1)	0.00048 (1)	0.00067(1.2)	$0.00052 \ (0.91)$	0.0015(1
$\hat{\mu},  ext{nonpar}$	$0.00043 \ (0.15)$	$0.00041 \ (0.89)$	2.1e-06 (0.0037)	2e-06 (0.0035)	9.8e-06 (0.0
$\mu, \xi$	0 (0)	0 (0)	0 (0)	0 (0)	0(0)
$\mu,\hat{\xi}$	0.0012 (0.43)	0.0012(2.5)	$3e-05 \ (0.053)$	$1.4e-05 \ (0.024)$	1.1e-05 (0.0
$\hat{\mu}$ , par	0.00017(0.06)	0.00017(0.36)	7.4e-07 (0.0013)	$3.1e-07 \ (0.00054)$	3.1e-07 (0.0
$\hat{\omega},  ext{nonpar}$	$0.0012 \ (0.42)$	0.0012(2.5)	4e-06 (0.007)	8.1e-07 (0.0014)	6.3e-06 (0.0
$\hat{\omega}$ , par	$0.00016 \ (0.056)$	$0.00016 \ (0.34)$	7.7e-07 (0.0013)	$3.2e-07 \ (0.00055)$	3.1e-07 (0.0

Table 5: Model 5

Estimator	IMSE	IMSE   $Y < q_{.25}$	IMSE   $q_{.25} < Y < q_{.5}$	IMSE   $q_{.5} < Y < q_{.75}$	IMSE   $q_{.75} < Y$
(12) $\hat{f}_{\hat{\mu},\text{nonpar}}$	0.0011(1)	0.00012(1)	2e-04 (1)	0.00023(1)	0.00052(1)
(13) $\hat{f}_{\mu,\xi}$	0.0016(1.5)	0.00015(1.2)	0.00027(1.3)	9.1e-05 (0.39)	0.0011(2.1)
(14) $\hat{f}_{\mu,\hat{\xi}}$	0.0018(1.7)	0.00019(1.6)	0.00029(1.4)	$9.7e-05 \ (0.42)$	0.0012(2.3)
(15) $\hat{f}_{\hat{\mu},\mathrm{par}}$	0.0017(1.6)	0.00023(1.9)	4e-04 (1.9)	$0.00014 \ (0.59)$	0.00098(1.9)
(20) $f_{\hat{\mu},\text{nonpar}}^{\dagger}$	0.0015(1.4)	0.00043 (3.5)	$0.00015 \ (0.73)$	0.00041 (1.8)	$0.00051 \ (0.99)$
$(21) f_{\mu,\xi}^{\dagger}$	$0.00094 \ (0.87)$	9.8e-05 (0.81)	$0.00018 \ (0.86)$	$0.00021\ (0.9)$	$0.00045 \ (0.87)$
(22) $f_{\mu,\hat{\xi}}^{\dagger,\hat{\zeta}}$	$0.001\ (0.96)$	$0.00012 \ (0.99)$	$0.00019 \ (0.94)$	$0.00021 \ (0.91)$	$0.00051 \ (0.98)$
(23) $f_{\hat{\mu}, \text{par}}^{\dagger}$	$0.001 \ (0.94)$	0.00013(1)	0.00019 (0.91)	$0.00022 \ (0.95)$	$0.00048 \ (0.93)$
(25) $f_{\hat{\omega},\text{nonpar}}^{\dagger}$	0.0015(1.4)	0.00046 (3.8)	$0.00014 \ (0.69)$	4e-04 (1.7)	$5e-04 \ (0.97)$
(26) $f_{\hat{\omega}, \text{par}}^{\dagger}$	$0.001 \ (0.93)$	0.00012(1)	0.00018 (0.89)	0.00022 (0.94)	0.00048 (0.92)
(4) p	0.015(14)	0.0072(59)	0.00052(2.6)	0.0033(14)	0.0037(7.1)
f	0 (0)	0 (0)	0 (0)	0 (0)	0 (0)
(hat25) $\hat{f}_{\hat{\omega},\text{nonpar}}$	0.001 (0.96)	0.00014(1.2)	$0.00019 \ (0.94)$	0.00022 (0.97)	$0.00048 \ (0.92)$
(hat26) $\hat{f}_{\hat{\omega},par}$	0.0017(1.6)	0.00023(1.9)	0.00039(1.9)	$0.00013 \ (0.57)$	0.00097(1.9)
$\hat{\mu}$ , nonpar	$0.00041 \ (0.38)$	0.00039(3.2)	$2.7e-06 \ (0.013)$	$2.8e-06 \ (0.012)$	1e-05 (0.02)
$\mu, \xi$	0 (0)	0 (0)	0 (0)	0 (0)	0 (0)
$\mu,\hat{\xi}$	0.00089(0.83)	0.00086(7)	2.1e-05 (0.1)	$9.2e-06 \ (0.04)$	$7.1e-06 \ (0.014)$
$\hat{\mu}, \mathrm{par}$	0.00016 (0.15)	0.00016(1.3)	$7.7e-07 \ (0.0038)$	$3.3e-07 \ (0.0014)$	$3.2e-07 \ (0.00061)$
$\hat{\omega}$ , nonpar	0.0014(1.3)	0.0014(12)	$4.5e-06 \ (0.022)$	$8.1e-07 \ (0.0035)$	$5.4e-06 \ (0.01)$
$\hat{\omega}$ , par	$0.00015 \ (0.14)$	0.00015 (1.2)	8e-07 (0.0039)	$3.3e-07 \ (0.0014)$	3.1e-07 (6e-04)