# Daniel Brosch

# Curriculum Vitae

# Personal Details

Date of birth November 18, 1996

Place of birth Leverkusen, Germany

Citizenship German

## PhD-Thesis

title Symmetry Reduction in Convex Optimization with Applications in

Combinatorics

main supervisor Etienne de Klerk

co-supervisor Monique Laurent

summary We explore different approaches to and applications of symmetry re-

duction in convex optimization. Using tools from semidefinite programming, representation theory and algebraic combinatorics, we solve or bound hard problems coming from combinatorial optimization, energy

minimization, queuing theory, and extremal combinatorics.

scheduled defense October 19, 2022.

date

#### Education

September 2022 - Senior Scientist, Dept. of Mathematics, AAU, Austria

2018–2022 **PhD-candidate**, *Tilburg University*, the Netherlands

Under supervision of Etienne de Klerk and Monique Laurent, as early stage

researcher of the Marie-Curie innovative training network MINOA.

January 2020 - **Secondment**, Centrum Wiskunde & Informatica, Amsterdam, the

March 2020 Netherlands

October 2019 - **Secondment**, *Ortec*, Zoetermeer, the Netherlands

December 2019

November 2022

2017–2018 Mathematics MSc, University of Cologne, cum laude

Thesis: Semidefinite Bounds for Unequal Error Protection Codes, under

supervision of Frank Vallentin.

- 2015–2017 **Mathematics BSc**, *University of Cologne*, *cum laude*Thesis: *The Banach-Tarski Paradox*, under supervision of *Alexander Lytchak*.
- 2012–2015 **Project**, *Schülerinnen und Schüler an der Universität*, University of Cologne

Project that allowed me to attend university early in parallel to high school.

2008–2015 **Abitur**, *Otto-Hahn-Gymnasium*, Monheim am Rhein Abitur in Mathematics, Physics, Latin, Philosophy

# **Papers**

## Accepted

- Jordan symmetry reduction for conic optimization over the doubly nonnegative cone: theory and software, Optimization Methods and Software, joint work with Etienne de Klerk, https://doi.org/10.1080/10556788.2021.2022146

  We extend the Jordan Reduction method to the doubly nonnegative cone, and describe a Julia software package implementing it.
- Optimizing hypergraph-based polynomials modeling joboccupancy in queueing with redundancy scheduling, SIAM Journal on Optimization, joint work with Monique Laurent and Andries Steenkamp, https://doi.org/10.1137/20M1369592

  We show that a family of highly symmetric polynomials is convex, thus (partially) solving a problem coming from queueing with redundancy scheduling. To do this, we exploit the symmetries of the Hessians of the polynomials algebraically.
- Minimum energy configurations on a toric lattice as a quadratic assignment problem, Discrete Optimization, joint work with Etienne de Klerk, https://doi.org/10.1016/j.disopt.2020.100612 We bound the potential energy of charged particles on an infinite, periodic grid from below, using semidefinite programming and symmetry reduction based on the Jordan Reduction method.

### **Preprints**

New lower bounds on crossing numbers of  $K_{m,n}$  from permutation modules and semidefinite programming, joint work with  $Sven\ Polak$ , https://arxiv.org/abs/2206.02755 We symmetry reduce SDP-based bounds for the crossing number of complete bipartite graphs, and improve bounds both in the finite case and in the limit. We also introduce a new, slightly weaker, but computationally more efficient bound for the crossing number of  $K_{m,n}$ , allowing us to compute bounds for bigger parameters m and n.

## Work in progress

#### 2020- More efficient and flexible Flag-SOS hierarchies

We exploit the symmetries of the SOS and moment hierarchies fully for the class of  $S_n$ -invariant polynomials over the k-subset-hybercube. This leads to computationally more efficient hierarchies equivalent to Razborov's Flag-SOS hierarchies, and extends their use case to finite and degenerate problems.

#### Software

#### 2021 SDPSymmetryReduction.jl

Julia package for automatic symmetry reduction of SDPs using the Jordan Reduction method. Available at https://github.com/DanielBrosch/SDPSymmetryReduction.jl

# Work in Progress

#### 2021- FlagSOS.jl

Extendable Julia package for solving fully symmetry-reduced Flag-SOS problems for a variety of combinatorial objects.

# Programming Knowledge

Well familiar with Julia, C/C++, Python, Java and Matlab. Some experience with SageMath, Javascript and C#.

# **Teaching**

Summer semester Linear Algebra for Data Science

2022 Tutorials

Winter semester Linear Optimization

2021-2022 Tutorials and computer labs

#### Talks

July 26, 2022 ICCOPT, Betlehem, PA, USA

Moebius-Transformation Based Symmetry Reduction for Optimization in Binary Variables.

April 12, 2022 Workshop on Conic Linear Optimization for Computer-Assisted Proofs, Oberwolfach

The Symmetries of Flag-Algebras.

April 1, 2022 **Discrete Math Seminar**, University of Massachusetts Amherst Symmetry reduced Flag-hierarchies.

March 23, 2022	<b>Polynomial optimization reading group</b> , CWI, Amsterdam Symmetry reduced Flag-hierarchies.
August 20, 2021	SIAM AG21
	More efficient and flexible Flag-Algebras coming from polynomial optimiza-
Luly 20, 22, 2021	tion. SIAM OP21
July 20–23, 2021	More efficient and flexible Flag-Algebras coming from polynomial optimiza-
	tion.
February 2021	Virtual OR seminar, Tilburg University
	More efficient and flexible Flag-Algebras.
January 2021	<b>Oberseminar</b> <i>Reelle Geometrie und Algebra</i> , Uni Konstanz More efficient and flexible Flag-Algebras.
January 2021	Shared seminar Cologne Oberseminar/CWI reading group More efficient and flexible Flag-Algebras.
February 26 2020	Polynomial optimization reading group, CWI, Amsterdam
	A two-part introduction to symmetry reduction for SDPs
	ICCOPT, Berlin
G	Minimum energy configurations on a toric lattice as a quadratic assignment problem.
	Conferences/Workshops/Summer Schools/Courses
September 5–9.	, - , , , , , , , , , , , , , , , , , ,
September 5–9, 2022	Conferences/Workshops/Summer Schools/Courses Final POEMA workshop, Paris
2022	, - , , , , , , , , , , , , , , , , , ,
2022 July 23–28, 2022	Final POEMA workshop, Paris
2022 July 23–28, 2022 June 7–9, 2022	Final POEMA workshop, Paris  ICCOPT, Betlehem, PA, USA
2022 July 23–28, 2022 June 7–9, 2022 April 10–15, 2022	Final POEMA workshop, Paris  ICCOPT, Betlehem, PA, USA  Nordic Combinatorial Conference (NORCOM), Tromsø  Workshop on Conic Linear Optimization for Computer-Assisted
2022 July 23–28, 2022 June 7–9, 2022 April 10–15, 2022	Final POEMA workshop, Paris  ICCOPT, Betlehem, PA, USA  Nordic Combinatorial Conference (NORCOM), Tromsø  Workshop on Conic Linear Optimization for Computer-Assisted  Proofs, Oberwolfach
2022 July 23–28, 2022 June 7–9, 2022 April 10–15, 2022  June 21–29, 2021 April 16, 2021	Final POEMA workshop, Paris  ICCOPT, Betlehem, PA, USA  Nordic Combinatorial Conference (NORCOM), Tromsø  Workshop on Conic Linear Optimization for Computer-Assisted  Proofs, Oberwolfach  MINOA Doctoral School 2021, Online
2022 July 23–28, 2022 June 7–9, 2022 April 10–15, 2022  June 21–29, 2021 April 16, 2021 March 4–5, 2021	Final POEMA workshop, Paris  ICCOPT, Betlehem, PA, USA  Nordic Combinatorial Conference (NORCOM), Tromsø  Workshop on Conic Linear Optimization for Computer-Assisted Proofs, Oberwolfach  MINOA Doctoral School 2021, Online  General Julia training (POEMA), Online
2022 July 23–28, 2022 June 7–9, 2022 April 10–15, 2022  June 21–29, 2021 April 16, 2021 March 4–5, 2021	Final POEMA workshop, Paris  ICCOPT, Betlehem, PA, USA  Nordic Combinatorial Conference (NORCOM), Tromsø  Workshop on Conic Linear Optimization for Computer-Assisted Proofs, Oberwolfach  MINOA Doctoral School 2021, Online  General Julia training (POEMA), Online  Second MINOA ESR days, Online
2022 July 23–28, 2022 June 7–9, 2022 April 10–15, 2022  June 21–29, 2021 April 16, 2021 March 4–5, 2021 March 1–3, 2021	Final POEMA workshop, Paris  ICCOPT, Betlehem, PA, USA  Nordic Combinatorial Conference (NORCOM), Tromsø  Workshop on Conic Linear Optimization for Computer-Assisted Proofs, Oberwolfach  MINOA Doctoral School 2021, Online  General Julia training (POEMA), Online  Second MINOA ESR days, Online  Annual MINOA Conference 2021, Online
2022 July 23–28, 2022 June 7–9, 2022 April 10–15, 2022  June 21–29, 2021 April 16, 2021 March 4–5, 2021 March 1–3, 2021 January–March 2021 December 1, 2020	Final POEMA workshop, Paris  ICCOPT, Betlehem, PA, USA  Nordic Combinatorial Conference (NORCOM), Tromsø  Workshop on Conic Linear Optimization for Computer-Assisted Proofs, Oberwolfach  MINOA Doctoral School 2021, Online  General Julia training (POEMA), Online  Second MINOA ESR days, Online  Annual MINOA Conference 2021, Online  POEMA 3 <sup>rd</sup> Workshop, Online  Complementary Skills Session on intellectual property rights,

May 27–	POEMA Online Learning Weeks, Online
September 16, 2020	
January 6–10, 2020	2 <sup>nd</sup> MINOA conference, Aussois, France
January 6–10, 2020	24 <sup>th</sup> Workshop on Combinatorial Optimization, Aussois, France
September 9–	Interior Point Methods, LNMB PhD Course, Etienne de Klerk,
November 11, 2019	Utrecht, the Netherlands
August 5–8, 2019	<b>6</b> <sup>th</sup> International Conference on Continuous Optimization (IC-COPT), Berlin, Germany
June 24–28, 2019	${f 1}^{ m st}$ MINOA PhD school, Mixed-Integer Nonlinear Optimization meets Data Science , Ischia, Italy
January 14–16, 2019	1 <sup>st</sup> MINOA conference, Aussois, France
January 14–16, 2019	23 <sup>rd</sup> Workshop on Combinatorial Optimization, Aussois, France
January 7-11, 2019	$44^{\text{th}}$ conference on the mathematics of operations research, Lunteren, the Netherlands
	<b>Networks and Semidefinite Programming</b> , <i>LNMB PhD Course</i> , Monique Laurent, Utrecht, the Netherlands
2019-Present	<b>CWI reading group on polynomial optimization</b> , hosted by Monique Laurent and Sven Polak, CWI, Amsterdam
2020-Present	Oberseminar, hosted by Frank Vallentin, Cologne

Last updated on September 20, 2022.