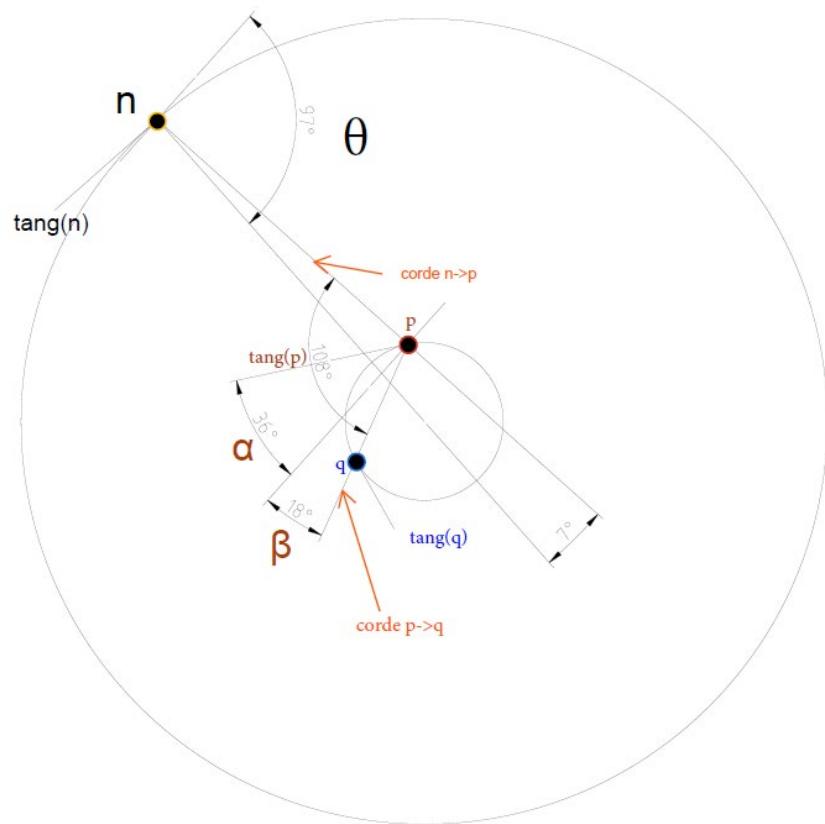


# Dyadic Phase Transport in Semiprime Integers

## 1. Dataset and scope

We analyze a dataset of **500,000 semiprime integers**  $n = pq$ , restricted to the **64-bit regime**, where  $p$  and  $q$  are prime factors, started with this conceptual's representation show bellow.



For each triplet  $(n, p, q)$ , the dataset contains:

- the dyadic level  $k_x = \lfloor \log_2 x \rfloor$ ,
- angular quantities  $\theta_n, \theta_{p_{\min}}$ ,
- and a normalized intra-dyadic imbalance flag allowing identification of the smaller and larger factor.

All arithmetic relations were validated:

- $n = pq$  holds for 100% of entries,
- both factors are prime,
- dyadic levels match bit-length definitions exactly.

This ensures that all observed effects are **structural**, not artefacts of corrupted data.

## 2. Phase composition hypothesis

Let us associate to each integer  $x$  an angular quantity  $\theta_x \in [0, 2\pi)$ , interpreted as a *phase coordinate* on its dyadic circle.

We test the hypothesis that the phase of a semiprime integer is governed by a **composition law** of the phases of its prime factors:

$$\theta_n \approx \text{wrap}_{2\pi}(\theta_p + \theta_q)$$

This relation is **not imposed** by construction:

we previously verified that  $\theta_n$  is neither the trivial fractional logarithmic phase of  $n$ , nor a local geometric angle derived from the direct chord  $n \rightarrow p$ .

## 3. Empirical phase alignment

Define the residual phase error:

$$\delta = \text{wrap}_\pi(\theta_n - (\theta_p + \theta_q))$$

Over the full dataset, we observe:

- mean absolute error:

$$\langle |\delta| \rangle \approx 0.162 \text{ rad}$$

- median absolute error:

$$\text{median}(|\delta|) \approx 0.124 \text{ rad}$$

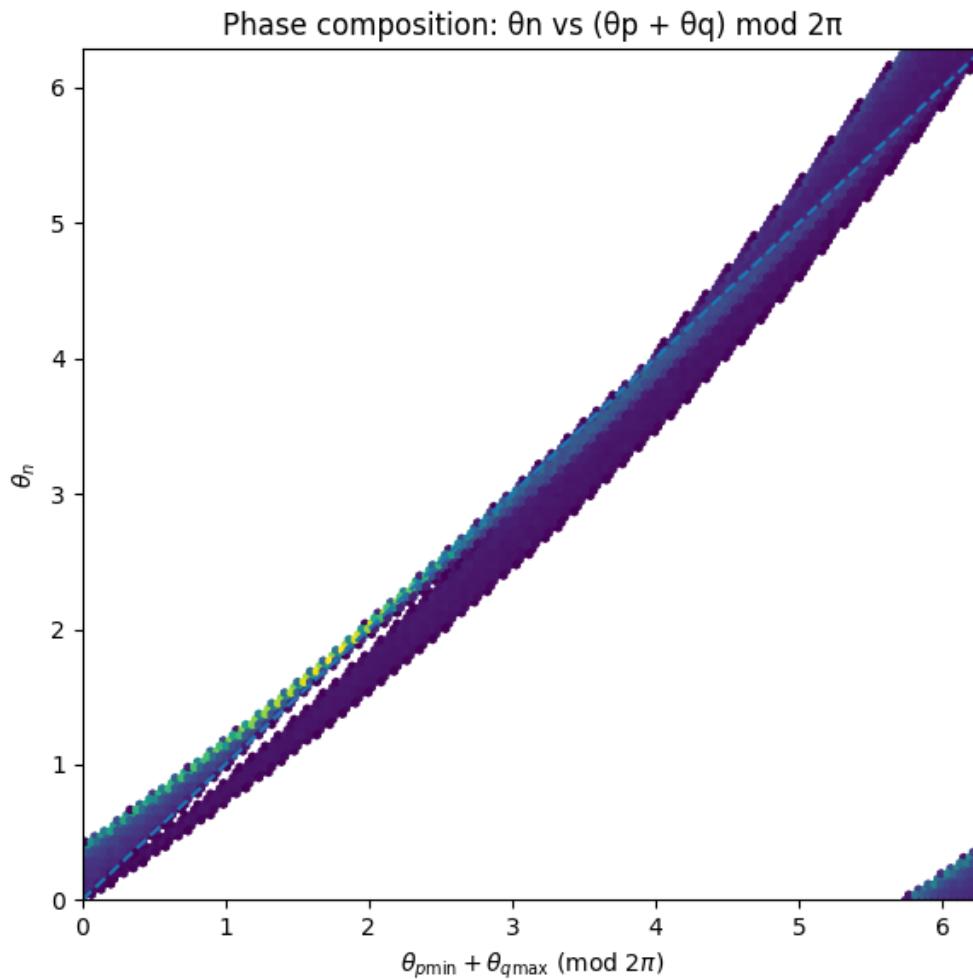
- 90th percentile:

$$P_{90}(|\delta|) \approx 0.374 \text{ rad}$$

The signed residual is centered near zero:

$$\mathbb{E}[\delta] \approx 0.014 \text{ rad}$$

This demonstrates a **strong phase alignment** between  $\theta_n$  and the composed phase  $\theta_p + \theta_q$ , with no systematic angular bias.



*Fig1. Phase of Phase of semiprime integers versus the composed phase of their prime factors. Each point represents a semiprime  $n=pq$ . The horizontal axis shows the composed phase  $(\theta_{p\min}+\theta_{q\max})\bmod 2\pi$ , while the vertical axis shows  $\theta_n$ . The clear alignment along the diagonal indicates that the phase of a semiprime is strongly governed by the sum of the phases of its prime factors.*

#### 4. Dyadic carry bifurcation

When both prime factors lie in the same dyadic band  $k_p = k_q = k$ , the product satisfies:

$$\log_2 n = 2k + (u_p + u_q)$$

leading to two possible dyadic levels:

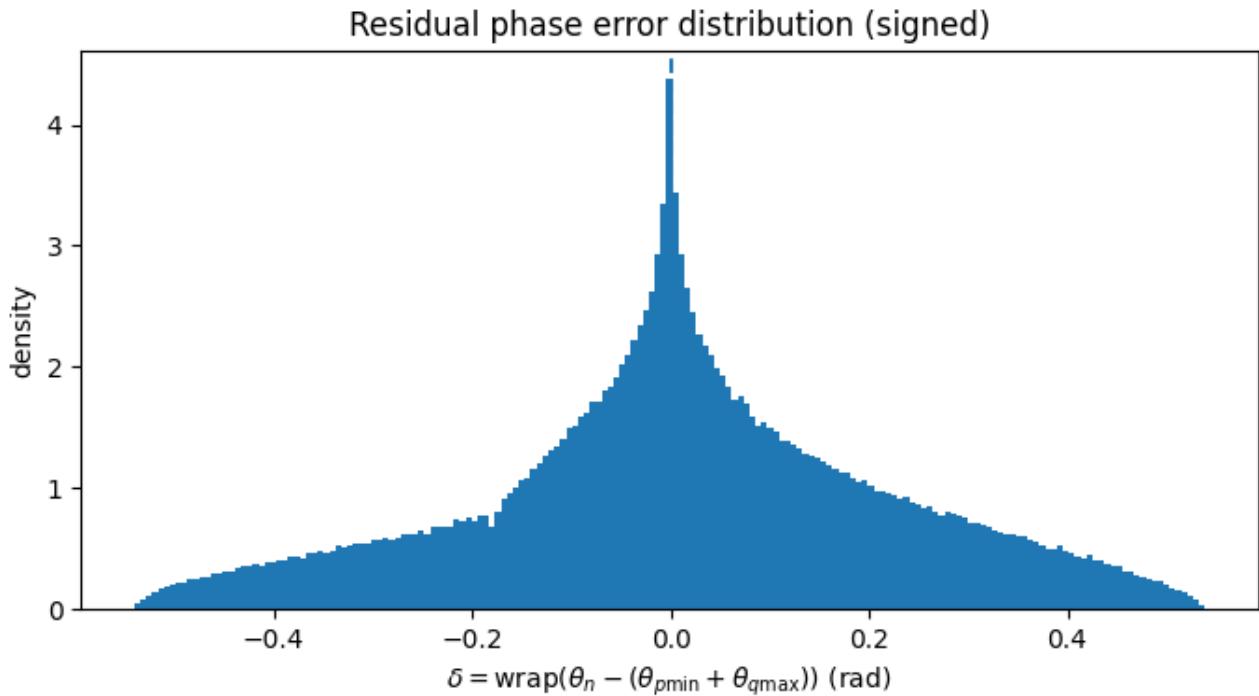
$$k_n \in \{2k, 2k + 1\}$$

Segmenting the dataset accordingly yields:

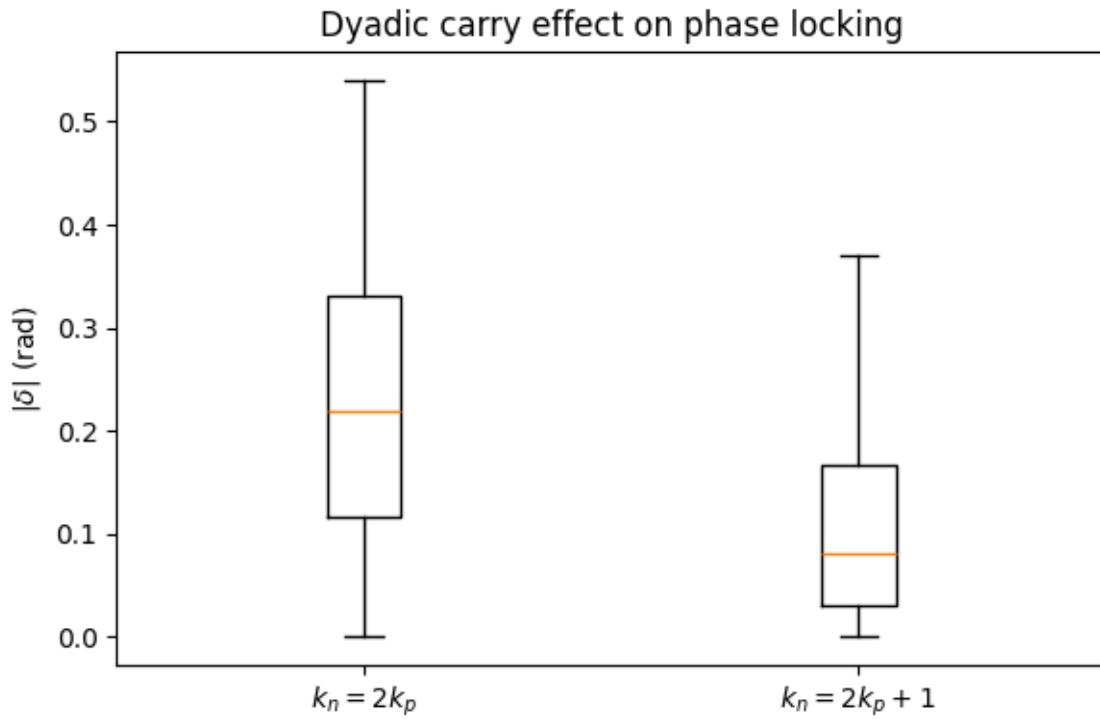
Dyadic case	median	$\delta$	mean	$\delta$
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$k_n = 2k$	$\sim 0.218$ rad	$\sim 0.228$ rad		
$k_n = 2k + 1$	$\sim 0.081$ rad	$\sim 0.120$ rad		

The **carry case**  $k_n = 2k + 1$  exhibits a **significantly tighter phase locking**.

This establishes that **dyadic carry is not a passive arithmetic effect**, but directly influences angular transport.



*Fig2 Distribution of the signed residual phase error. The histogram shows  $\delta = \text{wrap}(\theta_n - (\theta_{p\min} + \theta_{q\max}))$ . The distribution is centered near zero with finite dispersion, indicating unbiased but non-exact phase transport from the factors to the semiprime.*



*Fig3 Effect of dyadic carry on phase locking. Boxplots of the absolute residual  $|\delta|$  are shown for two dyadic cases:  $k_n=2kp$  (no carry) and  $k_n=2kp+1$  (carry). The carry case exhibits significantly tighter phase alignment, demonstrating that dyadic sca*

## 5. Dependence on factor imbalance

Define the intra-dyadic imbalance:

$$\Delta u = |u_p - u_q| \text{ with } u_x = \log_2 x - \lfloor \log_2 x \rfloor$$

We observe a strong monotonic relationship between phase error and imbalance:

- Pearson correlation:

$$\text{corr}(|\delta|, \Delta u) \approx 0.374$$

Binned medians show a clear increase:

$ \Delta u $ range	median $ \delta $
$[0.0 - 0.1]$	$\sim 0.12$ rad
$[0.4 - 0.5]$	$\sim 0.13$ rad
$[0.6 - 0.7]$	$\sim 0.19$ rad
$[0.8 - 0.9]$	$\sim 0.37$ rad
$[0.9 - 1.0]$	$\sim 0.47$ rad

Thus:

- **balanced factors** ( $u_p \approx u_q$ ) yield strong phase coherence,
- **unbalanced factors** lead to progressive phase dispersion.

## 6. Canonical formulation

The observed behavior is compactly summarized by:

$$\boxed{\theta_n = \theta_p + \theta_q + \varepsilon(\Delta u, \text{carry})}$$

where:

- $\varepsilon \rightarrow 0$  as  $\Delta u \rightarrow 0$ ,
- $|\varepsilon|$  increases monotonically with factor imbalance,
- the dyadic carry case  $k_n = 2k + 1$  minimizes  $|\varepsilon|$ .

This defines a **dyadic phase transport law** for semiprime integers.

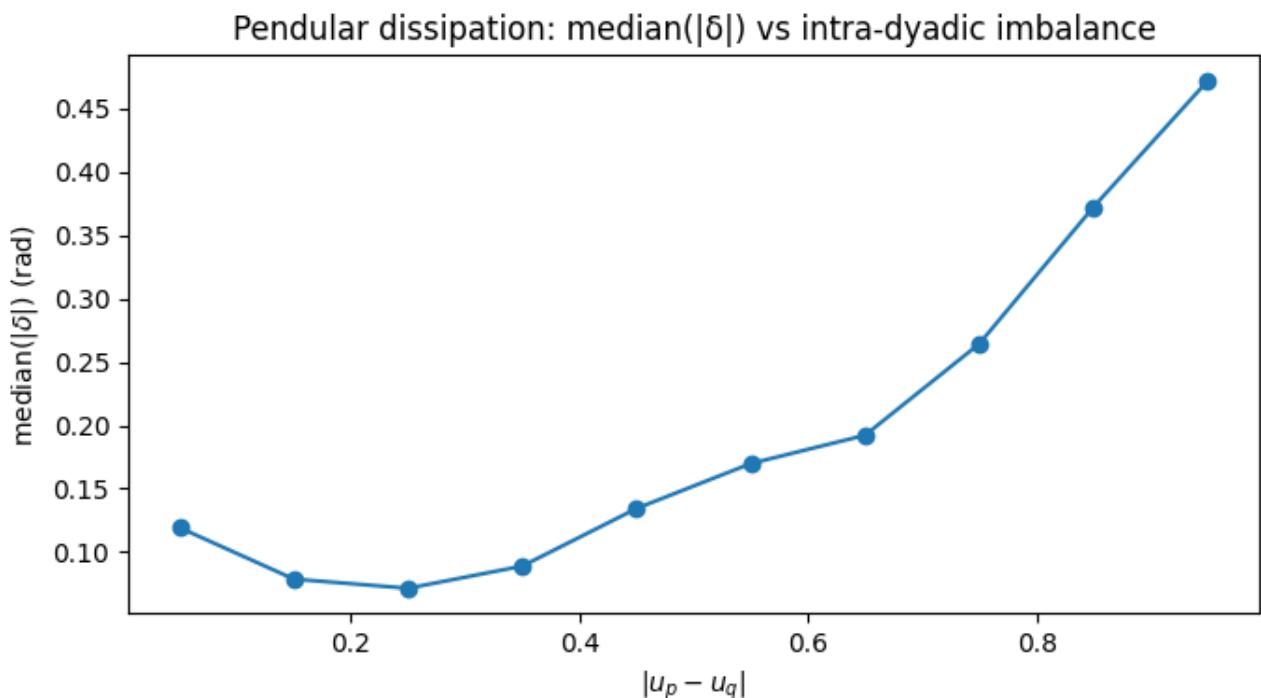


Fig4 Phase dispersion as a function of intra-dyadic factor imbalance. The plot shows the median absolute residual median( $|\delta|$ ) as a function of the imbalance  $|u_p - u_q|$ , where  $ux = \log_2(x) - \lfloor \log_2(x) \rfloor$ . Phase dispersion increases monotonically with factor imbalance, revealing a pendular dissipation law: balanced factors yield strong phase coherence, while unbalanced factors progressively weaken phase locking.

## 7. Interpretation (kept deliberately minimal)

These results show that:

- multiplication of integers induces a **non-local angular structure**,
- semiprimes inherit a **composed phase** from their factors,
- dyadic scaling governs the stability of this transport.

No appeal is made here to analytic continuation, zeta functions, or spectral conjectures.

The phenomenon is **empirical, geometric, and reproducible**.