

Modeling the Tournament of Officials

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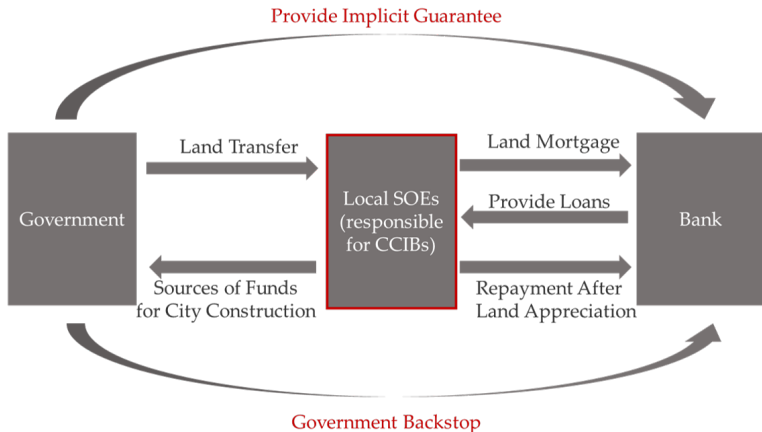
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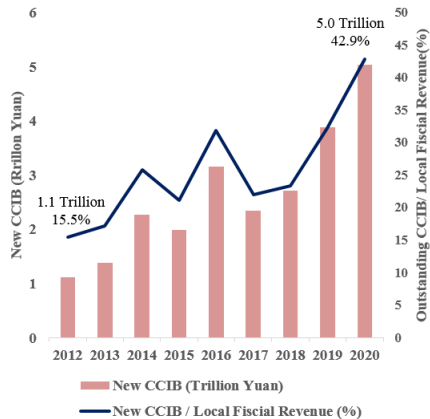
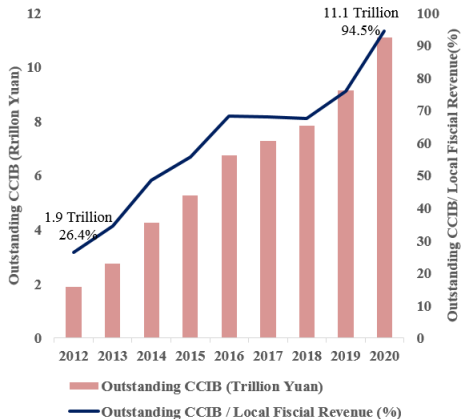
Overview

- 1 Question: Why Local Governments Borrow so Much?
 - Facts
 - Theories
- 2 Xiong (2018): The Mandarin Model of Growth
 - Model Setup
 - Selfish Official: Underinvestment
 - Overcome Underinvestment Problem by Tournament
 - Problem: Excessive Leverage
- 3 Discussion

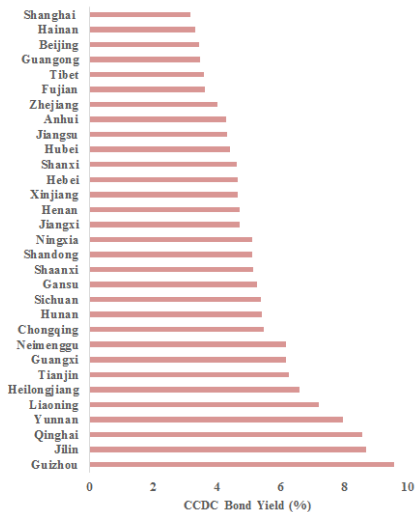
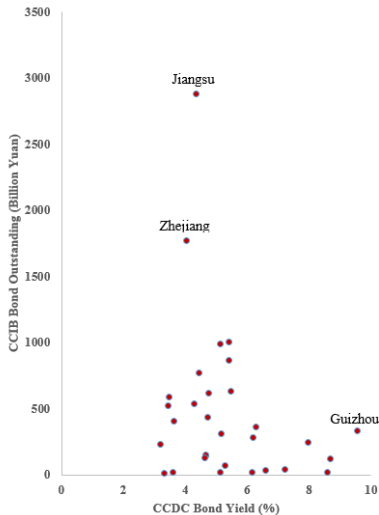
City Construction Investment Bond (CCIB)



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Theories

- Theory 1: Tournament of Officials
 - $\text{Debt} \uparrow \Rightarrow \text{GDP} \uparrow \Rightarrow \text{likelihood of promotion} \uparrow$
 - Li and Zhou (2005), Zhou (2007), etc.
 - Luo and She (2015), Chen and Li (2015), etc.
 - But questions remain:
 - How to endogenize officials' debt decisions in the macro model?
 - What is the impact of tournament on social welfare?
- Theory 2: Mismatch of Revenue and Responsibility
 - Empirical: Ji et al. (2019): tournament in East, mismatch in the West
- Theory 3: Mismatch of Term
 - Classical theory: Alberto and Guido (1990);
 - Luo and She (2015): Official terms: 4-5 years Bond: >7 years.

- 1 Question: Why Local Governments Borrow so Much?
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Mechanism

- **Basic assumption:** social infrastructure are **long-last public goods**
 - \Rightarrow You cannot exclude others and future people from gain from it.
- What is the gain/loss if a official invest in infrastructure:
 - Selfish (or shortsighted) officials:
 - Loss: government spending \downarrow : \Rightarrow enjoyment \downarrow ; prob. of win election \downarrow ;
 - Gain: Productivity $\uparrow \Rightarrow$ tax in my term \uparrow .
 - Selfless social planner (Social Optimal):
 - Additional gain: productivity $\uparrow \Rightarrow$ people's earning \uparrow .
 - Selfish (or shortsighted) officials with tournament:
 - Additional gain: my ability in eyes of central government $\uparrow \Rightarrow$ prob. of promotion \uparrow .

Representative Firms

- There are M regions indexed by $i = 1, 2, \dots, M$:
 - Each region is a open economy with perfect capital flow;
 - Interest rate is exogenously given on R ;
 - Labor market is local:
 - Each region have labor supply $L_{it} = 1$, earning wage Φ_{it} .
- Production function:

$$Y_{it} = A_{it} K_{it}^{\alpha_i} L_{it}^{1-\alpha_i} G_{it}^{1-\alpha_i} \quad (1)$$

- G_{it} : Public infrastructure (electricity, roads, schools, etc)
- G_{it} are public goods invested by local governments.

Representative Firms

- Firms' problem:

$$\max_{\{K_{it}, L_{it}\}} A_{it} K_{it}^{\alpha_i} L_{it}^{1-\alpha_i} G_{it}^{1-\alpha_i} - \Phi_{it} L_{it} - R K_{it} \quad (2)$$

- By solving the firms problem with $L_{it} = 1$:

$$K_{it} = \left(\frac{\alpha_i A_{it}}{R} \right)^{1/(1-\alpha_i)} G_{it} \quad (3)$$

$$Y_{it} = \left(\frac{\alpha_i}{R} \right)^{\alpha_i/(1-\alpha_i)} A_{it}^{1/(1-\alpha_i)} G_{it} \quad (4)$$

- K_{it} and Y_{it} are linear in G_{it} .

OLG Households

- Households' problem:

$$\max_{C_{it}^t, C_{it+1}^t} E_t \{ \ln(C_{it}^t) + \beta \ln(C_{it+1}^t) \} \quad (5)$$

$$\text{s.t. } C_{it}^t + S_{it}^t \leq (1 - \tau)\Phi_{it}L_{it} \quad (6)$$

$$C_{it+1}^t = (1 - \tau)RS_{it}^t \quad (7)$$

- τ is the tax rate on wage and capital return.

OLG Households

- By solving out the problem:

$$C_{it}^t = \frac{1}{1+\beta} (1-\alpha_i)(1-\tau) \left(\frac{\alpha_i}{R}\right)^{\alpha_i/(1-\alpha_i)} A_{it}^{1/(1-\alpha_i)} G_{it} \quad (8)$$

$$C_{it+1}^t = \frac{\beta}{1+\beta} R(1-\alpha_i)(1-\tau)^2 \left(\frac{\alpha_i}{R}\right)^{\alpha_i/(1-\alpha_i)} A_{it}^{1/(1-\alpha_i)} G_{it} \quad (9)$$

- Consumption in each period is linear in G_{it} .

Local Officials

- Local government officials are **selfish (or shortsighted)**:
 - They care about earning of government officials E_{it}^G :

$$V(W_{it}) = \max_{E_{it}^C} E_t [\gamma \ln(E_{it}^G) + \beta V(W_{it+1})] \quad (10)$$

- Governments' wealth are tax and infrastructure stock:

$$W_{it} = \tau Y_{it} + (1 - \delta_G) G_{it} \quad (11)$$

- Government pay their officials or invest in local infrastructure:

$$G_{it+1} + E_{it}^G = W_{it} \quad (12)$$

- Government problem is defined by (10), (11) and (12).

Local Officials

- For comparison, we can define a **social planner** problem:

$$V\left(W_{it}^{\text{planner}}\right) = \max_{C_{it}^t, C_{it}^{t-1}, E_{it}^G, G_{it+1}} E_t \left[\ln(C_{it}^t) + \ln(C_{it}^{t-1}) + \gamma \ln E_{it}^G + \beta V\left(W_{it+1}^{\text{planner}}\right) \right]$$

$$W_{it}^{\text{planner}} = Y_{it} + (1 - \delta_G) G_{it}$$

$$C_{it}^t + C_{it}^{t-1} + E_{it}^G + C_{it+1} = W_{it}^{\text{planner}}$$

- Question: What is the problem of selfish government officials?

Selfish Official: Underinvestment

Proposition 1: Infrastructure of Selfish Officials

In each period, the selfish local government allocates a fixed fraction β of government budget to local infrastructure:

$$G_{it+1} = \beta [\tau Y_{it} + (1 - \delta_G) G_{it}]$$

Proposition 2: Infrastructure of Social Planner

In the first-best benchmark, the social planner allocates a fixed fraction β of the aggregate social budget to infrastructure:

$$G_{it+1}^{\text{planner}} = \beta [Y_{it} + (1 - \delta_G) G_{it}]$$

Information Asymmetry

- Question: how to solve the underinvestment problem?
- Tournament: local officials care about how their ability in the eyes of central government:

$$V(W_{it}) = \max_{G_{it+1}} E_t [\gamma \ln(W_{it} - G_{it+1}) + \chi_i (\hat{a}_{it+1} - \bar{a}_i) + \beta V(W_{it+1})]$$

- $a_{it+1} \sim N(\bar{a}_{it+1}, \sigma_a^2)$ official's ability to boost local economy
- Their ability in the eyes of central government is:

$$\hat{a}_{it+1} = E[a_{it+1} \mid \{Y_{it+1}\}_{i=1, \dots, M}]$$

Information Asymmetry

- Productivity is of each region is given by:

$$A_{it} = e^{f_t + a_{it} + \varepsilon_{it}}$$

- $f_t \sim N(\bar{f}, \sigma_f^2)$ i.i.d. countrywide common shock;
- $a_{it} \sim N(\bar{a}_i, \sigma_a^2)$ i.i.d. official's ability;
- $\varepsilon_{it} \sim N(0, \sigma_\varepsilon^2)$ i.i.d. idiosyncratic noise.

- Information Asymmetry:

- Local GDP Y_{it+1} is known to central government;
- Local infrastructure stock G_{it+1} is unknown to central government,
- However, central government known the maximization problem of local official and deduct G_{it+1}^* from Y_{it+1} .**

Signal Jamming Mechanism

$$\ln(Y_{it+1}) = \frac{1}{1 - \alpha_i} (f_{t+1} + a_{it+1} + \varepsilon_{it+1}) + \frac{\alpha_i}{1 - \alpha_i} \ln\left(\frac{\alpha_i}{R}\right) + \ln(G_{it+1})$$

- To infer the ability of local officials, central government expected G_{it+1}^* and deduct irrelevant parts and form a statistic z_{it+1} :

$$z_{it+1} \equiv (1 - \alpha_i) \left\{ y_{it+1} - \left[\frac{\alpha_i}{1 - \alpha_i} \ln\left(\frac{\alpha_i}{R}\right) + \ln(G_{it+1}^*) \right] \right\}$$

Signal Jamming Mechanism

- In the eyes of local government officials:

$$z_{it+1} = f_{t+1} + a_{it+1} + \varepsilon_{it+1} + (1 - \alpha_i) [\ln(G_{it+1}) - \ln(G_{it+1}^*)] \quad (13)$$

- In equilibrium:

$$z_{it+1} = f_{t+1} + a_{it+1} + \varepsilon_{it+1} \quad (14)$$

Signal Jamming Mechanism

$$\ln(Y_{it+1}) = \frac{1}{1 - \alpha_i} (f_{t+1} + a_{it+1} + \varepsilon_{it+1}) + \frac{\alpha_i}{1 - \alpha_i} \ln\left(\frac{\alpha_i}{R}\right) + \ln(G_{it+1})$$

- Central government cannot separate the effects of a_i and $\ln(G)$;
 - \Rightarrow **Pretending to be smart** gives local official incentives to rise G .

Signal Jamming Mechanism

- Question: Why does this mechanism work when central government know local official will cheat them?

Signal Jamming Mechanism

- Using the **property of joint normal distribution** (see Appendix):

$$\begin{aligned}
 \hat{a}_{it+1} &= E \left[a_{it+1} \mid \{z_{it+1}\}_{i=1, \dots, M} \right] \\
 &= \bar{a}_i + h_1 (z_{it+1} - \bar{z}_{it+1}) - h_2 \sum_{j \neq i} (z_{jt+1} - \bar{z}_{jt+1}) \\
 &= \bar{a}_i + h_1 \left[(f_{t+1} - \bar{f}) + (a_{it+1} - \bar{a}_i) + \varepsilon_{it+1} + (1 - \alpha_i) (\ln G_{it+1} - \ln G_{it+1}^*) \right] \\
 &\quad - h_2 \sum_{j \neq i} \left[(f_{t+1} - \bar{f}) + (a_{jt+1} - \bar{a}_j) + \varepsilon_{jt+1} + (1 - \alpha_j) (\ln G_{jt+1} - \ln G_{jt+1}^*) \right]
 \end{aligned}$$

- $h_1 > 0$ and $h_2 > 0$ are parameters:

$$h_1 = \frac{\sigma_a^2 (\sigma_a^2 + \sigma_\varepsilon^2 + (M-1)\sigma_f^2)}{(\sigma_a^2 + \sigma_\varepsilon^2) (\sigma_a^2 + \sigma_\varepsilon^2 + M\sigma_f^2)} \quad h_2 = \frac{\sigma_a^2 \sigma_f^2}{(\sigma_a^2 + \sigma_\varepsilon^2) (\sigma_a^2 + \sigma_\varepsilon^2 + M\sigma_f^2)}$$

Local Officials' Problem with Tournament

$$V(W_{it}) = \max_{G_{it+1}} E_t [\gamma \ln(W_{it} - G_{it+1}) + \chi_i (\hat{a}_{it+1} - \bar{a}_i) + \beta V(W_{it+1})]$$

- Take in above equations:

$$\max_{G_{it+1}} E_t [\gamma \ln(W_{it} - G_{it+1}) + \kappa_i \ln G_{it+1} + \beta V(W_{it+1})] \quad (15)$$

- $\kappa_i = h_1(1 - \alpha_i)\chi_i > 0$ is a parameter.
- Local Official's problem with tournament is defined as (15) with constraints (11), (12).

Tournament

Proposition 3: Infrastructure with Tournament

The officials' career concerns lead to greater infrastructure investment:

$$G_{it+1}^{\text{Tournament}} = \left[\frac{\kappa_i}{\gamma + \kappa_i} (1 - \beta) + \beta \right] (\tau Y_{it} + (1 - \delta_G) G_{it})$$

Mechanism

- Selfish (or shortsighted) officials:

$$V(W_{it}) = \max_{E_{it}^C} E_t \left[\gamma \ln(E_{it}^G) + \beta V(W_{it+1}) \right]$$

$$G_{it+1} = \beta [\tau Y_{it} + (1 - \delta_G) G_{it}]$$

- Social planner:

$$V(W_{it}^{\text{planner}}) = \max_{C_{it}^t, C_{it}^{t-1}, E_{it}^G, G_{it+1}} E_t \left[\ln(C_{it}^t) + \ln(C_{it}^{t-1}) + \gamma \ln E_{it}^G + \beta V(W_{it+1}^{\text{planner}}) \right]$$

$$G_{it+1}^{\text{planner}} = \beta [Y_{it} + (1 - \delta_G) G_{it}]$$

- Selfish officials with tournament:

$$V(W_{it}) = \max_{G_{it+1}} E_t [\gamma \ln(W_{it} - G_{it+1}) + \chi_i (\hat{a}_{it+1} - \bar{a}_i) + \beta V(\tau Y_{it+1} + (1 - \delta_G) G_{it+1})]$$

$$G_{it+1}^{\text{Tournament}} = \left[\frac{\kappa_i}{\gamma + \kappa_i} (1 - \beta) + \beta \right] (\tau Y_{it} + (1 - \delta_G) G_{it})$$

Excess Leverage

- If we allowed the local government to borrow:

$$V(W_{it}) = \max_{G_{it+1}} E_t [\gamma \ln(W_{it} - G_{it+1}) + \chi_i (\hat{a}_{it+1} - \bar{a}_i) + \beta V(\tau Y_{it+1} + (1 - \delta_G) G_{it+1})]$$

$$W_{it} = \tau Y_{it} + (1 - \delta_G) G_{it} - RD_{it-1}$$

$$G_{it+1} + E_{it}^G = W_{it} + D_{it}$$

- The social planner's problem becomes:

$$V(W_{it}^{\text{planner}}) = \max_{G_{it+1}, C_{it}^t, C_{it}^{t-1}, E_{it}^G, D_{it}} E_t \left[\ln(C_{it}^t) + \ln(C_{it}^{t-1}) + \gamma \ln E_{it}^G + \beta V(W_{it+1}^{\text{planner}}) \right]$$

$$W_{it}^{\text{planner}} = Y_{it} + (1 - \delta_G) G_{it} - RD_{it-1}$$

$$C_{it}^t + C_{it}^{t-1} + G_{it+1} + E_{it}^G = W_{it}^{\text{planner}} + D_{it}$$

Excess Leverage

Excessive Leverage of Officials

Both the officials and the social planner would choose a debt level of $d_{it} = D_{it}/G_{it+1}$ in interval $[0, (1 - \delta_G)/R]$ based on problem:

$$\max_{d_{it}} \Psi \ln \left(\frac{1}{1 - d_{it}} \right) + E_t \left[\ln \left(\tau \left(\frac{\alpha_i}{R} \right)^{\alpha_i/(1-\alpha_i)} A_{it+1}^{1/(1-\alpha_i)} + (1 - \delta_G) - R d_{it} \right) \right]$$

in which

$$\Psi^{\text{Planner}} = 1 \leq \Psi^{\text{Official}} = 1 + \frac{1 - \beta}{\beta} \frac{\kappa_i}{\gamma + \kappa_i}$$

The officials debt choice is always higher than the planners and the officials debt choice is increasing with his career incentive parameter κ_i .

Excessive Leverage: Numerical Example

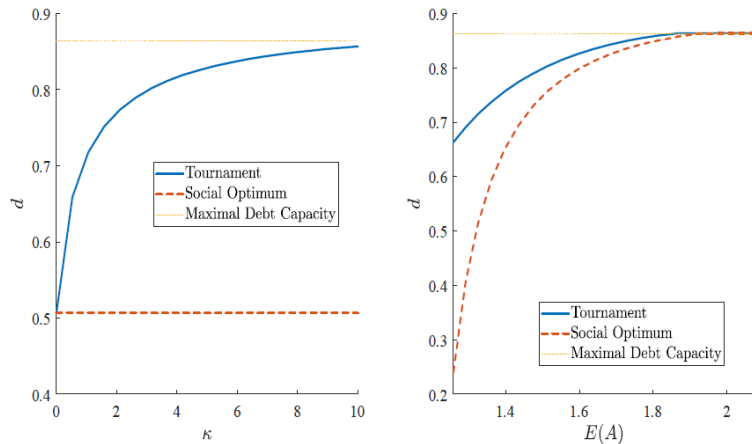


Figure 1: Leverage with Career Incentives and Expected Growth

Discussion

- Insights:
 - Theory of second best: use friction to correct friction;
 - Micro foundation: information friction in a bureaucratic system:
 - Why SOEs prefer to borrow and extend their scale;
 - 'Neijuan': e.g. *Ju Xiaolian* in Han Dynasty.
- Modeling simplification:
 - Technology A is not persistent \Rightarrow forgettable past information;
 - All government investments are homogeneous and efficient;
 - Government are able to disinvest in infrastructure;
 - Partial equilibrium of small open economy;
 - No land market.

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Thanks for listening!