EAFIT UNIVERSITY DEPARTMENT OF INFORMATICS AND SYSTEMS PROJECT CHOICE

Third Report

May 17, 2022

Course

Numerical analysis

Teacher

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Semester

2022 - 1

Project's name

Numerical Algorithms

Repository

This project has a GitHub repository where the evidence related with it will be. https://github.com/DanielHernandezO/NumericalMethodsProject

Members

- 1. Jose Miguel Blanco Velez
- 2. Neller Pellegrino Baquero
- 3. Samuel David Villegas Bedoya
- 4. Daniel Andres Hernandez Oyola

Project's description

Webpage used to calculate data using different types of numerical methods with the option of visualising them in a 2d graph.

Added values

- 1. The project will be done in english
- 2. The project will have its documentation in latex
- 3. The numerical algorithms can be found in multiple programming languages
- 4. The project will have extra numerical methods

1 Crout - Matlab

Input data

$$A = \begin{pmatrix} 4 & -1 & 0 & 3\\ 1 & 15.5 & 3 & 8\\ 0 & -1.3 & -4 & -1.1\\ 14 & 5 & -2 & 30 \end{pmatrix}$$
$$B = \begin{pmatrix} 1\\ 1\\ 1\\ 1 \end{pmatrix}$$

Result

U =

2 Crout - JavaScript

Input data

$$A = \begin{pmatrix} 4 & -1 & 0 & 3\\ 1 & 15.5 & 3 & 8\\ 0 & -1.3 & -4 & -1.1\\ 14 & 5 & -2 & 30 \end{pmatrix}$$
$$B = \begin{pmatrix} 1\\ 1\\ 1\\ 1 \end{pmatrix}$$

 \mathbf{Result}

```
L:
 4.0000
                  0
                             0
                                         0
 1.0000
           15.7500
                             0
                                         0
           -1.3000
 0.0000
                      -3.7523
                                         0
14.0000
                      -3.6193
            8.5000
                                  16.0714
U:
    -0.2500
               0.0000
                          0.7500
0
               0.1905
           1
                          0.4603
           0
                     1
                          0.1337
0
           0
                     0
                                1
 X:
 0.4853
 0.2078
 -0.2503
 -0.2445
```

3 Doolittle - Matlab

Input data

$$A = \begin{pmatrix} 4 & -1 & 0 & 3\\ 1 & 15.5 & 3 & 8\\ 0 & -1.3 & -4 & -1.1\\ 14 & 5 & -2 & 30 \end{pmatrix}$$
$$B = \begin{pmatrix} 1\\ 1\\ 1\\ 1 \end{pmatrix}$$

 \mathbf{Result}

U =

4 Doolittle - Javascript

Input data

$$A = \begin{pmatrix} 4 & -1 & 0 & 3\\ 1 & 15.5 & 3 & 8\\ 0 & -1.3 & -4 & -1.1\\ 14 & 5 & -2 & 30 \end{pmatrix}$$
$$B = \begin{pmatrix} 1\\ 1\\ 1\\ 1 \end{pmatrix}$$

 \mathbf{Result}

```
L:
     1
                0
                               0
                1
0.2500
                               0
0.0000
         -0.0825
                               0
3.5000
           0.5397
                     0.9645
                               1
U:
4.0000
         -1.0000
                      0.0000
                                 3.0000
                      3.0000
                                 7.2500
     0
         15.7500
     0
                     -3.7525
                                -0.5019
                0
                                16.0713
     0
                            0
X:
 0.4853
 0.2078
-0.2503
-0.2445
```

5 Cholesky - Matlab

Input data

$$A = \begin{pmatrix} 4 & -1 & 0 & 3\\ 1 & 15.5 & 3 & 8\\ 0 & -1.3 & -4 & -1.1\\ 14 & 5 & -2 & 30 \end{pmatrix}$$

$$B = \begin{pmatrix} 1\\ 1\\ 1\\ 1 \end{pmatrix}$$

```
x =
   0.4853
    0.2078
  -0.2503
  -0.2445
L =
   2.0000 + 0.0000i
                      0.0000 + 0.0000i
                                         0.0000 + 0.0000i
                                                             0.0000 + 0.0000i
  0.5000 + 0.0000i
                      3.9686 + 0.0000i
                                         0.0000 + 0.0000i
                                                             0.0000 + 0.0000i
  0.0000 + 0.0000i
                    -0.3276 + 0.0000i
                                         0.0000 + 1.9371i
                                                             0.0000 + 0.0000i
   7.0000 + 0.0000i
                     2.1418 + 0.0000i
                                         0.0000 + 1.8683i
                                                             4.0089 + 0.0000i
U =
                    -0.5000 + 0.0000i
   2.0000 + 0.0000i
                                         0.0000 + 0.0000i
                                                             1.5000 + 0.0000i
  0.0000 + 0.0000i
                    3.9686 + 0.0000i
                                         0.7559 + 0.0000i
                                                             1.8268 + 0.0000i
   0.0000 + 0.0000i
                      0.0000 + 0.0000i
                                         0.0000 + 1.9371i
                                                             0.0000 + 0.2589i
   0.0000 + 0.0000i
                      0.0000 + 0.0000i
                                         0.0000 + 0.0000i
                                                             4.0089 + 0.0000i
```

6 Cholesky - Javascript

Input data

$$A = \begin{pmatrix} 4 & -1 & 0 & 3\\ 1 & 15.5 & 3 & 8\\ 0 & -1.3 & -4 & -1.1\\ 14 & 5 & -2 & 30 \end{pmatrix}$$
$$B = \begin{pmatrix} 1\\ 1\\ 1\\ 1 \end{pmatrix}$$

 \mathbf{Result}

```
2
0.5
0
                                   0
                                          0
         3.905124837953327
                                   0
                                          0
      -0.33289588782552954
                                NaN
                                          0
        0.3841106397986879
                                NaN
                                       NaN
U:
                    0.5
                                                0
                                                     0.3841106397986879
    3.905124837953327
                           -0.33289588782552954
                      0
                                              NaN
                                                                      NaN
                      0
                                                0
                                                                      NaN
X:
NaN
NaN
NaN
VaN
```

7 Heun - Matlab

Input data

$$f(t,y) = (y - t^2 + 1)$$

left end point right end point=2 number of subintervals= 10 alpah = 1 **Result**

0.0000 1.00000000 0.2000 1.43991111 0.4000 1.95980255 0.6000 2.55966996 0.8000 3.23950802 1.0000 3.99931024 1.2000 4.83906868 1.4000 5.75877366 1.6000 6.75841334 1.8000 7.83797327 2.0000 8.99743580

8 Linear - Matlab

Input data

Result

ans =

-12.5000 3.0000 1.6667 3.0000 -7.0000 29.0000

9 Linear - Javascript

Input data

Result

C:\Users\Jose\Desktop\analisis\NumericalMethodsProject>node index.js
[[[-12.5], [3]], [[1.666666666666665], [3]]

10 Cuadratica - Matlab

Input data

Result

ans =

```
0 -12.5000 3.0000
4.7222 -12.5000 3.0000
-22.8333 152.8333 -245.0000
```

11 Cuadratica - Javascript

Input data

Result

```
[
    [ [ 0 ], [ -12.5000000000001 ], [ 3 ] ],
    [ [ 4.72222222222221 ], [ -12.50000000000001 ], [ 3 ] ],
    [ -22.83333333333333 ],
    [ 152.8333333333333 ],
    [ -245.000000000001 ]
    ]
]
```

12 Cubica - Matlab

Input data

```
ans =

2.5333    7.6000    -7.4333    3.0000
-1.5222    7.6000    -7.4333    3.0000
2.0333    -24.4000    88.5667    -93.0000
```

. .

13 Cubica - Javascript

Input data

Tabla =
$$\begin{vmatrix} x & -1 & 0 & 3 & 4 \\ y & 15.5 & 3 & 8 & 1 \end{vmatrix}$$

Result

```
[
[
[
[ 2.53333333333333],
[ 7.6000000000001],
[ -7.43333333333],
[ 3 ]
],
[ -1.5222222222222215],
[ 7.600000000000001],
[ -7.4333333333333],
[ 3 ]
],
[ [ 2.033333333333333],
[ 3 ]
],
[ [ 2.03333333333333],
[ -24.400000000000000],
[ 88.5666666666666],
[ -93.00000000000001]
]
]
```

14 Newton - Matlab

Input data

ans =

15.5000 -12.5000 3.5417 -1.1417

15 Newton - Javascript

Input data

Tabla =
$$\begin{vmatrix} x & -1 & 0 & 3 & 4 \\ y & 15.5 & 3 & 8 & 1 \end{vmatrix}$$

Result

C:\Users\Jose\Desktop\analisis\NumericalMethodsProject>node index.js
[15.5, -12.5, 3.5416666666666666, -1.1416666666666666]

16 Lagrange - Javascript

Input data

Result

C:\Users\Jose\Desktop\analisis\NumericalMethodsProject>node index.js
[-1.14166666666666666, 5.825, -5.5333333333335, 3]

17 Lagrange - Matlab

Input data

Result

-1.1417 5.8250 -5.5333 3.0000

18 Simple LU - JavaScript

Input data

$$A = \begin{pmatrix} 4 & -1 & 0 & 3\\ 1 & 15.5 & 3 & 8\\ 0 & -1.3 & -4 & -1.1\\ 14 & 5 & -2 & 30 \end{pmatrix}$$
$$B = \begin{pmatrix} 1\\ 1\\ 1\\ 1 \end{pmatrix}$$

```
0
                                                 0
                                                     0
0.25
                                                 0
                                                     0
       -0.08253968253968254
                                                     0
         0.5396825396825397
                               0.9644670050761421
                               0
    15.75
                                                   7.25
0
        0
            -3.7523809523809524
                                    -0.5015873015873017
0
        0
                                     16.071065989847714
Z =
               0.75
  1.061904761904762
-3.9289340101522843
  0.48531269740998106,
  0.2078332280480101,
  -0.2503158559696778,
  -0.24447252053063806
```

19 Simple LU - Matlab

Input data

$$A = \begin{pmatrix} 4 & -1 & 0 & 3\\ 1 & 15.5 & 3 & 8\\ 0 & -1.3 & -4 & -1.1\\ 14 & 5 & -2 & 30 \end{pmatrix}$$
$$B = \begin{pmatrix} 1\\ 1\\ 1\\ 1 \end{pmatrix}$$

Result

L = 1.0000000000000000 0.25000000000000 1.00000000000000 0 0 -0.082539682539683 1.000000000000000 3.50000000000000 0.539682539682540 0.964467005076142 1.00000000000000 υ = 4.00000000000000 -1.00000000000000 0 3.00000000000000 0 15.7500000000000 3.000000000000 7.2500000000000 0 0 -3.752380952380952 -0.501587301587302 0 0 16.071065989847714 1.0000000000000000 0.7500000000000000 1.061904761904762 -3.928934010152284 x =

20 Pivot LU - JavaScript

Input data

$$A = \begin{pmatrix} 4 & -1 & 0 & 3\\ 1 & 15.5 & 3 & 8\\ 0 & -1.3 & -4 & -1.1\\ 14 & 5 & -2 & 30 \end{pmatrix}$$
$$B = \begin{pmatrix} 1\\ 1\\ 1\\ 1\\ 1 \end{pmatrix}$$

```
0
                                                                 0
                                                                     0
0.07142857142857142
                                                                 0
                                                                     0
                       -0.0858490566037736
                                                                 1
                                                                     0
 0.2857142857142857
                      -0.16037735849056603
                                              -0.28831562974203334
U =
14
 0
     15.142857142857142
                           3.142857142857143
                                                  5.857142857142858
 0
                      0
                          -3.730188679245283
                                                -0.5971698113207548
 0
                                                 -4.804248861911987
        0 0
   0
       1 0
Bn =
1
0.9285714285714286
1.0797169811320755
1.1745068285280729
 0.4853126974099811,
 0.20783322804801013,
  -0.2503158559696778,
  -0.24447252053063806
```

21 Pivot LU - Matlab

Input data

$$A = \begin{pmatrix} 4 & -1 & 0 & 3\\ 1 & 15.5 & 3 & 8\\ 0 & -1.3 & -4 & -1.1\\ 14 & 5 & -2 & 30 \end{pmatrix}$$
$$B = \begin{pmatrix} 1\\ 1\\ 1\\ 1 \end{pmatrix}$$

Result

L =

```
    1.00000000000000
    0
    0
    0

    0.071428571428571
    1.0000000000000
    0
    0

    0
    -0.085849056603774
    1.000000000000
    0

    0.285714285714286
    -0.160377358490566
    -0.288315629742033
    1.00000000000000
```

U =

P =

Bn =

1 1 1

z =

- 1.000000000000000 0.928571428571429
- 1.079716981132075
- 1.174506828528073

x =

0.485312697409981 0.207833228048010 -0.250315855969678 -0.244472520530638

${\bf 22} \quad {\bf Trapezoid\ compound\ -\ JavaScript}$

Input data

$$a = 1$$

$$b = 2$$

$$n = 10$$

$$f(x) = e^x - 2x$$

(index)	хi	fxi	А		
0	1	0.7182818284590451	0.7182818284590451		
1	1.1	1.6083320478928655	2.3266138763519106		
2	1.2	1.8402338454730947	4.166847721825006		
3	1.3	2.138593335238488	6.305441057063494		
4	1.4	2.5103999336893477	8.815840990752841		
5	1.5	2.963378140676129	11.77921913142897		
6	1.6	3.5060648487902295	15.2852839802192		
7	1.700000000000000002	4.147894783454401	19.433178763673602		
8	1.8	4.899294928825891	24.332473692499494		
9	1.9	5.7717888845585374	30.10426257705803		
10	2	3.3890560989306495	33.49331867598868		
A = 1.6746659337994343					

23 Trapezoid compound - Matlab

Input data

$$a = 1$$

$$b = 2$$

$$n = 10$$

$$f(x) = e^x - 2x$$

Result

Xi	Fxi	A
1.0000	0.7183	0.7183
1.1000	1.6083	2.3266
1.2000	1.8402	4.1668
1.3000	2.1386	6.3054
1.4000	2.5104	8.8158
1.5000	2.9634	11.7792
1.6000	3.5061	15.2853
1.7000	4.1479	19.4332
1.8000	4.8993	24.3325
1.9000	5.7718	30.1043
2.0000	3.3891	33.4933
	1.0000 1.1000 1.2000 1.3000 1.4000 1.5000 1.6000 1.7000 1.8000	1.0000 0.7183 1.1000 1.6083 1.2000 1.8402 1.3000 2.1386 1.4000 2.5104 1.5000 2.9634 1.6000 3.5061 1.7000 4.1479 1.8000 4.8993 1.9000 5.7718

A =

1.6747

Simpson - JavaScript 24

Input data

a = 1

b = 2

n = 10

$$f(x) = e^x - 2x$$

(index)	хi	fxi	А		
0	1	0.7182818284590451	0.7182818284590451		
1	1.1	3.216664095785731	3.934945924244776		
2	1.2	1.8402338454730947	5.775179769717871		
3	1.3	4.277186670476976	10.052366440194847		
4	1.4	2.5103999336893477	12.562766373884195		
5	1.5	5.926756281352258	18.489522655236453		
6	1.6	3.5060648487902295	21.99558750402668		
7	1.700000000000000002	8.295789566908802	30.291377070935482		
8	1.8	4.899294928825891	35.19067199976137		
9	1.9	11.543577769117075	46.73424976887844		
10	2	3.3890560989306495	50.123305867809094		
A = 1.6707768622603032					

25 Simpson - Matlab

Input data

$$a = 1$$

$$b = 2$$

$$n = 10$$

$$f(x) = e^x - 2x$$

Result

Counter	Xi	Fxi	A
1.0000	1.0000	0.7183	0.7183
2.0000	1.1000	3.2167	3.9349
3.0000	1.2000	1.8402	5.7752
4.0000	1.3000	4.2772	10.0524
5.0000	1.4000	2.5104	12.5628
6.0000	1.5000	5.9268	18.4895
7.0000	1.6000	3.5061	21.9956
8.0000	1.7000	8.2958	30.2914
9.0000	1.8000	4.8993	35.1907
10.0000	1.9000	11.5436	46.7342
11.0000	2.0000	3.3891	50.1233

A =

1.6708

${\bf 26}\quad {\bf Simpson}\ {\bf Simple}\ {\bf -}\ {\bf JavaScript}$

Input data

$$a = 1$$

$$b = 2$$

$$n = 9$$

$$f(x) = e^x - 2x$$

(index)	xi	fxi	A
0	1	0.7182818284590451	0.7182818284590451
1	1.1111111111111111	2.44652866588578	3.164810494344825
2	1.222222222222223	2.8508362279633763	6.015646722308201
3	1.3333333333333333	2.254002456033021	8.269649178341222
4	1.444444444444444	4.051821971680084	12.321471150021306
5	1.55555555555556	4.879820245595901	17.201291395617208
6	1.666666666666665	3.9223134342733896	21.123604829890596
7	1.7777777777777777	7.0834141053263195	28.207018935216915
8	1.8888888888888888	8.50272040107713	36.70973933629405
9	2	3.3890560989306495	40.0987954352247

A = 1.6707831431343625

27 Simpson Simple - Matlab

Input data

$$a = 1$$

$$b=2$$

$$n = 9$$

$$f(x) = e^x - 2x$$

Result

Counter	Xi	Fxi	A
1.0000	1.0000	0.7183	0.7183
2.0000	1.0833	2.3635	3.0818
3.0000	1.1667	2.6338	5.7156
4.0000	1.2500	1.9807	7.6963
5.0000	1.3333	3.3810	11.0773
6.0000	1.4167	3.8701	14.9474
7.0000	1.5000	2.9634	17.9108
8.0000	1.5833	5.1135	23.0243
9.0000	1.6667	5.8835	28.9077
10.0000	1.7500	4.5092	33.4169
11.0000	1.8333	7.7641	41.1810
12.0000	1.9167	8.8948	50.0758
13.0000	2.0000	3.3891	53.4649

A =

1.6708

28 jacobi - Matlab

Input data

$$A = \begin{pmatrix} 4 & -1 & 0 & 3\\ 1 & 15.5 & 3 & 8\\ 0 & -1.3 & -4 & -1.1\\ 14 & 5 & -2 & 30 \end{pmatrix}$$
$$B = \begin{pmatrix} 1\\ 1\\ 1\\ 1\\ 1 \end{pmatrix}$$
$$x0 = \begin{pmatrix} 0\\ 0\\ 0\\ 0 \end{pmatrix}$$

Result				
20.0000000000000000	0.523560004785802	0.254518224580359	-0.409622194215019	0.000769598898146
21.0000000000000000	0.523943421238336	0.254751901431433	-0.409833506856140	0.000581980955112
22.0000000000000000	0.524229864816185	0.254924984100144	-0.409993060766602	0.000437345449321
23.0000000000000000	0.524447106480190	0.255057107247651	-0.410113101999437	0.000330218043530
24.0000000000000000	0.524610005548426	0.255155697163931	-0.410203660392208	0.000248442296050
25.0000000000000000	0.524733205064977	0.255230535734461	-0.410271837862075	0.000187422179934
26.0000000000000000	0.524825781040666	0.255286615763212	-0.410323244719618	0.000141102408853
27.0000000000000000	0.524895684573456	0.255329050313967	-0.410361961355017	0.000106393026870
28.0000000000000000	0.524948275149107	0.255360924746978	-0.410391145961265	0.000080129148558
29.0000000000000000	0.524987950144451	0.255384999889262	-0.410413130827260	0.000060401258846
30.0000000000000000	0.525017819165938	0.255403108413074	-0.410429700335005	0.000045500530962
31.0000000000000000	0.525040341181347	0.255416771957328	-0.410442183729544	0.000034292711698
32.0000000000000000	0.525057303265795	0.255427057179971	-0.410451591320835	0.000025835995875
33.0000000000000000	0.525070089389608	0.255434813228340	-0.410458679451516	0.000019470213684
34.0000000000000000	0.525079721163651	0.255440654157096	-0.410464020846618	0.000014669798856
35.0000000000000000	0.525086980451755	0.255445057318882	-0.410468045468966	0.000011054701396
36.0000000000000000	0.525092449548966	0.255448374083469	-0.410471078209027	0.000008329473338
37.0000000000000000	0.525096571117290	0.255450873942363	-0.410473363362482	0.000006276644366
38.0000000000000000	0.525099676498614	0.255452757275854	-0.410475085302710	0.000004729418638
39.0000000000000000	0.525102016620934	0.255454176599820	-0.410476382792042	0.000003563776166
40.0000000000000000	0.525103779849087	0.255455245970705	-0.410477360484623	0.000002685320789
41.0000000000000000	0.525105108524583	0.255456051824416	-0.410478097185512	0.000002023460236
42.0000000000000000	0.525106109673854	0.255456659012126	-0.410478652306110	0.000001524697071
43.0000000000000000	0.525106864073963	0.255457116559210	-0.410479070596616	0.000001148893313
44.0000000000000000	0.525107432517472	0.255457461316841	-0.410479385786889	0.000000865705897
45.0000000000000000	0.525107860854829	0.255457721104288	-0.410479623287367	0.000000652326719
46.0000000000000000	0.525108183611137	0.255457916854707	-0.410479802248417	0.000000491537725
47.0000000000000000	0.525108426815271	0.255458064358137	-0.410479937098365	0.000000370382862
48.0000000000000000	0.525108610072691	0.255458175503237	-0.410480038710219	0.000000279089274
49.0000000000000000	0.525108748160840	0.255458259253653	-0.410480115276396	0.000000210298774
50.0000000000000000	0.525108852212271	0.255458322360613	-0.410480172970352	0.000000158463532
51.0000000000000000	0.525108930616973	0.255458369913002	-0.410480216443700	0.000000119405045
52.0000000000000000	0.525108989696140	0.255458405744405	-0.410480249201618	0.0000000089973674

29 gauss-seidel - Matlab

Input data

$$A = \begin{pmatrix} 4 & -1 & 0 & 3\\ 1 & 15.5 & 3 & 8\\ 0 & -1.3 & -4 & -1.1\\ 14 & 5 & -2 & 30 \end{pmatrix}$$
$$B = \begin{pmatrix} 1\\1\\1\\1\\1 \end{pmatrix}$$
$$x0 = \begin{pmatrix} 0\\0\\0\\0 \end{pmatrix}$$

Result

14.0000000000000000	0.523771039468388	0.254652177903460	-0.409850937440877	0.001245991200282
15.0000000000000000	0.524306977399777	0.254975125985672	-0.410103024684111	0.000746956331826
16.00000000000000000	0.524628265568755	0.255168729371301	-0.410254147872196	0.000447791093152
17.00000000000000000	0.524820873856912	0.255284792209243	-0.410344744356502	0.000268445228405
18.0000000000000000	0.524936340146210	0.255354370446767	-0.410399055829629	0.000160929598099
19.0000000000000000	0.525005560760193	0.255396081740605	-0.410431614886814	0.000096475305962
20.0000000000000000	0.525047057663135	0.255421087145966	-0.410451133639366	0.000057835754084
21.00000000000000000	0.525071934543803	0.255436077577567	-0.410462834890390	0.000034671820080
22.00000000000000000	0.525086847926438	0.255445064156122	-0.410469849645823	0.000020785327808
23.00000000000000000	0.525095788315090	0.255450451498947	-0.410474054905046	0.000012460547242
24.00000000000000000	0.525101147967639	0.255453681144417	-0.410476575906000	0.000007469944136
25.0000000000000000	0.525104361013130	0.255455617276977	-0.410478087214927	0.000004478139227
26.0000000000000000	0.525106287194208	0.255456777964528	-0.410478993225958	0.000002684589144
27.00000000000000000	0.525107441915969	0.255457473782376	-0.410479536368379	0.000001609378027
28.0000000000000000	0.525108134157399	0.255457890916580	-0.410479861975550	0.000000964802245
29.0000000000000000	0.525108549147585	0.255458140983382	-0.410480057173027	0.000000578387027
30.0000000000000000	0.525108797929074	0.255458290895341	-0.410480174191503	0.000000346735877
31.00000000000000000	0.525108947070504	0.255458380765708	-0.410480244342634	0.000000207863875
32.00000000000000000	0.525109036478949	0.255458434641883	-0.410480286397370	0.000000124611825
33.0000000000000000	0.525109090078206	0.255458466939984	-0.410480311608665	0.000000074703250

30 s.o.r - Matlab

Input data

$$A = \begin{pmatrix} 4 & -1 & 0 & 3\\ 1 & 15.5 & 3 & 8\\ 0 & -1.3 & -4 & -1.1\\ 14 & 5 & -2 & 30 \end{pmatrix}$$
$$B = \begin{pmatrix} 1\\ 1\\ 1\\ 1 \end{pmatrix}$$
$$x0 = \begin{pmatrix} 0\\ 0\\ 0\\ 0 \end{pmatrix}$$

\mathbf{Result}

	16.0000000000000000	0.525048838054285	0.255562087609626	-0.410492655431864	0.000267368334562
	17.0000000000000000	0.525153096855929	0.255388792096719	-0.410431010542021	0.000211426878513
	18.0000000000000000	0.525083032330798	0.255496702359134	-0.410531691160648	0.000163371507257
:	19.0000000000000000	0.525121506112613	0.255442774363417	-0.410441485182732	0.000111917733452
	20.0000000000000000	0.525105541319758	0.255461263177453	-0.410504216337229	0.000067319451869
	21.00000000000000000	0.525108394432681	0.255461653797037	-0.410468618237813	0.000035714388124
	22.00000000000000000	0.525111497554948	0.255453839646213	-0.410484215061002	0.000017718668531
	23.00000000000000000	0.525106824710537	0.255462595617494	-0.410480615160611	0.000010557546628
	24.00000000000000000	0.525110917873488	0.255455725721314	-0.410478506228640	0.000008270250935
	25.00000000000000000	0.525108112407864	0.255460070529084	-0.410482345141617	0.000006440904033
	26.0000000000000000	0.525109680330846	0.255457853352381	-0.410478807970147	0.000004459353879
	27.00000000000000000	0.525109010211074	0.255458650387605	-0.410481311714314	0.000002711652727
	28.0000000000000000	0.525109149635733	0.255458624953548	-0.410479866117868	0.000001452527181
	29.0000000000000000	0.525109257661341	0.255458336405102	-0.410480516916483	0.000000720047620
	30.0000000000000000	0.525109078935774	0.255458675557160	-0.410480350801202	0.000000417805257
:	31.00000000000000000	0.525109239686291	0.255458403801543	-0.410480280920073	0.000000323380915
:	32.00000000000000000	0.525109127597958	0.255458578544970	-0.410480426786329	0.0000000253724307
	33.0000000000000000	0.525109191360249	0.255458487567299	-0.410480288304344	0.000000177538239
	34.0000000000000000	0.525109163313918	0.255458521682970	-0.410480388092254	0.000000109124253
	35.0000000000000000	0.525109169889426	0.255458519030165	-0.410480329483345	0.0000000059036251

31 Vandermonde - Matlab

Input data

Result

Ux =

-(137*x^3)/120

Px =

 $-(137*x^3)/120 + (233*x^2)/40 - (83*x)/15 + 3$

32 euler - Matlab

Input data

$$x = 2$$

$$xf = 4$$

$$y = 4$$

$$y = 0.5$$

$$f(x) = 0.1 * \sqrt{y} + 0.4 * x^2$$

Result

```
Resolucion de ecuaciones diferenciales ordinarias por el metodo de euler Ingrese la derivada:
0.1*sqrt(y) + 0.4*x^2

Ingrese el valor inicial de X:
2

Ingrese el valor final de X:
4

Ingrese el valor incial de Y:
4

Ingrese el paso:
0.5

x y

2.0 4.0000
2.5 4.9000
3.0 6.2607
3.5 8.1858
4.0 10.7788
```

Members signatures

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