Design of an Adaptive Hearing Aid

Daniel Edwards - 1055301
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School of Electrical & Information Engineering, University of the Witwatersrand, Private Bag 3, 2050, Johannesburg, South Africa

Abstract

This is my abstract

Contents

1 Introduction

define what adaptive means

2 Background

Hearing loss is a common problem in society. In *2016*, the University of the Witwatersrand released a statement saying that in South Africa, approximately 20% of the population suffers from a form of hearing loss [1]. As a result of hearing loss, an individual can suffer from loneliness, isolation, dependence, depression and frustration. These are signs of poor quality of [2]. The amount of people with an impaired quality of life provides motivation for the necessity of devices to improve an individuals hearing namely; a hearing aid.

3 Design Research

****Talk about conductive hearing loss
Many factors contribute to hearing loss. A common type is conductive hearing loss [3]. This is a result of age, excessive noise or various diseases [4]. This is a permanent form of hearing loss which can be treated with hearing assisting devices [4]. This section presents an analysis of existing solutions to this problem and a literature review.

3.1 Existing Solutions

Two main hearing assisting devices exist for sensorineural hearing impairments namely; hearing aids and cochlear implants [5]. Cochlear implants are typically used in cases of extreme sensorineural hearing loss. These devices work well in quiet environments [6]. However, cochlear implant users battle to perceive speech in noisy environments [6] and thus, the individuals quality of life is not improved. Therefore, this design will make use of hearing aid technology.

There are two main types of hearing aids, analogue and digital. Analogue hearing aids amplify all sounds, which includes the important sound and noise which is not ideal [7]. Ricketts [8] states that the largest problem for the hearing impaired is listening in noisy situations. Digital hearing aids however, contain a signal processing element which gives them additional functionality such as filtering noise and isolating sounds in specific directions [8].

put something in about Ricketts and avoiding noise - isolation, say something about adaptive

3.2 Literature Review

Sebastian *et al.* [9] defines a hearing aid, as an electro-acoustic device with the purpose of making speech intelligible. This purpose, together with the patients quality of life, must be at the center of each design decision.

Audiograms, performed by audiologiests, are used to detect hearing impairments on a patient [10]. An audiogram illustrates the hearing threshold of a person at different pitches and frequencies [9]. These graphs illustrate the frequencies at which the patient battles to hear. Frequency response matching is a technique utilised by hearing aids to correct the audiogram of the patient. Kakol *et al.* mention that in many cases, patients experience hearing difficulties at different frequency ranges [11]. Therefore, by correcting the audiogram at the required frequencies, the patients hearing can be improved. This correction can be implemented with a series of filters which apply gain to various frequency bands [11]. This method is also mentioned by Sebastian *et al.* and is referred to as selective amplification [9].

Sebastian *et al.* provide an frequency response matching (FRM) investigation between uniform and non-uniform filter banks [9]. The frequency bands in uniform filter banks are equally spaced whereas non-uniform filter banks are arbitrary. Non-uniform filter banks are the preferred choice as they allow for an audiogram to be correct at the precise frequency bands that are affected by hearing loss [9]. According to Sebastian *et al.*, the frequency bands at the critical hearing frequencies should be narrow for the best compensation [9]. Therefore, this design will consider narrow frequency band, non-uniform filter banks for audiogram correction.

Chang *et al.* give further insight into the types of filter banks by providing four different types namely; uniform, critical-like, symmetric and 1/3 octave [12]. The 1/3 octave filter bank proved to have the best audiogram matching. However, it had a $78ms$ delay at $24kHz$ compare to a $27ms$ delay when parallel *IIR* filters were used. Shearman [13] states a better understanding of how people perceive sound can be achieved by using octave analysis as breaking signals in octaves allows for the quality of the signal to be measured. This design aims to optimise the sound quality to improve the patients quality of life and thus, octave analysis must be considered.

Dhawan *et al.* simulate filtering in a hearing aid while using a wavelet filter to reduce noise. Additive white Gaussian noise (AWGN) was used to simulate the auditory noise [14]. Noise reduction is a critical component of this design and thus, the effect of these noise reduction techniques will be investigated within this system.

Ricketts [8] provides hearing aid performance metrics to raise the hearing capability of a hearing impaired individual to that of a normal hearing person. Normal hearing people, require an SNR[1] of at least $+6dB$. as suggested by [15]. Hearing impaired individuals however, require an SNR greater than $+6dB$ to achieve sufficient hearing [16]. This increase SNR requirement is because impaired hearing caused by poor hearing thresholds, results in noise related problems [8]. For children, a SNR of $+15dB \rightarrow +30dB$ is required for educational purposes. Ricketts also stated that by tuning the hearing aid to listen in the direction of the source can improve the SNR by about $3dB \rightarrow 6dB$.

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[1]Signal to noise ratio.

Chen *et al.* [17] suggest that using multiple microphones results in better extraction, separation of frequencies and localization of the source whilst reducing noise, interference, echo and reverberation. This provides motivation for utilising a multiple microphone array in this design. Resource [18] provides a comparison between two microphone array designs namely; broadside and endfire. This paper shows that the broadside configuration attenuates the signal less at low frequencies and has a larger bandwidth compared to the endfire configuration. The endfire configuration however, had better directivity when placed in the desired sound direction [18]. In addition, McCowan [19] states that voice is a broadband signal. Therefore, in terms of array configuration, a trade-off must be made between bandwidth and directivity performance.

Munir [20] states that in telephony systems, a frequency range of $300Hz$ to $3.4kHz$ is used because this is the frequency range of voice. The human ear however, can detect a frequency range of $20Hz$ to $20kHz$. Audiograms however, typically test upto a maximum frequency of $8kHz$ [21]. Since this system aims to correct audiograms, this frequency range must be considered.

McCowan [19] provides a comprehensive explanation of the wave propagation and various algorithms to determine directivity. This paper evaluates the performance of these algorithms within this context to determine the optimum solution.
    Put something in about the number of bands that increases the matching error Put the stuff about the audiogram gain factor thingy
mention stuff about why digital is better than analog
talk about group delay

4 Design Objectives

What the design intends to solve.

5 Design Requirements

6 Design Assumptions and Constrains

6.1 Assumptions

This paper presents a theoretical design and hence, assumptions can be made. This design is not limited by cost, power or space requirements. This design is considered for adult hearing only. The directionality component considers a $2D$ wave in a plane instead of a $3D$ wave. Finally, it is assumed that the speaker is deep inside the ear and hence separated from the microphone significantly enough such that feedback cancellation is not required.

6.2 Constraints

This system is constrained to a bandwidth of $20Hz$ to $8kHz$ to correspond to the audiogram frequency range.

constrains: 8kHz, response time

7 Design Methodology

The design of this system consists of two main subsystems. The first is the audiogram correction using an adaptive filter bank. The second, is applying directionality techniques to the signal to allow for the user to listen in specific directions. These subsystems will be amalgamated into a single system. This paper focuses on the adaptive hearing subsystem.

In this system, the adaptive filtering component is optimised for the audiogram matching error and response time.

Mention the compression aspect
compare a bunch of different designs
find the best one
choose DSP and stuff from there
digital filters
ideal filter bank

8 Adaptive Filter Design

State the factors that contribute to the optimisation
The adaptive filter is a filter bank which consists of an array of bandpass filters. Each of the bandpass filters operate with a particular frequency range and gain. This design subsection aims to utilise this frequency bank rectify a patients audiogram. This audiogram is presented in Section 8.1.

Approach: Research proved that there are multiple filter bank types used to rectifying a patients audiogram. To determine the optimum design, each of these systems will be considered. Sections 9.1, 9.2, 9.3 and 9.4 present the design of the uniform, critical-like, symmetric and 1/3 octave filter banks with similar design consideration discussed in Section 8.3...XXX. These designs will also be compared to the ANSIXXX specification presented in Section 10.

Mention stuff about uniform and non-uniform filter banks

8.1 Audiogram

The audiogram considered in this design corresponds to a patient with conductive hearing loss. Audiologists measure a patients hearing typically at $125Hz$, $250Hz$, $500Hz$, $1kHz$, $2kHz$, $4kHz$ and $8kHz$ REF. MATLAB's `pchip` function was used to interpolate these values to provide hearing threshold values for the full $125Hz$ to $8kHz$ range. Reference [22]

provides audiograms for normal hearing and conductive hearing loss. Figure 1 illustrates these audiograms.
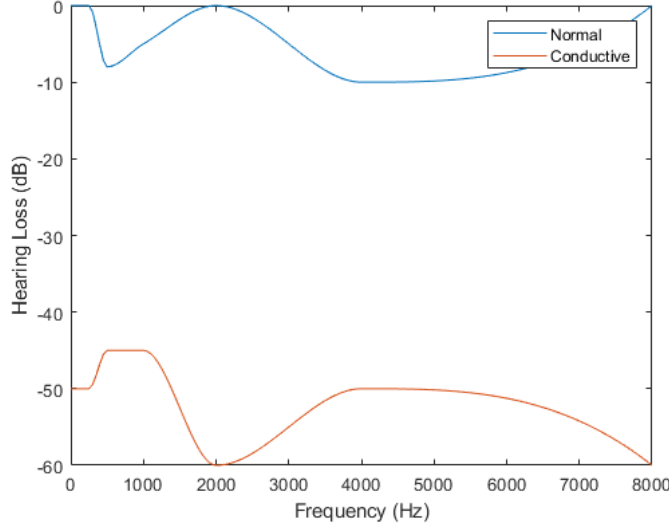

Figure 1: Audiogram for Normal Hearing and Conductive Hearing Loss

The filter bank aims match the conductive hearing loss patients audiogram to the normal hearing audiogram.

8.2   Insertion Gain

The filter bank corrects the audiogram by applying gain to particular frequencies. This is defined as insertion gain. In this design, the insertion gain is calculated using the NAL-R formulas given in equation 1.

$$
\begin{aligned}
H_{3FA} &= (H_{500} + H_{1k} + H_{2k})/3 \\
X &= 0.15 \times H_{3FA} \\
IG_i &= X + (0.31 \times H_i) + k_i
\end{aligned}
\tag{1}
$$

Where X is XXXXXX, IG_i is the insertion gain, H_i is the audiogram value at the ith sampled frequency and k_i is a constant at the ith sampled frequency given by Table 1 in Appendix B. Similarly to the audiogram, the insertion gain values were interpolated using MATLAB's pchip function. The insertion gains for the full frequency range is illustrated in Figure 2.

8.3   Number of Filters

As stated above, the filter bank consists of multiple bandpass filters, each with a specific sub-band. Therefore, the number of filters used must be investigated, particularly for the uniform, critical-like, symmetric and 1/3 octave filter banks designs. A uniform filter bank was used to investigate the effect that increasing the number of filters has on matching error and computational complexity. Appendix C provides the details of the filters used in this
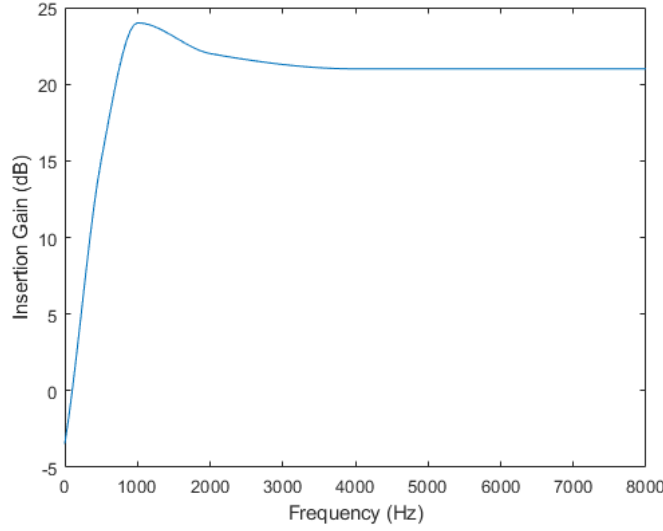
Figure 2: Interpolated Insertion Gain for Full Frequency Range
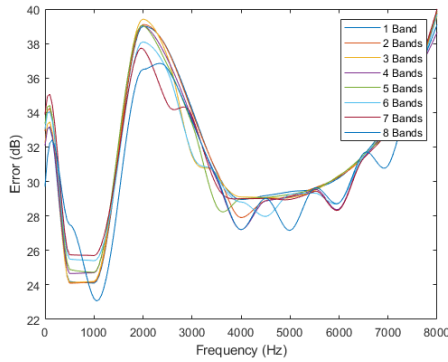
Figure 3: Matching Error Across Frequency Spectrum per Filter Bank
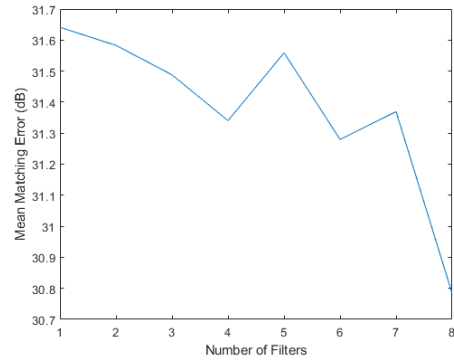
Figure 4: Mean Matching Error per Filter Bank

investigation. Figure 3 and 4 illustrate the matching error for each band across the frequency range and the mean error for each number of frequency bands respectively.

This section investigates the effect of increases the number of filters in the filter bank. The large errors therefore, are not a concern at this point. Figure 4 illustrates that increasing the number of bands, decreases the mean matching error. Therefore, the design should aim to maximise the number of filters.

the number of filters emphaisies the frequency bands that need to be adjusted.

9 Uniform, Critical-like, Symmetric and $1/3$ Octave Filter Bank Design

This section aims to optimise the structure of the filter bank's frequency bands. Therefore, a comparison between a uniform (Section 9.1), critical-like (Section 9.2), symmetric (Section 9.3) and 1/3 octave (Section 9.4) filter banks will be made. The best performing filter bank will then be compared to the ANSIXXX designed in Section 10. To draw a fair comparison, all of the filters will be design with the parameters given in Table 2 in Appendix C. Each filter bank will consist of 8 bandpass filters. Furthermore, since a comparison is being drawn, the same insertion gain method as in Section 8.2 will be used.

9.1 Uniform Filter Bank Design

A uniform filter bank consist of an array of evenly spaced, filters with equal bandwidths [12]. Uniform filter banks are simple and easy to implement. However, for a sufficient resolution, uniform filter banks requires more bands than non-uniform filter banks for a good fit. The additional filters implies that more computations are required and thus, the filter bank's group delay is potentially increased [23]. Section 8.3's simulation utilised a uniform filter bank which yielded a mean matching error of $30.78dB$.

9.2 Critical-like Filter Bank Design

This filter is forms part of the non-uniform filter bank category. This filter design attempts to account for the psychoacoustic characteristics using the critical bands of the Bark Scale [24]. Table 11 in Appendix D provides the Bark scale's critical frequency band information. In this investigation, we are limited to using 8 filters and a maximum frequency of $8kHz$. Therefore, the filters will correspond to the frequency bands in Table 12 of Appendix E. This design achieved an average and maximum matching error of $0.8957dB$ and $11.4dB$ respectively. The matching error for the full frequency spectrum is illustrated in Figure 5.

9.3 Symmetric Filter Bank Design

Symmetric filter banks provde an improvement on the uniform filter bank. The non-uniform sub-bands are symmetric about the center frequency of the frequency spectrum, in this case $4kHz$. Symmetric filter banks have the ability of enhancing the matching error of low and high, or mid frequencies [9]. Figure 1 illustrates that the threshold of a conductive hearing loss patient is worse at the low and high frequencies. Therefore, the frequency bands will be chosen such that these frequencies are emphasised. Table 13 in Appendix F illustrates the bands used in this investigation. Simulation illustrated that the symmetric filter bank acheived an average error of $0.795dB$ with a maximum matching error of $6.44dB$. The matching error for the full frequency spectrum is illustrated in Figure 6.
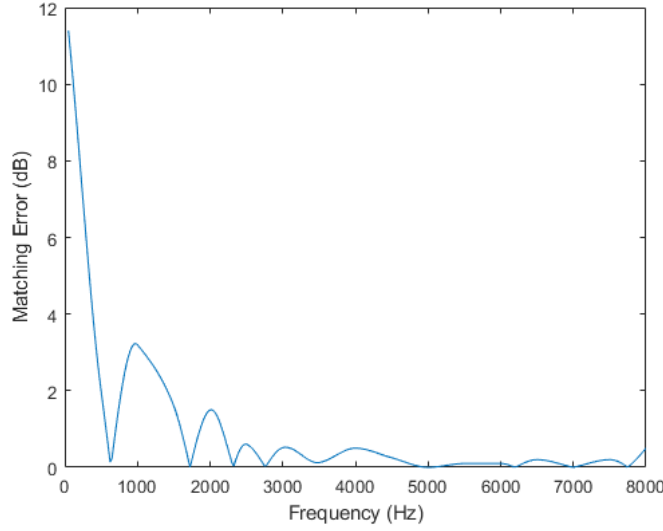
Figure 5: Matching Error for Critical-Like Filter Bank

9.4 Octave Filter Bank Design

As stated above, separating a frequency spectrum into octaves allows for the quality of sound to be measure and by derivative, improved [13]. It is therefore natural for a filter bank to be designed using this principle. Each filter bank sub-band will have a center frequency relative to the reference sub-band center frequency $f_c[0] = 1000Hz$ [25]. The center frequency of each sub-band is calculated using equation 2. The corresponding upper (f_{cu}) and lower (f_{cl}) passband frequencies are calculated using equation 3 [25].

$$f_c[k-1] = f[k]/2 \tag{2}$$

$$f_{cu}[k] = \frac{f_c[k]}{2^{1/2}}$$
$$f_{cl}[k] = 2^{1/2} \times f_c[k] \tag{3}$$

The center frequencies for this filter bank are chosen to be $63Hz$, $125Hz$, $250Hz$, $500Hz$, $1kHz$, $2kHz$, $4kHz$ and $8kHz$ which results in the filter specifications given in Table 14 of Appendix G.
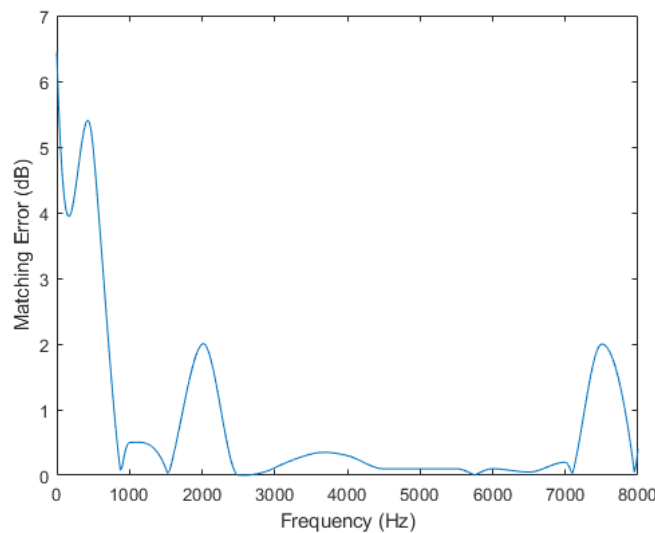
Figure 6: Matching Error for Symmetric Filter Bank

10 ANSIXXXX Design

11 Dynamic Compression Design

12 Success Criterion

13 Critical Evaluation of Results

13.1 Socioeconomic Impacts of Design

14 Future Recommendations

15 Conclusion

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Appendix

A   Impact Appendix - Non-Technical thing

B   Insertion Gain Parameters

The values of k_i is determined by Table 1.

Table 1: k_i Parameter at Specific Frequency Values

Frequency (Hz)	250	500	1000	2000	3000	4000	6000
$k_i(dB)$	-17	-8	1	-1	-2	-2	-2

C   Number of Filters Investigation

In this investigation, a filter bank was constructed. Each filter was designed using `Simulink's` digital bandpass filter. The design settings used are given in Table 2.

Table 2: Filter Design Settings

Impulse Response	FIR
Order Mode	Minimum
Filter Type	Single-rate
Input Sample Rate	$20kHz$
Passband ripple	$1dB$
Transition Band	$200Hz$
Design Method	Equiripple
Structure	Direct-form FIR

The order of an FIR filter corresponds to the window length. Therefore, it is set to a minimum to keep the results consistent. Tables 3 to 10 provide the filter range and gains used in this investigation. f_{s1}, f_{p1}, f_{p2} and f_{s2} correspond to the lower stopband frequency, the lower pass band frequency, the upper passband frequency and the upper stopband frequency respectively. A_{s1} and A_{s2} correspond to the lower and upper stopband attenuations.

D   Bark-Scale

Table 11 provides the critical frequency bands of the Bark-scale [26].

E   Critical-Like Filter Bank Frequency Bands

Within the Bark range, bands 22,23 and 24 fall outside of the $8kHz$ constraint and are therefore, ignored. The remaining 21 bands are divided into 8 sub-bands by grouping together

Table 3: Filter Parameters - 1 Band

Parameter	Filter 1
$f_{s1}(Hz)$	$20Hz$
$f_{p1}(Hz)$	$250Hz$
$f_{p2}(Hz)$	$8000Hz$
$f_{s2}(Hz)$	$8200Hz$
$A_{s1}(dB)$	$G1dB + 3$
$A_{s2}(dB)$	$G1dB + 3$

Table 4: Filter Parameters - 2 Bands

Parameter	Filter 1	Filter 2
$f_{s1}(Hz)$	20	3800
$f_{p1}(Hz)$	250	4000
$f_{p2}(Hz)$	4000	8000
$f_{s2}(Hz)$	4200	8200
$A_{s1}(dB)$	$G1dB + 3$	$G1dB + G2dB + 3$
$A_{s2}(dB)$	$G1dB + G2dB + 3$	$G2dB + 3$

Table 5: Filter Parameters - 3 Bands

Parameter	Filter 1	Filter 2	Filter 3
$f_{s1}(Hz)$	20	2800	5550
$f_{p1}(Hz)$	250	3000	5750
$f_{p2}(Hz)$	3000	5750	8000
$f_{s2}(Hz)$	3200	5950	8200
$A_{s1}(dB)$	$G1dB + 3$	$G1dB + G2dB + 3$	$G2dB + G3dB + 3$
$A_{s2}(dB)$	$G1dB + G2dB + 3$	$G2dB + G3dB + 3$	$G3dB + 3$

Table 6: Filter Parameters - 4 Bands

Parameter	Filter 1	Filter 2	Filter 3	Filter 4
$f_{s1}(Hz)$	20	1800	3800	5800
$f_{p1}(Hz)$	250	2000	4000	6000
$f_{p2}(Hz)$	2000	4000	6000	8000
$f_{s2}(Hz)$	2200	4200	6200	8200
$A_{s1}(dB)$	$G1dB + 3$	$G1dB + G2dB + 3$	$G2dB + G3dB + 3$	$G3dB + G4dB + 3$
$A_{s2}(dB)$	$G1dB + G2dB + 3$	$G2dB + G3dB + 3$	$G3dB + G4dB + 3$	$G4dB + 3$

Table 7: Filter Parameters - 5 Bands

Parameter	Filter 1	Filter 2	Filter 3	Filter 4	Filter 5
$f_{s1}(Hz)$	20	1700	3350	5000	6650
$f_{p1}(Hz)$	250	1900	3550	5200	6850
$f_{p2}(Hz)$	1900	3550	5200	6850	8000
$f_{s2}(Hz)$	1100	3750	5400	7050	8200
$A_{s1}(dB)$	$G1dB + 3$	$G1dB + G2dB + 3$	$G2dB + G3dB + 3$	$G3dB + G4dB + 3$	$G4dB + G5dB + 3$
$A_{s2}(dB)$	$G1dB + G2dB + 3$	$G2dB + G3dB + 3$	$G3dB + G4dB + 3$	$G4dB + G5dB + 3$	$G5dB + 3$

Table 8: Filter Parameters - 6 Bands

Parameter	Filter 1	Filter 2	Filter 3	Filter 4	Filter 5	Filter 6
$f_{s1}(Hz)$	20	1300	2800	4300	5800	7300
$f_{p1}(Hz)$	250	1500	3000	4500	6000	7500
$f_{p2}(Hz)$	1500	3000	4500	6000	7500	8000
$f_{s2}(Hz)$	1700	3200	4700	6200	7700	8200
$A_{s1}(dB)$	$G1dB+3$	$G1dB+G2dB+3$	$G2dB+G3dB+3$	$G3dB+G4dB+3$	$G4dB+G5dB+3$	$G5dB+G6dB+3$
$A_{s2}(dB)$	$G1dB+G2dB+3$	$G2dB+G3dB+3$	$G3dB+G4dB+3$	$G4dB+G5dB+3$	$G5dB+G6dB+3$	$G6dB+3$

Table 9: Filter Parameters - 7 Bands

Parameter	Filter 1	Filter 2	Filter 3	Filter 4	Filter 5	Filter 6	Filter 7
$f_{s1}(Hz)$	20	1200	2350	3500	4650	5800	6950
$f_{p1}(Hz)$	250	1400	2550	3700	4850	6000	7150
$f_{p2}(Hz)$	1400	2550	3700	4850	6000	7150	8000
$f_{s2}(Hz)$	1600	2750	3900	5050	6200	7350	8200
$A_{s1}(dB)$	$G1dB+3$	$G1dB+G2dB+3$	$G2dB+G3dB+3$	$G3dB+G4dB+3$	$G4dB+G5dB+3$	$G5dB+G6dB+3$	$G6dB+G7dB+3$
$A_{s2}(dB)$	$G1dB+G2dB+3$	$G2dB+G3dB+3$	$G3dB+G4dB+3$	$G4dB+G5dB+3$	$G5dB+G6dB+3$	$G6dB+G7dB+3$	$G7dB+3$

2 or 3 sub-bands. According to the audiogram used in this design, the greatest hearing loss occurs within the $1kHz$ to $3kHz$ range. Therefore, a greater resolution is required within this frequency range. The frequency bands used in this investigation are therefore given in Table 12.

F   Symmetric Filter Bank Frequency Bands

Table 13 summarises the frequency bands used to investigate the performance of the symmetric filter bank design. Because the human hearing frequency spectrum begins at $20Hz$, the first sub-band is not symmetric to the last sub-band. However, there is only a 4% difference which is negligible. The transition bandwidth for the first sub-band however, will be $20Hz$. Since only the transition bandwidth of the first sub-band is affected, this affect is also ignored.

G   Octave Filter Bank Frequency Bands

Table 14 illustrates the frequency bands used in the octave filter bank design. Within the audio range, there exists bands at $16Hz$, $31.25Hz$ and $16kHz$. However, these bands are ignored as this design is restricted to using 8 bands and, $16kHz$ violates the Nyquist sampling criteria.

Table 10: Filter Parameters - 8 Banks

Parameter	Filter 1	Filter 2	Filter 3	Filter 4	Filter 5	Filter 6	Filter 7	Filter 8
$f_{s1}(Hz)$	20	800	1800	2800	3800	4800	5800	6800
$f_{p1}(Hz)$	250	1000	2000	3000	4000	5000	6000	7000
$f_{p2}(Hz)$	1000	2000	3000	4000	5000	6000	7000	8000
$f_{s2}(Hz)$	1200	2200	3200	4200	5200	6200	7200	8200
$A_{s1}(dB)$	$G1dB+3$	$G1dB+G2dB+3$	$G2dB+G3dB+3$	$G3dB+G4dB+3$	$G4dB+G5dB+3$	$G5dB+G6dB+3$	$G6dB+G7dB+3$	$G7dB+G8dB+3$
$A_{s2}(dB)$	$G1dB+G2dB+3$	$G2dB+G3dB+3$	$G3dB+G4dB+3$	$G4dB+G5dB+3$	$G5dB+G6dB+3$	$G6dB+G7dB+3$	$G7dB+G8dB+3$	$G8dB+3$

Table 11: Bark-scale Critical Frequency Bands

Number	Center Frequency (Hz)	Cut-Off Frequency (Hz)	Bandwidth (Hz)
		20	
1	60	100	80
2	150	200	100
3	250	300	100
4	350	400	100
5	450	510	110
6	570	630	120
7	700	770	140
8	840	920	150
9	1000	1080	160
10	1170	1270	190
11	1370	1480	210
12	1600	1720	240
13	1850	2000	280
14	2150	2320	320
15	2500	2700	380
16	2900	3150	450
17	3400	3700	550
18	4000	4400	700
19	4800	5300	900
20	5800	6400	1100
21	7000	7700	1300
22	8500	9500	1800
23	10500	12000	2500
24	13500	15500	3500

Table 12: Frequency Range per Sub-band for Critical-Like Filter Bank

Band	Number	Center Frequency (Hz)	Cut-Off Frequency (Hz)	Bandwidth (Hz)
			20	
	1	60	100	80
1	2	150	200	100
	3	250	300	100
	4	350	400	100
2	5	450	510	110
	6	570	630	120
	7	700	770	140
3	8	840	920	150
	9	1000	1080	160
4	10	1170	1270	190
	11	1370	1480	210
5	12	1600	1720	240
	13	1850	2000	280
6	14	2150	2320	320
	15	2500	2700	380
	16	2900	3150	450
7	17	3400	3700	550
	18	4000	4400	700
	19	4800	5300	900
	20	5800	6400	1100
8	21	7000	7700	1300

Table 13: Symmetric Filter Bank Frequency Bands

Band Number	Lower Passband Frequency (Hz)	Upper Passband Frequency (Hz)	Bandwidth (Hz)
1	20	500	480
2	500	1000	500
3	1000	2000	1000
4	2000	4000	2000
5	4000	6000	2000
6	6000	7000	1000
7	7000	7500	500
8	7500	8000	500

Table 14: Octave Filter Bank Frequency Bands

Band	Center Frequency (Hz)	Lower Passband Frequency (Hz)	Upper Passband Frequency (Hz)
1	63	45	89
2	125	88	177
3	250	177	354
4	500	354	707
5	1000	707	1414
6	2000	1414	2828
7	4000	2828	5657
8	8000	5657	11314