$$s_{i,j} = \max \begin{cases} s_{i-1,j} \\ s_{i,j-1} \\ s_{i-1,j-1}, \text{ if } a_i = b_j \end{cases}$$