

String Comparison

CMSC 423

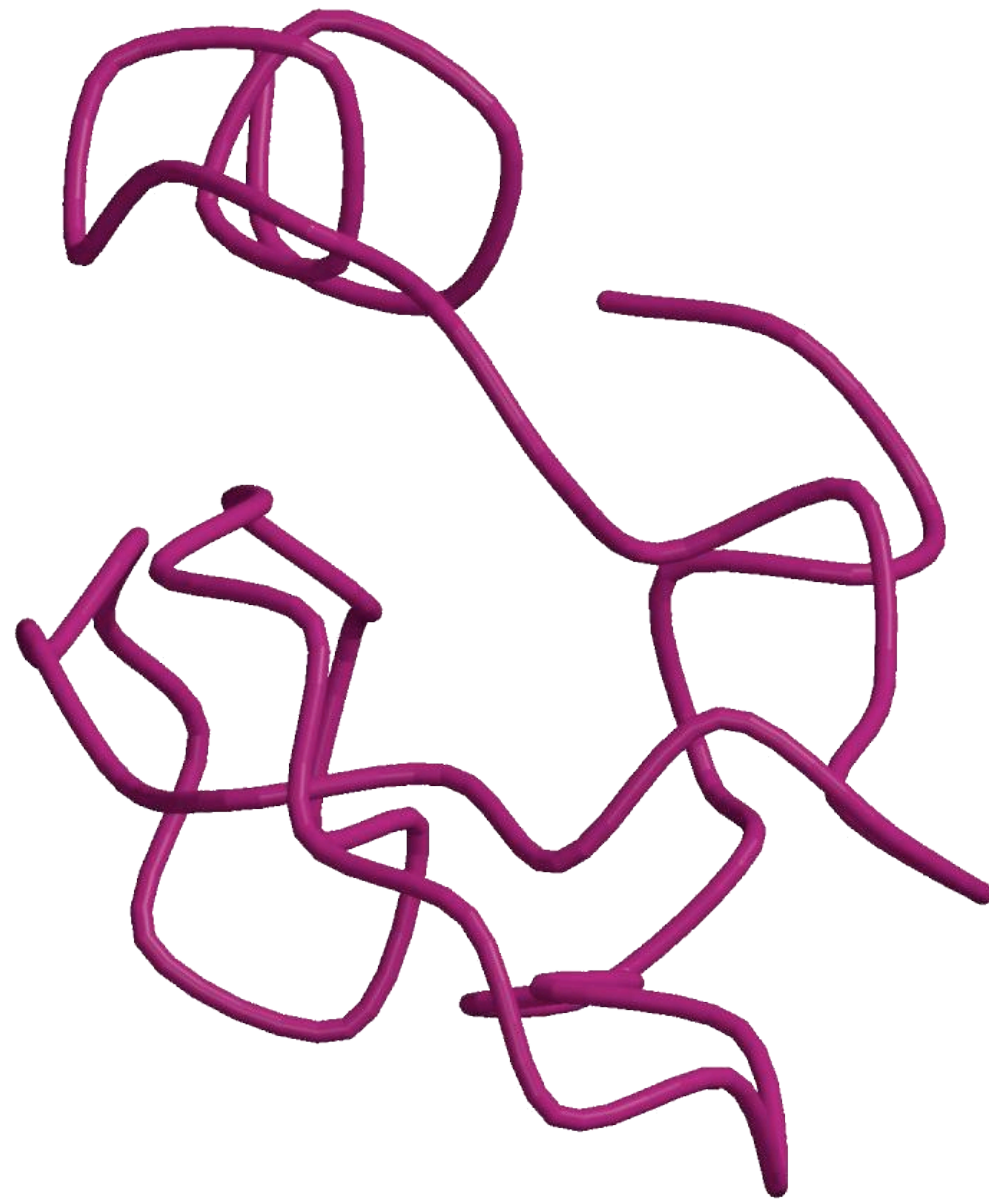
Why compare DNA or protein sequences?

Partial CTCF protein sequence in 8 organisms:

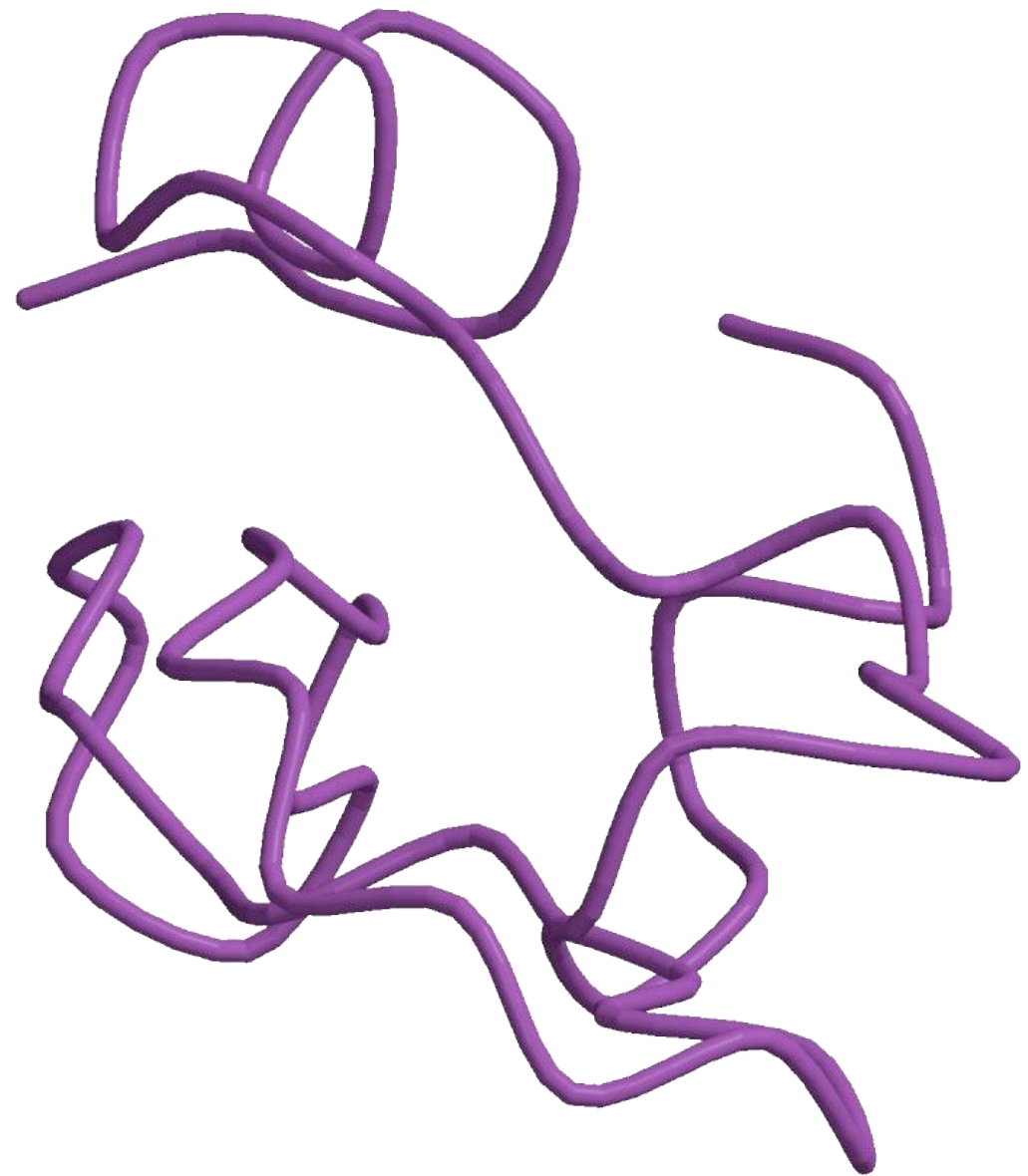
<i>H. sapiens</i>	-EDSSDS-ENAE PDLDDNEDEEEPAVEIEPEPE-----PQPVTTPA
<i>P. troglodytes</i>	-EDSSDS-ENAE PDLDDNEDEEEPAVEIEPEPE-----PQPVTTPA
<i>C. lupus</i>	-EDSSDS-ENAE PDLDDNEDEEEPAVEIEPEPE-----PQPVTTPA
<i>B. taurus</i>	-EDSSDS-ENAE PDLDDNEDEEEPAVEIEPEPE-----PQPVTTPA
<i>M. musculus</i>	-EDSSDSEENAE PDLDDNEEEEEPAVEIEPEPE--PQPQP P P P P Q P V A P A
<i>R. norvegicus</i>	-EDSSDS-ENAE PDLDDNEEEEEPAVEIEPEPEPQPQPQPQPQPQP V A P A
<i>G. gallus</i>	-EDSSDSEENAE PDLDDNEDEEETAVEIEAEPE-----VSAEAPA
<i>D. rerio</i>	DDDDDDSDDEHGE PDLDDIDEEDEDDL-LDEDQMGLLDQAPPSVPI P-APA

- Identify important sequences by finding conserved regions.
- Find genes similar to known genes.
- Understand evolutionary relationships and distances (*D. rerio* aka zebrafish is farther from humans than *G. gallus* aka chicken).
- Interface to databases of genetic sequences.
- As a step in genome assembly, and other sequence analysis tasks.
- Provide hints about protein structure and function (next slide).

Sequence can reveal structure



(a) 1dtk



(b) 5pti

1dtk	XAKYCKLPLRIGPCKRKIPSFYKWKAKQCLPFDYSGCGGNANRFKTIEECRRTC VG-
5pti	RPDFCLEPPYTGPCKARIIRYFYNAKAGLCQTFVYGGCRAKRNNFKSAEDCMRTC GGA

Simple String Comparison Problems

Given: Two strings

$$a = a_1a_2a_3a_4\dots a_m$$

$$b = b_1b_2b_3b_4\dots b_n$$

where a_i, b_i are letters from some alphabet like {A,C,G,T}.

Compute how **similar** the two strings are.

What do we mean by “similar”?

Longest Common Subsequence: the longest subsequence with matching characters from the two strings.

A	T	–	G	T	T	A	T	A
A	T	C	G	T	–	C	–	C

Simple String Comparison Problems

Given: Two strings

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where a_i, b_i are letters from some alphabet like {A,C,G,T}.

Compute how **similar** the two strings are.

What do we mean by “similar”?

Edit distance between strings a and b = the smallest number of the following operations that are needed to transform a into b :

- mutate (replace) a character
- delete a character
- insert a character

riddle $\xrightarrow{\text{delete}}$ ridle $\xrightarrow{\text{mutate}}$ riple $\xrightarrow{\text{insert}}$ triple

Representing edits as alignments

prin-ciple
| | | | | | | | xx
prinncipal
(1 gap, 2 mm)

prin-cip-le
| | | | | | | |
prinncipal-
(3 gaps, 0 mm)

misspell
| | | | | | | |
mis-pell
(1 gap)

prehistoric
| | | | | | | |
---historic
(3 gaps)

aa-bb-ccaabb
| x | | | | | |
ababbbc-a-b-
(5 gaps, 1 mm)

al-go-rithm-
| | xx | | x |
alKhwariz-mi
(4 gaps, 3 mm)

NCBI BLAST DNA Alignment

>gb|AC115706.7| Mus musculus chromosome 8, clone RP23-382B3, complete sequence

```
Query 1650 gtgtgtgtgggtgcacatttgtgtgtgtgtgcgcctgtgtgtgtgggtgcctgtgtgtgt 1709
          ||||| ||| | ||||| | ||||| ||| || |||||
Sbjct 56838 GTGTGTGTGGAAGTGAGTTCATCTGTGTGTGCACATGTGTGTGCA--TGCATGCATGTGT 56895

Query 1710 gtg-gggcacatttgtgtgtgtgtgtgtgcctgtgtgtgggtgcacatttgtgtgtgtgc 1768
          || |||| | || ||| ||||| ||||| ||| ||| ||||| |||
Sbjct 56896 GTCCGGGCA-----TGCATGTCTGTGTGCATGTGTGTGTGTGTGCAT--GTGTGAGTAC 56947

Query 1769 ctgtgtgtgtgtgcctgtgtgtgggggtgcacatttgtgtgtgtgtgtgcctgtgtgtgg 1828
          ||||| ||| ||| |||| | ||| ||| |||| | |||| |
Sbjct 56948 CTGTGTGTGTATGCTTGTATGTGTGTGTGTGCATGTGTGTAGGTGTGTATATGTGTAAGT 57007

Query 1829 ggggtgcacatttgtgtgtgtgtgtgtgcctgtgtgtgtgggtgcacatttgtgtgtgtgtgt 1888
          ||| ||||| ||||| |||| | ||| |||| | ||||| |||
Sbjct 57008 T-----CATCTGTGTGTATGTGTG--TGTGAGAGTGCATGCA---TGTGTGTGTGAGT 57055

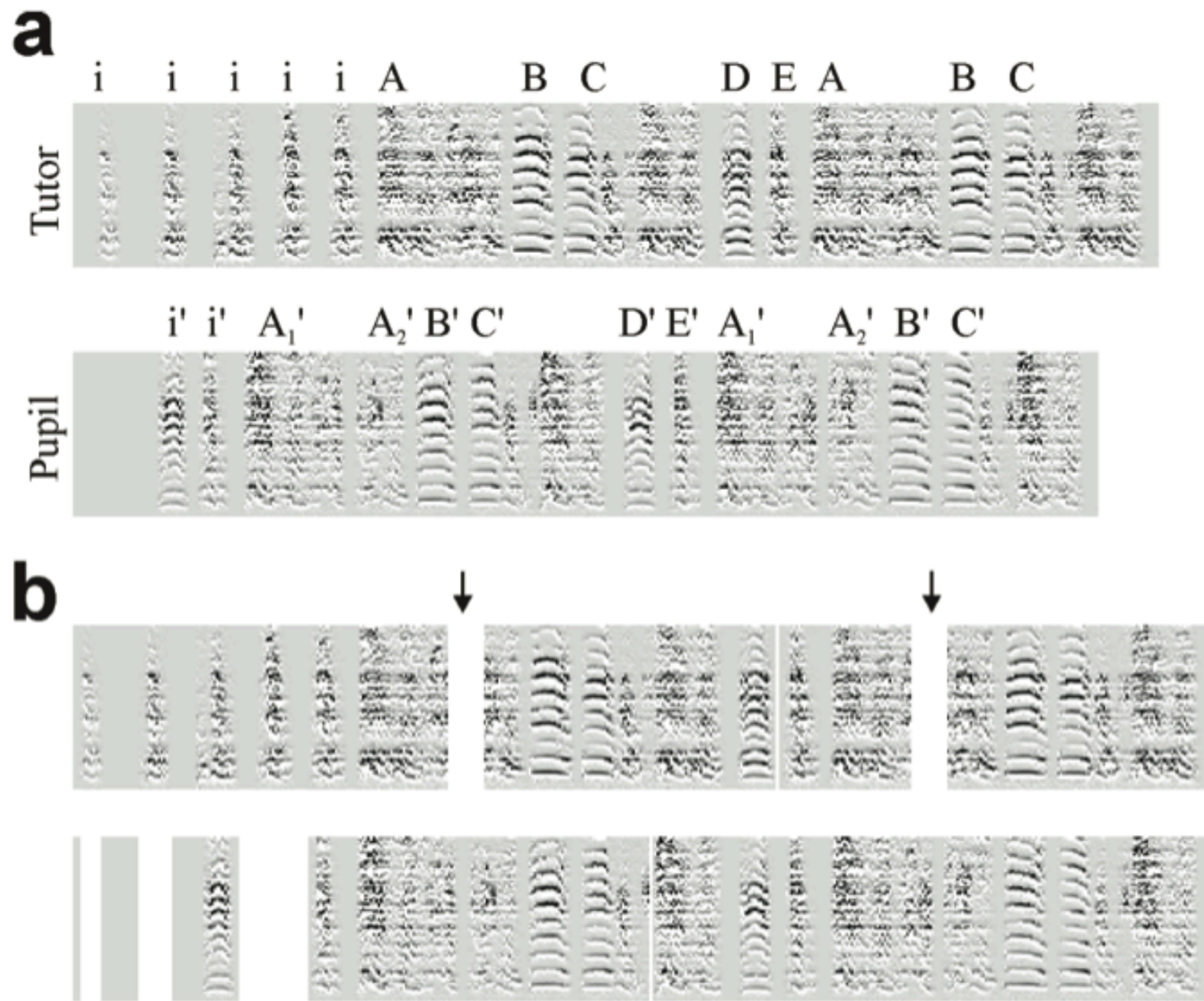
Query 1889 gcctgtgtgt--gtgggtgcacatttgtgtgtgtgtgcctgtg--tgtgt--gggtgcac 1942
          | | |||| ||| ||| || ||| | | |||| | |||| | ||| |
Sbjct 57056 TCATCTGTGTCAGTGTATGCTTATGGGTATAACT-TAACTGTGCATGTGTAAGTGTGTTC 57114

Query 1943 atttgtgtgtgtgtgtgcctgtgtgtgtgggtgcacatttgtgtgtgtgcctgtgtgtgg 2002
          || |||| | ||||| ||||| || ||| | ||||| |||||
Sbjct 57115 ATCTGTGTATGTGTGTG--TGTGTGAGTTAGTTCA----TCTGTGTGTGAGAGTGTGTGA 57168

Query 2003 gtgcacatttgtgtgtgtgtgtgcctgtgtgtgtgtgcctgtgtgtgtgggtgcacatttgt 2062
          | | ||| ||||| || | ||| || ||| |||| | ||| ||| |||
Sbjct 57169 G--CTCATCTGTGTGTGAGTTCATCTGTATGAGTG--TGTGTATGTGTGTGTACAAATGA 57224

Query 2063 gtgtgtgtgtgcctgtgtgtgtgggtgcacatttgtgtgtgtgtgtgtgcctgtgtgtgt 2122
          || | |||| | ||||| || ||| |||| | || |||| ||||
Sbjct 57225 GTTCATCTGTGCATGTGTGTGTG-----TTTAAGTGTGTTTCATCTG--TGTGCGTGT 57274
```

Comparing Bird Songs



Tracing Textual Influences

Example from
Horton, Olsen, Roe,
Digital Studies / Le
champ
numérique, Vol 2,
No 1 (2010)

This later play
by Markham
references
Shakespeare's
poem.

Common
passages
identified by
sequence
alignment
algorithms.

She locks her lily fingers one in one. "Fondling," she saith, "since I have hemmed thee here Within the circuit of this ivory pale, I'll be a park, and thou shalt be my deer; Feed where thou wilt, on mountain or in dale: Graze on my lips; and if those hills be dry, Stray lower, where the pleasant fountains lie." Within this limit is relief enough.... (Shakespeare, *Venus and Adonis* [1593])

Pre. Fondling, said he, since I haue hem'd thee heere, VWithin the circuit of this Iuory pale.

Dra. I pray you sir help vs to the speech of your master.

Pre. Ile be a parke, and thou shalt be my Deere: He is very busie in his study. Feed where thou wilt, in mountaine or on dale. Stay a while he will come out anon. Graze on my lips, and when those mounts are drie, Stray lower where the pleasant fountaines lie . Go thy way thou best booke in the world.

Ve. I pray you sir, what booke doe you read? (Markham, *The dumbe knight. A historicall comedy...* [1608])

Algorithm for Computing Longest Common Subsequence

Consider the last characters of each string:

$$\begin{aligned}a &= a_1a_2a_3a_4\dots a_m \\ b &= b_1b_2b_3b_4\dots b_n\end{aligned}$$

One of these possibilities must hold:

1. (a_m, b_n) are matched to each other
2. a_m is not matched at all
3. b_n is not matched at all
4. a_m is matched to some b_j ($j \neq n$) and b_n is matched to some a_k ($k \neq m$).

Algorithm for Computing Edit Distance

Consider the last characters of each string:

$$\begin{aligned}a &= a_1a_2a_3a_4\dots a_m \\ b &= b_1b_2b_3b_4\dots b_n\end{aligned}$$

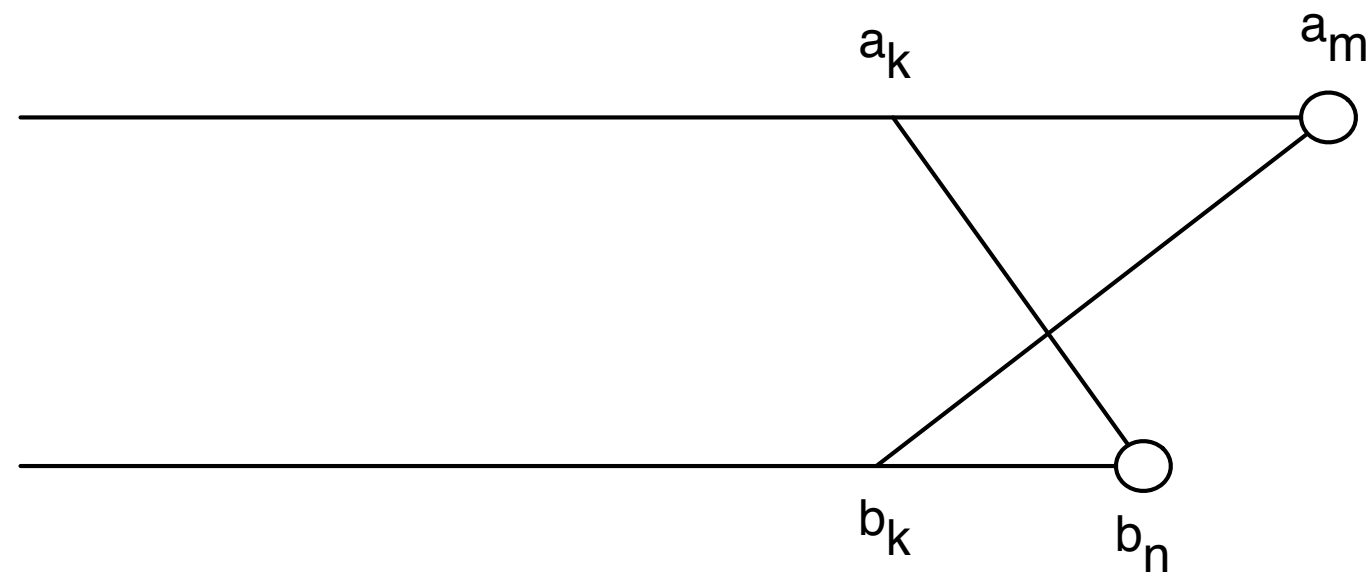
One of these possibilities must hold:

1. (a_m, b_n) are matched to each other
2. a_m is not matched at all
3. b_n is not matched at all
4. a_m is matched to some b_j ($j \neq n$) and b_n is matched to some a_k ($k \neq m$).

#4 can't happen! Why?

No Crossing Rule Forbids #4

4. a_m is matched to some b_j ($j \neq n$) and b_n is matched to some a_k ($k \neq m$).



So, the only possibilities for what happens to the last characters are:

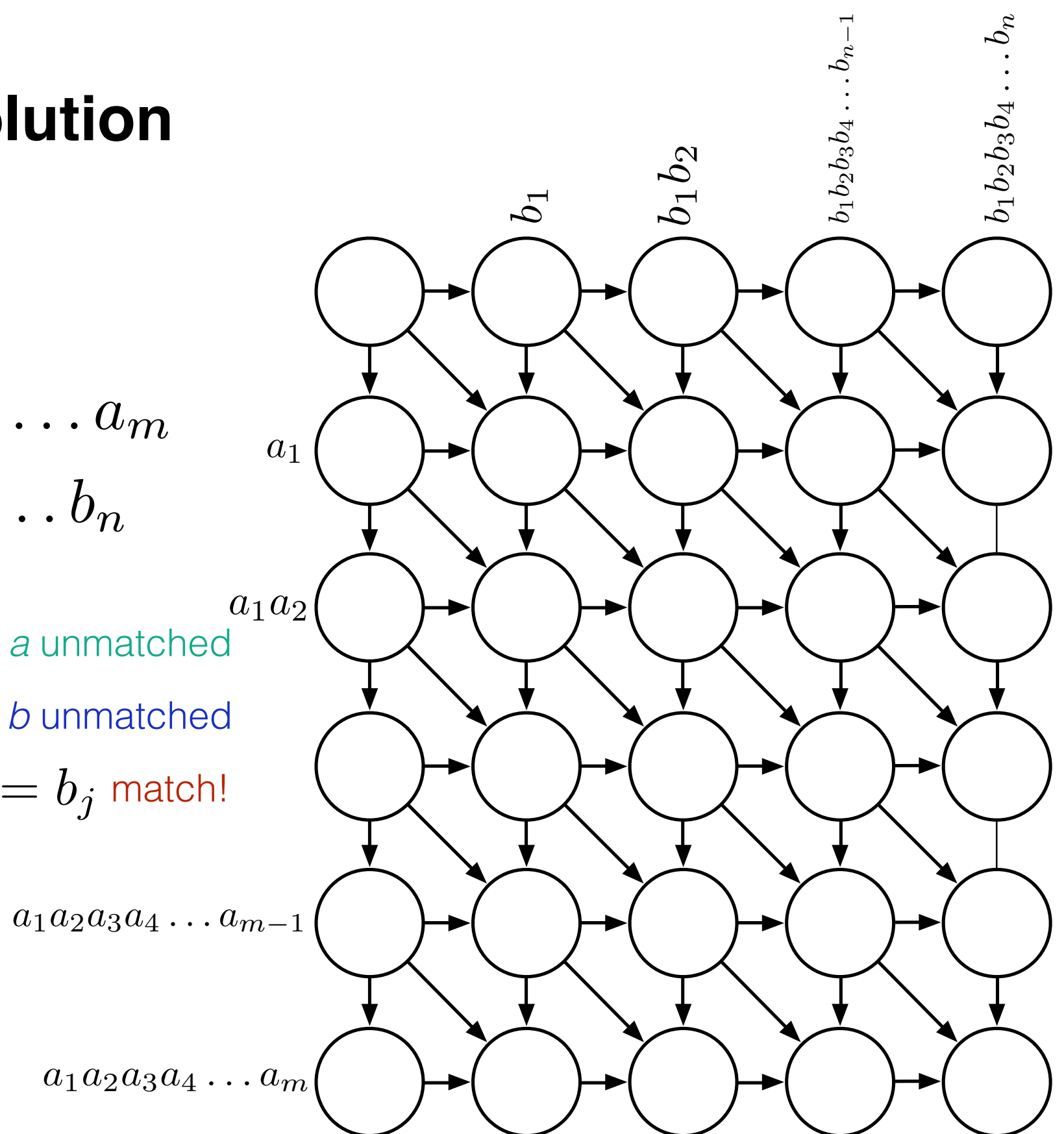
1. (a_m, b_n) are matched to each other
2. a_m is not matched at all
3. b_n is not matched at all

Recursive Solution

$$a = a_1 a_2 a_3 a_4 \dots a_m$$

$$b = b_1 b_2 b_3 b_4 \dots b_n$$

$$s_{i,j} = \max \begin{cases} s_{i-1,j} & \text{char in } a \text{ unmatched} \\ s_{i,j-1} & \text{char in } b \text{ unmatched} \\ s_{i-1,j-1}, & \text{if } a_i = b_j \text{ match!} \end{cases}$$



Dynamic Programming

The previous algorithm to solve LCS is an example of **dynamic programming**

Main idea of dynamic programming: solve the subproblems in an order so that when you need an answer, it's ready.

Requirements for DP to apply:

1. Optimal value of the original problem can be computed from some similar subproblems.
2. There are only a polynomial # of subproblems
3. There is a “natural” ordering of subproblems, so that you can solve a subproblem by only looking at **smaller** subproblems.

Serena Williams Winning Problem



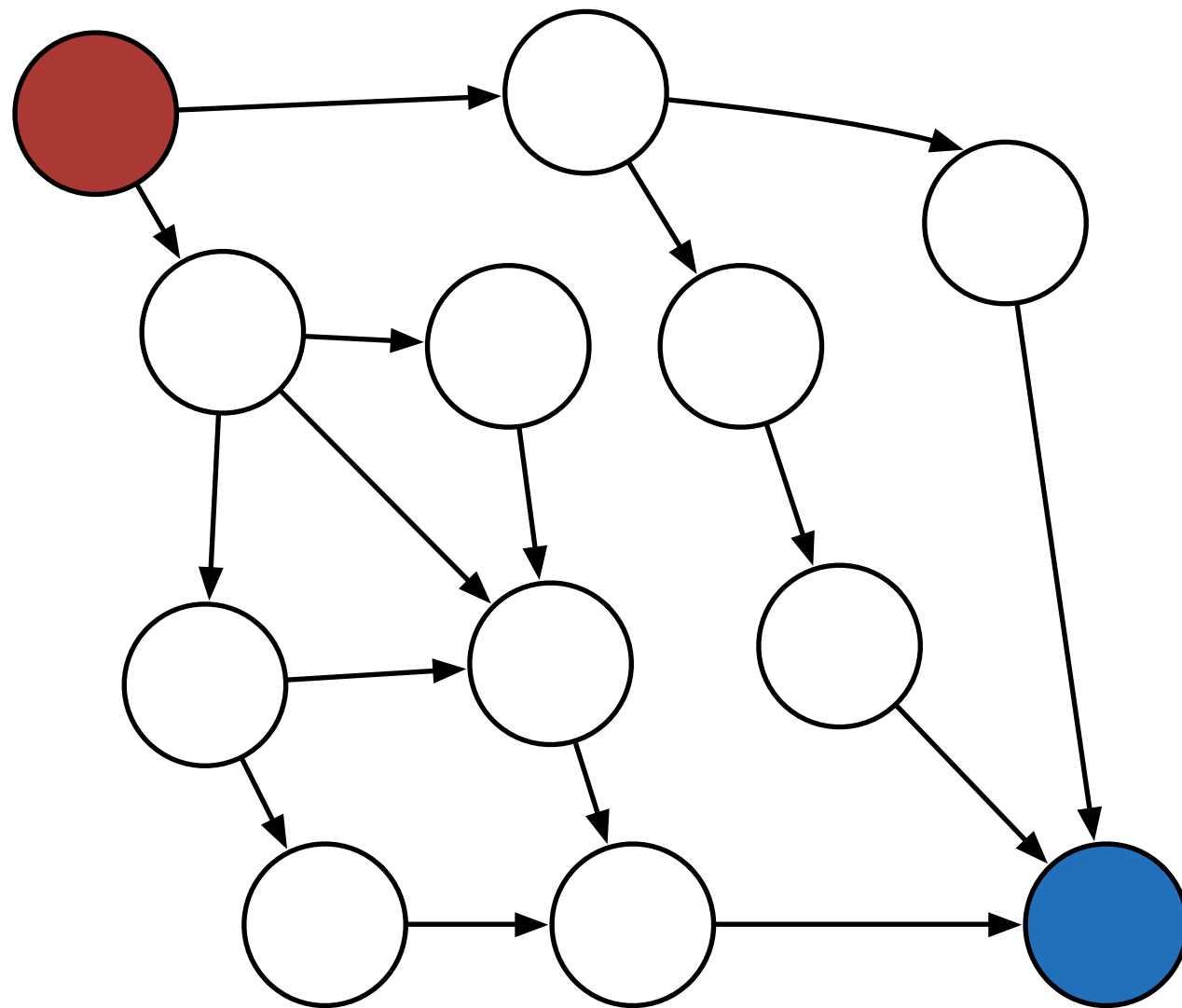
p : the probability that **Serena** beats
here **opponent** in a given single set

$q=(1-p)$: the probability that the **opponent** beats
Serena in a given single set

What is the probability that **Serena** wins
a best-of-five match? vs.

What is the probability that **Serena** wins
a best-of-three match?

Longest Path in a DAG



Longest Path in a DAG

