## String Comparison

**CMSC 423** 

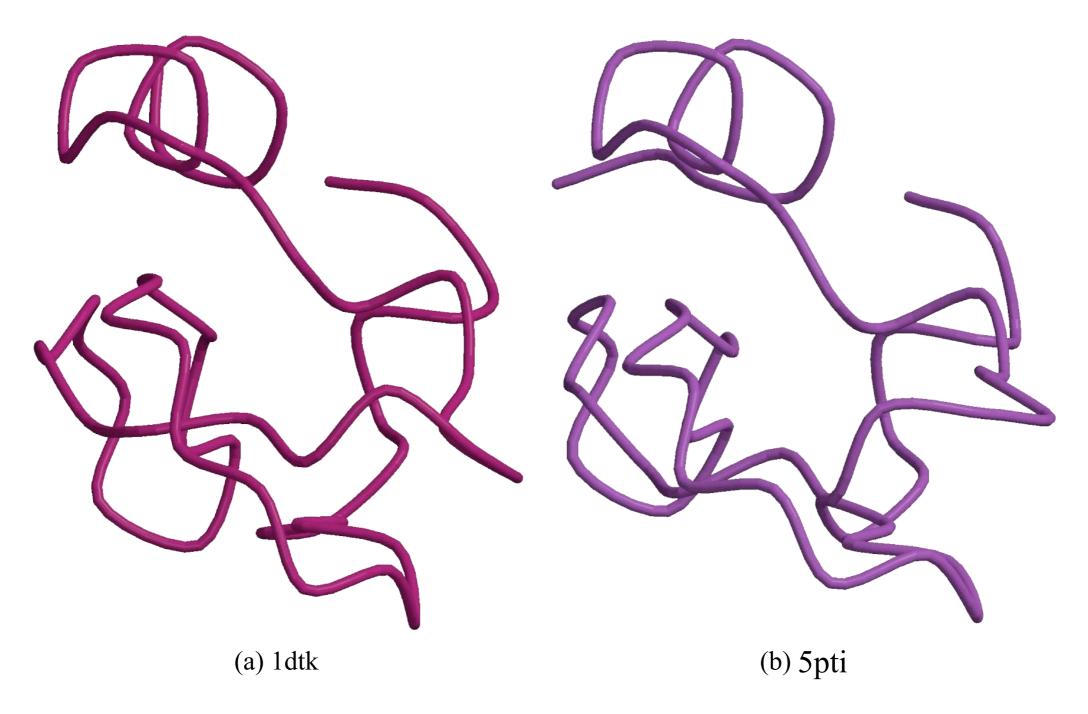
# Why compare DNA or protein sequences?

#### Partial CTCF protein sequence in 8 organisms:

```
H. sapiens
               -EDSSDS-ENAEPDLDDNEDEEEPAVEIEPEPE-----POPVTPA
P. troglodytes
               -EDSSDS-ENAEPDLDDNEDEEEPAVEIEPEPE-----POPVTPA
               -EDSSDS-ENAEPDLDDNEDEEEPAVEIEPEPE-----PQPVTPA
C. lupus
B. taurus
               -EDSSDS-ENAEPDLDDNEDEEEPAVEIEPEPE-----POPVTPA
M. musculus
               -EDSSDSEENAEPDLDDNEEEEEPAVEIEPEPE--PQPQPPPPPQPVAPA
R. norvegicus
               -EDSSDS-ENAEPDLDDNEEEEEPAVEIEPEPEPOPOPOPOPOPOPAPA
G. gallus
               -EDSSDSEENAEPDLDDNEDEEETAVEIEAEPE-----VSAEAPA
D. rerio
               DDDDDDSDEHGEPDLDDIDEEDEDDL-LDEDOMGLLDOAPPSVPIP-APA
```

- Identify important sequences by finding conserved regions.
- Find genes similar to known genes.
- Understand evolutionary relationships and distances (D. rerio aka zebrafish is farther from humans than G. gallus aka chicken).
- Interface to databases of genetic sequences.
- As a step in genome assembly, and other sequence analysis tasks.
- Provide hints about protein structure and function (next slide).

## Sequence can reveal structure



1dtk XAKYCKLPLRIGPCKRKIPSFYYKWKAKQCLPFDYSGCGGNANRFKTIEECRRTCVG-5pti RPDFCLEPPYTGPCKARIIRYFYNAKAGLCQTFVYGGCRAKRNNFKSAEDCMRTCGGA

#### Simple String Comparison Problems

**Given**: Two strings

$$a = a_1 a_2 a_3 a_4 ... a_m$$
  
 $b = b_1 b_2 b_3 b_4 ... b_n$ 

where  $a_i$ ,  $b_i$  are letters from some alphabet like {A,C,G,T}.

Compute how similar the two strings are.

What do we mean by "similar"?

Longest Common Subsequence: the longest subsequence with matching characters from the two strings.

#### Simple String Comparison Problems

**Given**: Two strings

$$a = a_1 a_2 a_3 a_4 ... a_m$$
  
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Compute how similar the two strings are.

#### What do we mean by "similar"?

**Edit distance** between strings a and b = the smallest number of the following operations that are needed to transform a into b:

- mutate (replace) a character
- delete a character
- insert a character

$$riddle \xrightarrow{delete} ridle \xrightarrow{mutate} riple \xrightarrow{insert} triple$$

## Representing edits as alignments

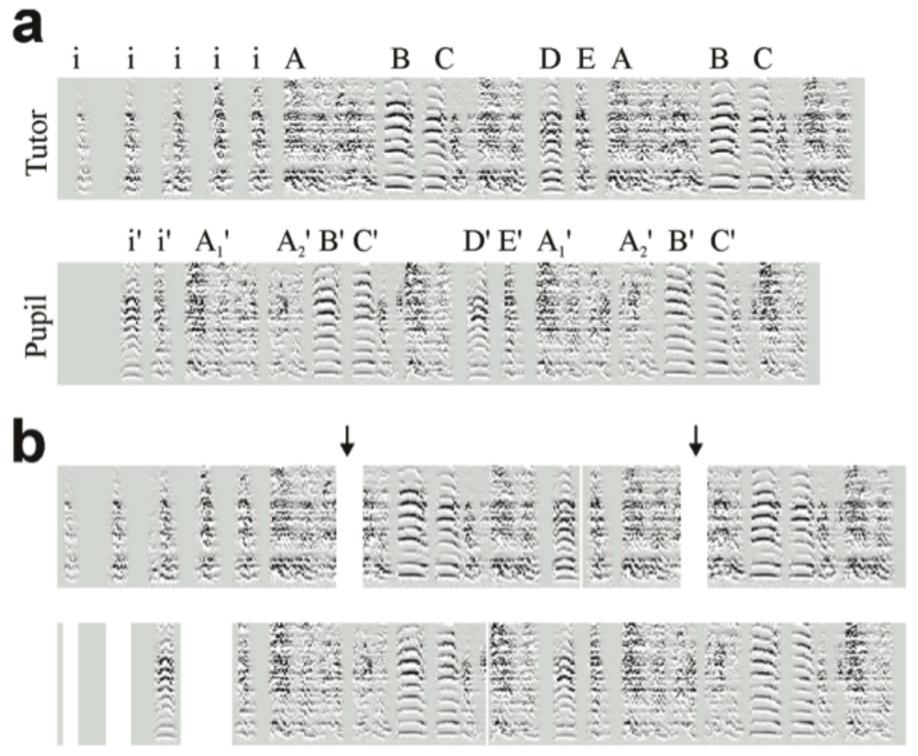
```
prin-ciple
                          prin-cip-le
prinncipal
                          prinncipal-
(1 gap, 2 mm)
                          (3 gaps, 0 mm)
                         prehistoric
misspell
                         ---historic
mis-pell
(1 gap)
                          (3 gaps)
aa-bb-ccaabb
                          al-go-rithm-
                          ababbbc-a-b-
                          alKhwariz-mi
(5 gaps, 1 mm)
                          (4 gaps, 3 mm)
```

## NCBI BLAST DNA Alignment

>gb|AC115706.7| Mus musculus chromosome 8, clone RP23-382B3, complete sequence

Query	1650	gtgtgtgtgggtgcacatttgtgtgtgtgtgcgcctgtgtgtg	1709
Sbjct	56838	GTGTGTGTGGAAGTGAGTTCATCTGTGTGTGCACATGTGTGCATGCATGCATGTGT	56895
Query	1710	gtg-gggcacatttgtgtgtgtgtgtgtgcctgtgtgtggggtgcacatttgtgtgtg	1768
Sbjct	56896	GTCCGGGCATGCATGTCTGTGTGTGTGTGTGTGTGTGTGTGTGTGTGTG	56947
Query	1769	ctgtgtgtgtgtgcctgtgtgtgggggtgcacatttgtgtgtg	1828
Sbjct	56948	CTGTGTGTGTATGCTTGTGTGTGTGTGTGTGTGTGTGTGT	57007
Query	1829	gggtgcacatttgtgtgtgtgtgtgcctgtgtgtgtgtgggtgcacatttgtgtgtg	1888
Sbjct	57008	TCATCTGTGTGTGTGTGTGTGAGAGTGCATGCATGTGTGTGTGAGT	57055
Query	1889	gcctgtgtgtgtgggtgcacatttgtgtgtgtgtgtgcctgtgtgtgtgggtgcac	1942
Sbjct	57056	TCATCTGTGTCAGTGTATGCTTATGGGTATAACT-TAACTGTGCATGTGTAAGTGTGTTC	57114
Query	1943	atttgtgtgtgtgtgtgtgtgtgtgtgtgtgcacatttgtgtgtg	2002
Sbjct	57115	ATCTGTGTATGTGTGTGTGTGAGTTAGTTCATCTGTGTGTGAGAGTGTGTGA	57168
Query	2003	gtgcacatttgtgtgtgtgtgcctgtgtgtgtgtgtgtgt	2062
Sbjct	57169	G-CTCATCTGTGTGAGTTCATCTGTATGAGTG-TGTGTATGTGTGTGTACAAATGA	57224
Query	2063	gtgtgtgtgtgcctgtgtgtgtgggtgcacatttgtgtgtg	2122
Sbjct	57225		57274

## Comparing Bird Songs



Florian et al. Hidden Markov Models in the Neurosciences

## Tracing Textual Influences

Example from Horton, Olsen, Roe, Digital Studies / Le champ numérique, Vol 2, No 1 (2010) She locks her lily fingers one in one. "Fondling," she saith, "since I have hemmed thee here Within the circuit of this ivory pale, I'll be a park, and thou shalt be my deer; Feed where thou wilt, on mountain or in dale:

Graze on my lips; and if those hills be dry, Stray lower, where the pleasant fountains lie." Within this limit is relief enough.... (Shakespeare, Venus and Adonis [1593])

This later play by Markham references Shakespeare's poem.

Common passages identified by sequence alignment algorithms.

Pre. Fondling, said he, since I haue hem'd thee heere,

VVithin the circuit of this Iuory pale.

Dra. I pray you sir help vs to the speech of your master.

Pre. <u>Ile be a parke</u>, and thou shalt be my <u>Deere</u>: He is very busie in his study. <u>Feed where thou wilt</u>, in mountaine or <u>on dale</u>. Stay a while he will come out anon. <u>Graze on my lips</u>, and when those mounts are drie, <u>Stray lower where the pleasant fountaines lie</u>. Go thy way thou best booke in the world.

Ve. I pray you sir, what booke doe you read? (Markham, The dumbe knight. A historicall comedy... [1608])

#### Algorithm for Computing Longest Common Subsequence

Consider the last characters of each string:

$$a = a_1 a_2 a_3 a_4 ... a_m$$
  
 $b = b_1 b_2 b_3 b_4 ... b_n$ 

#### One of these possibilities must hold:

- 1.  $(a_m, b_n)$  are matched to each other
- 2.  $a_m$  is not matched at all
- 3.  $b_n$  is not matched at all
- 4.  $a_m$  is matched to some  $b_j$  ( $j \neq n$ ) and  $b_n$  is matched to some  $a_k$  ( $k \neq m$ ).

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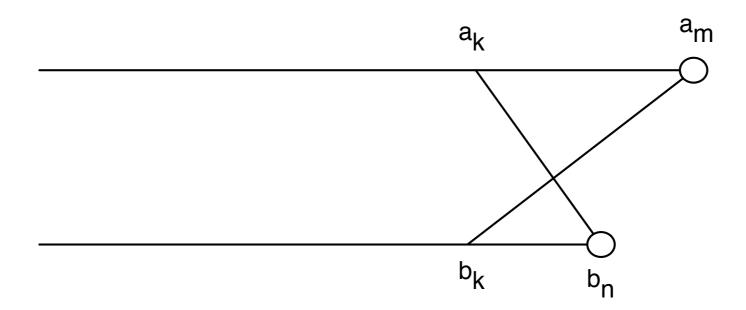
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## No Crossing Rule Forbids #4

4.  $a_m$  is matched to some  $b_j$  ( $j \neq n$ ) and  $b_n$  is matched to some  $a_k$  ( $k \neq m$ ).



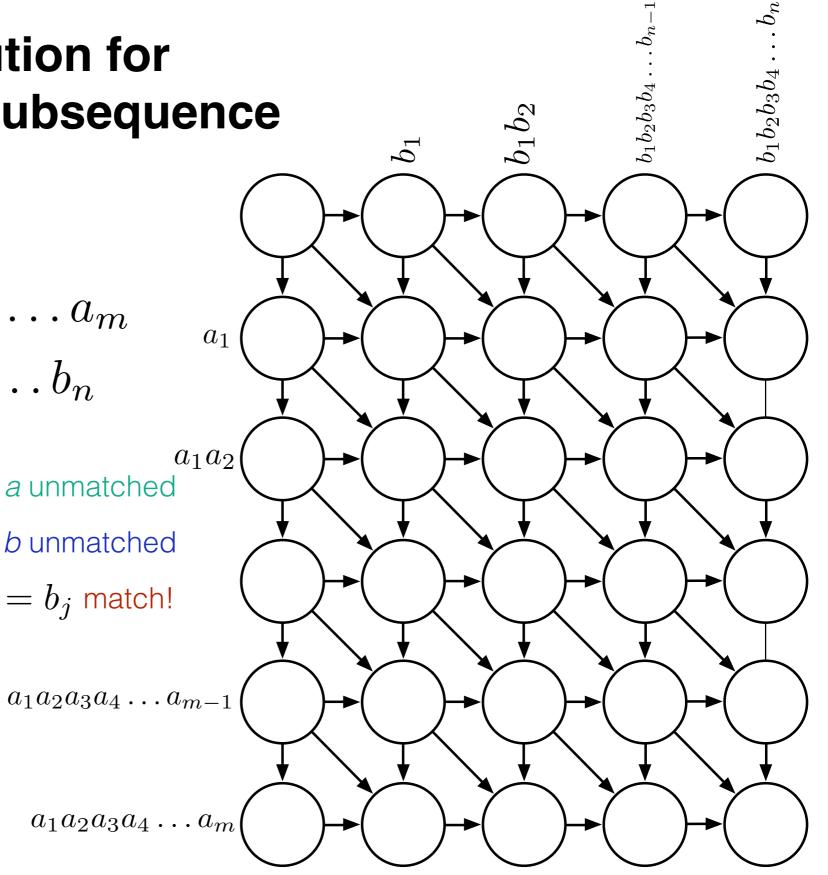
So, the only possibilities for what happens to the last characters are:

- 1.  $(a_m, b_n)$  are matched to each other
- 2.  $a_m$  is not matched at all
- 3.  $b_n$  is not matched at all

### Recursive Solution for Longest Common Subsequence

$$a = a_1 a_2 a_3 a_4 \dots a_m$$
$$b = b_1 b_2 b_3 b_4 \dots b_n$$

$$s_{i,j} = \max egin{cases} s_{i-1,j} & ext{char in $a$ unmatched} \ s_{i,j-1} & ext{char in $b$ unmatched} \ s_{i-1,j-1} + 1, & ext{if $a_i = b_j$ match!} \end{cases}$$



## Dynamic Programming

# The previous algorithm to solve LCS is an example of dynamic programming

Main idea of dynamic programming: solve the subproblems in an order so that when you need an answer, it's ready.

#### Requirements for DP to apply:

- 1. Optimal value of the original problem can be computed from some similar subproblems.
- 2. There are only a polynomial # of subproblems
- 3. There is a "natural" ordering of subproblems, so that you can solve a subproblem by only looking at **smaller** subproblems.

#### Serena Williams Winning Problem



p: the probability that Serena beats here opponent in a given single setq=(1-p): the probability that the opponent beatsSerena in a given single set

What is the probability that Serena wins a best-of-five match? vs.
What is the probability that Serena wins a best-of-three match?