A* Revisited

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1 Overview

This report is designed to accompany and supplement the submitted application, which has been designed by us to emulate and improve on the A* algorithm as it was presented in class. Out additions to the assignment include a complete rewrite of the codebase from Javascript to C++, similar efficiency tricks as were employed in the submitted assignment to increase speed, as well as an implementation of Jump Point Search, which can drastically speed up times for specific map types.

2 Problem: Flexibility and Performance

This project managed to combine two of our favourite aspects of the semester: The fantastic SFML C++ library, as well as the A* pathfinding algorithm. After making numerous concessions to achieve the best speed we could in the assignment's Javascript environment, we decided that the speed of a compiled language and the flexibility of a visualization library like SFML would provide us with both adequate performance and challenge. Additionally, by using a binary application, we would be able to load arbitrary maps from disk dynamically, which would allow us to test in multiple environments quickly.

The A* pathfinding algorithm is said to be one of the most well known algorithms in computer science. First published in 1968¹ it is essentially the single-path version of Dijkstras algorithm with the addition of a heuristic function. Through it's use of an (admissible) heuristic, it is guaranteed to be optimal in that any similar search function can not explore fewer nodes than A*.

For our problem instance, we will be exploring the performance of our algorithm compared to the assignment paths, as well as some arbitrary environments.

¹Hart, P. E.; Nilsson, N. J.; Raphael, B. (1968). "A Formal Basis for the Heuristic Determination of Minimum Cost Paths".

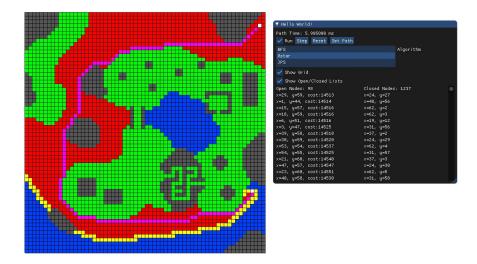


Figure 1: A screenshot of our application

3 Methodology

The project can be broadly broken up into 3 steps:

- Creating the GUI and visualization / loading of maps
- Implementing the A* algorithm
- Optimizing the A* algorithm

Though our initial intentions were that the first two would be trivial, in practice they proved to be more difficult than we expected. Discussion of the particulars of C++ and our implementation of the GUI are beyond the scope of this report, however.

The A* algorithm

While the A* algorithm is deceptively simple, the choice of data structures, looking conditions, heuristics and many other elements can have a massive impact on performance. We will discuss several optimizations in detail:

- Caching the open list for O(1) lookup
- using an efficient open list structure for min-retrieval
- Minimizing node size

Algorithm 1 A* Search: basic version

```
initialize open list with first location
initialize an empty closed list
for infinity do
  if open list is Empty then
    return failure
  end if
  current node = node in open list with lowest f score
  if current node is goal node then
    return success: reconstruct path
  end if
  if current node is in the closed list then
    continue
  end if
  for Each legal neighbour of current node do
    let node N be a node constructed from the neighbour
    let N's g-cost = the g-cost of current node + travel distance
    let N's f-cost = the result of a heuristic h(N)
    let N's parent = current node
    add N to the open list
  end for
end for
```

Caching the Open List

In order to prevent the open list from being overtaken by a large number of duplicates, it is nessecary to see if any of the legal neighbours of a node are already present on the open list. To this end, we elected to use an array of the same size as the problem space. By storing a node's G cost in the [x][y] location of this 2d array, we can see if our newly expanded node exists already with a lower score - meaning there is already a faster route to it. In such a case we can avoid creating a new node, avoid calculating and of it's scores, and save on both space and time.

Open list data structure

Because A* requires repeated access to the lowest element, the ideal data structure for the open list is a priority queue. Much has been written about priority queues and their usefulness for the A* algorithm, including the creation of abstract and confounding data structures such as the Fibonacci Heap² or Brodal queues³. For our implementation we have elected to use a binary min-heap as implemented by the C++ STL. This data structure provides $O(\log_n)$ retrieval of the minimum element.

Minimizing Node Size

Despite best efforts to prune nodes, the open list will invariably contain many nodes, and minimizing their size is paramount to being able to work on larger maps. As such each element of a node must be carefully considered. As such, our pathfinding nodes contain very little actual data:

- unsigned integer index
- unsigned integer sector
- unsigned integer g-score
- (A* only) unsigned integer f-score

Heuristics

For our heuristic we elected to use primarily euclidean distance, however our algorithm has 4 as well as 8 directional Manhattan distance available. While euclidean distance, with it's expensive floating point operations, is undoubtedly slower, it is also the most accurate and as such the choice of heuristics is always one of inherent tradeoff.

 $^{^2}$ Fredman, Michael Lawrence; Tarjan, Robert E. (July 1987). "Fibonacci heaps and their uses in improved network optimization algorithms" Journal of the Association for Computing Machinery.

 $^{^3{\}rm Gerth}$ Stølting Brodal (1996). Worst-case efficient priority queues. Proc. 7th ACM-SIAM Symposium on Discrete Algorithms

Results & Discussion

We were able to consistently beat the times of our A* implementation from assignment 2 on several of the maps. In particular this time seems most significant on the smaller maps, which is likely a result of JIT compilation of various javascript functions.

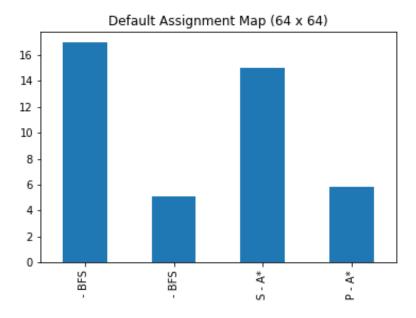


Figure 2: Comparison of Javascript and CPP application times

All these tests were carried out on a desktop computer running the Windows 7 operating system, with an Intel i5 3.4Ghz processor and 16GB of DDR3 RAM.

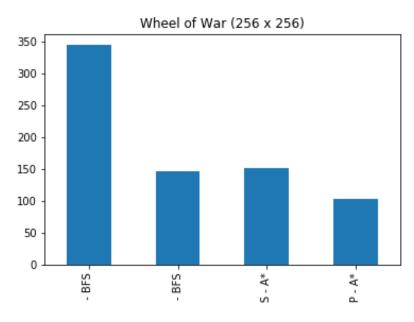


Figure 3: Comparison of Javascript and CPP application times

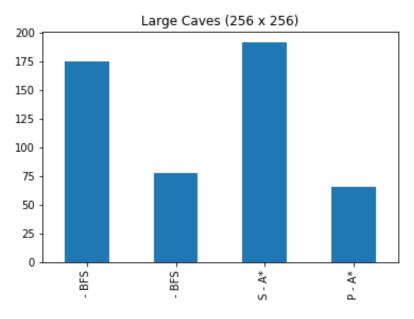


Figure 4: Comparison of Javascript and CPP application times

4 Conclusion (AND JPS)

In conclusion we are quite pleased with the performance of our C++ implementation of both the suite and the A* algorithm. In addition to being very performant, the code is written using many OOP features and laid out in a way that would make using it as a library on another project much easier to implement than a javascript application.

4.1 JPS

One of our ambitions was to implement Jump Point search, being excited for the performance gains it promises. While we have implemented JPS in our assignment, our current implementation is very inefficient. It offers time savings when used in open areas on larger maps, but in maps with tight corners and small areas performs worse than our vanilla A*. Nevertheless the logic is extremely promising, as the debug output shows just how few nodes are expanded using this technique.

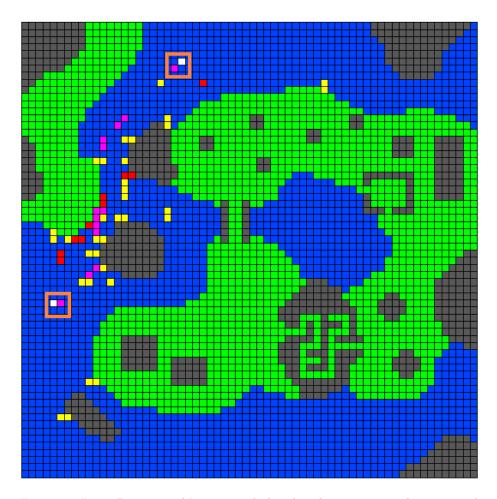


Figure 5: Jump Point search's open and closed node structure. The start and end points are accentuated by orange squares